

UI9CS076

## DFA - Deterministic Finite Automata

1. Construct DFA for  $\Sigma = \{a, b\}$  that accepts

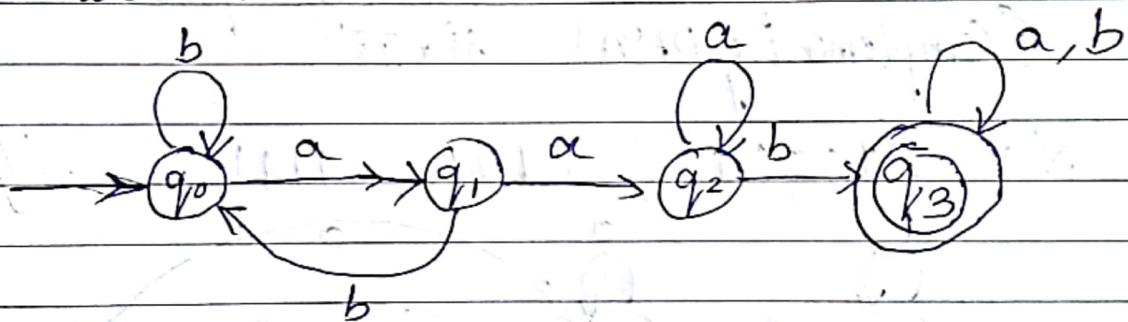
a) All string with aab as substring

All string of sub language having 'aab'  
length of substring = 3

$\Rightarrow$  Minimum DFA states =  $3+1=4$

$\alpha = \{ \underline{aab}, \underline{aab}aab, \underline{baa}aab, \underline{bbaa}aab \dots \}$

DFA is



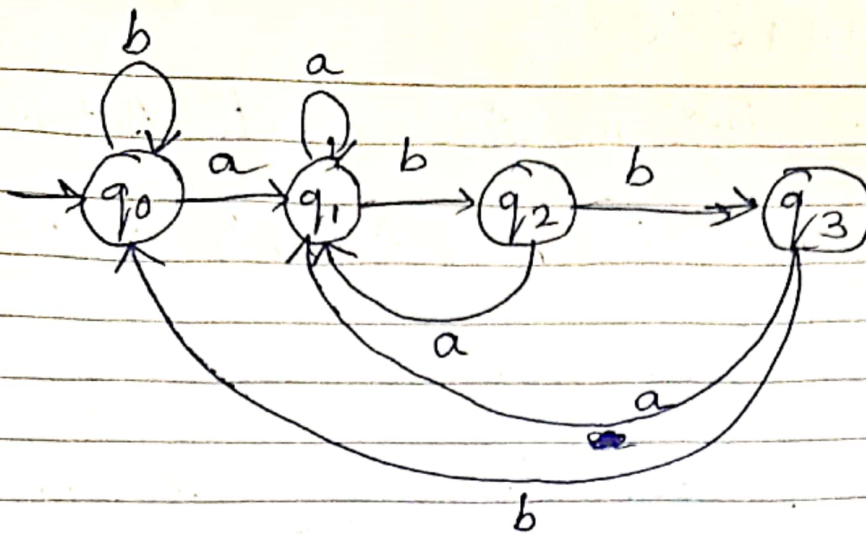
b) All strings ending with 'abb'

All strings of language ending with 'abb'

Length of substring = 3

Min DFA states = 4

$\alpha = \{ \underline{abb}, \underline{babb}, \underline{aabb}, aabbab\underline{abb} \dots \}$

