Assignment 5

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You may work in pairs or individually for this assignment. Make sure you join a group in Canvas if you are working in pairs. Turn in this assignment as an HTML or PDF file to ELMS. Make sure to include the R Markdown or Quarto file that was used to generate it. Include the GitHub link for the repository containing these files.

Github Link

- https://github.com/krliu67/Assignment_SURV727/tree/main/a5

```r
library(censusapi)
library(tidyverse)
library(magrittr)
library(factoextra)
library(dplyr)
library(stringr)
library(ggplot2)
library(MASS)
```

Exploring ACS Data

In this notebook, we use the Census API to gather data from the American Community Survey (ACS). This requires an access key, which can be obtained here:

- https://api.census.gov/data/key_signup.html

```r
cs_key <- read.table("cs_key.txt")[1,1]
```

```r
acs_il_c <- getCensus(name = "acs/acs5",
                    vintage = 2016,
                    vars = c("NAME", "B01003_001E", "B19013_001E", "B19301_001E"),
                    region = "county:*",
                    regionin = "state:17",
                    key = cs_key) %>%
            rename(pop = B01003_001E,
                   hh_income = B19013_001E,
                   income = B19301_001E)
head(acs_il_c)
```

```
##    state county                    NAME     pop hh_income income
## 1     17    067   Hancock County, Illinois  18633    50077  25647
## 2     17    063    Grundy County, Illinois  50338    67162  30232
## 3     17    091  Kankakee County, Illinois 111493    54697  25111
## 4     17    043    DuPage County, Illinois 930514    81521  40547
## 5     17    003 Alexander County, Illinois   7051    29071  16067
## 6     17    129    Menard County, Illinois  12576    60420  31323
```

Pull map data for California into a data frame.

```
il_map <- map_data("county", region = "illinois")
head(il_map)
```

```
##          long      lat group order   region subregion
## 1 -91.49563 40.21018     1     1 illinois     adams
## 2 -90.91121 40.19299     1     2 illinois     adams
## 3 -90.91121 40.19299     1     3 illinois     adams
## 4 -90.91121 40.10704     1     4 illinois     adams
## 5 -90.91121 39.83775     1     5 illinois     adams
## 6 -90.91694 39.75754     1     6 illinois     adams
```

Join the ACS data with the map data. Not that `il_map` has a column `subregion` which includes county names. We need a corresponding variable in the ACS data to join both data sets. This needs some transformations, among which the function `tolower()` might be useful. Call the joined data `acs_map`.

```
# Clean data in acs_il_c
acs_il_c %<>%
  separate(NAME, c("location","state_name"), sep = ",")

for (i in 1:dim(acs_il_c)[1]) {
  acs_il_c$location[i] <- gsub(" County","",acs_il_c$location[i])
  acs_il_c$location[i] <- tolower(acs_il_c$location[i])
}
# Join the ACS data with the map data.
acs_il_map <- inner_join(acs_il_c,il_map,by = join_by(location == subregion))
```

