

## Tutorial 5

1. Write difference between Moore Machine and Mealy machine.

Basis of Comparison	Mealy Machine	Moore Machine
Definition	Defined as a machine in theory of computation whose output depends on current state and current inputs.	Defined as a machine in theory of computation whose output depends on only its current state.
Tuple	It has 6 tuples $(Q, q_0, \delta, O, \delta, \lambda')$	It has also 6 tuples $(Q, q_0, \delta, O, \delta, \lambda)$
State	Less states than Moore machine	More <del>on faster</del> states than Mealy.
Output	Output depends on present state, present input  Output is placed on transition	Output depends only on present state  Output is placed on states.
Reaction to input	React faster to inputs. They react in same clock cycle.	More logic required to decode output resulting in more circuit delays.

They react

They react  
one clock later

Value of output function	Function of transition and changes when input logic on present state is done.	Function of current state changes at clock edges whenever state change occur.
State requirement	Fewer states for synthesis.	More states for synthesis.
Hardware Req.	Less hardware to design.	More hardware to design.
Counter	Not a Mealy machine	Is a Moore machine.
Design	Not always easy	Easy.

②. Define Moore machine and Mealy machine

There are 2 types of finite automata state machines that generate output.

Moore Machine

It is a finite state machine whose outputs depend on only present state.

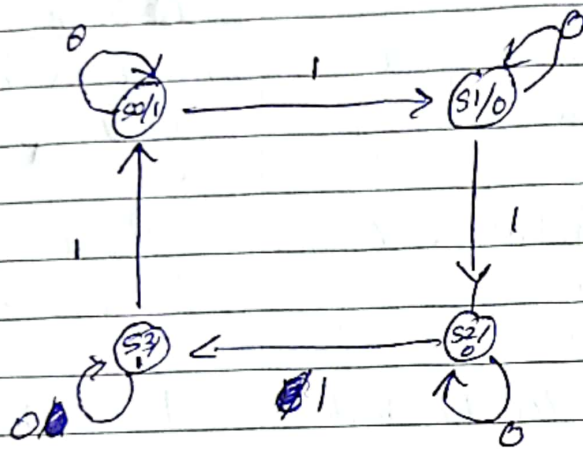


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It can be described by 6 tuple

$(Q, \Sigma, O, \delta, X, q_0)$

- $Q$  is finite set of states
- $\Sigma$  is finite set of symbols - input alphabet
- $O$  is " " " " - output alphabet
- $\delta$  is input transition function  $\delta: Q \times \Sigma \rightarrow Q$
- $X$  is output " "  $X: Q \rightarrow O$
- $q_0$  is initial state



## Mealy machine

It is a finite state machine whose output depends on present state as well as present input.

It has 6 tuple  $(Q, \Sigma, O, \delta, X, q_0)$

$Q$  is finite set of states

$\Sigma$  is finite set of symbols - input alphabet

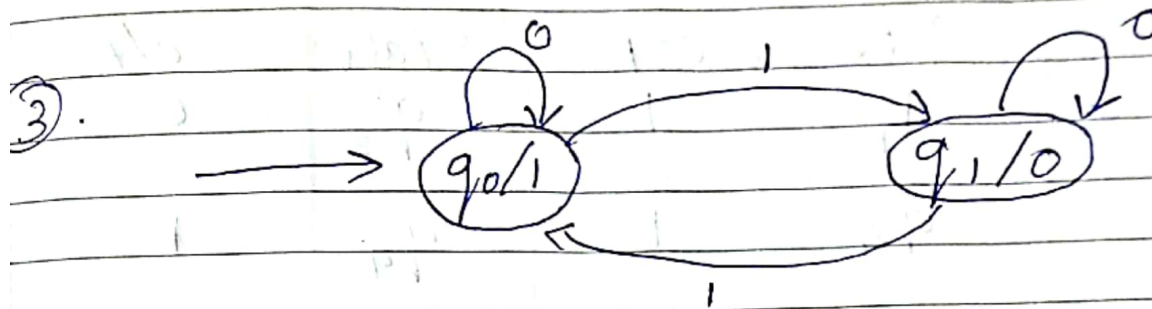
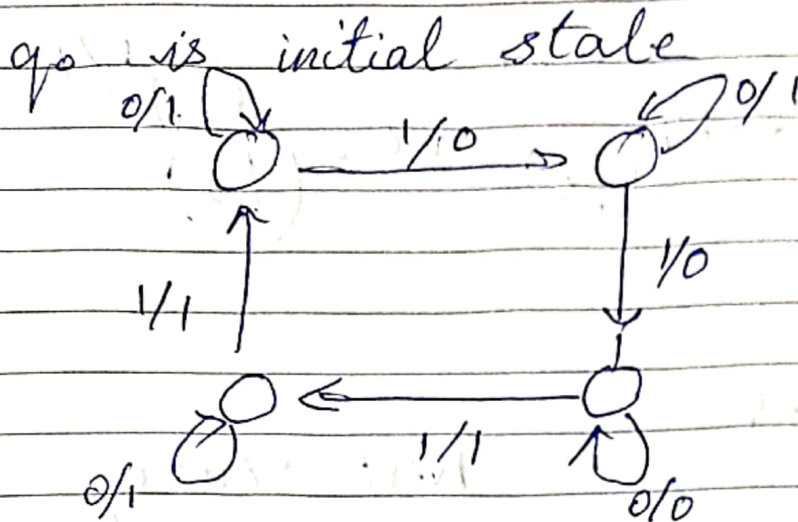
$O$  " " " " - output " "

