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VI9 CS 076

Tutorial - 13

1. A language is recursive if there exists a TM that decides  $L$ .

A language is recursively enumerable if there exists a TM  $M$  that accepts  $L$ .

Closure

Union

If  $L_1, L_2$  are 2 recursive languages their union  $L_1 \cup L_2$  will be recursive because if TM halts for  $L_1, L_2$  it will also halt for  $L_1 \cup L_2$ .

Concatenation

If  $L_1$  and  $L_2$  are 2 recursive languages their concatenation  $L_1 \cdot L_2$  will be recursive.

For example,

$$L_1 = \{ a^n b^n c^n \mid n \geq 0 \}$$

$$L_2 = \{ d^m e^m f^m \mid m \geq 0 \}$$

$$L_3 = L_1 \cdot L_2$$

$\{ a^n b^n c^n d^m e^m f^m \mid n \geq 0 \text{ \& } m \geq 0 \}$   
is also recursive.

Kleen Closure

If  $L_1$  is recursive its  
Kleen closure  $L_1^*$  will also be  
recursive

$$L_1 = \{ a^n b^n c^n \mid n \geq 0 \}$$

$$L_1 = \{ a^n b^n c^n \mid n \geq 0 \}^* \text{ is also recursive}$$

Intersection & complement

If  $L_1, L_2$  are 2 recursive languages

$$L_1 = \{ a^n b^n c^n d^m \mid n \geq 0, m \geq 0 \}$$

$$L_2 = \{ a^n b^n c^n d^n \mid n \geq 0, m \geq 0 \}$$

$$L_3 = L_1 \cap L_2$$

$$= \{ a^n b^n c^n d^n \mid n \geq 0 \} \text{ will be recursive}$$

Similarly complemented recursive language  
 $L_1$  which is  $\Sigma^* - L_1$ ,  
will also be recursive.

2. Explain NP simple and NP hard classes

NP complex problems are hardest problems  
in NP set

A decision problem  $L$  is NP.

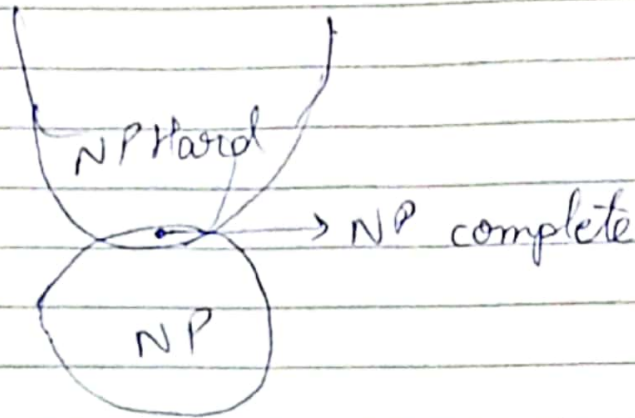
-  $L$  is in NP

- Every NP problem in NP is reducible to  $L$   
in polynomial time.

A problem is NP hard it follows 2nd property  
mentioned above doesn't need to follow



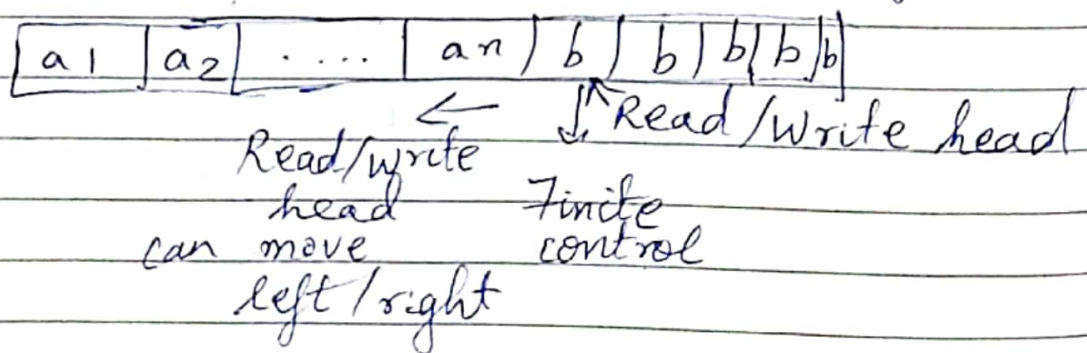
property 1.