After you do this, plot a map of Illinois with Counties colored by per capita income.

```
ggplot(acs_il_map) + geom_polygon(aes(x = long, y = lat, group = group, fill = income))
```
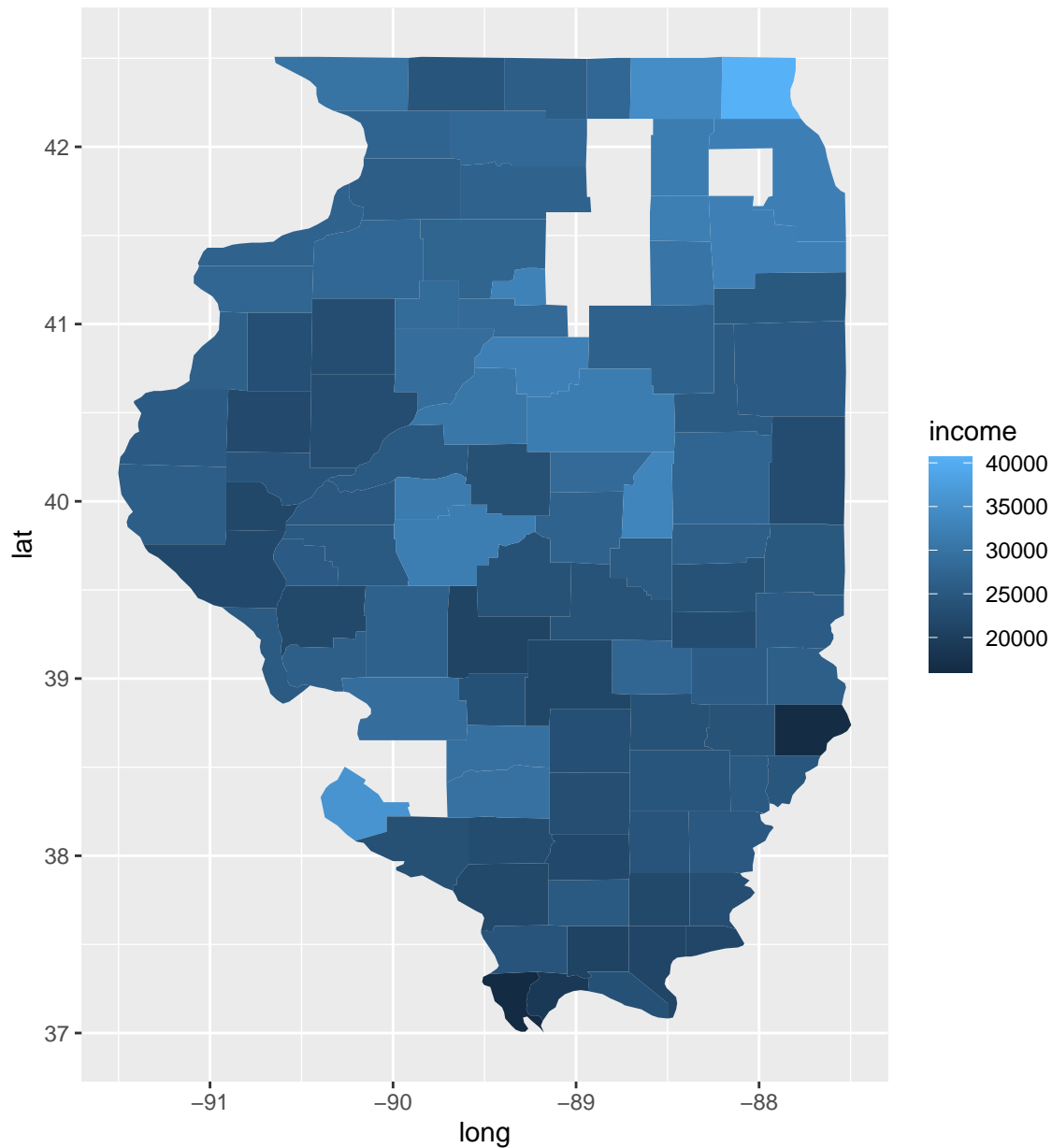
Hierarchical Clustering

We want to find clusters of counties that are similar in their population, average household income and per capita income.

First, clean the data so that you have the appropriate variables to use for clustering.

```
cleaned_acs_il_c <- acs_il_c %>% dplyr::select(location, pop, hh_income, income) %>% na.omit()
```

Next, create the distance matrix of the cleaned data. This distance matrix can be used to cluster counties, e.g. using the ward method.

```
# Create the distance matrix
dist_mtx_acs_il_c <- dist(cleaned_acs_il_c[, -1])  # excluding the county identifier
# Perform hierarchical clustering
hc_c <- hclust(dist_mtx_acs_il_c, method = "ward.D2")
```

Plot the dendrogram to find a reasonable number of clusters. Draw boxes around the clusters of your cluster solution.

```
# Plot the dendrogram
plot(hc_c)
```