$\delta$  is input transition function

$$\delta: Q \times \Sigma \rightarrow Q$$

$X$  is output transition function

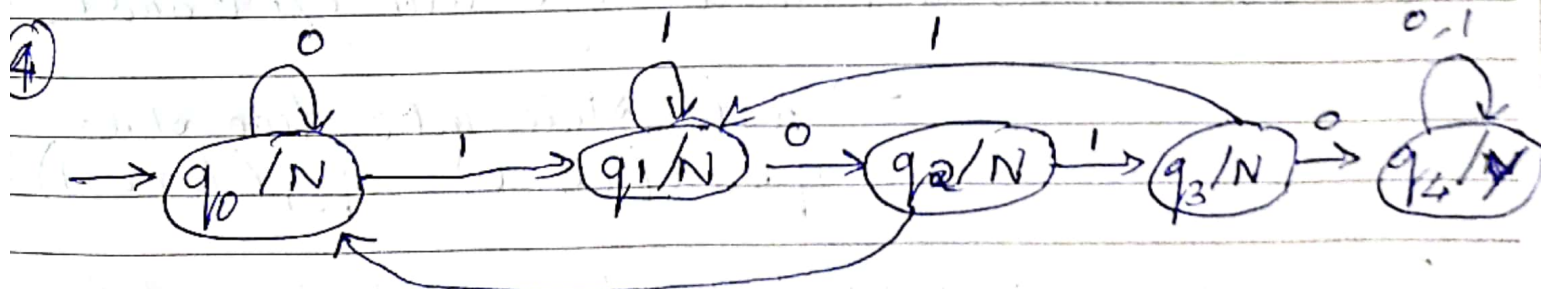
$$X: Q \times \Sigma \rightarrow O$$



$q_0$  accepts even number of 1s  
 $q_1$  accepts odd number of 1s.

When at state  $q_0$ , output is 1  
 otherwise all other states have 0.

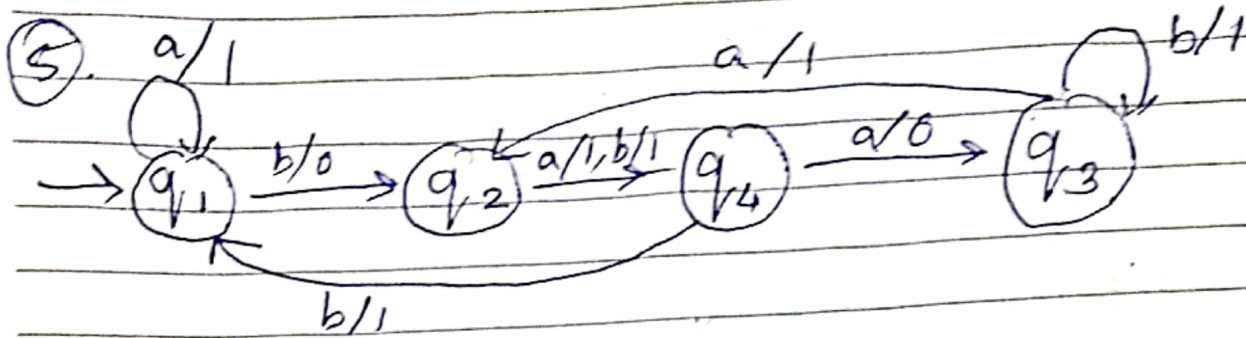
We move from  $q_1$  to  $q_0$  when input is 1  
 since there is no restriction on number  
 of zeroes, self loop of 0 applied both states.



Here only final state  $q_4$  gives Y since 1010 is  
 formed. All other states produces N or  
 does self loop.