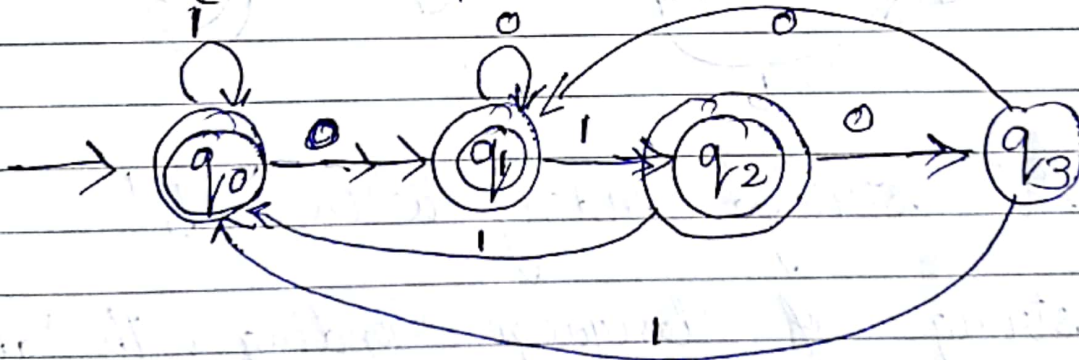


Q2] Design DFA on alphabet  $\Sigma = \{0, 1\}$  that accepts

a) All strings not ending with 010

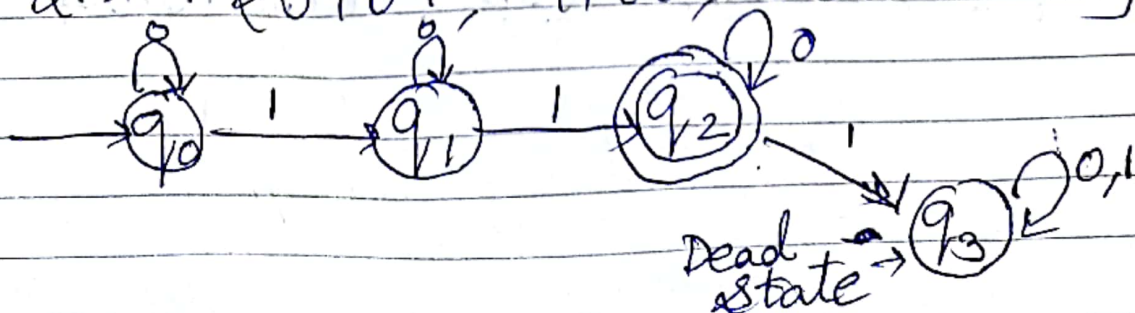
For NOT ending -- exchange final & non final (Complement of DFA) states

$\alpha = \{10001, 0101, 1111, \dots\}$



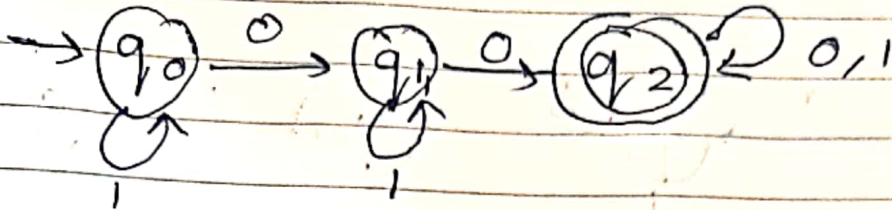
b) All strings with exactly two 1's

Dead state represent  $\alpha = \{0101, 1100, 0011, \dots\}$





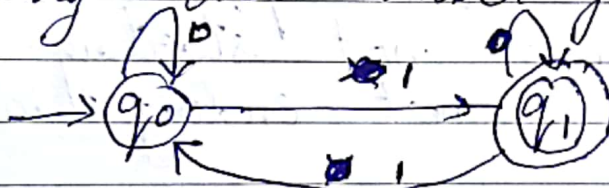
- c) All strings with at least two 0's  
 $\Sigma = \{010, 00111, 0000, 0100, \dots\}$



- ③. Construct DFA for  $\Sigma = \{0, 1\}$  that have odd number of 1s and even number of 0s

