MATH 425 8/31/2022 Example: Suppose I flipa fair coin 4 times. What is the probability that the number of times I come up is even? Solution: Il possihilitées

each of the out comes has probability 16 (equal by symmetry) 12, 13, 14, 23, 24, 34

4 $\pm i mos$ Answer: $\frac{1}{16} \pm \frac{6}{16} \pm \frac{1}{16} = \frac{8}{16} = \frac{1}{2}$

Holow, up: Work is the probability
that in 4 flips, It come up an even
It of times and I come up an odd
number of times?

Counting motheds i'm probability theory Basio country principle: Country ordered n-tuples (s,, s,, --- sm) where s. e S. (Si, -.. Sm) are soti. Suppose the ket Si has N. elements: |Si| = Nr.

= TV,-.. The set of all med n-typles is denoted by $S_1 \times S_2 \times \cdots \times S_m = \prod S_n$ Cantesvar product). René Descartes

Examples: Suppose I cast a standard due and other flop a win 2 times. What is other public det the number that comes up on the dec place the number of times H come up on the coin is 4? Solution: Sample pace

S= 21,...,6} × 2H,T y × 2H,T y orthones

$$E=\{(4, T, T), (3, H, T), (3, T, H), (2, M, H)\}$$

$$|E|=4 \qquad P(E|=\frac{|E|}{|S|}=\frac{4}{|S|}=\frac{|I|}{|S|}$$

Permutations

Example; How way times con ve avange 3 différent books on a book shelf? Moly Drch M Ross: Roh. R Calculus 3 Solutor: Poch om hook and put il on the

to it on the ught: 2 choices les book only divice By have countries promorph, # of chares MCR

RMC RCM CMR CRM

Avanging n different hooks on a holf: M·(n-1). (n-4. ... 2. | =: n! (n feboral) choice These choices are called permutations. arranging the numbers (1,2,...n) in a vow (to ony reder) Example: Suppose in a lotter, I am askad to a wange the number 1,2,3,4,5 in an order and I win if the order modeler an order chosen at the draw. What are the chances of winning? Solution: Sample speces: permutation of 21,2,3,4,5) Equally likely out comes. Closure of winnings

Example: Suppose a study plan ce purices pudang 4 jarticular hooke en matte, 3 in physics and 2 in chamity. Sapposer I buy all of steen at once and. arrange them of the Molf so each keyest rosetter. Fyfor a student in woon next to mine also did the same they

independants. What u the polariebt that we will have the some arrangement? Solution. First choose Hes order of ruly peets: 3! Then choose order of books within each subject: 4!.3!.2!

151 = 3!.41.31.2!

$$3! = 6$$
 $4! = 24$
 $6.24.6.2$
 72
 24
 1728
 1728
 1728
 1728
 1728

Example: How may different "words"

(including nonvaried ones) can we make
using all the letters of the word PEPPER? Solution: 6! « overcounts 1 swapping the same letters Answer: 6! = 1-2:3.4.5.6 = 60]

(including nonsemical ones) (an I much using all the letters of the word REFEREE? 4) Suppose I cash a Hundard die and flip a fait coin three times.
What is the probability that the number of times I come up a equal to the number that comes up on the dee!