### 3. Expt One tap turing machine

A turing machine consists of a tape of infinite length on which reads and write operation can be performed.

The tape consists of infinite cells on which each cell either contains input symbol.



A TM is expressed as

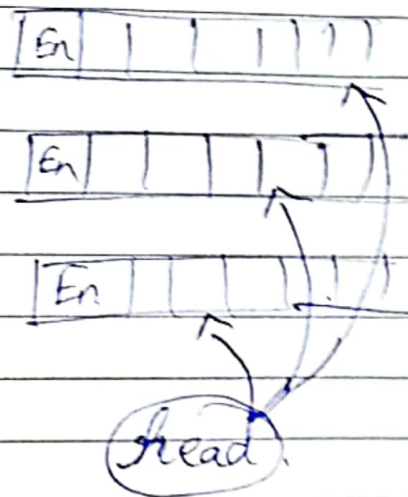
T-Tuple  $(Q, T, B, \Sigma, \delta, q_0, F)$

- $Q$  : Finite set of state
- $T$  : Tape of alphabet
- $B$  : Blank symbol
- $\Sigma$  : input alphabet
- $\delta$  :  $Q \times T \rightarrow Q \times T \times \{L, R\}$
- $q_0$  : Initial state
- $F$  : Final states set

## Multitape Turing machine

Multitape Turing machines have multiple tapes where each tapes accesses with a separate head. Each head can move independently on other heads.

Initially the input on tape 1 and others are blank. At ~~the~~ first the first tape is occupied by input and other tapes are kept blank.



A multitape Turing machine can describe as 6 tuple

- $Q$  : Finite set of states
- $\Sigma$  : Tape alphabet
- $B$  : Blank symbol
- $q$  : retains on states & symbol.
- $q_0$  : Initial state
- $F$  : Set of final state



- (Q4). A Turing machine is said to be universal Turing machine if accept
- The input data accept
  - An algorithm for computing

A general purpose TM will be called a universal TM if it is powerful enough to simulate behaviour of any digital computer.

A universal TM can simulate behaviour of arbitrary TM

The model of universal TM is considered to be theoretical breakthrough that led to the concept of stored program.

By modifying our basic model of TM we can design a universal Turing machine.

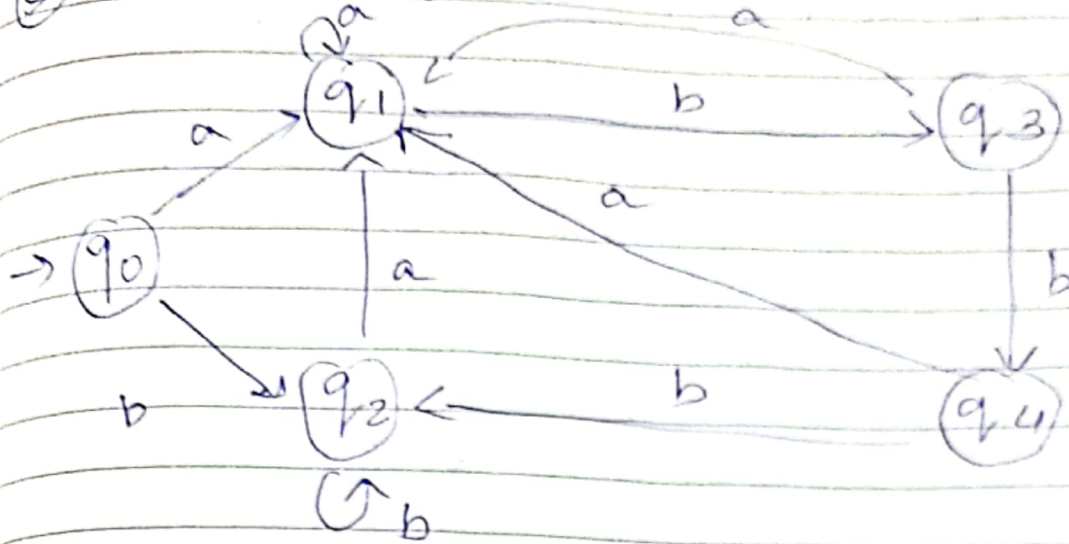
We modify our basic model by

- Increase the number of read/write head

- Increase number of dimensions of input tape

- Adding a special purpose memory.