Cluster Dendrogram

dist_mtx_acs_il_c
hclust (*, "ward.D2")
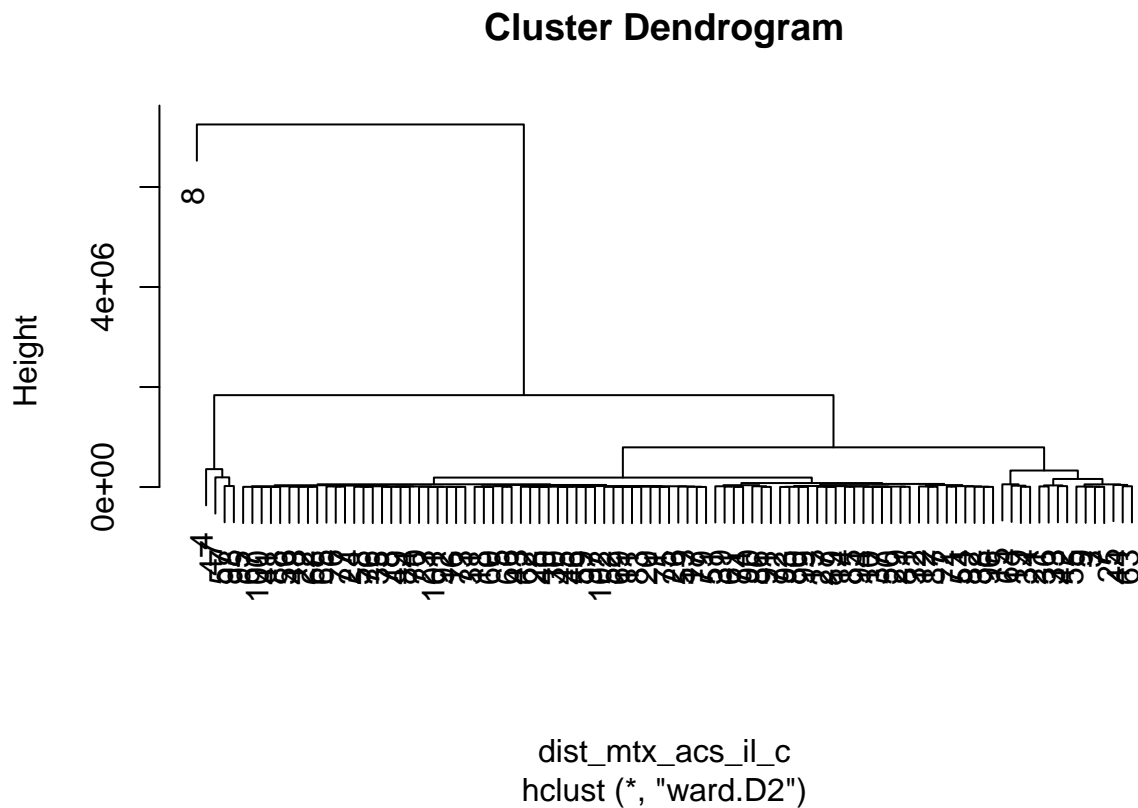
```
  #+ rect.hclust(hc_c,k = 3)  # Here 'k' is the number of clusters you choose
# Cut the dendrogram to form clusters
clusters <- cutree(hc_c, k = 5)
# Merge the cluster memberships with the original data
cleaned_acs_il_c$cluster <- clusters
```

