

U19CS076 DAA ASSIGNMENT 4

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Q1. Assist an architect in drawing the skyline of a city given the locations of the buildings in the city. All buildings are rectangular in shape and they share a common bottom (a flat surface). A building is specified by an ordered triplet (L_i, R_i, H_i) where L_i and R_i are the left and right (x) coordinates, respectively, of the building i ($0 < L_i < R_i$) and H_i is the height of the building.

- For example, the input can be as follows.

(33, 41, 5)
(4, 9, 21)
(30, 36, 9)
(14, 18, 11)
(2, 12, 14)
(34, 43, 19)
(23, 25, 8)
(14, 21, 16)
(32, 37, 12)
(7, 16, 7)
(24, 27, 10)

The pseudocode/program should give the minimum number of points on graph (coordinates) as output to assist the architect in drawing the skyline.

- 1.1. Write a pseudocode (using an incremental/conventional approach) to find the skyline.
Analyze the time complexity.

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Skyline Problem

Incremental Approach

We convert all co-ordinates (x, y, z) to (x, h, f) through make_input function.

Here f is flag which determines whether a building start at x coord ($f=1$) or end at x coord ($f=0$).

We create the structure of (x, h, f) into an array and sort in ascending order of x .

Make_output function converts input to skyline

Make_output (sky [i])

Cost

// Declare ~~vec~~ height array, set prev=0

// Sort height

For $i=0$ to $\text{sky.size}()-1$

Set $\text{tmp} = \text{sky}[i].h$

IF ($\text{sky}[i].f = 1$)

For $j=0$ to $\text{height.size}()-1$

IF $\text{tmp} \geq \text{height}[j]$

break

Shift & insert elements $\text{tmp} \dots j$

Else

$k = \text{find tmp in height}[]$

Erase k

Set $\text{max} = \text{height}[0]$

If $\text{prev} \neq \text{max}$

Declare $\text{temp1}, \text{temp2}$

Set $\text{temp1}.x = \text{sky}[i].x$

$C_1 \quad n$

$C_2 \quad n(n-1)$

$C_3 \quad n-1$

$C_4 \quad n(n-1)$

$C_5 \quad 1$

$C_6 \quad 1$

$C_7 \quad n-1$

$C_8 \quad \log(n-1)$

$C_9 \quad n-1$

$C_{10} \quad n-1$

$C_{11} \quad n-1$

$C_{12} \quad n-1$

			(cost
		temp1.h = max	$C_{13} = n-1$
		temp1.f = 1	$C_{14} = n-1$
		* If sky[] not empty	$C_{15} = n-1$
		Set temp2.x = sky[sky.size(i-1)].x	$C_{16} = n-1$
		temp2.h = sky[sky.size(i-1)].h	
		temp2.f = sky[sky.size(i-1)].f	
		If temp2.x = temp1.x	$C_{17} = n-1$
		IF (temp2.h < temp.h)	$C_{18} = n-1$
		Push back last element	$C_{19} = n-1$
		Push in struct temp3	$C_{20} = n-1$
		ELSE	
		Push in temp struct in sky[]	$C_{21} = n-1$
		Else	
		Push back temp3 in skyout	$C_{22} = n-1$
		Size = Size + 1	$C_{23} = n-1$
		Set prev = max	$C_{24} = n-1$
		Push in {sky[i-1], x, 0, 1}	$C_{25} = 1$

Time complexity analysis

$$\begin{aligned}
 T(n) = & C_1(n) + C_2(n-1) + C_3(n-1) + C_4(n-1) + C_5 \\
 & + (C_5 + C_6) \left[K \frac{(n-3)}{2} \right] + C_7 n + C_8 \log n (n-1) + \\
 & C_9 n(n-1) + C_{10} \frac{(n-1)^2}{2} + C_{11}(n-1) + \\
 & [C_{12} + C_{13} + C_{14} + C_{15} + C_{16} + C_{17} + C_{18} + C_{19} + C_{20} \\
 & + C_{21} + C_{22} + C_{23} + C_{24}](n-1) + C_{25}
 \end{aligned}$$

$$\begin{aligned}
 T(n) = & A(n) + B(1) + C_8(n \log n) + C_9 n^2 \\
 & + (C_5 + C_6) \left(K n / 2 \right)
 \end{aligned}$$

$$\begin{aligned}
 = & A n^2 + B n + C \rightarrow \text{for best and worst} \\
 = & \Theta(n^2) \quad \text{Case}
 \end{aligned}$$