⑤. Minimize DFA



Step 1 → Given DFA attributes no dead state  
inaccessible states

Step 2 → Draw a state transition table

	a	b
→ q <sub>0</sub>	q <sub>1</sub>	q <sub>2</sub>
q <sub>1</sub>	q <sub>1</sub>	q <sub>3</sub>
q <sub>2</sub>	q <sub>1</sub>	q <sub>2</sub>
q <sub>3</sub>	q <sub>1</sub>	*q <sub>4</sub>
*q <sub>4</sub>	q <sub>1</sub>	q <sub>2</sub>

Step 3

Now using equivalence theorem

$$P_0 = \{q_0, q_1, q_2, q_3\} \{q_4\}$$

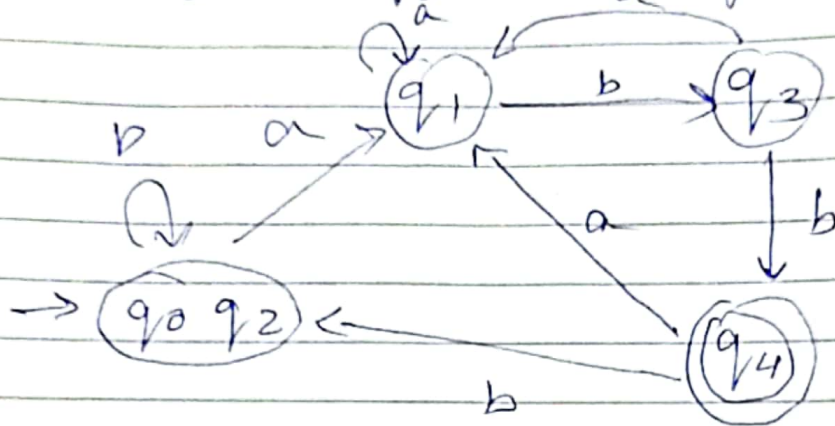
$$P_1 = \{q_0, q_1, q_2\} \{q_3\} \{q_4\}$$

$$P_2 = \{q_0, q_2\} \{q_1\} \{q_3\} \{q_4\}$$

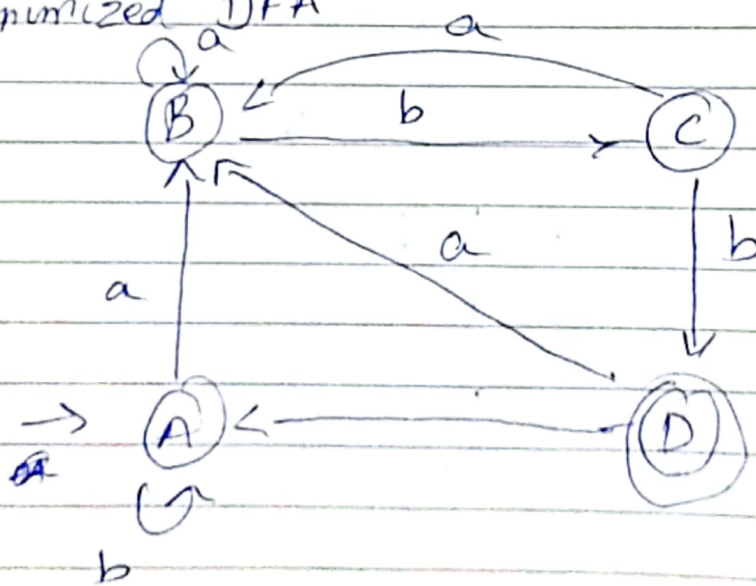
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$$P_3 = \{q_0, q_2\} \{q_1\} \{q_3\} \{q_4\}$$