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Transition table

Next State

Present State	Next State			
	a		b	
	State	o/p	State	o/p
$q_1$	$q_1$	1	$q_2$	0
$q_2$	$q_4$	1	$q_4$	1
$q_3$	$q_2$	1	$q_3$	1
$q_4$	$q_3$	0	$q_1$	1

For state  $q_1$ , it has single incident edge with o/p 0.

→ No need to split data in Moore machine

For state  $q_2$ , 2 incident edge with o/p 0 and 1.

→ Split state into two states  $q_{20}$  (for o/p 0),  $q_{21}$  (for o/p 1)

For state  $q_3$ , 2 incident edge with o/p 0 and 1.

→ Split state into two states  $q_{30}$  (for o/p 0),  $q_{31}$  (for o/p 1)

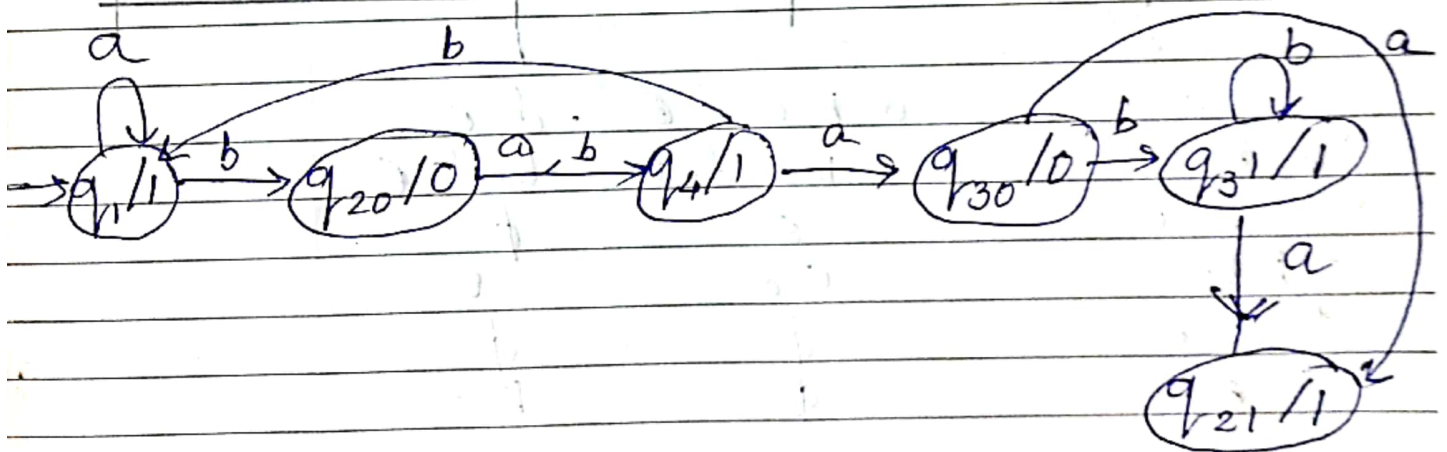
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For state  $q_4$ , only one incident edge with  $O/P = 0$ .

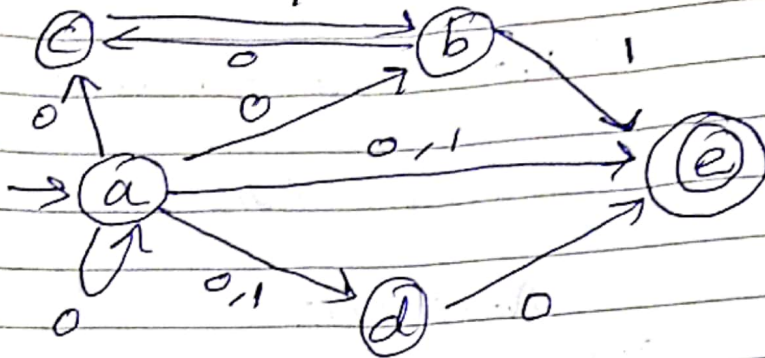
$\Rightarrow$  No need to split

$\Rightarrow$  Moore machine Transition table

Present State	Next State		Output
	$a=0$	$a=1$	
$q_1$	$q_1$	$q_2$	1
$q_{20}$	$q_4$	$q_4$	0
$q_{21}$	$\phi$	$\phi$	1
$q_{30}$	$q_{21}$	$q_{31}$	0
$q_{31}$	$q_{21}$	$q_{31}$	1
$q_4$	$q_3$	$q_4$	1



⑥. Convert NFA to DFA



NFA

	$\delta$	0	1
$\rightarrow a$		$\{a, b, c, d, e\}$	$\{d, e\}$
b		$\{c\}$	$\{e\}$
c		$\emptyset$	$\{b\}$
d		$\{e\}$	$\emptyset$
* e		$\emptyset$	$\emptyset$

