sproof.sty: Structural Markup for Proofs*

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Abstract

The sproof package is part of the STEX collection, a version of TEX/IATEX that allows to markup TEX/IATEX documents semantically without leaving the document format, essentially turning TEX/IATEX into a document format for mathematical knowledge management (MKM).

This package supplies macros and environment that allow to annotate the structure of mathematical proofs in STEX files. This structure can be used by MKM systems for added-value services, either directly from the STEX sources, or after translation.

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1 Introduction

The sproof (semantic proofs) package supplies macros and environment that allow to annotate the structure of mathematical proofs in STEX files. This structure can be used by MKM systems for added-value services, either directly from the STEX sources, or after translation. Even though it is part of the STEX collection, it can be used independently, like it's sister package statements.

STEX is a version of TEX/LATEX that allows to markup TEX/LATEX documents semantically without leaving the document format, essentially turning TEX/LATEX into a document format for mathematical knowledge management (MKM).

```
\begin{sproof}[id=simple-proof,for=sum-over-odds]
              We prove that \sum_{i=1}^n{2i-1}=n^{2} by induction over n
           \begin{spfcases}{For the induction we have to consider the following cases:}
              \begin{spfcase}{$n=1$}
                \begin{spfstep}[display=flow] then we compute $1=1^2$\end{spfstep}
             \end{spfcase}
             \begin{array}{ll} \begin{array}{ll} & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ 
                      \begin{sproofcomment}[display=flow]
                          This case is not really necessary, but we do it for the
                          fun of it (and to get more intuition).
                     \end{sproofcomment}
                     \begin{spfstep}[display=flow] We compute $1+3=2^{2}=4$.\end{spfstep}
             \end{spfcase}
             \begin{spfcase}{$n>1$}
                     \begin{spfstep}[type=assumption,id=ind-hyp]
                          Now, we assume that the assertion is true for a certain $k\geq 1$,
                          i.e. \sum_{i=1}^k{(2i-1)}=k^{2}.
\end{spfstep}
                     \begin{sproofcomment}
                          We have to show that we can derive the assertion for $n=k+1$ from
                          this assumption, i.e. \sum_{i=1}^{k+1}{(2i-1)}=(k+1)^{2}.
                     \end{sproofcomment}
                     \begin{spfstep}
                          We obtain \sum_{i=1}^{k+1}{2i-1}=\sum_{i=1}^{k}{2i-1}+2(k+1)-1
                          \begin{justification}[method=arith:split-sum]
                          by splitting the sum. \end{justification}
                     \end{spfstep}
                     \begin{spfstep}
                          Thus we have \sum_{i=1}^{k+1}{(2i-1)}=k^2+2k+1
                          \begin{justification} [method=fertilize] by inductive hypothesis.\end{justification}
                     \end{spfstep}
                     \begin{spfstep}[type=conclusion]
                          We can \begin{justification}[method=simplify]simplify\end{justification}
                          the right-hand side to ${k+1}^2$, which proves the assertion.
                     \end{spfstep}
             \end{spfcase}
                \begin{spfstep}[type=conclusion]
                    We have considered all the cases, so we have proven the assertion.
                \end{spfstep}
          \end{spfcases}
      \end{sproof}
```

Example 1: A very explicit proof, marked up semantically

We will go over the general intuition by way of our running example (see Figure 1 for the source and Figure 2 for the formatted result).¹

EdNote:1

¹EDNOTE: talk a bit more about proofs and their structure,... maybe copy from OMDoc spec.

2 The User Interface

2.1 Package Options

showmeta

The sproof package takes a single option: showmeta. If this is set, then the metadata keys are shown (see [Koh10a] for details and customization options).

2.2 Proofs and Proof steps

sproof

The proof environment is the main container for proofs. It takes an optional KeyVal argument that allows to specify the id (identifier) and for (for which assertion is this a proof) keys. The regular argument of the proof environment contains an introductory comment, that may be used to announce the proof style. The proof environment contains a sequence of \step, proofcomment, and pfcases environments that are used to markup the proof steps. The proof environment has a variant Proof, which does not use the proof end marker. This is convenient, if a proof ends in a case distinction, which brings it's own proof end marker with it. The Proof environment is a variant of proof that does not mark the end of a proof with a little box; presumably, since one of the subproofs already has one and then a box supplied by the outer proof would generate an otherwise empty line. The \spfidea macro allows to give a one-paragraph description of the proof

sProof

\spfidea

spfsketch

For one-line proof sketches, we use the \spfsketch macro, which takes the KeyVal argument as sproof and another one: a natural language text that sketches the proof.

spfstep

Regular proof steps are marked up with the step environment, which takes an optional KeyVal argument for annotations. A proof step usually contains a local assertion (the text of the step) together with some kind of evidence that this can be derived from already established assertions.