1.2. Write a program using an incremental (conventional) approach to find the skyline.

```
#include<bits/stdc++.h>
using namespace std;
struct initial{
    int x;
    int y;
    int h;
};
struct skyline{
    int x;
    int h;
    int f; //flag if 1 then start of building if 0 then end of building
};
struct initial c[]={ //input
    {31, 41, 5},
    {4, 9, 21},
    {30, 36, 9},
    {14, 18, 11},
    {2, 12, 14},
    {34, 43, 19},
    {23, 25, 8},
    {14, 21, 16},
    {32, 37, 12},
    {7, 16, 7},
    {24, 27, 10}
};

vector<struct skyline> in;
vector<struct skyline> out;
int size=0;
void make_input(vector<struct skyline> &in);
void sort(int n);
void make_output(vector<struct skyline> &out);
int main()
{
    int i;
    make_input(in);
    sort(in.size());
    /*cout<<"\n\nBuilding coords are : "<<endl;
    for(i=0;i<in.size();i++)
    {
        cout<<"( "<<in[i].x<<" , "<<in[i].h<<" )"<<endl;
    }
    */
    make_output(out); //skyline function
}
```

```

void make_input(vector<struct skyline> &in)
{
    int i;
    cout<<"\n\nEntered input was : "<<endl;
    for(i=0;i<11;i++)
    {
        cout<<" ("<<c[i].x<<" , "<<c[i].h<<" , "<<c[i].y<<" ) "<<"\t";
    }
    struct skyline s;
    for(i=0;i<11;i++)
    {
        s.x=c[i].x;
        s.h=c[i].h;
        s.f=1;
        in.push_back(s);
        s.x=c[i].y;
        s.h=c[i].h;
        s.f=0;
        in.push_back(s);
    }
    /*cout<<"\n\nNow modified input is : "<<endl;
    for(i=0;i<in.size();i++)
    {
        cout<<" ("<<in[i].x<<" , "<<in[i].h<<" ) "<<endl;
    }*/
}

void sort(int n) //for sorting
{
    int i;
    for(int i = 0 ; i < in.size() ; i++)
    {
        bool swap = false;
        for (int j = 0 ; j < in.size()-i-1 ; j++)
        {
            if(in[j].x > in[j+1].x)
            {
                int x1, h1, f1;
                x1 = in[j].x;
                h1 = in[j].h;
                f1 = in[j].f;
                in[j].x = in[j+1].x;
                in[j].h = in[j+1].h;
                in[j].f = in[j+1].f;
                in[j+1].x = x1;
                in[j+1].h = h1;
                in[j+1].f = f1;
            }
        }
    }
}

```

```

        swap = true;
    }
}
if(!swap)
    break;
}
}
void make_output(vector<struct skyline> &out)
{
    vector<int> height; //height vector is made such that it is sorted in //descending order
    int temp,prev=0,max;
    struct skyline s1,s2,s3;
    int i,j,l;
    for(i=0;i<in.size();i++)
    {
        temp=in[i].h;
        if(in[i].f==1) //start of building
        {
            if(height.empty()==true) //no height in the vector
            {
                if(i!=0) //to append the points when a skyline starts
                {
                    s1.x=in[i-1].x;
                    s1.h=0;
                    s1.f=0; //flags not relevant
                    out.push_back(s1);
                    size++;
                }
                else
                {
                    //for first case initialise
                    x and h with 0
                    s1.x=0;
                    s1.h=0;
                    s1.f=1;
                    out.push_back(s1);
                    size++;
                }
                height.push_back(temp);
            }
            else //height vector not empty
            {
                for(j=0;j<height.size();j++)
                {
                    if(temp>=height[j])
                        break;
                }
            }
        }
    }
}

```

```

        height.push_back(0);
        for(l=height.size()-1; l>j; l--) //shifting right
        {
            height[l]=height[l-1];
        }
        height[j]=temp; //height added to vector
    }
    max=height[0]; //since its in desc order
}
else //f==0 i.e. end of building
{
    auto k=find(height.begin(),height.end(),temp);
    height.erase(k);
    max=height[0];
}
if(prev!=max)
{
    s3.x=in[i].x;
    s3.h=max;
    s3.f=1;
    if(size!=0) //size here is size of out
    {
        s2.x=out[size-1].x;
        s2.h=out[size-1].h;
        s2.f=out[size-1].f;
        if(s2.x==s3.x)
        {
            if(s2.h<s3.h)
            {
                out.pop_back(); //to remove repeated pts
                out.push_back(s3);
            }
        }
        else
        {
            out.push_back(s3);
        }
    }
    else
    {
        out.push_back(s1); //appending the original point
    }
    size++;
    prev=max; //changing previous max height
}
}