Visualize the county clusters on a map. For this task, create a new `acs_map` object that now also includes cluster membership as a new column. This column should be called `cluster`.

```
acs_map <- inner_join(cleaned_acs_il_c,il_map,by = join_by(location == subregion))
ggplot(acs_map) + geom_polygon(aes(x = long, y = lat, group = group, fill = factor(cluster))) + theme_m
```
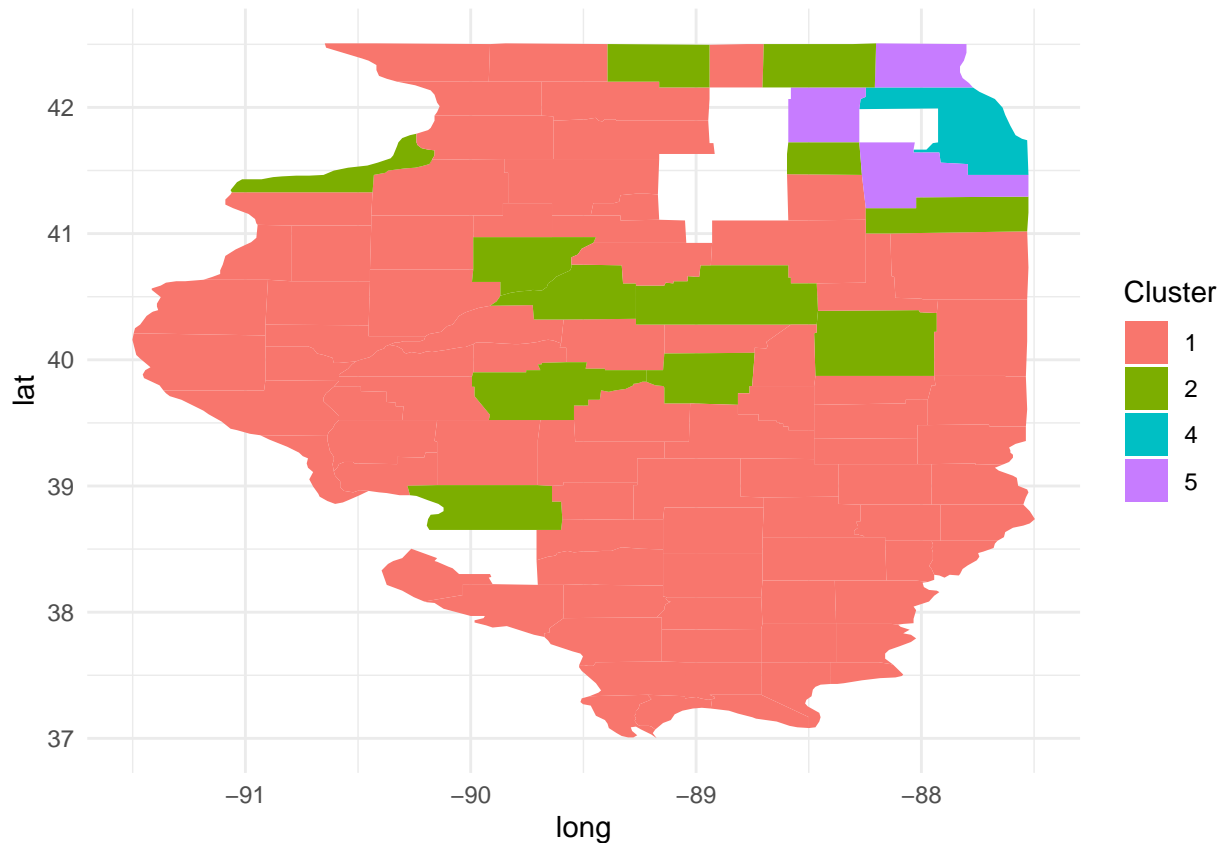
Census Tracts

For the next section we need ACS data on a census tract level. We use the same variables as before.

```r
acs_il_t <- getCensus(name = "acs/acs5",
                      vintage = 2016,
                      vars = c("NAME", "B01003_001E", "B19013_001E", "B19301_001E"),
                      region = "tract:*",
                      regionin = "state:17",
                      key = cs_key) %>% rename(pop = B01003_001E,
                    hh_income = B19013_001E,
                    income = B19301_001E)
acs_il_t[acs_il_t == -666666666] <- NA
head(acs_il_t)
```

```
##   state county  tract                                          NAME  pop
## 1    17    031 806002 Census Tract 8060.02, Cook County, Illinois 7304
## 2    17    031 806003 Census Tract 8060.03, Cook County, Illinois 7577
## 3    17    031 806400    Census Tract 8064, Cook County, Illinois 2684
## 4    17    031 806501 Census Tract 8065.01, Cook County, Illinois 2590
## 5    17    031 750600    Census Tract 7506, Cook County, Illinois 3594
## 6    17    031 310200    Census Tract 3102, Cook County, Illinois 1521
##   hh_income income
## 1     56975  23750
```

```
## 2        53769   25016
## 3        62750   30154
## 4        53583   20282
## 5        40125   18347
## 6        63250   31403
```

```r
# Clean NAME in acs_il_t
acs_il_t %<>%
  separate(NAME, c("ct","location","state_name"), sep = ",")
for (i in 1:dim(acs_il_t)[1]) {
  acs_il_t$location[i] <- gsub(" County","",acs_il_t$location[i])
  acs_il_t$location[i] <- tolower(acs_il_t$location[i])
}
acs_il_t$ct <- trimws(acs_il_t$ct)
acs_il_t$location <- trimws(acs_il_t$location)
acs_il_t$state_name <- trimws(acs_il_t$state_name)
```

