



```
92. What should be time complexity of:
         for (inti=1 to u)
             i=i*2; \rightarrow o(1)
for i => 1, 2, 4, 6, 8 .... n times
       ie Muies is a GP
   50 a=1, u=2/1
    Kth value of GIP:
            th = ank-1
            t_h = 1(2)^{k-1}
             2n=2^k
          lag_2(2n) = k lag_2
           lag 2 + lag n = le
           leg 2 n+1 = le (Neglecting 61?)
  So, Time Complexity T(n) > 0 (lag, n) - Ans.
```

13. T(n) = [3T(n-1) if n > 0 otherwise 14) ie $T(n) \Rightarrow 3T(n-1) - (1)$ $T(n) \Rightarrow 1$ put $n \Rightarrow n-1$ in (1) $T(n-1) \Rightarrow 3T(n-2) - (2)$ put (2) in (1) $T(n) \Rightarrow 3 \times 3T(n-2)$ $T(n) \Rightarrow 9T(n-2) \rightarrow (3)$ put $n \Rightarrow n-2$ in (1) T(n-2) = 3T(n-3)put in (3). $T(n) = 27T(n-3) \rightarrow 4$

Generalising series,

$$T(h) = 3^{k} T(n-k) - (5)$$

for leth terms, Let $n-k=1$ (Base Case)

$$h = n-1$$
put in (5)

$$T(n) = 3^{n-1} T(1)$$

$$T(n) = 3^{n-1} \qquad (neglecting 3')$$

$$T(n) = 0 (3^{n})$$

8th.
$$T(n) = \begin{cases} 2T(n-1)-1 & \text{if } n > 0, \\ 0+kn \text{ with } 1 \end{cases}$$

$$T(n) = 2T(n-1)-1 \rightarrow (1)$$

put $n = n-1$

$$T(n-1) = 2T(n-2)-1 \rightarrow (2)$$

put $im(1)$

$$T(n) = 2 \times (2T(n-2)-1)-1$$

$$= 4T(n-2)-2-1 - (3)$$

put $n = n-2$ in (1)

$$T(n-2) = 2T(n-3)-1$$

Put $im(1)$

$$T(n) = 8T(n-3)-4-2-1 - (4)$$

Generalizing series

$$T(n) = 2^{k} T(n-k) - 2^{k-1} - 2^{k-2} \dots 2^{n}$$

$$k^{+k} \text{ true}$$

Let $n-k=1$

$$k=n-1$$

$$T(n) = 2^{k-1} T(1) - 2^{k} \left(\frac{1}{2} + \frac{1}{2^{2}} + \dots + \frac{1}{2^{k}}\right)$$
 $2 \cdot 2^{k-1} - 2^{k-1} \left(\frac{1}{2} + \frac{1}{2^{2}} + \dots + \frac{1}{2^{k}}\right)$

in Suius in GP.

a=1/2 , n=1/2.

So,

$$T(n) = 2^{n-1} \left(1 - (1/2)^{n-1}\right)$$

 $= 2^{n-1} \left(1 - 1 + (1/2)^{n-1}\right)$
 $= 2^{n-1} \left(1 - 1 + (1/2)^{n-1}\right)$
 $= \frac{2^{n-1}}{2^{n-1}}$
 $= T(n) = O(1)$ Ans

Alde
$$5 = 1 + 3 + 6 + 10 + ... T_{n-1} + T_n \rightarrow 2$$

 $0 = 1 + 2 + 3 + 4 + ... n - T_n$
 $T_k = 1 + 2 + 3 + 4 + ... + k$
 $T_k = \frac{1}{2}k(k+1)$
for k intentions

$$\frac{K(K+1)}{2} < = W$$

1+2+3+ ... k <= n

$$\frac{k^2+K}{2} < = n$$

```
94. Time (amplexity of

Vaid f (int n)

int i, count = 0;

far (i = 61; i ≠ i (= n; ++i))

3

L. As i² = n

i = In

i = 1, 2, 3, 4, ... In

x = 1+2+3+4+...+In

T(n) ≥ In + (In +1)

T(n) = n ≠ In

T(n) = 0(n) → Ans.

85. Time Complexity of
```

97 Time Complexity of

void f (int n)

int i, j, h, count = 0;

for (int i = n/2; i <= n; ++1?)

for (j=1; j <= n; j=j*2)

for (h=1; h <= n; h= h+2)

count ++;

Le since, for h=h²

k=1,2,4,8,... h

Series is in GP

×10, a=1, n=2

$$\frac{A(h^{n}-1)}{h-1}$$

$$= \frac{1(2^{k}-1)}{1}$$

$$h = 2^{k}-1$$

$$h+1=2^{k}$$

$$\log_{2}(n)=k$$

```
& Time Complexity of
          void function ( int n)
              of (n==1) return;
              for (i=1 ton) {
             for (j=1 to n) {
             prints (" *"),
          function (n-3);
  4 fu (i= 1 to n)
       me get jen times energ turn
            ... i* j = n2
          Now, T(n) = n^2 + T(n-3);
               T(n-3) = (n23)2 + T(n-6);
               T(n-6) = (n 0) 2 + T(n-9);
              and T(1)=1;
       Now, substitute each value in T(n)
         T(u) = n^2 + (n-3)^2 + (n-6)^2 + \dots + 1
               h = (n-1)/3 total terms = k+1
    T(n) = n^2 + (n-3)^2 + (n-6)^2 + \dots +
     T(n) = ~ 4 n2
      T(n) ~ (k-1)/3 + n2
      50, T(n) 20(n3) - Ans
```

```
9. Time Complexity of :-
     vaid function ( int n)
        for (intil=1 to n) f
         for (intj=1; j <= n; j=j+i) [
            printif (" * "),
                j=1+2+... (n>,j+i)
     i = 1
- for
                j=1+3+5... (n) j+i)
               j=1+4+7... (n)j+i)
      nt term of AP is
         T(n)= a + d * m
```

T(m) = 1 + d xm

(n-1)/d=n for i=1 (n-1)/1 times i=2 (n-1)/2 times

T(n) 2 lijs + lijz+... ln-1/n-1 $2(n-1) + (n-2) + (n-3) + \cdots +$ 2 n+n/2 + n/3 + .. n/n-1 - nx1 2 n [1+1/2+1/3+·· 1/n-1]- N+1 z nx lagn - n+1 Since IX = lag x

T(n) = O(nlagn) - Ans.

```
For the Function n-1 R & Cm. what is the asymptotic Relationship b/ro these functions?

Assume that h>=1 EJ C>1 are constants. Find out the value of C d no. of which relationship holds.

If Asymmen nh and cm.

Relationship b/w nh & Cm is

nh = 0 (cm)

nh < a c c n)

t n > no h constant, a > 0

for no=1; C=2

$\Rightarrow$ 1k < a^2
```

 $H_0 = 1 & C = 2 \rightarrow \text{Ans}$