```

```

s3.x=in[i-1].x; //appending the last point
s3.h=0;
s3.f=1;
out.push_back(s3);
//displaying
cout<<"\n\nSkyline output is : "<<endl;
for(i=0;i<out.size();i++)
{
    cout<<"( "<<out[i].x<<" , "<<out[i].h<<" ) "<<endl;
}
}

```

Result;



```

Select D:\svn\sem4\daa\assgn4skyline.exe
Entered input was :
( 31 , 5 , 41 )      ( 4 , 21 , 9 ) ( 30 , 9 , 36 )      ( 14 , 11 , 18 )      ( 2 , 14 , 12 )      ( 34 , 19 , 43 )
( 23 , 8 , 25 )      ( 14 , 16 , 21 )      ( 32 , 12 , 37 )      ( 7 , 7 , 16 ) ( 24 , 10 , 27 )

Skyline output is :
( 0 , 0 )
( 2 , 14 )
( 4 , 21 )
( 9 , 14 )
( 12 , 7 )
( 14 , 16 )
( 21 , 0 )
( 23 , 8 )
( 24 , 10 )
( 27 , 0 )
( 30 , 9 )
( 32 , 12 )
( 34 , 19 )
( 43 , 0 )

-----
Process exited after 0.08736 seconds with return value 0
Press any key to continue . . .

```


1.3. Write a pseudocode to find the skyline using the divide and conquer approach. Analyze the time complexity

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Divide and Conquer Approach

There are 2 structures \rightarrow building (x, y, h) and point coordinates of (x, y)

skyline (int l, int h, vector <building> sky)

Declare vector <struct ^{points} sky> skyline

IF $l > h$

return skyline vector

ELSE IF $l = h$

Push back skyline $\{sky[l].x, sky[l].h\},$
 $\{sky[l].y, 0\}$

ELSE

Set $mid = l + [(h-l)/2]$

Set vector <struct points> sky_l = skyline(l, mid, sky)

Set vector <struct points> sky_h = skyline(mid+1, h, sky)

Return merge_sky(sky_l, sky_h)

merge_sky(vector <points> sky_l, vector <points> sky_h)

Set $l = 0, h = 0$

set vector <points> merged_sky

while $i < sky_l.size()$ & $j < sky_h.size()$

IF sky_l or sky_h is empty
break

Set temp of <struct points>

IF $sky_l[i].x < sky_h[j].x$

temp.x = sky_l[i].x

temp.y = sky_l[i].y

IF $sky_l[i].y < h - h$

```

    temp.y = h-h
    hl = sky-l[i].y
    i += 1
ELSE IF sky-l[i].x > sky-h[j].x
    temp.x = sky-h[j].x
    temp.y = sky-h[i].y
    IF sky-h[i].y < hl
        temp.y = h-l
        h-h = sky-h[i].y
        j += 1
    ELSE
        temp.x = sky-h[j].x
        temp.y = max[sky-l[j].y, sky-h[j].y]
        h-l = sky-l[j].y
        h-h = sky-h[j].y
        i += 1
        j += 1
    Push in 'temp' in merged_sky

IF i >= sky-l.size()
    While j < sky-h.size()
        push_back sky-h[j] in merged_sky
        j += 1
IF j >= sky-h.size()
    While i < sky-l.size()
        push_back sky-l[i] in merged_sky
Set inx = 1, push back 0 in redundant vector
While (inx < merged_sky.size())
    IF merged_sky[inx].y = merged_sky[inx-1].y
        redundant.pushback(1) into redundant
    ELSE
        push 0 into redundant
    inx += 1

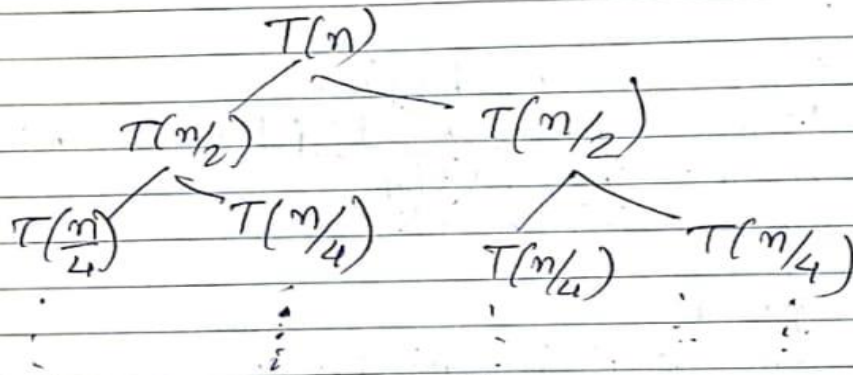
```

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```
For For i = 0 to redundant.size()
    IF redundant[i] = 1
        merged_sky[i].x = -1
return merged_sky
```

Time complexity analysis

Recursion Tree Method



$T(n)$ can be written as
$$T(n) = 2T(n/2) + \theta(n)$$

\rightarrow Merge will take $\theta(n)$

also $\theta(n) = cn$

$$T(n) = 2T(n/2) + cn$$

$$\text{and } T(n/2) = 2T(n/4) + cn/2$$

$$\text{|||ly } T(n) = 4T(n/4) + cn + cn$$
$$T(n) = 2^h T(n/2^h) + cn 2^h$$

$$2^h = n \rightarrow h = \log n$$

$$T(n) = n T(1) + cn (\log n)$$

$$T(n) = cn \log n + n + 1 = \theta(n \log n)$$

1.4. Write a program using the divide-and-conquer approach to find the skyline.

```
#include <bits/stdc++.h>
using namespace std;
struct input{
    int x;
    int y;
    int h;
};
struct sky{
    int x;
    int y;
};
vector<struct input> in{
    {31, 41, 5},
    {4, 9, 21},
    {30, 36, 9},
    {14, 18, 11},
    {2, 12, 14},
    {34, 43, 19},
    {23, 25, 8},
    {14, 21, 16},
    {32, 37, 12},
    {7, 16, 7},
    {24, 27, 10}
};

vector<struct sky> out;
vector<struct sky> mergesky(vector<sky> sky_l, vector<struct sky> sky_h);
vector<struct sky> skyline(int l, int h, vector<struct input> sky1);

int main()
{
    out=skyline(0,in.size()-1,in);
    out.insert(out.begin(),{0,0});
    int i;
    cout<<"Skyline output for Divide and Conquer method!\n";
    for(i=0;i<out.size();i++)
    {
        if(out[i].x!=-1) //we made it to remove redundant pts
        {
            cout<<" ("<<out[i].x<<" , "<<out[i].y<<" ) ";
            cout<<endl;
        }
    }
    return 0;
}
```

```

vector<struct sky> merge(vector<struct sky> sky_l,vector<struct sky> sky_h)
{
    int h_l=0, h_h=0;
    int ind=0;
    int i=0,j=0;
    vector<struct sky> merged_sky;
    while(i < sky_l.size() && j<sky_h.size())
    {
        if(sky_l.empty() || sky_h.empty())
        {
            break;
        }
        struct sky temp;
        if(sky_l[i].x < sky_h[j].x)
        {
            temp.x=sky_l[i].x;
            temp.y=sky_l[i].y;
            //if the height of selected coordinate is less than previous height of other skyline
            then update height of the coordinate of point to be inserted
            if(sky_l[i].y < h_h)
            {
                temp.y=h_h;
            }
            h_l=sky_l[i].y; //changing h_l which is previous height of sky_l vector
            i++;
        }
        else if(sky_l[i].x > sky_h[j].x) //similar with sky_h vector
        {
            temp.x=sky_h[j].x;
            temp.y=sky_h[j].y;
            if(sky_h[j].y < h_l)
            {
                temp.y=h_l;
            }
            h_h = sky_h[j].y;
            j++;
        }
        else //if both are equal then point would be the x
        coordinate of either one y would be max height
        {
            temp.x = sky_h[j].x;
            temp.y = max(sky_l[i].y,sky_h[j].y);
            h_l = sky_l[i].y;
            h_h = sky_h[j].y;
            i++;
            j++;
        }
    }
}

```

```

        }
        merged_sky.push_back(temp);
    }
    if(i>= sky_l.size()) //adding the remaining points of sky_l
    {
        while(j< sky_h.size())
        {
            merged_sky.push_back(sky_h[j]);
            j++;
        }
    }
    if(j>= sky_h.size()) //adding the remaining points of sky_h
    {
        while(i< sky_l.size())
        {
            merged_sky.push_back(sky_l[i]);
            i++;
        }
    }
    int inx = 1;
    vector<int> redundant;
    redundant.push_back(0);
    while(inx < merged_sky.size())
    {
        if(merged_sky[inx].y == merged_sky[inx-1].y)
        {
            redundant.push_back(1);
        }
        else
        {
            redundant.push_back(0);
        }
        inx++;
    }
    for(i=0;i<redundant.size();i++)
    {
        if(redundant[i]==1)
        {
            merged_sky[i].x=-1;
        }
    }
    return merged_sky;
}
vector<struct sky> skyline(int l,int h,vector<struct input> sky1)
{
    vector<struct sky> sky_line;


```



```

if(l > h)
{
    return sky_line;
}
else if(l==h)
{
    struct sky p={sky1[l].x,sky1[l].h};
    sky_line.push_back(p);
    p.x=sky1[l].y;
    p.y=0;
    sky_line.push_back(p);
    return sky_line;
}
else
{
    int mid=l+((h-l)/2);
    vector<struct sky> sky_l=skyline(l,mid,sky1);
    vector<struct sky> sky_h=skyline(mid+1,h,sky1);
    return merge(sky_l,sky_h);
}
}

```

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Skyline output for Divide and Conquer method!

```

( 0 , 0 )
( 2 , 14 )
( 4 , 21 )
( 9 , 14 )
( 12 , 7 )
( 14 , 16 )
( 21 , 0 )
( 23 , 8 )
( 24 , 10 )
( 27 , 0 )
( 30 , 9 )
( 32 , 12 )
( 34 , 19 )
( 43 , 0 )

```

Process exited after 0.1035 seconds with return value 0
Press any key to continue . . .

2. Given two matrices A and B, answer the following questions.

2.1. Write a pseudocode (using an incremental/conventional approach) to multiply the given matrices. Analyze the time complexity.

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Matrix Multiplication (Brute Force)

Set A and B matrices and take input r_1, c_1 and r_2, c_2 and follow rule $c_1 = r_2$
 Set C as result matrix

matrix-mult (A[][], B[][]) cost

for $i = 0$ to $i = r_1 - 1$ $\rightarrow C_1 n$
 | for $j = 0$ to $j = c_2 - 1$ $\rightarrow C_2 n(n-1)$
 | | for $k = 0$ to $k = c_1 - 1$ $\rightarrow C_3 n(n-1)(n-1)$
 | | | $c[i][j] += a[i][k] * b[k][j]$ $\rightarrow C_4 (n^2)(n-1)(n-1)$
 | | |
 |
 Return c

Time complexity

$$T(n) = C_1(n) + C_2(n)(n-1) + C_3(n)(n-1)(n-1) + C_4(n-1)(n-1)(n-1)$$

$$T(n) = (C_3 + C_4)n^3 + (C_2 - 2C_3 - 3C_4)n^2 + (C_3 + C_4 + 3C_4)n + C_1$$

$$= An^3 + Bn^2 + Cn + D$$

$$T(n) = \Theta(n^3)$$

2.2. Write a program using an incremental (conventional) approach to multiply the given matrices.

```
#include <bits/stdc++.h>
using namespace std;
int ** matrix_allocate(int n)
{
    int ** mat = new int *[n];
    for (int i = 0; i < n; ++i)
```