Doing separately

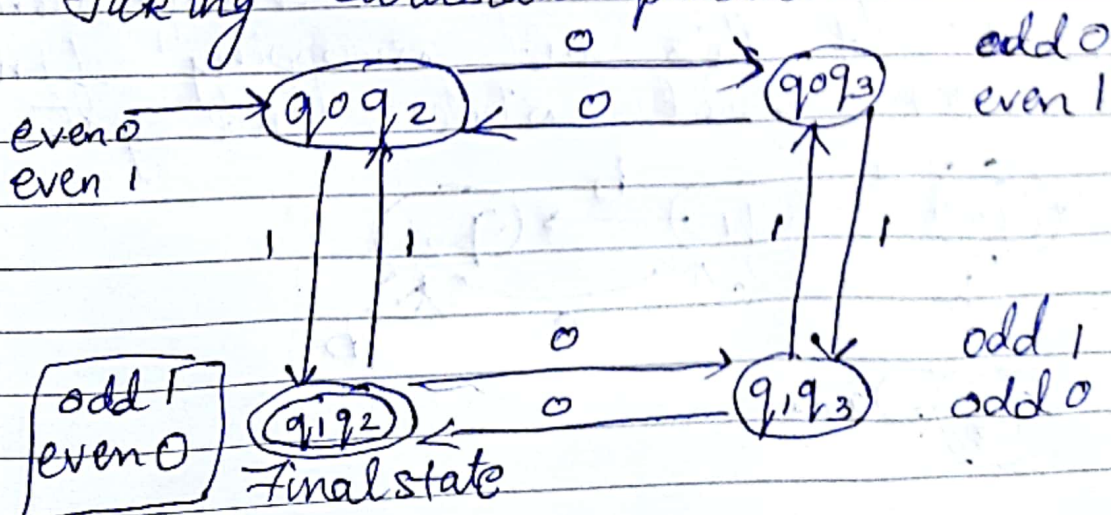
- Accepting odd number of 1s



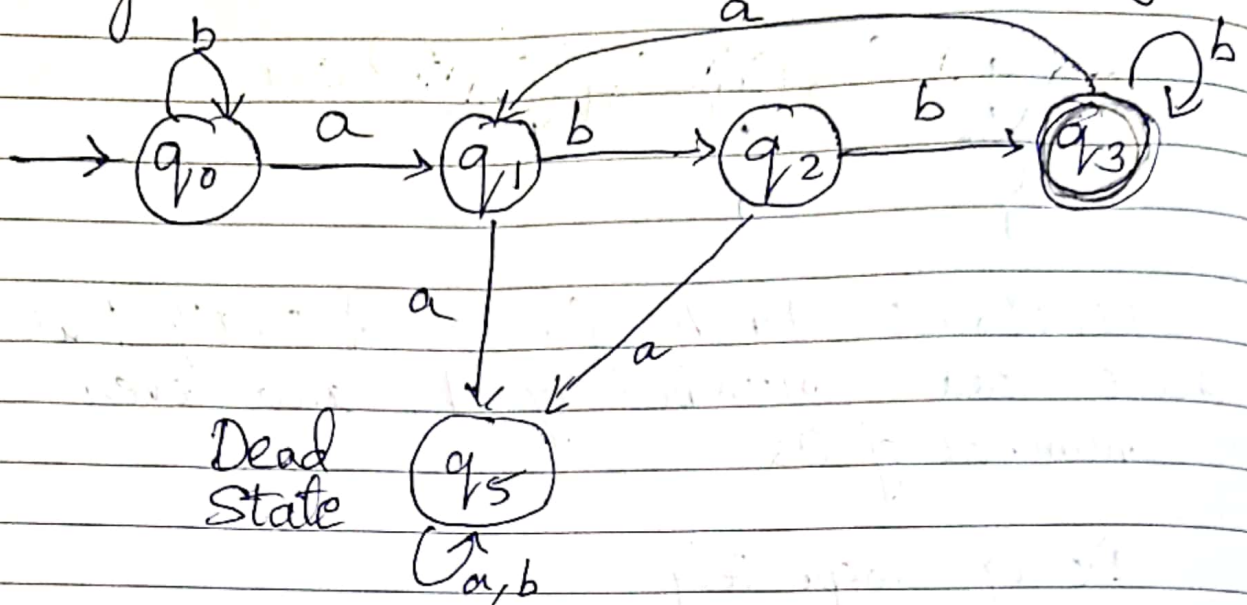
- Accepting even number of 0s



Taking cartesian product



Q4] Construct a DFA which accepts all strings over  $\Sigma = \{a, b\}$  in which every 'a' should be followed by 'b'.



Q5] Construct DFA which accepts a language of all strings not starting with 'a' or not ending with 'b'.

Let not starting with 'a' =  $P$   
 not ending with 'b' =  $Q$

According to De Morgan Law  $(P \cup Q)^c = P^c \cap Q^c$

$\Rightarrow$  Starting with A and ending with B  
 Drawing DFA of this and swapping final and non-final states, we get:

