DCpic (5.0) — Manual de Utilização 2013/05/01 (v15)

Pedro Quaresma CISUC/Departamento de Matemática, Universidade de Coimbra 3001-454 COIMBRA, PORTUGAL

pedro@mat.uc.pt phone: +351-239 791 137 fax: +351-239 832 568

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Resumo

O *DCpic* é um conjunto de comandos para a escrita de grafos, para tal desenvolveu-se um conjunto de comandos, com uma sintaxe simples, que permite a construção de quase todo o tipo de grafos.

Originalmente o *DCpic* (**D**iagramas **C**omutativos utilizando o **PiC**TeX) foi concebido para a construção de diagramas comutativos tal como são usados em Teoria das Categorias [3, 6], temos então grafos etiquetados e com elementos nos nós. A partir da versão 4.0 o conjunto de comandos foi alterada de forma a considerar-se também a construção de grafos dirigidos, e grafos não dirigidos. A forma de os especificar recorre à colocação dos diferentes objectos (nós e arestas) num dado referencial ortonormado,

O DCpic está baseado no PTCTFX necessitando deste para poder ser usado.

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The Current Maintainer of this work is Pedro Quaresma (pedro@mat.uc.pt). This work consists of the files dcpic.sty.

Coimbra, 2013/04/21 Pedro Quaresma

1 História

- 11/1990 versão 1.0
- 10/1991 versão 1.1
- 9/1993 versão 1.2: argumento "distância entre as extremidades da seta e os objectos" passou a ser opcional; uma nova opção para as "setas" (opção 3).
- 2/3/1995 versão 1.3: foi acrescentado o tipo de seta de aplicação (opção 4) a distância da etiqueta à seta respectiva passou a ser fixa (10 unidades de medida).
- 15/7/1996 versão 2.1: o comando mor passou a ter uma sintaxe distinta. Os parâmetros 5 e 6 passaram a ser a distância entre os objectos e os extremos da seta o parâmetro 7 é o nome do morfismo e os parâmetros 8 e 9, colocação do morfismo e tipo de morfismo passaram a ser opcionais.
- **5/2001 versão 3.0:** implementação do comando **cmor** baseado no comando de desenho de curvas quadráticas pelo PICT_FX.
- 11/2001 versão 3.1: modificação das pontas das setas de forma a estas ficarem semelhantes às setas (símbolos) dos TeX.
- 1/2002 versão 3.2: modificação dos comandos obj e mor de forma a introduzir a especificação lógica dos morfismos, isto é, passa-se a dizer qual é o objecto de partida e/ou o objecto de chegada em vez de ter de especificar o morfismo em termos de coordenadas. Por outro lado o tamanho das setas passa a ser ajustado automaticamente em relação ao tamanho dos objectos.
- 5/2002 versão 4.0: versão incompatível com as anteriores. Modificação dos comandos begindo e obj. O primeiro passou a ter um argumento (obrigatório) que nos permite especificar o tipo de grafo que estamos a querer especificar:
 - commdiag (0), para diagramas comutativos;
 - digraph (1), para grafos orientados;
 - undigraph (2), para grafos não orientados.

O comando obj modificou a sua sintaxe passou a ter um (após a especificação das coordenadas, um argumento opcional, um argumento obrigatório, e um argumento opcional. O primeiro argumento opcional dá-nos a etiqueta que serve como referência para a especificação dos morfismos, na sua ausência usa-se o argumento obrigatório para esse efeito, o argumento obrigatório dá-nos o "conteúdo" do objecto, nos diagramas comutativos é centrado no ponto dado pelas coordenadas sendo o argumento seguinte simplesmente ignorado, nos grafos o "conteúdo" é colocado numa posição a norte, a noroeste, a este, ..., sendo que a posição concreta é especificada pelo último dos argumentos deste comando, o valor por omissão é o norte.

3/2003 - versão 4.1: a pedido de Jon Barker < jeb1@soton.ac.uk> criei um novo tipo de seta, a seta de sobrejecção. Para já a dupla seta só fica bem nas setas horizontais ou verticais.

- 12/2004 versão 4.1.1: nova versão das setas de sobrejecção que corrigue completamente os problemas da solução anterior.
- 3/2007 versão 4.2: acrescenta a directiva "providespackage". Acrescenta linhas a ponteado e a tracejado.
- 5/2008 versão 4.2.1: apaga alguns contadores para tentar diminuir o excessivo uso dos mesmos por parte do PiCTeX.
- 8/2008 versão 4.3: graças a Ruben Debeerst <debeerst@mathematik.uni-kassel.de>, acrescentei uma nova "seta" a "equalline". Após isso decidi também acrescentar setas duplas, com o mesmo ou diferentes sentidos. Acrescentou-se também a seta nula, isto é, sem representação gráfica, a qual pode ser usada para acrescentar etiquetas a outras "setas".
- 12/2008 version 4.3.1: para evitar conflitos com outros pacotes o comando "id" é internalizado. O comando "dasharrow" é modificado para "dashArrow" para evitar um conflito com o AMSTeX.
- 12/2009 version 4.3.2: para evitar um conflito com o pacote "hyperref" mudou-se o contador "d" para "deuc", aproveitei e mudei os contadores "x" e "y" para "xO" e "yO"
- 4/2013 version 4.4.0: graças a Xingliang Liang jkl9543@gmail.com> acrescentou-se uma nova seta "dotarrow".
- **4/2013 version 5.0: uma nova unidade para o sistema de coordenadas**, 1/10 da anterior. Esta nova unidade permite corriguir um problema com a construção das setas duplas, além de permitir uma especificação mais fina dos diagramas.

2 Introdução

O conjunto de comandos DCpic é um conjunto de comandos TeX [4] dedicado à escrita de diagramas tal como são usados em Teoria das Categorias [3, 6], assim como de grafos dirigidos e não dirigidos [2].

Pretendeu-se com a sua escrita ter uma forma simples de especificar grafos, fazendo-o através da especificação de um conjunto de "objectos" (nós do grafo) colocados num dado referencial ortonormado, e através de um conjuntos de morfismos (arestas) que os são posicionados explicitamente no referido referencial, ou então, a são posição é dada especificando qual é o seu nó de partida e qual é o seu nó de chegada.

O gráfico em si é construído recorrendo aos comandos gráficos do PICTEX.

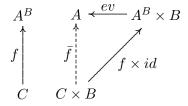
3 Utilização

Antes de mais é necessário carregar os dois conjuntos de comandos acima referidos, no caso de um documento LATEX [5] isso pode ser feito com o seguinte comando (no preâmbulo).

\usepackage{dcpic,pictex}

Nos outros formatos ter-se-á de usar um comando equivalente. Após isso os diagramas podem ser escritos através dos comandos disponibilizados pelo DCpic. Por exemplo, os comandos:

produzem o seguinte diagrama:



O meio ambiente begindo, endos permite-nos construir um grafo por colocação dos objectos num referencial ortonormado tendo a origem em (0,0). As arestas (morfismos) vão ligar pares de nós (objectos) entre si.

4 Comandos Disponíveis

De seguida apresenta-se a descrição dos comandos, a sua sintaxe e a sua funcionalidade. Os argumentos entre parêntesis rectos são opcionais.

\begindc{#1}[#2] - entrada no ambiente de escrita de grafos:

#1 - tipo de grafo

 $0 \equiv \text{commdiag, diagrama comutativo};$

 $1 \equiv \text{digraph}, \text{ grafo orientado};$

 $2 \equiv \text{ \undergo}$ undigraph, grafo não orientado;

 $3 \equiv \text{cdigraph}$, grafo orientado, com objectos circunscritos;

 $4 \equiv \text{cundigraph}, \text{ grafo não orientado, com objectos circunscritos.}$

#2 – factor de escala (opcional)

valor por omissão: 300

\enddc - saída do meio ambiente para a escrita de grafos.

\obj(#1, #2) [#3] {#4} [#5]: comando de colocação dos nós (objectos).

```
#1 e #2 – coordenadas do centro da caixa que vai conter o texto
```

#3 – etiqueta para identificar o objecto (opcional)

#4 – texto (conteúdo do nó)

#5 – colocação relativa do objecto (opcional)

 $0 \doteq \text{\ } \text{centrado}$

 $1 \doteq \setminus \text{north}, \text{ norte}$

 $2 \doteq \text{ } \setminus \text{northeast, nordeste}$

 $3 \doteq \text{\east, este}$

 $4 \doteq$ \southeast, sudeste

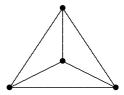
 $5 \doteq \text{south, sul}$

 $7 \doteq \text{\west, oeste}$

 $8 \doteq \text{ northwest, noroeste}$

A etiqueta explícita-se quando não é possível usar o objecto como forma de identificação do nó, por exemplo num dado grafo não orientado os nós podem não ter conteúdo e como tal serem todos iguais em termos de identificação:

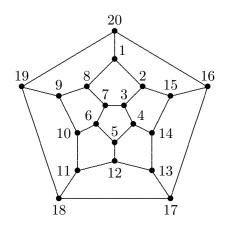
Em alguns casos, por exemplo comandos dos LATEX complexos, pode ser necessário explicitar o argumento #3 mesmo que seja através da etiqueta vazia []. Esse especificar da etiqueta vazia torna-se necessário para que o mecanismo interno do DCpic de comunicação entre comandos (pilhas) não se baralhe e entre num ciclo infinito.



foi produzido por:

```
 \begin{array}{l} \left\lceil \frac{1}{1} \right\rceil \\ \left\lceil \frac{1
```

O parâmetro referente à colocação do objecto só é relevante quando se pensa na identificação dos nós num dado grafo orientado (ou não), por exemplo o grafo "Around the Word" [2]:



foi produzido por

```
\begindc{\undigraph}[70]
\langle \mathbf{obj}(8,7)\{11\}[\backslash \mathbf{west}]
\begin{picture}(12,8) & \{12\} & [\south] \\ & \begin{picture}(16,7) & \{13\} & [\end{picture} \end{picture}
\langle \mathbf{obj}(8,11)\{10\}[\backslash \mathbf{west}]
\langle \mathbf{obj}(10,12)\{6\}[\backslash \mathbf{northwest}]
\backslash obj (12,10) {5}
\langle \mathbf{obj}(14,12) \{4\} [\langle \mathbf{northeast} ] 
\backslash \mathbf{obj}(16,11)\{14\}[\backslash \mathbf{east}]
\backslashobj(2,16){19}
\odot{obj}(9,16){8}
\backslash obj (11,14) {7}
\obj(13,14){3}
\backslashobj (15,16){2}
\backslashobj (18,15) {15}
\langle \mathbf{obj}(22,16) \{ 16 \}
\langle \mathbf{obj}(12,19)\{1\}[\backslash \mathbf{northeast}]
\mbox{mor}\{18\}\{17\}\{\}\mbox{mor}\{18\}\{11\}\{\}\mbox{mor}\{18\}\{19\}\{\}\}
\mathbf{11}_{12}_{12}_{13}_{11}_{10}_{10}_{11}_{10}_{12}_{13}_{13}_{10}
\mor{12}{5}{}\mor{10}{6}{}\mor{10}{9}{}
\mor{5}{6}{}\mor{5}{4}{}\mor{13}{17}{}
\mbox{mor}\{13\}\{14\}\{\}\mbox{mor}\{9\}\{19\}\{\}\mbox{mor}\{9\}\{8\}\{\}
\mbox{mor}\{6\}\{7\}\{\}\mbox{mor}\{4\}\{3\}\{\}\mbox{mor}\{4\}\{14\}\{\}
\mathbf{19}{20}{}\setminus\mathbf{mor}{8}{1}{}\setminus\mathbf{mor}{8}{7}{}
\mathbf{16}{20}{}\\mathbf{mor}{1}{20}{}\\mathbf{mor}{1}{20}{}\\mathbf{mor}{15}{16}{}
\enddc
```

\mor{#1}{#2}[#5,#6]{#7}[#8,#9]: Comando de colocação da seta (morfismo) de ligação de dois objectos – Primeira variante.

A numeração errada dos argumentos é aqui feita propositadamente, aquando da explicação da segunda variante deste comando compreender-se-á o porquê desta opção de escrita.

```
\#1 – referência do nó de partida
```

#2 – referência do nó de chegada

- #5 e #6 distância do centro dos objectos às extremidades inicial e final respectivamente da seta. Valores por omissão: 10, 10 (para diagramas) 2, 2 (para os grafos)
 - #7 texto, "nome" do morfismo
 - #8 colocação do nome do morfismo em relação à seta. Valor por omissão, \atleft.

 - $-1 \doteq \exists$ atleft, à esquerda
 - #9 tipo da seta. Valor por omissão, \solidarrow.
 - $0 \doteq \slash$ solidarrow, seta sólida
 - $1 \doteq \langle dashArrow, seta tracejada \rangle$
 - $2 \doteq \langle dot Arrow, seta ponteada$
 - $3 \doteq \$ solidline, linha sólida
 - $4 \doteq \forall$ dashline, linha a tracejado
 - $5 \doteq \langle dotline, linha a ponteado \rangle$
 - $6 \doteq \text{injectionarrow}$, seta de injecção. Valor anterior 3 (versão < 4.2)
 - $7 \doteq \text{la plicationarrow}$, seta de aplicação. Valor anterior 4 (versão < 4.2)
 - $8 \doteq \text{varjectivearrow}$, seta de função sobrejectiva. Valor anterior 5 (versão < 4.2)

 - $10 \doteq \text{doublearrow}$, seta dupla
 - $11 \doteq \text{\double opposite}$, seta dupla em sentidos opostos
 - $12 \doteq \text{nullarrow}$, seta nula, serve o propósito de acrescentar etiquetas as outras "setas".
- \mor(#1,#2)(#3,#4)[#5,#6]{#7}[#8,#9]: Comando de colocação da seta (morfismo) de ligação de dois objectos Segunda variante.
 - #1 e #2 coordenadas do nó de partida
 - #3 e #4 coordenadas do nó de chegada

Todos os outros argumentos têm o significado já explicado (por isso a numeração errada). É de notar que para a primeira variante é feito o cálculo das coordenadas dos nós de forma automática e depois são passados esses valores para a segunda variante do comando.

\cmor(#1) #2(#3,#4){#5}[#6] comando para a especificação de setas curvas. O algoritmo de construção das setas é o do PICTEX o que implica que se está a especificar uma linha quadrática através de um número ímpar de pontos.

#1—lista de pontos, em número ímpar

#2—direccionamento da seta

 $0 \doteq \text{pup}$, apontar para cima

 $1 \doteq \pdown$, apontar para baixo

 $2 \doteq \text{pright}$, apontar para a direita

 $3 \doteq \$ pleft, apontar para a esquerda

#3—abcissa do morfismo

#4—ordenada do morfismo

#5-morfismo

#6—tipo de "seta", valor por omissão: 0, seta sólida.

Os restantes valores possíveis são os descritos na variante anterior.

O comando cmor no caso em que não tem o último parâmetro opcional tem de ser seguido por um espaço. O espaço antes do direccionamento da seta é obrigatório.

No caso de se ter o valor 2 ("\solidline") o valor para o direccionamento da seta não é tipo em conta, no entanto dado se tratar de um do parâmetro obrigatório é necessário dar-lhe um valor

5 Alguns Exemplos

5.1 Setas Duplas, Transformações Naturais, ...

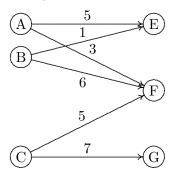
É de notar que alguns casos aparentemente omissos na actual versão podem perfeitamente ser construídos através de uma utilização imaginativa dos actuais comandos. Por exemplo os seguintes diagramas:

$$A \xrightarrow{g} B \qquad \qquad A \xrightarrow{\downarrow \sigma} B$$

Podem ser construídos com a actual versão. Eis como:

```
 \begindc {\o \{ \} [30] \\ \o [20,5) {\$A\$} \\ \o [20,5) {\$B\$} \\ \o [20,5) {\$A\$} \\ \o [20,5) {\$B\$} \\ \o [20,5) {\$B\$} \\ \o [20,6) {\$ \o [20,6) {\S [20
```

5.2 Grafos Orientados com Objectos Circunscritos

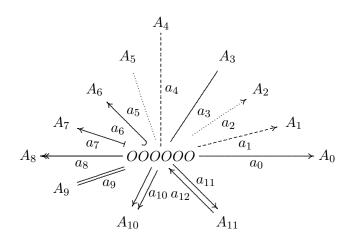


Foi produzido através dos seguintes comandos:

```
 \begindc {\ondiag} [250] \\ \begindc {\ondia
```

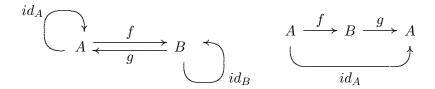
5.3 Diferentes Tipos de Setas/Linhas

```
\begin{c} \mathbf{(commdiag)} [250] \
 \obj (10,10)[A]{$00000$}
   \langle \mathbf{obj} (15, 10) [A0] \{ A_{-0} \}
 \langle \mathbf{obj} (14, 11) [A1] \{ \$A_1 \$ \}
 \obj (13,12) [A2] {$A_2$} \obj (12,13) [A3] {$A_3$}
 \obj (9,13) [A5] {$A_5$}
   \backslashobj (8,12) [A6] {$A_6$}
 \langle \mathbf{obj} (6, 10) [A8] \{ \$A_{-}8\$ \}
 \\ \begin{align*} \\ \begin{align*} \\ \begin{align*} \begin{align
 \langle \mathbf{obj}(12,8)[A11] \{ A_{11} \}
 \mor{A}{A0}{$a_0$}[\atright,\solidarrow]
\mor{A}{A1}{$a_1$}[\atright,\dashArrow]
\label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
 \operatorname{\mathsf{Mor}}\{A\}\{A5\}\{\$a_{-}5\$\}[\ \mathsf{atleft}\ ,\ \mathsf{dotline}]
 \label{localization} $$\operatorname{A}_{A}_{A_{0}}^{A_{0}}^{a_{0}}^{a_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{0}}^{A_{
 \operatorname{\mathsf{Mor}}\{A\}\{A9\}\{a_{-}9\}\}[\operatorname{\mathsf{atleft}},\operatorname{\mathsf{equalline}}]
 \label{lem:mor} $$\operatorname{A}_{A10}^{s_1(10)}^{s_1(10)}_{atleft,\doublearrow} $$\operatorname{A}_{A11}^{s_1(11)}^{s_1(11)}_{atleft,\doubleopposite}$$
 \operatorname{\mathsf{Nor}}\{A\}\{A11\}\{a_{-}\{12\}\}\}[\operatorname{\mathsf{atright}},\operatorname{\mathsf{nullarrow}}]
      enddc
```



5.4 Diagramas com Setas Curvas

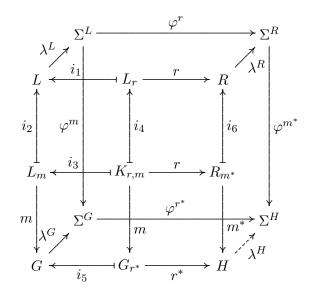
```
\begindc{\commdiag}[30]
\backslash obj (14,11) { $A$}
\mathbf{mor}(14,12)(39,12)\{\$f\$\}
\mor(39,10)(14,10){$g$}
\operatorname{\mathsf{cmor}}((10,10)(6,11)(5,15)(6,19)(10,20)(14,19)(15,15))
   \operatorname{\mathbf{pdown}}(2,20) { $ id _A$}
\backslash \mathbf{cmor}((40,7)(41,3)(45,2)(49,3)(50,7)(49,11)(45,12))
   \protect\operatorname{\mathbf{pleft}}(54,3)\{\$\operatorname{id}\_B\$\}
\enddc
\begin{c} \mathbf{(commdiag)} [30]
\backslash \mathbf{obj} (10, 15) [A] \{\$A\$\}
\obj (40,15)[Aa]{$A$}
\langle \mathbf{obj}(25, 15)[B] \{\$B\$\}
\mor{A}{B}{$f$}
\mor{B}{Aa}{$g$}
\operatorname{\mathsf{cmor}}((10,11)(11,7)(15,6)(25,6)(35,6)(39,7)(40,11))
   \pup(25,3){$ id_A$}
\enddc
```



5.5 Um Exemplo Complexo

O diagrama seguinte foi proposto por Feruglio [1] como um caso de teste. Como é possível ver o DCpic produz o diagrama correctamente a partir de uma especificação simples.

```
\langle \mathbf{obj} (1,3) [Lm] \{ L_m \} 
\obj (3,3) [Krm] {$K_{r}, m}$}
\obj(5,3)[Rmstar]{\$R_{m^*}}
 \langle \mathbf{obj} (1,5) [L] \{ L \} \}
\langle \mathbf{obj} (3,5) [Lr] \{ L_r \} 
\backslashobj (5,5)[R]{$R$}
\begin{tabular}{ll} $$ \obj(2,6)[SigmaL]_{$\Sigma^L$} \\ obj(6,6)[SigmaR]_{$\Sigma^R$} \end{tabular}
\mathbf{Gr}{SigmaG}{\mathbf{S}}
\label{localization} $$\operatorname{Krm}_{Lm}_{s, \alpha}(s) = \operatorname{Lm}_{s, \alpha}(s) - \operatorname{Lm}_{s, \alpha}(s) = \operatorname{Lm}_{s, \alpha}(s) - \operatorname{Lm}_{s, \alpha}(s) -
 \operatorname{\mathbf{Mor}}\{\operatorname{Krm}\}\{\operatorname{Rmstar}\}\{\$r\$\}
\operatorname{\mathsf{Nor}} \left\{ \operatorname{\mathsf{Krm}} \right\} \left\{ \operatorname{\mathsf{Lr}} \right\} \left\{ \operatorname{\mathsf{si}} \left[ \operatorname{\mathsf{Atright}} \right] \right\} \left[ \operatorname{\mathsf{Atright}} \right]
\operatorname{\mathsf{Mor}}\{\operatorname{Grstar}\}\{\operatorname{\mathsf{barraA}\$m\$}\}
 \mor{Rmstar}{R}{$i_6$}[\atright,\aplicationarrow]
\mor{Rmstar}{H}{\barraB$m^*$}
\operatorname{\mathsf{Mor}}\{\operatorname{Lr}\}\{\operatorname{L}\}\{\text{$i=1$}\ [\atright,\aplicationarrow]
\operatorname{\mathbf{Lr}}_{R}^{Lr}_{R}^{R}
\mor{SigmaL}{SigmaG}{\$\varphi^m\$}[\atright,\solidarrow] \mor{SigmaL}{SigmaR}{\$\varphi^r\$}
 \mathbf{GigmaR} { \mathbf{SigmaH} } { \mathbf{varphi}^{m*} }
  enddc
```



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A O Código

%% DC-PiCTeX

```
%% Copyright (c) 1990-2013 Pedro Quaresma, University of Coimbra, Portugal
%% 11/1990 (version 1.0);
           10/1991 (version 1.1);
             9/1993 (version 1.2);
%%
%%
             3/1995 (version 1.3);
%% 7/1996 (version 2.1);
%% 5/2001 (version 3.0);
         11/2001 (version 3.1);
%%
             1/2002 (version 3.2)
%% 5/2002 (version 4.0);
          3/2003 (version 4.1);
                  12/2004 (version 4.1.1)
%%
%%
           3/2007 (version 4.2)
%%
                     5/2008 (version 4.2.1)
            8/2008 (version 4.3)
%%
%%
                  12/2008 (version 4.3.1)
%%
                  12/2009 (version 4.3.2)
             4/2013 (version 4.4.0)
%%
              5/2013 (version 5.0)
\immediate\write10{Package DCpic 2013/05/01 v5.0}
\label{lem:providesPackage(dcpic) [2013/05/01 v5.0]} $$ \Pr[2013/05/01 v5.0] $$
%% Version X.Y.Z
         X - major versions
%%
           Y - minor versions
           Z - bug corrections
%%
%%
%% Copyright (c) 1990-2013 Pedro Quaresma <pedro@mat.uc.pt>
%%
% This work may be distributed and/or modified under the
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% of this license or (at your option) any later version.
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% http://www.latex-project.org/lppl.txt
% and version 1.3 or later is part of all distributions of LaTeX
% version 2005/12/01 or later.
\% This work has the LPPL maintenance status 'maintained'.
% The Current Maintainer of this work is Pedro Quaresma (pedro@mat.uc.pt).
% This work consists of the files dcpic.sty.
%% Coimbra, 1st of May, 2013 (2013/05/01)
%% Pedro Quaresma
%% DCpic is a package of \TeX\ macros for graph modelling in a
\hfill 
\mbox{\ensuremath{\%}{\sc h}} the use of \PiCTeX\ a powerful graphical engine, and a simple
```

```
%% specification syntax. A graph is described in terms of its objects
\% and its edges. The objects are textual elements and the edges can
\ensuremath{\mbox{\%}} have various straight or curved forms.
%%
%%
\ensuremath{\text{\%}}\xspace A graph in DCpic is a "picture" in \PiCTeX, in which we place our
    {\em objects} and {\em morphisms} (edges). The user's commands in
%%
   DCpic are: {\tt begindc} and {\tt enddc} which establishe the
%%
    coordinate system where the objects will by placed; {\tt obj}, the
    command which defines the place and the contents of each object;
    {\rm tt\ mor}, and {\rm tt\ cmor}, the commands which define the
   morphisms, linear and curved edges, and its labels.
%%
%%
   Example:
     \begindc{\commdiag}[3]
%%
      \obj(10,15){$A$}
%%
%%
      \obj(25,15){$B$}
%%
      \obj(40,15){$C$}
%%
      \mor{$A$}{$B$}{$f$}
%%
      \mor{$B$}{$C$}{$g$}
%%
      \cmor((10,11)(11,7)(15,6)(25,6)(35,6)(39,7)(40,11))
%%
       \pup(25,3){$g\circ f$}
%%
%%
%% NOTES:
%%
      all the numeric values should be integer values.
%%
%% Available commands:
%%
%% The environment:
     \begindc{#1}[#2]
          #1 - Graph type
%%
%%
            0 = "commdiag" (commutative diagram)
            1 = "digraph" (direct graph)
%%
            2 = "undigraph" (undirect graph)
%%
%%
            3 = "cdigraph" with incircled objects
%%
            4 = "cundigraph" with incircled objects
%%
           (optional) #2 - magnification factor (default value, 300)
%%
%%
     \enddc
%%
%% Objects:
     \obj(#1,#2)[#3]{#4}[#5]
%%
               #1 and #2 - coordenates
%% (optional) #3 - Label, to be used in the morphims command, if not
%%
                    present the #4 will be used to that purpose
               #4 - Object contents
\mbox{\ensuremath{\mbox{\%}}{\mbox{\%}}} (optional) #5 - placement of the object (default value \north)
%%
                      0="\pcent", center
                      1="\north", north
%%
                      2="\northeast", northeast
%%
%%
                      3="\east", east
%%
                      4="\southeast", southeast
                      5="\south", south
%%
%%
                      6="\southwest", southwest
                      7="\west", west
%%
                      8="\northwest", northwest
%%
%%
    !!! Note !!!
   if you omit the #3 argument (label) and the #4 argument is a
    complex LaTeX command this can cause this command to crash. In
%%
   this case you must specify a label (the empty label [], if you do
\mbox{\ensuremath{\mbox{\sc W}}}\mbox{\sc n} needed it it for nothing).
%% Morphims (linear edges). This commando has to two major variants
%% i) Starting and Ending objects specification
    \mor{#1}{#2}[#5,#6]{#7}[#8,#9]
```

```
%% As you can see this first form is (intencionaly) badly formed, the
\ensuremath{\mbox{\%}}\xspace arguments #3 and #4 are missing (the actual command is correctly
%%
%%
          #1 - The starting object reference
%%
          #2 - The ending object reference
%%
%% from this two we will obtain the objects coordinates, and also the
%% dimensions of the enclosing box.
\% The objects box dimensions are used to do an automatic adjustment of
%% the edge width.
\%\% from #1 we obtain (x,y), (#1,#2) in the second form
\%\% from #2 we obtain (x',y'), (#3,#4) in the second form
%%
\% this values will be passed to the command second form
%%
%%ii) Two points coordinates specification
%%
    \mor(#1,#2)(#3,#4)[#5,#6]{#7}[#8,#9]
%%
%% Now we can describe all the arguments
%%
%%
            #1 and #2 - coordinates (beginning)
            #3 and #4 - coordinates (ending)
\%(optional)#5,#6 - correction factors (defaul values, 100 and 100 (10pt))
            #5 - actual beginning of the edge
            #6 - actual ending of the edge
#7 - text (morphism label)
%%
%%
%%(optional)#8,#9
            #8 - label placement
%%
                  1 = "\atright", at right, default value
                -1 = "\atleft", at left
%%
            #9 - edge type
%%
%%
                  0 = "\solidarrow", default edge
                 1 = "\dashArrow"
%%
                 2 = "\dotArrow (thanks to Xingliang Liang <jkl9543@gmail.com>)
%%
%%
                 3 = "\solidline"
                 4 = "\dashline"
%%
                 5 = "\dotline"
%%
%%
                  6 = "\injectionarrow"
                 7 = "\aplicationarrow"
%%
%%
                 8 = "\surjectivearrow"
%%
                 9 = "\equalline" (thanks to Ruben Debeerst <debeerst@mathematik.uni-kassel.de>)
                 10 = "\doublearrow"
%%
%%
                 11 = "\doubleopposite"
                 12 = "\nullarrow" (to allow adding labels to existing arrows)
%%
%%
%% Notes: the equalline "arrow" does not provide a second label.
%%
%% Curved Morphisms (quadratic edges):
%%
    \cmor(#1) #2(#3,#4){#5}[#6]
%%
            #1 - list of points (odd number)
%%
             #2 - tip direction
                0 = "\pup", pointing up
%%
                1 = "\pdown", pointing down
2 = "\pright", pointing right
3 = "\pleft", pointing left
%%
%%
%%
            \#3 and \#4 - coordenates of the label
%%
%%
            #5 - morphism label
%%(optional)#6 - edge type
                0 ="\solidarrow", default value
                1 = "\dashArrow"
%%
                 2 = "\solidline"
%%
```

```
%% Notes: insert a space after the command.
                   the space after the list of points is mandatory
%%
%% Examples:
%% \documentclass[a4paper,11pt]{article}
%% \usepackage{dcpic,pictexwd}
%% \begin{document}
%% \begindc[3]
%% \obj(14,11){$A$}
%% \obj(39,11){$B$}
%% \mor(14,12)(39,12){$f$}%[\atright,\solidarrow]
\mbox{\color=10} \mbo
%% \cmor((10,10)(6,11)(5,15)(6,19)(10,20)(14,19)(15,15))
         \pdown(2,20){$id_A$}
\% \cmor((40,7)(41,3)(45,2)(49,3)(50,7)(49,11)(45,12))
%%
         \pleft(54,3){$id_B$}
%% \enddc
%%
%% \begindc{\commdiag}[3]
%% \obj(10,15)[A]{$A$}
%% \obj(40,15)[Aa]{$A$}
%% \obj(25,15)[B]{$B$}
%\% \operatorname{A}{B}{\frac{\$f}}%[\operatorname{ht,\solidarrow}]
%% \mor{B}{Aa}{$g$}%[\atright,\solidarrow]
%% \cmor((10,11)(11,7)(15,6)(25,6)(35,6)(39,7)(40,11))
%%
         \pup(25,3){$id_A$}
%% \enddc
%%
%% \newcommand{\barraA}{\vrule height2em width0em depth0em}
%% \newcommand{\barraB}{\vrule height1.6em width0em depth0em}
%% \begindc{\commdiag}[35]
%% \obj(1,1)[Gr]{$G$}
%% \obj(3,1)[Grstar]{$G_{r^*}$}
%% \obj(5,1)[H]{$H$}
%% \obj(2,2)[SigmaG]{$\Sigma^G$}
%% \obj(6,2)[SigmaH]{$\Sigma^H$}
%% \obj(1,3)[Lm]{$L_m$}
%% \obj(3,3)[Krm]{$K_{r,m}$}
%% \obj(5,3)[Rmstar]{$R_{m^*}$}
%% \obj(1,5)[L]{$L$}
%% \obj(3,5)[Lr]{$L_r$}
%% \obj(5,5)[R]{$R$}
%% \obj(2,6)[SigmaL]{$\Sigma^L$}
%% \obj(6,6)[SigmaR]{$\Sigma^R$}
%% \mor{Gr}{SigmaG}{$\lambda^G$}
%% \mor{Grstar}{Gr}{$i_5$}[\atleft,\aplicationarrow]
%% \mor{Grstar}{H}{$r^*$}[\atright,\solidarrow]
%% \mor{H}{SigmaH}{$\lambda^H$}[\atright,\dashArrow]
%% \mor{SigmaG}{SigmaH}{$\varphi^{r^*}$}[\atright,\solidarrow]
%% \mor{Lm}{Gr}{$m$}[\atright,\solidarrow]
%% \mor{Lm}{L}{$i_2$}[\atleft,\aplicationarrow]
%% \mor{Krm}{Lm}{$i_3\quad$}[\atright,\aplicationarrow]
%% \mor{Krm}{Rmstar}{$r$}
%% \mor{Krm}{Lr}{$i_4$}[\atright,\aplicationarrow]
%% \mor{Krm}{Grstar}{$m$}
%% \mor{Rmstar}{R}{$i_6$}[\atright,\aplicationarrow]
%% \mor{Rmstar}{H}{$m^*$}
%% \mor{L}{SigmaL}{$\lambda^L$}
%% \mor{Lr}{L}{$i_1\quad$}[\atright,\aplicationarrow]
%% \mor{Lr}{R}{$r$}
%% \mor{R}{SigmaR}{$\lambda^R$}[\atright,\solidarrow]
%% \mor{SigmaL}{SigmaG}{$\varphi^m$}[\atright,\solidarrow]
%% \mor{SigmaL}{SigmaR}{$\varphi^r$}
%% \mor{SigmaR}{SigmaH}{$\varphi^{m^*}$}
%% \enddc
```

```
%% \end{document}
%% Modifications (9/1993)
         argument "distance" between de tip of the arrow and the objects
%%
         became optional; a new option for the "arrows" (option 3)
%% 2/3/1995 (version 1.3)
         adds "the aplication arrow" (option 4); the distance between
         the label and the "arrow" is now a fixed value (100 units).
%%
%% 15/7/1996 (version 2.1)
         The comand "\mor" has a new sintax. The 5th and 6th
%%
         parameters are now the distance between the two objects and
%%
         the arrow tips. The 7th parameter is the label. The 8th e 9th
%%
         parameters (label position and type of arrow) are now optional
%%
%% 5/2001 (version 3.0)
         Implementation of the comand "\cmor" based on the quadratic
%%
         curver comand of PiCTeX
%%
%% 11/2001 (version 3.1)
%%
         Changes on the tips of the arrow to became more LaTeX style
%%
         (after a conversation on EuroTeX 2001).
%%
%% 1/2002 (version 3.2)
%%
         Modification of the commands "obj" and "mor" in such a way
%%
         that allows the logical specification of the morphisms, that
%%
         is, it is now possible to specify the starting object and the
%%
         ending object instead of specify the coordinates.
%%
%%
         The length of the arrows is automatically trimmed to the
%%
         objects' size.
%%
%% 5/2002 (version 4.0)
         New syntax for the commands "begindc" e "obj"
%%
%% !!! New syntax !!!
         The command "begindc" now have an obligatory argument, this
%%
%%
         argument allows the specification of the graph type
           "commdiag" (0), commutative diagrams
"digraph" (1), directed graphs
%%
%%
%%
           "undigraph" (2), undirected graphs
%%
         The command "obj" has a new syntax: after the coordinates
         specification, an optional argument specifying a label, an
%%
%%
         obligatory argument given the "value" of the object and the
         final optional argument used in the graphs to set the
%%
%%
         relative position of the "value" to the "dot" defining the
%%
         objects position, the default value is "north".
%%
%% 3/2003 (version 4.1)
         Responding to a request of Jon Barker <jeb1@soton.ac.uk> I
%%
%%
         create a new type of arrow, the surjective arrow.
%%
         For now only horizontal and vertical versions, other angles
%%
         are poorly rendered.
%% 12/2004 (version 4.1.1)
%%
         New version for the surjective arrows, solve the problems
         with the first implementation of this option.
%%
%% 3/2007 (version 4.2)
%%
         Adds the "providespackage" directive that was missing.
%%
         Adds dashed lines, and dotted lines.
%% 5/2008 (version 4.2.1)
%%
         Deleting some counters, trying to avoid the problem "running
         out of counters", that occurs because of the use of {\tt PiCTeX}
%%
         and DCpic (only two...)
%% 8/2008 (version 4.3)
%%
         Thanks to Ruben Debeerst (debeerst@mathematik.uni-kassel.de),
         he added a new arrow "equalline". After that I
```

```
%%
         decided to add: the doublearrow; the doublearrow with
%%
         opposite directions; the null arrow. This last can be used as
%%
         a simple form of adding new labels.
%%12/2008 (version 4.3.1)
         The comand \id is internalised (\!id), it should be that way
%%
%%
         from the begining because it is not to be used from the
%%
%%
         The comand \dasharrow was changed to \dashArrow to avoid a
%%
         clash with the AMS command with the same name.
%%12/2009 (version 4.3.2)
         There is a conflict between dcpic.sty and hyperref in current
%%
%%
          texlive-2009 due to the one letter macro \d (thanks Thorsten
          S <thorsten.schwander@gmail.com>).
%%
          The \d changed to \d (Euclidian Distance). The \x and \y
%%
          changed to \x0 \y0
%% 4/2013 (version 4.4.0)
%%
         Thanks to Xingliang Liang <jkl9543@gmail.com>. He added a new
         arrow "dotarrow".
%% 5/2013 (version 5.0)
%%
         The base scale of the graph has changed from 1pt to .1pt to
%%
         solve a problem with the implementation of the oblique
%%
         equalline (Thanks to Antonio de Nicola).
%%
         The LaTeX circle and oval commands where replaced by the
%%
         PiCTeX circulararc and ellipticalarc commands to avoid
%%
         differences in scales.
      -----//-----
\catcode'!=11 % ***** THIS MUST NEVER BE OMITTED (See PiCTeX)
\newcount\aux%
\newcount\auxa%
\newcount\auxb%
\newcount\x0%
\newcount\y0%
\newcount\x1%
\newcount\yl%
\newcount\deuc%
\newcount\dnm%
\newcount\xa%
\newcount\xb%
\newcount\xmed%
\newcount\xc%
\newcount\xd%
\newcount\xe
\newcount\xf
\newcount\ya%
\newcount\yb%
\newcount\ymed%
\newcount\yc%
\newcount\yd
\newcount\ye
\newcount\yf
%% "global variables"
\newcount\expansao%
\newcount\tipografo%
                           version 4.0
\newcount\distanciaobjmor% version 4.0
\newcount\tipoarco%
                           version 4.0
\newif\ifpara%
%% version 3.2
\newbox\caixa%
\newbox\caixaaux%
\newif\ifnvazia%
\newif\ifvazia%
\newif\ifcompara%
\newif\ifdiferentes%
```

\newcount\xaux%

```
\newcount\yaux%
\newcount\guardaauxa%
\verb|\newcount\alt||
\newcount\larg%
\newcount\prof%
%% for the triming
\newcount\auxqx
\newcount\auxqy
\newif\ifajusta%
\newif\ifajustadist
\def\objPartida{}%
\def\objChegada{}%
\def\objNulo{}%
%% Stack specification
%%
%%
%% Emtpy stack
%%
\def\!vazia{:}
%% Is Empty? : Stack -> Bool
%% nvazia - True if Not Empy
%% vazia - True if Empty
\def\!pilhanvazia#1{\let\arg=#1%
\if:\arg\ \nvaziafalse\vaziatrue \else \nvaziatrue\vaziafalse\fi}
%%
\% Push : Elems x Stack -> Stack
%% Top : Stack -> Elems
\mbox{\%} the empty stack is not taken care
%% the element is "kept" ("guardado")
\def\!guarda(#1)(#2,#3)(#4,#5,#6){\def\!id{#1}%
\xaux=#2%
\yaux=#3%
\alt=#4%
\larg=#5%
\prof=#6%
\def\!topaux#1.#2:{\!guarda#1}
\def\!topo#1{\expandafter\!topaux#1}
%% Pop : Stack -> Stack
%%
\mbox{\%} the empty stack is not taken care
\def\!popaux#1.#2:{\def\pilha{#2:}}
\def\!retira#1{\expandafter\!popaux#1}
%% Compares words : Word x Word -> Bool
%%
%% compara - True if equal
\%\% diferentes - True if not equal
\ifx\argA\argB\comparatrue\diferentesfalse\else\comparafalse\diferentestrue\fi}
```

```
\def\!compara#1#2{\!comparaaux{#1}{#2}}
%% Private Macro
%% Absolute Value)
%% \absoluto{n}{absn}
%% input
%% n - integer
%% output
%% absn - |n|
\def\!absoluto#1#2{\aux=#1%
  \lim \a > 0
    #2=\aux
  \else
    \multiply \aux by -1
    #2=\aux
  fi
\mbox{\ensuremath{\mbox{\%}}{\mbox{\ensuremath{\mbox{\sc Name}}}} Name definitions for edge types and directions
\def\solidarrow{0}
\def\dashArrow{1}
\def\dotArrow{2}
\def\solidline{3}
\def\dashline{4}
\def\dotline{5}
\def\injectionarrow{6}
\def\aplicationarrow{7}
\def\surjectivearrow{8}
\def\equalline{9}
\def\doublearrow{10}
\def\doubleopposite{11}
\def\nullarrow{12}
\mbox{\ensuremath{\mbox{\sc M}}\sc M}\mbox{\sc Mame} 

 Mame definitions for edge label placement
\def \arright \{-1\}
\def \left\{ 1 \right\}
\%\% Tip direction for curved edges
\def\pdown{1}
\def\pright{2}
\left( \frac{3}{3} \right)
%% Type of graph
\def\commdiag{0}
\def\digraph{1}
\def\undigraph{2}
\def\cdigraph{3}
\def\cundigraph{4}
%% Positioning of labels in graphs
\left( \right) 
\def\north{1}
\def\northeast{2}
\left( \frac{3}{3} \right)
\def\southeast{4}
\left( \frac{5}{5} \right)
\def\southwest{6}
\def\west{7}
\def\northwest{8}
%%Private Macro
\% Adjust the distance between the arrows and the objects regarding
%% the dimensions of the objects.
%%
%% \alpha_x^{x}_{y}_{y}_{d}_{0bject} (ajusta = adjust)
%%
%% Input
\% (x,y) e (x1,y1) - start, end coordinates of arrow
```

```
\% d - distance specified by the user (default value, 100)
%% Objecto - reference of the object pointed by the arrow
%% Output
%% d - adjusted distance
%%
\ensuremath{\text{\%}}\xspace The adjusted distance is the greatest value between 100 and the
%% object's box dimensions. If the user specify a value this is not
%% altered.
%%
%% If the arrow is horizontal the length is used.
\ensuremath{\mbox{\%}}\xspace If the arrow is vertical the height is used for arrows in the 1st
\%\% or 2nd quadrante, or the depth if the arrow is in the 3rd or 4th
\% quadrante. If the arrow is oblique the value is chosen accordingly:
%% from 315 to 45 degrees length is used
%% from 45 to 135 degrees height is used
\%\% from 135 to 225 degrees length is used
%% from 225 to 315 degrees depth is used
\def\!ajusta#1#2#3#4#5#6{\aux=#5%
  \left| \right| = \#6\%
  \ifcase \tipografo
                         % commutative diagrams
    \ifnum\number\aux=100
      \ajustadisttrue % if needed, adjust
      \ajustadistfalse % if not, keeps unchanged
    \fi
  \else % graphs (directed, undirected, with frames)
   \ajustadistfalse
  \ifajustadist
   \let\pilhaaux=\pilha%
   \loop%
     \t \int \int \int \int dx \, dx
     \verb|\retira{\pi}| %
     \!compara{\!id}{\auxobj}%
     \ifnvazia%
   \repeat%
\mbox{\%} push the values into the stack
   \let\pilha=\pilhaaux%
   \ifvazia%
    \ifdiferentes%
\mbox{\ensuremath{\%}}\mbox{\ensuremath{\%}} It is not possible to make de adjustment given the fact that the
%% user did not provide a label for the object in question. We set a
%% value equal to the default value (100)
%%
     \arrowvert = 131072\% these values are for unit of .1pt
     \prof=65536%
     \alt=65536%
    \fi%
   \fi%
   \displaystyle \dot \ these values are for unit of .1pt
   \divide\prof by 6553%
   \divide\alt by 6553%
   \ifnum\number\y0=\number\y1
%% Case 1 -- horizontal arrow
%% with the division by 13107 we get half the size of the box, for a
\mbox{\%\%} centered text, the adding of 30 is an empirical adjustment.
    \advance\larg by 30
    \ifnum\number\larg>\aux
     #5=\larg
    \fi
   \else
    \ifnum\number\x0=\number\x1
     \ifnum\number\yl>\number\y0
```

```
%% Case 2.1 -- vertical arrow, down direction
%%
                    \ifnum\number\alt>\aux
                       #5=\alt
                   \fi
                \else
 %% Case 2.2 -- vertical arrow, up direction
\% with the division by 6553 we get the box height. The adjustment
%% of 50 is an empirical adjustment.
                   \advance\prof by 50
                   \ifnum\number\prof>\aux
                      #5=\prof
                   \fi
                \fi
             \else
%% Case 3 -- oblique arrow
%% Case 3.1 --- from 3150 to 450; |x-x1|>|y-y1|
%% Case 3.3 --- from 1350 to 2250; |x-x1|>|y-y1|; Length
                \average{$\mathbb{Z}$} \ave
                \advance \auxqx by -\xl
                \verb|\absoluto{\auxqx}{\auxqx}| %
                \ay = y0
                \advance \quad yl
                \!absoluto{\auxqy}{\auxqy}%
                \ifnum\auxqx>\auxqy
                    \injlies 100
                      \larg=100
                    \fi
                   \advance\arg by 30
                   #5=\larg
                \else
\% Case 3.2 --- from 450 to 1350; |x-x1| < |y-y1| e y>0; Length
                   \int \frac{y1}{y0}
                      \injlies 100
                           \larg=100
                       \fi
                    \advance\alt by 60
                      #5=\alt
                   \else
\% Case 3.4 -- from 225o to 315o; |x-x1| < |y-y1| e y<0; Depth
                  \advance\prof by 110
                      #5=\prof
                  \fi
                \fi
            \fi
 \fi} % the branch else is missing
%%Private Macro
%% Square root
%% raiz{n}{m} (raiz = root)
%% ->
%% n - natural number
%% <-
\% n - natural number
 \mbox{\%\%} \, m - greatest natural number less then the square root of n \,
 \def\!raiz#1#2{\auxa=#1%
      \auxb=1%
      \loop
             \aux=\auxb%
             \advance \aux by 1\%
             \multiply \aux by \aux%
             \ifnum \aux < \auxa%
                    \advance \auxb by 1%
                    \paratrue%
```

```
\else\ifnum \aux=\auxa%
      \advance \auxb by 1%
      \paratrue%
       \else\parafalse%
       \fi
    \fi
  \ifpara%
  \repeat
#2=\auxb}
%%Private Macro
\ensuremath{\mbox{\%}}\xspace Find the starting and ending points of the "arrow" and also the
%% label position (one coordinate at a time)
% ucoord{x1}{x2}{x3}{x4}{x5}{x6}{+|-1}
%% Input
%% x1,x2,x3,x4,x5
%% Output
%% x6
%%
%% x6 = x3 +|- ---- x4
%%
                  x5
\def\!ucoord#1#2#3#4#5#6#7{\aux=#2%
  \advance \aux by -#1%
  \multiply \aux by #4%
  \divide \aux by #5%
  \advance \aux by #3%
#6=\aux}
%%Private Macro
\% Euclidean distance between two points
%% quadrado = square
%%
% quadrado{n}{m}{1}
%% Input
%% n - natural number
%% m - natural number
%% Output
\% 1 = (n-m)*(n-m)
\def\!quadrado#1#2#3{\aux=#1%
  \advance \aux by -#2\%
  \multiply \aux by \aux%
#3=\aux
%%Private Macro
\ensuremath{\mbox{\%}}\xspace Euclidean distance between arrows and its tags
%%
%% Input
%%
       (x,y), (x',y') morphism's name (tag)
%% Output
       dnm - distance between an arrow and its tags
%%
%%
       (with a trim given by the tag's size
%% Observations
%%
       The trimming is for horizontal and vertical arrows
       only. Oblique arrows are dealt in a different way
%%
%%
%% Algorithm
%% caixa0 <- morfism name</pre>
\% if x-xl = 0 then
                                        {vertical arrow}
      aux <- caixa0 width
%%
       dnm <- converstion-sp-pt(aux)/2+3</pre>
                                        {non-vertical arrow}
%% else
    if y-y1 = 0 then
                                        {horizontal arrow}
```

```
%%
                         aux <- caixa0 height+depth
%%
                         dnm <- converstion-sp-pt(aux)/2+3</pre>
%%
                  else
                                                                                                  {oblique arrow}
%%
%%
                 endif
%% endif
%% endalgorithm
\def\!distnomemor#1#2#3#4#5#6{\setbox0=\hbox{#5}%
     \advance \aux by -#3
     \ifnum \aux=0
            \aux=\wd0 \divide \aux by 13107%2
            \advance \aux by 30
            #6=\aux
     \else
            \aux=#2
            \advance \aux by -#4
            \ifnum \aux=0
                    \aux=\ht0 \advance \aux by \dp0 \divide \aux by 13107\%2
                    \advance \aux by 30
                    #6=\aux%
            \else
            #6=30
            \fi
        \fi
}
%%
\mbox{\em \%} The environment "begindc...enddc"
%%
\def\begindc#1{\!ifnextchar[{\!begindc{#1}}{\!begindc{#1}[30]}}
\def\!begindc#1[#2]{\beginpicture
     \let\pilha=\!vazia
     \setcoordinatesystem units <.1pt,.1pt>
     \expansao=#2
     \ifcase #1
          \distanciaobjmor=100
          \tipoarco=0
                                                           % arrow
          \tipografo=0
                                                           % commutative diagram
     \or
          \distanciaobjmor=20
          \tipoarco=0
                                                            % arrow
                                                            % directed graph
          \tipografo=1
          \distanciaobjmor=10
                                                           % line
          \tipoarco=3
                                                            % undirected graph
          \tipografo=2
     \or
          \distanciaobjmor=80
                                                           % arrow
          \tipoarco=0
          \tipografo=3
                                                            % directed graph
          \distanciaobjmor=80
                                                           % line
          \tipoarco=3
          \tipografo=4
                                                            % undirected graph
     \fi}
\def\enddc{\endpicture}
\def\drawarrowhead <#1> [#2,#3]{%}
     \int $$ \left( \frac{1}{\#2}{\#3}}{\int ${1}{\#2}{\#3}}{\int ${1}{\#2}{\#3}}} \right) $$
% Xingliang Liang <jkl9543@gmail.com>
% ** \!ljoin (XCOORD,YCOORD)
\mbox{\ensuremath{\mbox{\%}}}\quad \mbox{\ensuremath{\mbox{**}}}\quad \mbox{\ensuremath{\mbox{Draws}}} \mbox{\ensuremath{\mbox{a}}} \mbox{\ensuremath{\mbox{straight}}} \mbox{\ensuremath{\mbox{line}}} \mbox{\ensuremath{\mbox{straight}}} \mbox{\ensuremath{\mbox{a}}} \mbox{\ensuremath{\mbox{c}}} \mbox{\ensuremath{\mbox{c}}} \mbox{\ensuremath{\mbox{c}}} \mbox{\ensuremath{\mbox{c}}} \mbox{\ensuremath{\mbox{c}}} \mbox{\ensuremath{\mbox{c}}} \mbox{\ensuremath{\mbox{**}}} \mbox{\ensuremath{\mbox{c}}} \mbox{\ensuremath{
                   by the most recent \!start, \!ljoin, or \!qjoin, and
```

```
ending at (XCOORD, YCOORD).
\def\!ljoindummy (#1,#2){%
  \advance\!intervalno by 1
  \xE=\M{\#1}\xunit \yE=\M{\#2}\yunit
  \!rotateaboutpivot\!xE\!yE
  \!ydiff=\!yE \advance \!ydiff by -\!yS%** ydiff = yE - yS
\!Pythag\!xdiff\!ydiff\!arclength% ** arclength = sqrt(xdiff**2+ydiff**2)
  \global\advance \totalarclength by \!arclength%
  %\!drawlinearsegment% ** set by dashpat to \!linearsolid or \!lineardashed \!xS=\!xE \!yS=\!yE% ** shift ending points to starting points
  \ignorespaces}
%% \!drawarrowhead{4pt}{DimC}{DimD} <xshift,yshift> from {\xa} {\ya} to {\xb} {\yb}
\def\!drawarrowhead#1#2#3<#4,#5> from #6 #7 to #8 #9 {%
% ** convert to dimensions
  \label{eq:loc=\!M{#8}\!xunit}
  \label{eq:loc=local} $$ \| vloc=\!M{\#9}\! vunit 
  \!dxpos=\!xloc \!dimenA=\!M{#6}\!xunit \advance \!dxpos -\!dimenA \!dypos=\!yloc \!dimenA=\!M{#7}\!yunit \advance \!dypos -\!dimenA
  \let\!MAH=\!M%
                                              ** save current c/d mode
  \!setdimenmode%
                                              ** go into dimension mode
  \!xshift=#4\relax \!yshift=#5\relax% ** pick up shift
  \!reverserotateonly\!xshift\!yshift% ** back rotate shift
  \advance\!xshift\!xloc \advance\!yshift\!yloc
% ** draw shaft of arrow
  \!xS=-\!dxpos \advance\!xS\!xshift
\!yS=-\!dypos \advance\!yS\!yshift
  \!start (\!xS,\!yS)
  \!ljoindummy (\!xshift,\!yshift)
\% ** find 32*cosine and 32*sine of angle of rotation
  \!Pythag\!dxpos\!dypos\!arclength
  \!divide\!dxpos\!arclength\!dxpos
  \!dxpos=32\!dxpos \!removept\!dxpos\!!cos
  \!divide\!dypos\!arclength\!dypos
  \!dypos=32\!dypos \!removept\!dypos\!!sin
% ** construct arrowhead
  \ \ \!halfhead{#1}{#2}{#3}%
                                              ** draw half of arrow head
                                              ** draw other half
  \l!halfhead{#1}{-#2}{-#3}%
  \left| \right| M = \| MAH\%
                                              ** restore old c/d mode
  \ignorespaces}
%% Public macro: "mor"
%% Funtion to built the "arrow" between two points
%%
\mbox{\ensuremath{\%}{\sc k}} The points that are uses to built all the elements of the "arrows"
%% are:
%%
%%
                    (xc,yc)
%%
                       0
                       ---0---
%%(x,y) (xa,ya) (xm,ym) (xb,yb)(x1,y1)
%% auxa - distance between (x,y) and (xa,ya), 10pt by default
\mbox{\%} auxb - distance between (x1,y1) and (xb,yb), 10pt by default
```

```
\def\mor{%
 \!ifnextchar({\!morxy}{\!morObjA}}
\def\!morxy(#1,#2){%
 \int {1}{\#2}}{\int {1}{\#2}}{\int {1}{\#2}}}
\def\!morxyl#1#2(#3,#4){%
 \def\!morObjA#1{%
 \let\pilhaaux=\pilha%
 \def\objPartida{#1}%
 \loop%
   \t \int t \, dx \, dx
   \!retira\pilha%
   \!compara{\!id}{\objPartida}%
   \ifcompara \nvaziafalse \else \!pilhanvazia\pilha \fi%
  \ifnvazia%
 \repeat%
 \ifvazia%
 \ifdiferentes%
%%
\mbox{\%} error message and ficticious parameters
%%
  Error: Incorrect label specification%
  \xaux=1%
  \yaux=1%
 fi%
 \fi%
 \left| \right| 
 \def\!morObjB#1#2#3{%
 \x0=#1
 \y0=#2
 \let\pilhaaux=\pilha%
 \loop
   \verb|\topo\pilha| %
   \!retira\pilha%
   \!compara{\!id}{\objChegada}%
   \ifcompara \nvaziafalse \else \!pilhanvazia\pilha \fi
 \repeat
 \ifvazia
 \ifdiferentes%
%% error message and ficticious parameters
%%
  Error: Incorrect label specification
  \x=\x0\%
  \advance\xaux by \x0\%
  \gamma = y0\%
  \advance\yaux by \y0%
 \fi
 \fi
 \let\pilha=\pilhaaux
 \!ifnextchar[{\!mora{\number\x0}{\number\xaux}{\number\yaux}}{\!mora{\number\x0}{\number\x0x3\}\\
\def\!mora#1#2#3#4[#5,#6]#7{%
 \label{limits} $$ \left(\frac{1}{morb}{#1}{#2}{#3}{#4}{#5}{#6}{#7}{1,\number\tipoarco} \right) $$
\def\!morb#1#2#3#4#5#6#7[#8,#9]{\x0=#1%
 \y0=#2%
 \x1=#3%
 \y1=#4%
 \multiply \x0 by \expansao%
 \multiply \y0 by \expansao%
 \multiply \xl by \expansao%
 <section-header>
%% Euclidean distance between two points
```

```
\% d = \sqrt((x-x1)^2+(y-y1)^2)
%%
   \deuc=\auxa%
   \advance \deuc by \auxb%
   \!raiz{\deuc}{\deuc}%
%% the point (xa,ya) is at a distance #5 (default value 100) from the
%% point (x,y)
%%
%% given the fact that we have two points (start,end) we need to
%% recover their value searching the stack
   \!compara{\objNulo}{\objPartida}%
   \ifdiferentes% adjusting only when needed
     \label{x0}{\x1}{\y0}{\y1}{\auxa}{\objPartida}%
     \ajustatrue
     \%\% save the value of aux (after adjustment) to be used in the case of
%% an injective morphism
   \guardaauxa=\auxa
%%
   \label{eq:linear_conditions} auxa has the value of the distance between the objects minus the
%% distance between the arrow and the objects (100 default value)
   \auxa=\deuc%
%%
%% the point (xb,yb) is at a distance #6 (default value 100) from the
%% point (x1,y1)
%%
   \auxb=#6
   \!compara{\objNulo}{\objChegada}%
   \ifdiferentes% adjusting only when needed
% adjustment
     \label{label} $$ \simeq {\x0}{\x1}{\y0}{\x1}{\auxb}{\chegada}%
     \def\objChegada{}% reset the value of the end object
   \advance \auxa by -\auxb%
   \advance \xmed by \xb%
   \divide \xmed by 2
   \mbox{\ymed=\ya}
   \advance \ymed by \yb%
   \divide \ymed by 2
%% find the coordinates of the label position: (xc,yc)
%%
\% after this the values of xmed and ymed are no longer important
%%
   \label{number} $$ \label{number}deuc}_{\number}\deuc}_{\number}deuc}_{\number}deuc}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_{\number}_
   %% draw the "arrow"
%%
\ifcase #9
                                    % 0=solid arrow
   \arrow < 4pt > [.2,1.1] from {\xa} {\ya} to {\xb} {\yb}
                                    % 1=dashed arrow
   \setdashes <2pt>
   \plot {\xa} {\ya} {\xb} {\yb} /
   \setsolid%
```

```
\or
                 % 2=dotted arrow (Xingliang Liang <jkl9543@gmail.com> - 4.4.0)
 \setdots <2pt>
 \plot {\xa} {\ya} {\xb} {\yb} /
 \setsolid%
 \displaystyle \drawarrowhead <4pt> [.2,1.1] from {\xa} {\ya} to {\xb} {\yb}
\or
                 % 3=solid line
 \setlinear
 \plot {\xa} {\ya} {\xb} {\yb} /
                 % 4=dashed line
\or
 \setdashes <2pt>
 \setlinear
 \plot {\xa} {\ya} {\xb} {\yb} /
 \setsolid
\or
                 % 5=dotted line
 \setdots <2pt>
 \setlinear
 \plot {\xa} {\ya} {\xb} {\yb} /
 \setsolid
                 % 6=injective arrow
%%
\%\% 30 units, the radius for the tail of the arrow
%%
%% recover the value of auxa
 \auxa=\guardaauxa
%% makes an adjustment to cope with the tail of the arrow, giving
%% space to the semi-circle
 \advance \auxa by 30%
%%
%% Note: the values of (xa,ya) will be modified, they will be
%% "pushed" further away from (x,y) in order to acomodate the tail
%% of the "arrow"
%%
\%\% find the point (xd,yd), the center of a 2pt (20*0.1) circle
%%
\label{lower} $$ \sup_{\mathbf{y}}_{\mathrm{number}}_{1}_{\mathrm{number}}_{20}_{\mathrm{number}}_{1}% $$
 %% building the "arrow"
 \arrow <4pt> [.2,1.1] from {\xa} {\ya} to {\xb} {\yb}
%% and its "tail"
 \circulararc -180 degrees from {\xa} {\ya} center at {\xd} {\yd}
                 % 7=maps "arrow" ("|-->")
\or
 \auxa=20 %
%%
%% Note: the values of xmed and ymed will be modified
%%
%% find the two points that defines the tail of the arrow (segment
%% (xmed,ymed)(xd,yd))
\!ucoord{\number\y0}{\number\y1}{\number\aa}{\number\deuc}{\xd}{1}%
%% building the "arrow"
 \label{eq:condition} $$\operatorname{\sqrt{4pt}} [.2,1.1] from {\xa} {\ya} to {\xb} {\yb}$
%% and its "tail"
 \setlinear
 % 8=surjective arrow ("-->>")
%% building arrow with the first tip
 \arrow <4pt> [.2,1.1] from {\xa} {\ya} to {\xb} {\yb}
%% and the second tip
 \setlinear
 \arrow < 6pt > [0,.72] from {\xa} {\ya} to {\xb} {\yb}
                 % 9=equalline
\or
```

```
%% by Ruben Debeerst: equal-line
\% sets the separation (distance) between the two parallel lines, if
%% horizontal or vertical 1pt (10*0.1) is enough, if not 1.1pt (11*0.1)
\auxa=11
\ifnum\number\y0=\number\y1
\auxa=10
\fi
\ifnum\number\x0=\number\x1
\auxa=10
\fi
%% the two parallel lines will be given by (xmed,ymed)(xd,yd), and
%% (xe,ve)(xf,vf)
   \label{lower} $$ \sup_{\mathbf x_0}_{\mathbf x_0}_{\mathbf x_0}_{\mathbf x_0}_{\mathbf x_0}^{\mathbf x_0}_{\mathbf x_0}^{\mathbf x_0}_{\mathbf x_0}^{-1}%
   \!ucoord{\number\y0}{\number\xb}{\number\auxa}{\number\deuc}{\xf}{1}%
   \setlinear
   \plot {\xmed} {\ymed} {\xe} {\ye} /
   \plot {\xd} {\yd} {\xf} {\yf} /
                                   % 10=double arrow
\or
%%
\%\% sets the separation (distance) between the two parallel lines, if
\mbox{\%}\mbox{\sc horizontal} or vertical 2pt is enough, if not 2.5pt. The extra space
%% is needed because of the arrow tip.
\auxa=25
\ifnum\number\y0=\number\y1
\auxa=20
\fi
\int \sum_{x=0}^{\infty} \sum_{x=0}^{\infty} x^{x} = \sum_{x=0}
\auxa=20
\fi
%% the two parallel lines will be given by (xmed,ymed)(xd,yd), and
%% (xe,ye)(xf,yf)
  \label{lower} $$ \sup_{\mathbb N^2}{\sum_{\mathbb N^2}_{\mathbb N^2}}{\sum_{\mathbb N^2}_{\mathbb N^2}} C_{\mathbb N^2}.
   \arrow <4pt> [.2,1.1] from {\xmed} {\ymed} to {\xe} {\ye}
  \arrow < 4pt > [.2,1.1] from {\xd} {\yd} to {\xf} {\yf}
\or
                                   \mbox{\ensuremath{\mbox{\%}}} 10=double arrow, opposite directions
%% sets the separation (distance) between the two parallel lines, if
%% horizontal or vertical 2pt is enough, if not 2.5pt. The extra space
%% is needed because of the arrow tip.
\auxa=22
\ifnum\number\y0=\number\y1
\auxa=20
\fi
\int \mathbb{Z} = \sum_{x\in \mathbb{Z}} \mathbb{Z}
\auxa=20
\fi
%% the two parallel lines will be given by (xmed,ymed)(xd,yd), and
%% (xe,ye)(xf,yf)
```

```
\label{lower} $$ \sup_{\mathbf x_0}{\sum_{x_0}^{number\x0}_{number\auxa}_{number\deuc}} {-1}% $$
 \arrow <4pt> [.2,1.1] from {\xmed} {\ymed} to {\xe} {\ye}
 \arrow < 4pt > [.2,1.1] from {\xf} {\yf} to {\xd} {\yd}
                 \% 11=null arrow (no arrow, only a label)
\or
%%
%% does not draw the arrow, it allows to put two labels in one "arrow"
%%
\fi
%% The label positioning.
%% If the arrows are horizontal or verticals the box is built centered
%% in the object center. If the arrows are oblique the box is built in
%% such a way to avoid the arrow label, having in account the
\mbox{\%\%} quadrante and the relative position of the arrow and the
%% corresponding label
\alpha=x
\advance \auxa by -\x0%
\ifnum \auxa=0
 \put {#7} at {\xc} {\yc}
\else
 \auxb=\yl
 \advance \auxb by -\y0\%
 \int \int u dx dx = 0  at {\xc} {\yc}
 \else
   \lim \ad > 0
    \ifnum \auxb > 0
      \ifnum #8=1
        \put {#7} [rb] at {\xc} {\yc}
      \else
       \put {#7} [lt] at {\xc} {\yc}
      \fi
     \else
      \ifnum #8=1
        \put {#7} [lb] at {\xc} {\yc}
      \else
       \put {#7} [rt] at {\xc} {\yc}
      \fi
    \fi
   \else
     \ifnum \auxb > 0
      \ifnum #8=1
        \put {#7} [rt] at {\xc} {\yc}
      \else
       \put {#7} [lb] at {\xc} {\yc}
      \fi
    \else
      \ifnum #8=1
       \put {#7} [lt] at {\xc} {\yc}
      \else
        \put {#7} [rb] at {\xc} {\yc}
      \fi
    \fi
   \fi
 \fi
\fi
}
%%
%% Curved arrow command
%%
%% \cmor(<list of points (n. odd)>){<label>}
```

```
%% The plot must be changed in such a way that its syntax is coherent
%% with the other commands
%%
\def\modifplot(#1{\!modifqcurve #1}
\def\! modifqcurve(\#1,\#2){\x0=\#1\%}
  \multiply \x0 by \expansao%
  \multiply \y0 by \expansao%
  \!start (\x0,\y0)
  \!modifQjoin}
\def': modifQjoin(#1,#2)(#3,#4){\x0=#1%}
  \y0=#2%
  \x1=#3%
  \yl=#4%
  \multiply \x0 by \expansao%
  \multiply \y0 by \expansao%
  \multiply \xl by \expansao%
  \multiply \yl by \expansao%
  \iny (x0,y0) (x1,y1)
                                     % \!qjoin is defined in QUADRATIC
  \!ifnextchar){\!fim}{\!modifQjoin}}
\def\!fim){\ignorespaces}
\ensuremath{\text{\%}}\xspace The command to draw the arrow tip receives the list of points, get
%% from it the last pair of points and depending of the user choice
\ensuremath{\text{\%\%}} the arrow tip is drawn.
\def\setaxy(#1{\!pontosxy #1}
\def\!pontosxy(#1,#2){%
  \!maispontosxy}
\def\!maispontosxy(#1,#2)(#3,#4){%
  \!ifnextchar){\!fimxy#3,#4}{\!maispontosxy}}
\def\!fimxy#1,#2){\x0=#1%
  \y0=#2
  \multiply \x0 by \expansao
  \multiply \y0 by \expansao
  \x1=\x0\%
  \yl=\y0%
  \aux=1%
  \multiply \aux by \auxa%
  \advance\xl by \aux%
  \aux=1%
  \multiply \aux by \auxb%
  \advance\yl by \aux%
  \arrow < 4pt > [.2,1.1] from {\x0} {\y0} to {\x1} {\y1}}
%%
%% The definition of the command "cmor"
%%
\def\cmor#1 #2(#3,#4)#5{%
  \left(\frac{41}{42},\frac{43}{45}\right)^{1}
\def\!cmora#1#2#3#4#5[#6]{%
  \ifcase #2% "\pup" (pointing up)
      \auxa=0% x do not change
      \auxb=1% y "up"
    \or% \pdown" (pointing down)
      \auxa=0% x do not change
      \auxb=-1% y "down"
    \or% "\pright" (pointing right)
      \auxa=1% x "right"
      \auxb=0% y do not change
    \or% "\pleft" (pointing left)
      \alpha=-1\% x "left"
      \auxb=0% y do not change
```

```
\fi % the line
  \ifcase #6 % arrow solid
    \modifplot#1% draw the line
    % and the arrow tip
    \setaxy#1
  \or % arrow (with tip) dashed
    \setdashes
    \modifplot#1% draw the line
    \setaxy#1
    \setsolid
  \or % arrow (without tip)
    \modifplot#1% draw the line
  \fi % injection morphism
%% label
  \x0=#3%
  \y0=#4%
  \multiply \x0 by \expansao%
  \multiply \y0 by \expansao%
  \put {#5} at {\x0} {\y0}}
%% Command to build the objects
%% \obj(x,y){<text>}[<label>]
%%
\def\obj(#1,#2){%
  \!ifnextchar[{\!obja{#1}{#2}}{\!obja{#1}{#2}[Nulo]}}
\def\!obja#1#2[#3]#4{%
  \!ifnextchar[{\!objb{#1}{#2}{#3}{#4}}{\!objb{#1}{#2}{#3}{#4}[1]}}
\def\!objb#1#2#3#4[#5]{%
  \x0=#1%
  \y0=#2%
  \def\!pinta{\normalsize$\bullet$}% sets the normal size of the bullet
  \def\!nulo{Nulo}%
  \def\!arg{#3}%
  \!compara{\!arg}{\!nulo}%
  \ifcompara\def\!arg{#4}\fi%
  \multiply \x0 by \expansao%
  \multiply \y0 by \expansao%
  \setbox\caixa=\hbox{#4}%
  \auxa=\wd\caixa \divide \auxa by 13107%2
  \advance \auxa by 50
  \auxb=\ht\caixa
  \advance \auxb by \number\dp\caixa
  \divide \auxb by 13107%2
  \advance \auxb by 50
  \ifcase \tipografo
                       % commutative diagrams
   \put{#4} at {\x0} {\y0}
  \or
                       % directed graphs
   \ifcase #5 % c=0, placement of the object (c=center)
     % n=1
      \advance \y0 by \number\auxb % height+depth+5
      \or
              % ne=2
      \begin{array}{l} \begin{array}{l} \begin{array}{l} \begin{array}{l} \\ \end{array} \end{array} \end{array} 
      \advance \auxa by -2 % para fazer o ajuste (imperfeito)
\advance \auxb by -2 % ao raio da circunferencia de centro (x,y)
      \advance \x0 by \number\auxa % width+5
      \advance \y0 by \number\auxb % height+depth+5
      % e=3
      \put{\!pinta} at {\x0} {\y0}
      \advance \x0 by \number\auxa \% width+5
      \put{#4} at {\x0} {\y0}
```

```
% se=4
   \begin{array}{l} \begin{array}{l} \begin{array}{l} \begin{array}{l} \\ \end{array} \end{array} \end{array} 
   \advance \auxa by -2 \% para fazer o ajuste (imperfeito)
    \advance \auxb by -2 % ao raio da circunferencia de centro (x,y)
   \advance \x0 by \number\auxa \% width+5
   \advance \y0 by -\number\auxb % height+depth+5
   \put{#4} at {\x0} {\y0}
            % s=5
 \or
   \begin{array}{l} \begin{array}{l} \begin{array}{l} \begin{array}{l} \\ \end{array} \end{array} \end{array} 
   \advance \y0 by -\number\auxb % height+depth+5
   % sw=6
    \put{\!pinta} at {\x0} {\y0}
   \advance \auxa by -20 \% adjusting to the radius of the circle
   \advance \auxb by -20 % with center in (x,y)
   \advance \x0 by -\number\auxa \% width+5
   \advance \y0 by -\number\auxb % height+depth+5
   \put{#4} at {\x0} {\y0}
            % w=7
    \put{\!pinta} at {\x0} {\y0}
    \advance \x0 by -\number\auxa % width+5
   \or
            % nw=8
   \begin{array}{l} \begin{array}{l} \begin{array}{l} \begin{array}{l} \\ \end{array} \end{array} \end{array} 
   \advance \auxa by -20 \% adjusting to the radius of the circle
   \advance \auxb by -20 % with center in (x,y)
    \advance \x0 by -\number\auxa \% width+5
   \advance \y0 by \number\auxb % height+depth+5
   \fi
\or
                      % undirect graphs
 \ifcase #5 % c=0
   \or
           % n=1
   \advance \y0 by \number\auxb % height+depth+5
   \put{#4} at {\x0} {\y0}
            % ne=2
    \put{\!pinta} at {\x0} {\y0}
   \advance \auxa by -20 % adjusting to the radius of the circle
   \advance \auxb by -20 % with center in (x,y)
   \advance \x0 by \number\auxa % width+5
   \advance \y0 by \number\auxb % height+depth+5
   % e=3
    \put{\!pinta} at {\x0} {\y0}
    \advance \xO by \number\auxa % width+5
   \or
            % se=4
   \advance \auxa by -20 % see above
   \advance \auxb by -20
   \advance \x0 by \number\auxa \% width+5
   \advance \y0 by -\number\auxb % height+depth+5
   % s=5
 \or
   \advance \y0 by -\number\auxb % height+depth+5
   % sw=6
   \begin{array}{l} \begin{array}{l} \begin{array}{l} \begin{array}{l} \\ \end{array} \end{array} \end{array} 
   \advance \auxa by -20 % see above
   \advance \auxb by -20
    \advance \x0 by -\number\auxa \% width+5
   \advance \y0 by -\number\auxb % height+depth+5
    \put{#4} at {\x0} {\y0}
```

```
% w=7
     \advance \x0 by -\number\auxa \% width+5
     \put{#4} at {\x0} {\y0}
             % nw=8
   \or
     \advance \auxa by -20 % see above \advance \auxb by -20
     \advance \x0 by -\number\auxa % width+5 \advance \y0 by \number\auxb % height+depth+5
     \fi
  \else % graphs with circular frames
    \in \mbox{\colored} \ set aux to be the greatest dimension
      \aux=\auxb
    \else
      \aux=\auxa
    \fi
\mbox{\ensuremath{\mbox{\%}}} if the length of the box is less then 1em, the size of the circle is
\% adjust in order not to be less then 10pt
    \ifdim\wd\caixa<1em
      \dim 99 = 10pt
      \aux=\dimen99
      \divide \aux by 13107
      \advance \aux by 50
    \fi
    \advance\aux by -20
    \x1=\x0
    \advance\x1 by \aux
\ifnum\aux<120 % gives (more or less) three digits
      \circulararc 360 degrees from {\xl} {\y0} center at {\x0} {\y0}
    \else
      \fi
    \fi
}
\catcode'!=12 % ***** THIS MUST NEVER BE OMITTED (see PiCTeX)
```