k-Means

As before, clean our data for clustering census tracts based on population, average household income and per capita income.

```r
cleaned_acs_il_t <- acs_il_t %>%
  dplyr::select(location, pop, hh_income, income) %>%
  na.omit()
```

Since we want to use K Means in this section, we start by determining the optimal number of K that results in Clusters with low within but high between variation. Plot within cluster sums of squares for a range of K (e.g. up to 20).

```r
# Compute WCSS for a range of K values
set.seed(123)  # Set seed for reproducibility
wcss <- map_dbl(1:20, function(k) {
  kmeans(cleaned_acs_il_t[,-1], centers = k, nstart = 20)$tot.withinss
})

# Create a dataframe for plotting
elbow_data <- tibble(k = 1:20, wcss = wcss)

# Plot the elbow plot
ggplot(elbow_data, aes(x = k, y = wcss)) +
  geom_line() +
  geom_point() +
  scale_x_continuous(breaks = 1:20) +
  labs(x = "Number of clusters (K)", y = "Within-cluster sum of squares (WCSS)",
       title = "Elbow Method for Optimal K") +
  theme_minimal()
```

Elbow Method for Optimal K
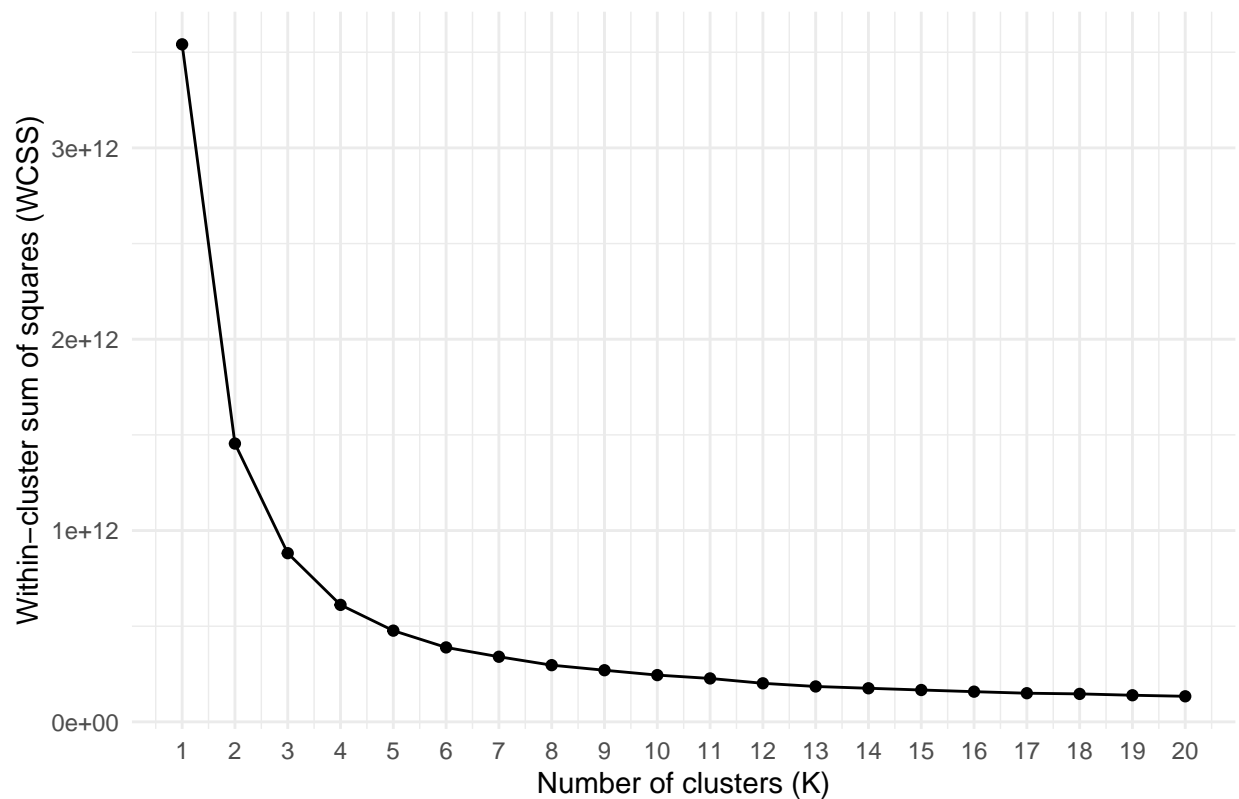
Run `kmeans()` for the optimal number of clusters based on the plot above.