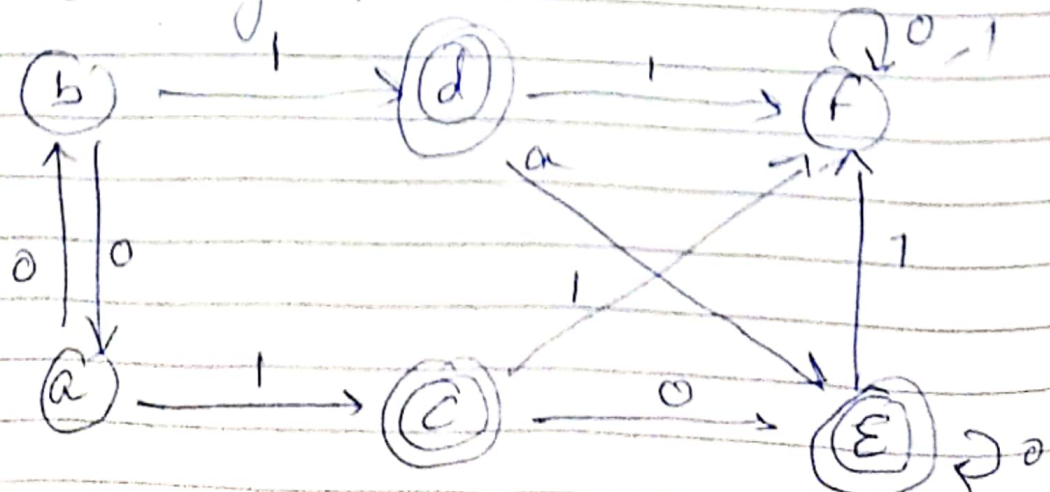
$P_2 = P_3$  so stop  
From  $P_3 \Rightarrow q_0$  &  $q_2$  equivalent, merged



Minimized DFA



⑥. Minimize given DFA





$P_0$  will have two set of states One set contain  $c, e, d$  which are final state

$$\text{So, } P_0 = \{ \{c, e, d\}, \{a, b, f\} \}$$

→ To calculate  $P_1$ , we check set of  $P_0$  partition

- 1)  $c$  &  $e$  are not distinguishable,  $c$  &  $d$  are also not,  $e$  &  $d$  are also not

So  $\{c, e, d\}$  not partitioned

- 2) So for set  $\{a, b, f\}$

→  $a, b, f$  not distinguishable

→ But  $a$  &  $f$  are

So set  $\{a, b, f\} \rightarrow \{a, b\}, \{f\}$ .

$$P_1 = \{ \{c, e, d\}, \{a, b\}, \{f\} \}$$

- 3) Now for set  $P_2$

We observe set  $\{c, e, d\}$  not partitioned

Set  $\{a, b\}$  will not partition as they are also not distinguishable &  $\{f\}$  same.

$$P_2 = \{ \{c, e, d\}, \{a, b\}, \{f\} \}$$

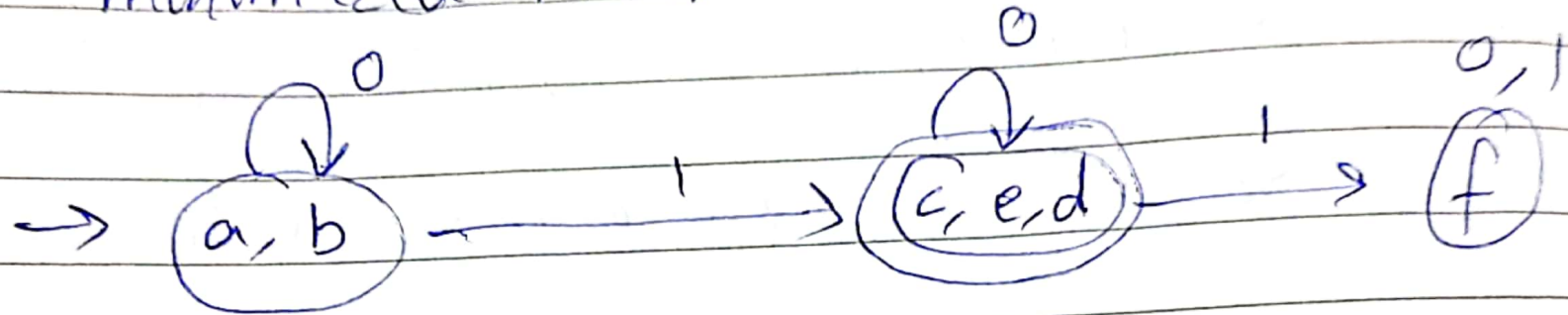
So this is final partition

Partition  $P_2$  means states  $c, e, d$  are merged into one.



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Minimized DFA



i.e.,