```

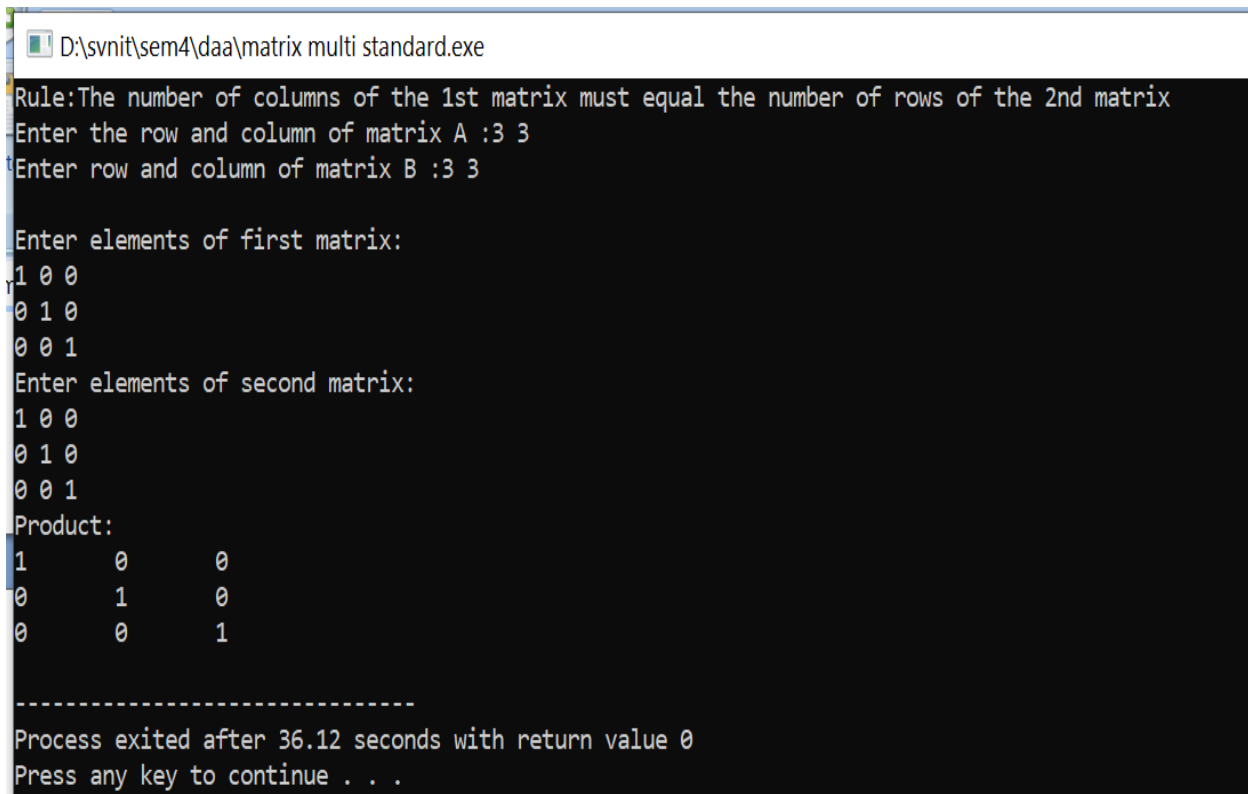
    {
        mat[i] = new int[n];
    }
    for(int i=0;i<n;i++)
    {
        for(int j=0;j<n;j++)
        {
            mat[i][j]=0;
        }
    }
    return mat;
}
int main() {
    int r1,c1,r2,c2;
    cout<<"Rule:The number of columns of the 1st matrix must equal the number of rows of
the 2nd matrix \n";
    cout<<"Enter the row and column of matrix A :";
    cin>>r1>>c1;
    cout<<"Enter row and column of matrix B :";
    cin>>r2>>c2;
    if(c1!=r2)
    {
        cout<<"Error!Refer Rule";
        return 0;}
    int n = max(r1,max(c1,max(r2,c2)));
    if(ceil(log(n))!=floor(log(n)))
    {
        n=pow(2,ceil(log2(n)));
    }
    int ** a = matrix_allocate(n);
    int ** b = matrix_allocate(n);
    int ** c = matrix_allocate(n);
    cout<<"\nEnter elements of first matrix: ";
    for (int i = 0; i < r1; i++)
    {
        for (int j = 0; j < c1; j++)
        {
            cin>>a[i][j];
        }
    }
    cout<<"Enter elements of second matrix: ";
    for (int i = 0; i < r2; i++)
    {
        for (int j = 0; j < c2; j++)
        {
            cin>>b[i][j];

```

```

    }
}
for (int i = 0; i < r1; i++)
{
    for (int j = 0; j < c2; j++)
    {
        c[i][j] = 0;
        for (int k = 0; k < c1; k++)
        {
            c[i][j] += a[i][k] * b[k][j];
        }
    }
}
cout<<"Product:\n";
for(int i=0;i<r1;i++)
{
    for(int j=0;j<c2;j++)
    {
        cout<<c[i][j]<<"\t";
    }
    cout<<"\n";
}
return 0;
}

```



```

D:\svn\sem4\daa\matrix multi standard.exe
Rule:The number of columns of the 1st matrix must equal the number of rows of the 2nd matrix
Enter the row and column of matrix A :3 3
Enter row and column of matrix B :3 3

Enter elements of first matrix:
1 0 0
0 1 0
0 0 1
Enter elements of second matrix:
1 0 0
0 1 0
0 0 1
Product:
1      0      0
0      1      0
0      0      1