Find the mean population, household income and per capita income grouped by clusters. In addition, display the most frequent county that can be observed within each cluster.

```r
k <- 3
# Create the distance matrix
dist_mtx_acs_il_t <- dist(cleaned_acs_il_t[, -1])   # excluding the county identifier
# Perform hierarchical clustering
hc_t <- hclust(dist_mtx_acs_il_t, method = "ward.D2")
# Cut the dendrogram to form clusters
clusters <- cutree(hc_t, k = k)
# Merge the cluster memberships with the original data
cleaned_acs_il_t$cluster <- clusters
```

```r
cleaned_acs_il_t %>% group_by(cluster) %>% summarise(m_pop = mean(pop),m_hh=mean(hh_income),m_inc=mean(
```

```
## # A tibble: 3 x 4
##   cluster m_pop    m_hh  m_inc
##     <int> <dbl>   <dbl>  <dbl>
## 1       1 3810.  45051. 22649.
## 2       2 4482. 117231. 59573.
## 3       3 4958.  77859. 38121.
```

```
cleaned_acs_il_t %>% group_by(cluster) %>% count(location) %>% top_n(1, wt = n)
```

```
## # A tibble: 3 x 3
## # Groups:   cluster [3]
##   cluster location     n
##     <int> <chr>    <int>
## 1       1 cook       864
## 2       2 cook       193
## 3       3 cook       255
```

```
# top_n Select top (or bottom) n rows (by value)
```

As you might have seen earlier, it's not always clear which number of clusters is the optimal choice. To automate K Means clustering, program a function based on `kmeans()` that takes K as an argument. You can fix the other arguments, e.g. such that a specific dataset is always used when calling the function.

```
optimize_kmeans <- function(k){
  scaled_data <- scale(cleaned_acs_il_t[, 2:4])
  set.seed(123)  # Set seed for reproducibility
  kmeans_result <- kmeans(scaled_data, centers = k, nstart = 20)$tot.withinss
  cluster_var_name <- paste("cluster_k", k, sep = "")
  cleaned_acs_il_t[[cluster_var_name]] <- kmeans_result
  return(cleaned_acs_il_t)
}

cleaned_acs_il_t <- optimize_kmeans(2)
```

We want to utilize this function to iterate over multiple Ks (e.g., K = 2, …, 10) and -- each time -- add the resulting cluster membership as a new variable to our (cleaned) original data frame (`acs_il_t`). There are multiple solutions for this task, e.g. think about the `apply` family or `for` loops.

```
k_values <- 2:10  # range of K

for (k in k_values) {
  cleaned_acs_il_t <- optimize_kmeans(k)
}
```

Finally, display the first rows of the updated data set (with multiple cluster columns).

```
head(cleaned_acs_il_t,1)
```

```
##   location  pop hh_income income cluster cluster_k2 cluster_k3 cluster_k4
## 1     cook 7304     56975  23750       1   5604.163   4151.776   3384.043
##   cluster_k5 cluster_k6 cluster_k7 cluster_k8 cluster_k9 cluster_k10
## 1   2857.685   2470.315   2164.351   1961.135   1798.685    1658.639
```