

STARTING TREE for LL and LR

```
graph TD; A((A)) --> T1((T1)); A --> B((B)); B --> T2((T2)); B --> T3((T3));
```

Before an insertion, height(left) and height(right) differ by 1.

Case 1: Left-Left Imbalance (Single Rotation)

```
graph TD; A((A)) --> T1((T1)); A --> B((B)); B --> T2((T2)); B --> T3((T3));
```

Then, there is an insertion somewhere in T1 that causes A's height to increase by 1. Now, height(left) and height(right) differ by 2.

Important Observations:

- All values in T1 are smaller than both A and B.
- All values in T2 are larger than A but smaller than B.
- All values in T3 are larger than B.

⇒ Since all values in T2 are larger than A but smaller than B, those values must lie to the right of A or the left of B.

```
for rotateLeftChild(A, parent(B))
  A = C.left
  B.left = A.right
  A.right = C
```

we can adjust for this imbalance with a **DOUBLE ROTATION** by rotating the root of children with its left child. After the re-balancing, A has the same height as it did in the original tree.

Case 2: Left-Right Imbalance (Double Rotation)

```
graph TD; A((A)) --> T1((T1)); A --> B((B)); B --> T2((T2)); B --> T3((T3));
```

A's insertion in T2 causes B to become the root of children.

Notice that a Single Rotation wouldn't fix things.

```
graph TD; A((A)) --> T1((T1)); A --> B((B)); B --> T2((T2)); B --> T3((T3));
```

```
graph TD; A((A)) --> T1((T1)); A --> B((B)); B --> T2((T2)); B --> T3((T3));
```

Step 1: Rotate A with Right child B.

Step 2: Rotate C with Right Child B.

after this rotation, either T2.L or T2.R will be no deeper than T1 and T3, but not both.

STARTING TREE for RR and RL

```
graph TD; A((A)) --> T1((T1)); A --> B((B)); B --> T2((T2)); B --> T3((T3));
```

Before an insertion, height(left) and height(right) differ by 1.

Case 4: Right-Right Imbalance (Single Rotation)

```
graph TD; A((A)) --> T1((T1)); A --> B((B)); B --> T2((T2)); B --> T3((T3));
```

Insertion into T3 causes B to be 2 levels deeper than T1, making A the root of children.

Remember: All values in T2 fall between A and B, so T2 must be connected to the left of B or the right of A.

Case 3: Right-Left Imbalance (Double Rotation)

```
graph TD; A((A)) --> T1((T1)); A --> B((B)); B --> T2((T2)); B --> T3((T3));
```

As with Case 2, an insertion into T3 cannot be solved with a single rotation. (We need to explicitly consider the root of T2, which is B here.)