[Final State]

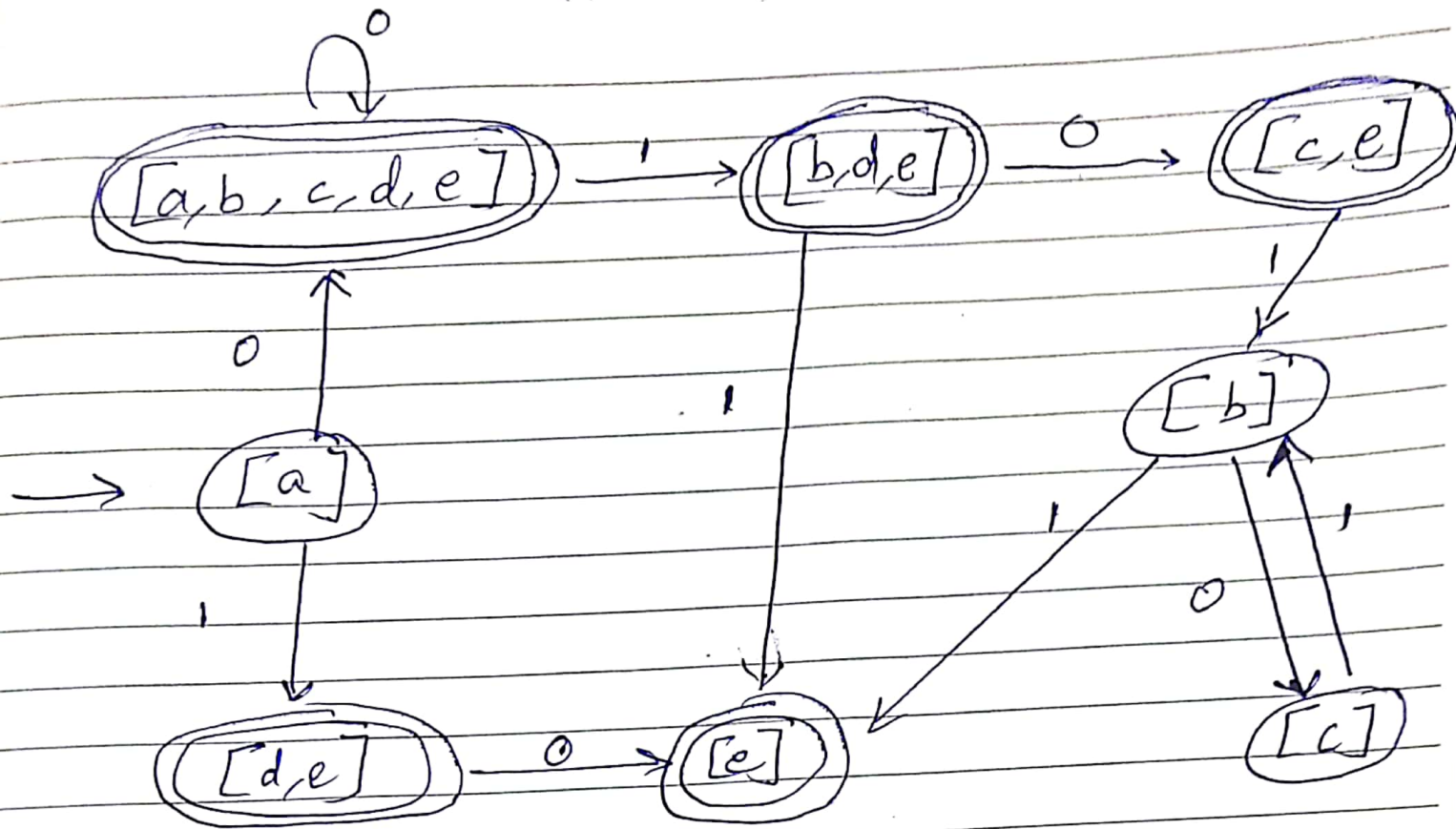
NFA  $\rightarrow$  DFA

	$\delta'$	0	1
$\rightarrow a$		$a, b, c, d, e$	$d, e$
* $a, b, c, d, e$		$a, b, c, d, e$	$b, d, e$
* $d, e$		$e$	$\emptyset$
* $b, d, e$		$c, e$	$e$
* $a, e$		$\emptyset$	$\emptyset$
* $b, c, e$		$\emptyset$	$b$
b		$c$	$e$
c		$\emptyset$	$b$

All \* are final states



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Dfa Chart.