-----
Process exited after 36.12 seconds with return value 0
Press any key to continue . . .

```

2.3. Write a pseudocode to multiply the given matrices using the divide and conquer approach. Analyze the time.

UI9CS076

Matrix multiplication (Divide & Conquer)
We use strassen matrix mult technique.

Matrix-mult ($A[][]$, $B[][]$, n)

Initialize matrix C

IF $n = 1$

1 $C[0][0] = a[0][0] * b[0][0]$

Set $a_{11}[][]$, $a_{12}[][]$, $a_{21}[][]$, $a_{22}[][]$ } $\Theta(1)$

1 $b_{11}[][]$, $b_{12}[][]$, $b_{21}[][]$, $b_{22}[][]$

1 of row, col size $n/2$

FOR $I = 0$ to $(N/2) - 1$

1 FOR $J = 0$ to $J = (N/2) - 1$

1 1 $a_{11}[i][j] = a[i][j]$

1 1 $a_{12}[i][j] = a[i][j + n/2]$

1 1 $a_{21}[i][j] = a[i + n/2][j]$

1 1 $a_{22}[i][j] = a[i + n/2][j + n/2]$ } $\Theta(n^2)$

1 1 $b_{11}[i][j] = b[i][j]$

1 1 $b_{12}[i][j] = b[i][j + n/2]$

1 1 $b_{21}[i][j] = b[i + n/2][j]$

1 1 $b_{22}[i][j] = b[i + n/2][j + n/2]$

Initialize $P_1[][]$, $P_2[][]$, $P_3[][]$, $P_4[][]$, $P_5[][]$,

1 $P_6[][]$, $P_7[][]$, $P_8[][]$

1 $C_{11}[][]$, $C_{12}[][]$, $C_{21}[][]$, $C_{22}[][]$

1 $P_1 = \text{Matrix-mult}(a_{11}, \text{matrix-sub}(b_{12}, b_{22}, n/2), n/2)$

1 $P_2 = \text{Matrix-mult}(\text{matrix-add}(a_{11}, a_{12}, n/2), b_{22}, n/2)$

1 $P_3 = \text{Matrix-mult}(\text{matrix-add}(a_{22}, a_{22}, n/2), b_{11}, n/2)$

1 $P_4 = \text{matrix-mult}(a_{22}, \text{matrix-sub}(b_{21}, b_{11}, n/2), n/2)$

1 $P_5 = \text{matrix-mult}(\text{matrix-add}(a_{11}, a_{22}, n/2), \text{matrix-add}(b_{11}, b_{22}, n/2), n/2)$

1 $P_6 = \text{matrix-mult}(\text{matrix-sub}(a_{12}, a_{22}, n/2), \text{matrix-add}(b_{21}, b_{22}, n/2), n/2)$

$\Theta(n^2)$

V19CS076

```

1 P7 = matrix_mult(matrix_sub(a11, a21, n/2), matrix_add(b11, b12, n/2), n/2)
11 7
1 C11 = matrix_sub(matrix_add(matrix_add(P5, P4, n/2), P6, n/2), P2, n/2)
1 C12 = matrix_add(P1, P2, n/2)
1 C21 = matrix_add(P3, P4, n/2)
1 C22 = matrix_sub(matrix_sub(matrix_add(P5, P1, n/2), P3, n/2), P7, n/2)
1
1 For i = 0 to n/2
1   For j = 0 to n/2
1     C[i][j] = C11[i][j]
1     C[i][j+n/2] = C12[i][j]
1     C[i+n/2][j] = C21[i][j]
1     C[i+n/2][j+n/2] = C22[i][j]
1 Return C

```

$\rightarrow \theta(1)$

The functions of add, subtract, join and ~~s~~ have been declared. They have complexity of $\Theta(n^2)$

$$T(n) = 7T(n/2) + \Theta(n^2)$$

By Master method

Master method
 $n^{\log_2 7} = n^{\log_2 7}$ ~~$f(n) = cn^2$~~
 $n^{\log_2 7} = n^{2.807} > f(n)$
 $T(n) = \Theta(n^{2.807})$

$$T(n) = \Theta(n^{2.807})$$

2.4. Write a program using the divide-and-conquer approach to multiply the given matrices.

```
#include <bits/stdc++.h>
using namespace std;
int **matrix_allocate(int n)
{
    int ** mat = new int *[n];
    int i,j;
    for (i = 0; i < n; ++i)
    {
        mat[i] = new int[n];
    }
    for(i=0;i<n;i++)
    {
        for(j=0;j<n;j++)
        {
            mat[i][j]=0;
        }
    }
    return mat;
}
int max(int a,int b)
{
    if(a>=b)
    {
        return a;
    }
    else
    {
        return b;
    }
}
void matrix_free(int ** m, int n)
{
    int i;
    for (i = 0; i < n; i++)
    {
        free(m[i]);
    }
    free(m);
}
int **matrix_add(int ** a, int ** b, int n)
{
    int i, j;
    int ** c = matrix_allocate(n);
    for (i = 0; i < n; i++)
```

```

        {
        for (j = 0; j < n; j++)
            {
                c[i][j] = a[i][j] + b[i][j];
            }
        }
    return c;
}
int **matrix_sub(int ** a, int ** b, int n)
{
    int i, j;
    int ** c = matrix_allocate(n);
    for (i = 0; i < n; i++)
    {
        for (j = 0; j < n; j++)
            {
                c[i][j] = a[i][j] - b[i][j];
            }
    }
    return c;
}
int **mul_strassen(int ** a, int ** b, int n)
{
    int i, j;
    int **c = matrix_allocate(n);
    if (n == 1)
    {
        c[0][0] = a[0][0] * b[0][0];
    }
    else
    {
        int ** a11 = matrix_allocate(n / 2);
        int ** a12 = matrix_allocate(n / 2);
        int ** a21 = matrix_allocate(n / 2);
        int ** a22 = matrix_allocate(n / 2);
        int ** b11 = matrix_allocate(n / 2);
        int ** b12 = matrix_allocate(n / 2);
        int ** b21 = matrix_allocate(n / 2);
        int ** b22 = matrix_allocate(n / 2);
        for (i = 0; i < n / 2; i++)
        {
            for (j = 0; j < n / 2; j++)
            {
                a11[i][j] = a[i][j];
                a12[i][j] = a[i][j + n / 2];
                a21[i][j] = a[i + n / 2][j];

```

```

        a22[i][j] = a[i + n / 2][j + n / 2];
        b11[i][j] = b[i][j];
        b12[i][j] = b[i][j + n / 2];
        b21[i][j] = b[i + n / 2][j];
        b22[i][j] = b[i + n / 2][j + n / 2];
    }
}
int** P1 = mul_strassen(a11, matrix_sub(b12, b22, n/2), n/2);
int** P2 = mul_strassen(matrix_add(a11, a12, n/2), b22, n/2);
int** P3 = mul_strassen(matrix_add(a21, a22, n/2), b11, n/2);
int** P4 = mul_strassen(a22, matrix_sub(b21, b11, n/2), n/2);
int** P5 = mul_strassen(matrix_add(a11, a22, n/2), matrix_add(b11, b22, n/2), n/2);
int** P6 = mul_strassen(matrix_sub(a12, a22, n/2), matrix_add(b21, b22, n/2), n/2);
int** P7 = mul_strassen(matrix_sub(a11, a21, n/2), matrix_add(b11, b12, n/2), n/2);

int** c11 = matrix_sub(matrix_add(matrix_add(P5, P4, n/2), P6, n/2), P2, n/2);
int** c12 = matrix_add(P1, P2, n/2);
int** c21 = matrix_add(P3, P4, n/2);
int** c22 = matrix_sub(matrix_sub(matrix_add(P5, P1, n/2), P3, n/2), P7, n/2);

for (i = 0; i < n / 2; i++)
{
    for (j = 0; j < n / 2; j++)
    {
        c[i][j] = c11[i][j];
        c[i][j + n / 2] = c12[i][j];
        c[i + n / 2][j] = c21[i][j];
        c[i + n / 2][j + n / 2] = c22[i][j];
    }
}
matrix_free(c11, n / 2);
matrix_free(c12, n / 2);
matrix_free(c21, n / 2);
matrix_free(c22, n / 2);
}
return c;
}
int main()
{
    int i, j;
    int r1, c1, r2, c2;
    cout<<"Rule:The number of columns of the 1st matrix must equal the number of rows of the 2nd matrix \n";
    cout<<"Enter row and column of matrix A :";
    cin>>r1>>c1;
    cout<<"Enter row and column of matrix B :";

```

```

cin>>r2>>c2;
if(c1!=r2)
{
    cout<<"Error!Refer Rule";
    return 0;
}
int n=max(r1,max(c1,max(r2,c2)));
if(ceil(log(n))!=floor(log(n)))
{
    n=pow(2,ceil(log2(n)));
}
int ** a = matrix_allocate(n);
int ** b = matrix_allocate(n);
cout<<"\nEnter elements of first matrix: ";
for (i = 0; i < r1; i++)
{
    for (j = 0; j < c1; j++)
    {
        cin>>a[i][j];
    }
}
printf("Enter elements of second matrix: ");
for (i = 0; i < r2; i++)
{
    for (j = 0; j < c2; j++)
    {
        cin>>b[i][j];
    }
}
int **c=mul_strassen(a, b, n);
cout<<"Product:\n";
for(i=0;i<r1;i++)
{
    for(j=0;j<c2;j++)
    {
        cout<<c[i][j]<<"\t";
    }
    cout<<"\n";
}
return 0;
}

```


D:\svn\sem4\daa\matrix mul d&C.exe

Rule: The number of columns of the 1st matrix must equal the number of rows of the 2nd matrix

Enter row and column of matrix A : 3 2

Enter row and column of matrix B : 2 3

Enter elements of first matrix:

3 2

3 1

1 2

Enter elements of second matrix:

1 2 3

2 1 3

Product:

7	8	15
---	---	----

5	7	12
---	---	----

5	4	9
---	---	---

Process exited after 20.13 seconds with return value 0

Press any key to continue . . .