Note that both \premise and \justarg can be used with an empty second argument to mark up premises and arguments that are not explicitly mentioned in the text.

2.3 Justifications

justification

This evidence is marked up with the justification environment in the sproof package. This environment totally invisible to the formatted result; it wraps the text in the proof step that corresponds to the evidence. The environment takes an optional KeyVal argument, which can have the method key, whose value is the name of a proof method (this will only need to mean something to the application that consumes the semantic annotations). Furthermore, the justification can contain "premises" (specifications to assertions that were used justify the step) and "arguments" (other information taken into account by the proof method).

\premise

The \premise macro allows to mark up part of the text as reference to an assertion that is used in the argumentation. In the example in Figure 1 we have used the \premise macro to identify the inductive hypothesis.

Proof: We prove that $\sum_{i=1}^{n} 2i - 1 = n^2$ by induction over n

P.1 For the induction we have to consider the following cases:

P.1.1 n = 1: then we compute $1 = 1^2$

P.1.2 n=2: This case is not really necessary, but we do it for the fun of it (and to get more intuition). We compute $1+3=2^2=4$

P.1.3 n > 1:

P.1.3.1 Now, we assume that the assertion is true for a certain $k \geq 1$, i.e. $\sum_{i=1}^{k} (2i-1) = k^2$.

P.1.3.2 We have to show that we can derive the assertion for n = k+1 from this assumption, i.e. $\sum_{i=1}^{k+1} (2i-1) = (k+1)^2$.

P.1.3.3 We obtain $\sum_{i=1}^{k+1} (2i-1) = \sum_{i=1}^{k} (2i-1) + 2(k+1) - 1$ by splitting the sum

P.1.3.4 Thus we have $\sum_{i=1}^{k+1} (2i-1) = k^2 + 2k + 1$ by inductive hypothesis.

P.1.3.5 We can simplify the right-hand side to $(k+1)^2$, which proves the assertion.

P.1.4 We have considered all the cases, so we have proven the assertion. \Box

Example 2: The formatted result of the proof in Figure 1

\justarg

The \justarg macro is very similar to \premise with the difference that it is used to mark up arguments to the proof method. Therefore the content of the first argument is interpreted as a mathematical object rather than as an identifier as in the case of \premise. In our example, we specified that the simplification should take place on the right hand side of the equation. Other examples include proof methods that instantiate. Here we would indicate the substituted object in a \justarg macro.

2.4 Proof Structure

spfcases

The pfcases environment is used to mark up a proof by cases. This environment takes an optional KeyVal argument for semantic annotations and a second argument that allows to specify an introductory comment (just like in the proof environment).

spfcase

The content of a pfcases environment are a sequence of case proofs marked up in the pfcase environment, which takes an optional KeyVal argument for semantic annotations. The second argument is used to specify the the description of the case under consideration. The content of a pfcase environment is the same as that of a proof, i.e. steps, proofcomments, and pfcases environments.

sproofcomment

The proofcomment environment is much like a step, only that it does not have an object-level assertion of its own. Rather than asserting some fact that is relevant for the proof, it is used to explain where the proof is going, what we are attempting to to, or what we have achieved so far. As such, it cannot be the target of a \premise.

2.5 Proof End Markers

Traditionally, the end of a mathematical proof is marked with a little box at the end of the last line of the proof (if there is space and on the end of the next line if there isn't), like so:

\sproofend

\sProofEndSymbol

The sproof package provides the \sproofend macro for this. If a different symbol for the proof end is to be used (e.g. q.e.d), then this can be obtained by specifying it using the \sProofEndSymbol configuration macro (e.g. by specifying \sProofEndSymbol{q.e.d}).

Some of the proof structuring macros above will insert proof end symbols for sub-proofs, in most cases, this is desirable to make the proof structure explicit, but sometimes this wastes space (especially, if a proof ends in a case analysis which will supply its own proof end marker). To suppress it locally, just set proofend={} in them or use use \sProofEndSymbol{}.

2.6 Configuration of the Presentation

Finally, we provide configuration hooks in Figure 1 for the keywords in proofs. These are mainly intended for package authors building on **statements**, e.g. for multi-language support.². The proof step labels can be customized via

EdNote:2

 $^{^2\}mathrm{EdNote}$: we might want to develop an extension sproof-babel in the future.

Environment	configuration macro	value
proof	\spf@proof@kw	Proof
sketchproof	\spf@sketchproof@kw	Proof Sketch

Figure 1: Configuration Hooks for Semantic Proof Markup

\pstlabelstyle

the \pstlabelstyle macro: \pstlabelstyle{\style\}} sets the style; see Figure 2 for an overview of styles. Package writers can add additional styles by adding a macro \pst@make@label@\style\ that takes two arguments: a commaseparated list of ordinals that make up the prefix and the current ordinal. Note that comma-separated lists can be conveniently iterated over by the LATEX \@for..:=...\do{...} macro; see Figure 2 for examples.

style	example	configuration macro
long	0.8.1.5	$\label@long#1#2{\@for\@I:=#1\do{\@I.}#2}$
angles	$\rangle\rangle\rangle$ 5	\def\pst@make@label@angles#1#2
		${\tt \{\ensuremath}\ensuremath{\ensuremath{\ensuremath}\ensuremath}\ensuremath}\ensuremath}$
short	5	\def\pst@make@label@short#1#2{#2}
empty		\def\pst@make@label@empty#1#2{}

Figure 2: Configuration Proof Step Label Styles

3 Limitations

In this section we document known limitations. If you want to help alleviate them, please feel free to contact the package author. Some of them are currently discussed in the TRAC.

- 1. The numbering scheme of proofs cannot be changed. It is more geared for teaching proof structures (the author's main use case) and not for writing papers.

 (reported by Tobias Pfeiffer; see [Ste], issue 1658) (fixed)
- 2. currently proof steps are formatted by the L^AT_EX description environment. We would like to configure this, e.g. to use the inparaenum environment for more condensed proofs. I am just not sure what the best user interface would be I can imagine redefining an internal environment spf@proofstep@list or adding a key prooflistenv to the proof environment that allows to specify the environment directly. Maybe we should do both.

4 The Implementation

The sproof package generates to files: the LATEX package (all the code between <code><*package</code>) and <code></package</code>) and the LATEXML bindings (between <code><*ltxml</code>) and <code></ltxml</code>). We keep the corresponding code fragments together, since the documentation applies to both of them and to prevent them from getting out of sync.

We first set up the Perl Packages for LATEXML

```
1 \*\ltxml\\
2 # -*- CPERL -*-
3 package LaTeXML::Package::Pool;
4 use strict;
5 use LaTeXML::Package;
6 RequirePackage('sref');
7 \/\ltxml\\\
```

4.1 Package Options

We declare some switches which will modify the behavior according to the package options. Generally, an option xxx will just set the appropriate switches to true (otherwise they stay false).³

```
8 \**package\
9 \DeclareOption{showmeta}{\PassOptionsToPackage{\CurrentOption}{metakeys}}
10 \ProcessOptions
11 \( / \package \)
12 \( * \text{lxml} \)
13 DeclareOption('showmeta','');
14 \( / \text{ltxml} \)
Then we make sure that the sref package is loaded [Koh10b].
15 \( * \package \)
16 \RequirePackage{sref}
17 \( / \package \)
```

4.2 Proofs

We first define some keys for the **proof** environment.

```
18 \( *\package \)
19 \\ \srefaddidkey\{spf\}
20 \\ \addmetakey\{spf\}\{display\}
21 \\ \addmetakey\{spf\}\{fron\}
22 \\ \addmetakey\{spf\}\{from\}
23 \\ \addmetakey\{spf\}\{type\}
24 \\ \addmetakey\{spf\}\{title\}
25 \\ \addmetakey\{spf\}\{title\}
26 \\ \addmetakey\{spf\}\{continues\}
27 \\ \addmetakey\{spf\}\{functions\}
28 \( /\package \)
```

 $^{^3\}mathrm{EdNote}\colon$ need an implementation for $\mathrm{LaTeXML}$

\spf@flow We define this macro, so that we can test whether the display key has the value flow

29 (package)\def\spf@flow{flow}

For proofs, we will have to have deeply nested structures of enumerated list-like environments. However, LATEX only allows enumerate environments up to nesting depth 4 and general list environments up to listing depth 6. This is not enough for us. Therefore we have decided to go along the route proposed by Leslie Lamport to use a single top-level list with dotted sequences of numbers to identify the position in the proof tree. Unfortunately, we could not use his pf.sty package directly, since it does not do automatic numbering, and we have to add keyword arguments all over the place, to accommodate semantic information.

pst@with@label

This environment manages¹ the path labeling of the proof steps in the description environment of the outermost proof environment. The argument is the label prefix up to now; which we cache in \pst@label (we need evaluate it first, since are in the right place now!). Then we increment the proof depth which is stored in \count10 (lower counters are used by TeX for page numbering) and initialize the next level counter \count\count10 with 1. In the end call for this environment, we just decrease the proof depth counter by 1 again.

```
30 (*package)
```

- 31 \newenvironment{pst@with@label}[1]%
- 32 {\edef\pst@label{#1}\advance\count10 by 1\count\count10=1}
- 33 {\advance\count10 by -1}

\the@pst@label

\the@pst@label evaluates to the current step label.

 $34 \end{abel} \pst@label{\number\countlo} \\$

\pstlabelstyle

\pstlabelstyle just sets the \pst@make@label macro according to the style.

- $35 \ensuremath{\mbox{def\pst@make@label@long#1#2{\ofor\0I:=#1\do{\0I.}#2}}$
- 36 \def\pst@make@label@angles#1#2{\ensuremath{\@for\@I:=#1\do{\rangle}}#2}
- ${\tt 37 \setminus def \setminus pst@make@label@short\#1\#2\{\#2\}}$
- 38 \def\pst@make@label@empty#1#2{}
- $39 \end{area} $$19 \end{area$
- 40 \pstlabelstyle{long}

\next@pst@label

\next@pst@label increments the step label at the current level.

41 $\def\next@pst@label{\global\advance\count\count10 by 1}$

\sproofend

This macro places a little box at the end of the line if there is space, or at the end of the next line if there isn't

- 42 \def\sproof@box{\hbox{\vrule\vbox{\hrule width 6 pt\vskip 6pt\hrule}\vrule}}
- 43 \def\spf@proofend{\sproof@box}
- 44 \def\sproofend\\ifx\spf@proofend\\@mpty\else\\fil\\null\nobreak\\fill\spf@proofend\par\smallskip
- 45 \def\sProofEndSymbol#1{\def\sproof@box{#1}}
- 46 (/package)
- 47 (ltxml)DefConstructor('\sproofend',"");

 $^{^{1}\}mathrm{This}$ gets the labeling right but only works 8 levels deep

```
spf@*@kw
           48 (*package)
           49 \def\spf@proofsketch@kw{Proof Sketch}
           50 \def\spf@proof@kw{Proof}
           51 (/package)
spfsketch
           52 (*package)
           53 \newcommand{\spfsketch}[2][]{\metasetkeys{spf}{#1}\sref@target
           54 \ \texttt{ifx\spf@display\spf@flow\else\{\stDMemph\{\texttt{ifx\spf@type}@empty\spf@proofsketch@kw\else\spf@type\}} \\
           55 \sref@label@id{this \ifx\spf@type\@empty\spf@proofsketch@kw\else\spf@type\fi}}
           56 (/package)
           57 (*ltxml)
           58 DefConstructor('\spfsketch OptionalKeyVals:pf{}',
           59
                     "<omdoc:proof "
                             . "?&defined(&KeyVal(#1,'id'))(xml:id='&KeyVal(#1,'id')')()>\n"
           60
                     . "?#2(<omdoc:omtext><omdoc:CMP>#2\n)()"
           61
                             . "</omdoc:proof>\n");
           63 DefConstructor('\sProofEndSymbol {}','');
           64 (/ltxml)
   sproof In this environment, we initialize the proof depth counter \count10 to 10, and set
           up the description environment that will take the proof steps. At the end of the
           proof, we position the proof end into the last line.
           65 (*package)
           66 \newenvironment{spf@proof}[2][]{\metasetkeys{spf}{#1}\sref@target
           67 \count10=10
           68 \ifx\spf@display\spf@flow\else{\stDMemph{\ifx\spf@type\@empty\spf@proof@kw\else\spf@type\fi}:}\
           69 \sref@label@id{this \ifx\spf@type\@empty\spf@proof@kw\else\spf@type\fi}
           70 \def\pst@label{}\newcount\pst@count% initialize the labeling mechanism
           71 \begin{description}\begin{pst@with@label}{P}}
           72 {\end{pst@with@label}\end{description}}
           73 \newenvironment{sproof}[2][]{\begin{spf@proof}[#1]{#2}}{\sproofend\end{spf@proof}}
           74 \newenvironment{sProof}[2][]{\begin{spf@proof}[#1]{#2}}{\end{spf@proof}}}
           75 (/package)
           76 (*ltxml)
           77 DefEnvironment('{sproof} OptionalKeyVals:pf{}',
           78
                     "<omdoc:proof "
           79
                             . "?&KeyVal(#1,'for')(for='&hash_wrapper(&KeyVal(#1,'for'))')()"
                                "?&defined(&KeyVal(#1,'id'))(xml:id='&KeyVal(#1,'id')')()>\n"
           80
                     . "?#2(<omdoc:omtext>"
           81
                                     "<omdoc:CMP>#2</omdoc:CMP>"
           82
                                    "</omdoc:omtext>\n)()"
           83
                             . "#body"
           84
                           . "</omdoc:proof>\n");
           86 DefMacro('\sProof','\sproof');
           87 DefMacro('\endsProof','\endsproof');
```

88 (/ltxml)

```
spfidea
               89 (*package)
               90 \newcommand{\spfidea}[2][]{\metasetkeys{spf}{#1}%
               91 \stDMemph{\ifx\spf@type\@empty{Proof Idea}\else\spf@type\fi:} #2\sproofend}
               92 (/package)
               93 (*ltxml)
               94 DefConstructor('\spfidea OptionalKeyVals:pf {}',
                         "<omdoc:proof "
               95
                                       "?&defined(&KeyVal(#1,'id'))(xml:id='&KeyVal(#1,'id')')()"
               96
                               . "?&KeyVal(#1,'for')(for='&hash_wrapper(&KeyVal(#1,'for'))')()>\n"
               97
                           "<omdoc:omtext><omdoc:CMP>#2</omdoc:omtext>\n"
               98
                         "</omdoc:proof>\n");
               99
               100 (/ltxml)
                   The next two environments (proof steps) and comments, are mostly semantical,
               they take KeyVal arguments that specify their semantic role. In draft mode, they
               read these values and show them. If the surrounding proof had display=flow,
               then no new \item is generated, otherwise it is. In any case, the proof step number
               (at the current level) is incremented.
      spfstep
              101 (*package)
              102 \newenvironment{spfstep}[1][]{\metasetkeys{spf}{#1}
              103 \ifx\spf@display\spf@flow\else\item[\the@pst@label]\fi
              104 \f(\stDMemph{\spf@title})) fi \}
              105 {\next@pst@label}
              106 (/package)
              107 (*ltxml)
              108 DefEnvironment('{spfstep} OptionalKeyVals:pf',
                               "<omdoc:derive "
              109
                                        "?&defined(&KeyVal(#1,'id'))(xml:id='&KeyVal(#1,'id')')()>"
              110
                          . "<omdoc:CMP>#body</omdoc:derive>\n",
              111
                           beforeConstruct=>sub {
              112
                            $_[0]->maybeCloseElement('omdoc:CMP');
              113
                           });#$
              115 (/ltxml)
sproofcomment
              116 (*package)
              117 \newenvironment{sproofcomment}[1][]{\metasetkeys{spf}{#1}
              118 \ifx\spf@display\spf@flow\else\item[\the@pst@label]\fi}
              119 {\next@pst@label}
              120 (/package)
              121 (*ltxml)
              122 DefEnvironment('{sproofcomment} OptionalKeyVals:pf',
                         "<omdoc:omtext "
              123
```

. "<omdoc:CMP>#body</omdoc:CMP>"

"</omdoc:omtext>");

"?&defined(&KeyVal(#1,'id'))(xml:id='&KeyVal(#1,'id')')()>"

124

125 126

127 (/ltxml)

The next two environments also take a KeyVal argument, but also a regular one, which contains a start text. Both environments start a new numbered proof level.

```
In the pfcases environment, the start text is displayed as the first comment of
          the proof.
         128 (*package)
         129 \newenvironment{spfcases}[2][]{\metasetkeys{spf}{#1}
         130 \def\@test{#2}\ifx\@test\empty\else
         131 \ifx\spf@display\spf@flow {#2}\else\item[\the@pst@label]{#2} \fi\fi
         132 \verb|\degin{pst@with@label}{\pst@label,\number\\count10}| \\
         133 {\end{pst@with@label}\next@pst@label}
         134 (/package)
         135 (*ltxml)
         136 DefEnvironment('{spfcases} OptionalKeyVals:pf {}',
         137
                    "<omdoc:derive "
                                  "?&defined(&KeyVal(#1,'id'))(xml:id='&KeyVal(#1,'id')')()>\n"
         138
                      "<omdoc:CMP>#2</omdoc:CMP>\n"
         139
                      "<omdoc:method xref='#proof-by-cases'>#body</omdoc:method>"
         140
         141
                   . "</omdoc:derive>\n");
         142 (/ltxml)
 spfcase In the pfcase environment, the start text is displayed specification of the case
          after the \item
         143 (*package)
         144 \newenvironment{spfcase}[2][]{\metasetkeys{spf}{#1}
         145 \ifx\spf@display\spf@flow\else\item[\the@pst@label]\fi
         146 \def\@test{#2}\ifx\@test\@empty\else{\stDMemph{#2}:}\fi
         147 \begin{pst@with@label}{\pst@label, \number\count\count10}}
         148 {\tt ifx spf@display spf@flow else sproofend fi\end {\tt pst@with@label} \next@pst@label} \\
         149 (/package)
         150 (*ltxml)
         151 DefEnvironment('{spfcase} OptionalKeyVals:pf{}',
         152
                    "<omdoc:proof "
                             . "?&defined(&KeyVal(#1,'id'))(xml:id='&KeyVal(#1,'id')')()>\n"
         153
                       "?#2(<omdoc:omtext>"
         154
                                     "<omdoc:CMP>#2</omdoc:CMP>"
         155
                                    "</omdoc:omtext>\n)()"
         156
                    . "#body"
         157
                  . "</omdoc:proof>\n");
         159 (/ltxml)
subproof In the subproof environment, a new (lower-level) proof environment is started.<sup>4</sup>
         160 (*package)
         161 \newenvironment{subproof}[1][]%
         162 {\begin{pst@with@label}{\pst@label, \number\count\count10}}
         163 {\ifx\spf@display\spf@flow\else\sproofend\fi\end{pst@with@label}}
```

EdNote:4

⁴EDNOTE: document this above

```
164 (/package)
165 (*ltxml)
166 DefEnvironment('{subproof}[]',
           "<omdoc:derive>"
167
                      "?#1(<omdoc:CMP>#1</omdoc:CMP>)()"
168
169
              "<omdoc:method>"
170
                         "<omdoc:proof>\n #body\n</omdoc:proof>"
              "</omdoc:method>"
171
                  ."</omdoc:derive>");
172
173 (/ltxml)
```

4.3 Justifications

We define the actions that are undertaken, when the keys for justifications are encountered. Here this is very simple, we just define an internal macro with the value, so that we can use it later.

```
174 \*package\)
175 \srefaddidkey{just}
176 \addmetakey{just}{method}
177 \addmetakey{just}{premises}
178 \addmetakey{just}{args}
179 \/package\)
180 \*ltxml\)
181 DefKeyVal('just','id','Semiverbatim');
182 DefKeyVal('just','method','Semiverbatim');
183 DefKeyVal('just','premises','Semiverbatim');
184 DefKeyVal('just','args','Semiverbatim');
185 \/ltxml\)
```

The next three environments and macros are purely semantic, so we ignore the keyval arguments for now and only display the content.⁵

justification

EdNote:5

```
186 (*package)
187 \newenvironment{justification}[1][]{}{}
188 (/package)
189 (*ltxml)
190 sub extractBodyText {
     my ($box, $remove) = @_;
     my $str = '';
192
     my @boxes = $box->unlist;
193
     foreach my $b(@boxes) {
194
       my $s = '';
195
       if ($b =~ /LaTeXML::Whatsit/) {
196
197
         my $body = $b->getBody;
         $s = $body ? extractBodyText($body, $remove) : '';
198
       } elsif ($b =~ /LaTeXML::Box/) {
199
         $s = $b->toString || '';
200
```

13

 $^{^5\}mathrm{EdNote}$: need to do something about the premise in draft mode.

```
@{$b}[0] = '', if $remove; }
         201
         202
                 $str .= $s; }
               str = s/s+//g;
         203
               $str; }
         204
         205
         206 DefEnvironment('{justification} OptionalKeyVals:just', sub {
         207 my ($doc, $keys, %props) = @_;
         208 my $text = extractBodyText($props{body}, 1);
         209 my $node = LookupValue('_LastSeenCMP');
         210 #$node->appendText($text) if $node;
         211 my $method = $keys ? $keys->getValue('method') : undef;
         212 $doc->openElement("omdoc:method", $method ? (xref => $method) : ());
         213 $doc->absorb($props{body}) if $props{body};
         214 $doc->closeElement("omdoc:method");
         215 return; });
         216 \langle /ltxml \rangle
\premise
         217 (*package)
         218 \newcommand{\premise}[2][]{#2}
         219 (/package)
         220 (*ltxml)
         221 DefMacro('\premise[]{}', sub {
                my (\$xref, \$text) = (\$_[1], \$_[2]);
         222
                my @res = (T_CS('\premise@content'));
         223
                push(@res, T_OTHER('['), $xref->unlist, T_OTHER(']')) if $xref;
         224
                push(@res, T_SPACE, $text->unlist) if $text;
         225
         226
                @res; });
         227 \ensuremath{\texttt{DefConstructor}('\premise@content[]',}
                             "<omdoc:premise xref='#1'/>");
         228
         229 (/ltxml)
\justarg the \justarg macro is purely semantic, so we ignore the keyval arguments for
          now and only display the content.
         230 (*package)
         231 \newcommand{\justarg}[2][]{#2}
         232 (/package)
         233 (*ltxml)
         234 DefMacro('\justarg[]{}', sub { (($_[1] ? $_[1] -> unlist : ()), }
         235 T_SPACE, $_[2]->unlist, T_SPACE); });
         236 Tag('omdoc:derive', afterClose=>sub {
                   my ($doc, $node) = @_;
         237
                   my @children = grep($_->nodeType == XML_ELEMENT_NODE, $node->childNodes);
         238
                   my $firstCMP = undef;
         239
                   foreach my $child(@children) {
         240
                     next unless ($child->localname || '') eq 'CMP';
         241
                     if ($child->hasChildNodes()) {
         242
                       next unless $#{$child->childNodes} == 0;
         243
         244
                       next unless $child->firstChild->nodeType == XML_TEXT_NODE; }
         245
```

4.4 Providing IDs for OMDoc Elements

To provide default identifiers, we tag all OMDoc elements that allow xml:id attributes by executing the numberIt procedure from omdoc.sty.ltxml.

```
253 \*|txm|\\
254 Tag('omdoc:proof',afterOpen=>\&numberIt,afterClose=>\&locateIt);
255 Tag('omdoc:derive',afterOpen=>\&numberIt,afterClose=>\&locateIt);
256 Tag('omdoc:method',afterOpen=>\&numberIt,afterClose=>\&locateIt);
257 Tag('omdoc:premise',afterOpen=>\&numberIt,afterClose=>\&locateIt);
258 Tag('omdoc:derive',afterOpen=>\&numberIt,afterClose=>\&locateIt);
259 \( /|txm| \)
```

5 Finale

Finally, we need to terminate the file with a success mark for perl. 260 (ltxml)1;

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Numbers written in italic refer to the page where the corresponding entry is described; numbers underlined refer to the code line of the definition; numbers in roman refer to the code lines where the entry is used.

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