

Immediate vs deferred assignment

Katharine Long

Department of Mathematics and Statistics, Texas Tech University

There are a number of ways to assign values to variables. Full documentation is at:

<http://reference.wolfram.com/language/guide/Assignments.html>

The most common assignment methods will be Immediate

- You will most often use immediate assignment (“=”)

Use this when the expression on the RHS of the assignment can be evaluated

In[1]:= `f[x_] = Sin[x] / (1 + x^2)`

Out[1]=
$$\frac{\sin(x)}{x^2 + 1}$$

The expressions 2 and $\frac{\sin(x)}{1+x^2}$ can be evaluated at the time of assignment, so immediate assignment is used.

- Deferred evaluation (“:=”)

If the RHS of the assignment can’t be evaluated at the time of assignment, use deferred evaluation. This is easiest to explain by example .

- Example: Writing a function to compute arc length of a function to be specified

Recall that the arc length of the curve defined by $f(x)$ is

$$L = \int_a^b \sqrt{1 + \left(\frac{df}{dx}\right)^2} dx.$$

We can’t evaluate the integral until the function $f(x)$ has been specified. In writing a Mathematica function to evaluate arc length given a function f , we must use deferred evaluation.

In[4]:= `arcLength[f_, a_, b_] := Integrate[Sqrt[1 + D[f, x]^2], {x, a, b}]`

The arc length of a constant function $f(x) = c$ on $[0, 1]$ is 1.

In[5]:= `arcLength[c, 0, 1]`

Out[5]= 1

The arc length of $f(x) = x$ on $[0, 1]$ is $\sqrt{2}$.

In[6]:= `arcLength[x, 0, 1]`

Out[6]= $\sqrt{2}$

The arc length of $f(x) = \frac{1}{2}x^2$ is $\int_0^1 \sqrt{1+x^2} \, dx$.

In[7]:= `arcLength[x^2/2, 0, 1]`

Out[7]= $\frac{1}{2}(\sqrt{2} + \sinh^{-1}(1))$

The arc length of $\sin(x)$ is an elliptic integral. There is no closed-form representation of this function.

In[8]:= `arcLength[Sin[x], 0, Pi/2]`

Out[8]= $\sqrt{2} E\left(\frac{1}{2}\right)$

If the integral can't be done in terms of known functions, it's returned unevaluated.

In[9]:= `arcLength[g[x], 0, 1]`

Out[9]= $\int_0^1 \sqrt{g'(x)^2 + 1} \, dx$

In[10]:= `arcLength[Exp[-x^2 + x], 0, 1]`

Out[10]= $\int_0^1 \sqrt{e^{2x-2x^2} (1-2x)^2 + 1} \, dx$

- Example: Writing a plotter for a function with a parameter

We can't plot $(x-t)^2$ against x until the parameter t has been given a value.

In[2]:= `doPlot[t_] := Plot[(x - t)^2, {x, -2, 2}, PlotRange -> {0, 12}]`

In[3]:= `GraphicsRow[{doPlot[0], doPlot[1/2], doPlot[1]}]`

