

Deep Learning

12. Recurrent Neural Networks

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So far...



Perceptron, MLP, Gradient Descent (Backpropagation)

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- Perceptron, MLP, Gradient Descent (Backpropagation)
- 2 CNNs

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- Perceptron, MLP, Gradient Descent (Backpropagation)
- 2 CNNs
- (3) 'Feedforward Neural networks'

Feedforward NNs: some observations



Size of the i/p is fixed(?!)

Feedforward NNs: some observations



- Size of the i/p is fixed(?!)
- Successive i/p are i.i.d.

Feedforward NNs: some observations



- Size of the i/p is fixed(?!)
- Successive i/p are i.i.d.
- 3 Processing of successive i/p is independent of each other



- Q deep
- G deep Search with Google
- (kuldeep birdar
- Q deepika padukone
- Q deepthi sunaina
- Q deepak bagga
- Q deepika pilli
- Q deepti sharma

Successive i/p are not independent



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- Successive i/p are not independent
- 2 Length of the i/p is not fixed $(\rightarrow predictions also)$



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- Successive i/p are not independent
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- Same underlying task at different 'time instances'



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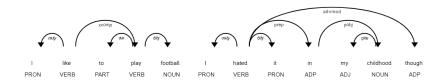
- Successive i/p are not independent
- ② Length of the i/p is not fixed (→ predictions also)
- Same underlying task at different 'time instances'
- 4 Sequence Learning Problems





Sentiment Analysis (Source)





POS-Tagging (Source:Kaggle)





Action Recognition (Source)



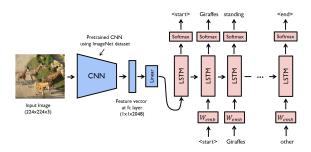


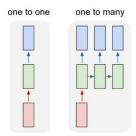
Image Captioning(Source)



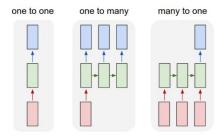




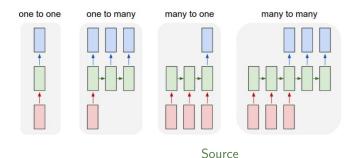




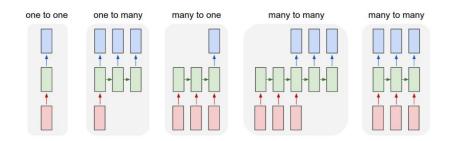














NNs designed to solve sequence learning tasks



- NNs designed to solve sequence learning tasks
- ② Characteristics



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- 2 Characteristics

 - ② Handle variable length of i/p

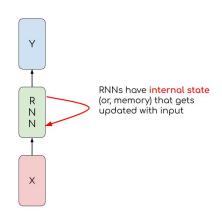


- NNs designed to solve sequence learning tasks
- ② Characteristics

 - 2 Handle variable length of i/p
 - 3 Same function applied at all time instances

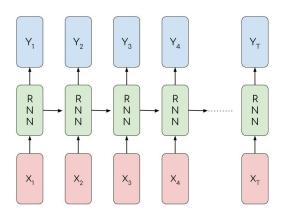
RNNs: internal state





RNNs: unfolding







 ${\color{blue} \Phi}$ Apply the same transformation at every time step \rightarrow 'Recurrent' NNs



- $\textcircled{\scriptsize 1}$ Apply the same transformation at every time step \rightarrow 'Recurrent' NNs
- $\mathbf{2}$ i/p sequence $x_t \in \mathbb{R}^{\mathbb{D}}$



- $\textbf{ 1 Apply the same transformation at every time step} \rightarrow \text{`Recurrent' NNs}$
- $\mathbf{2}$ i/p sequence $x_t \in \mathbb{R}^{\mathbb{D}}$
- $oldsymbol{3}$ Initial recurrent state $h_0 \in \mathbb{R}^{\mathbb{Q}}$

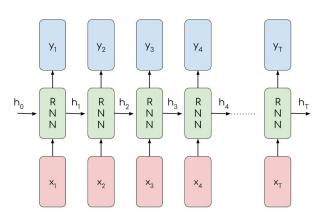


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- $\ \, \textbf{①} \,\,$ Apply the same transformation at every time step \rightarrow 'Recurrent' NNs
- $\mathbf{2}$ i/p sequence $x_t \in \mathbb{R}^{\mathbb{D}}$
- 3 Initial recurrent state $h_0 \in \mathbb{R}^{\mathbb{Q}}$
- **3** RNN model computes sequence of recurrent states iteratively $h_t = \phi(x_t, h_{t-1}; w)$



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Elmon RNN (1990)



① Start with $h_0 = 0$

Elmon RNN (1990)



- ① Start with $h_0 = 0$

Elmon RNN (1990)



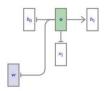
19

- ① Start with $h_0 = 0$
- $a h_t = tanh(W_{xh}.x_t + W_{hh}.h_{t-1} + b_h)$
- $y_t = softmax(W_{hy}.h_t + b_y)$

RNNs as computational graph



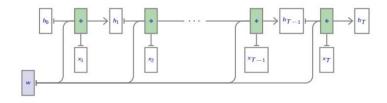
1 Use the same set of parameters at each time step



RNNs as computational graph



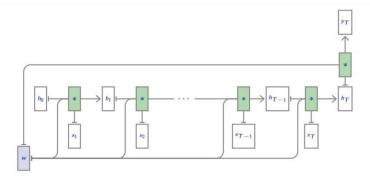
Use the same set of parameters at each time step



RNNs as computational graph



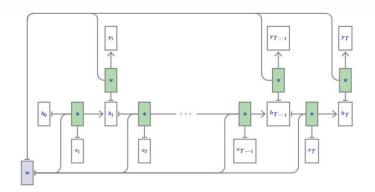
Use the same set of parameters at each time step



RNNs as computational graph



- Use the same set of parameters at each time step
- 2 Flexible to realize different variants (with some tricks!)

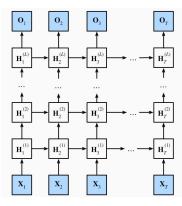


Multi-layered RNNs



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① Stack multiple RNNs between i/p and o/p layers



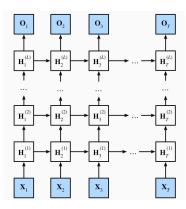
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Multi-layered RNNs



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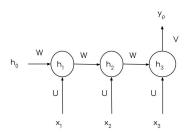
- Stack multiple RNNs between i/p and o/p layers
- $② \ \, H_t^{(l)} = W_{xh}^{(l)} \cdot H_t^{(l-1)} + W_{hh}^{(l)} \cdot H_{t-1}^{(l)} + b_h^{(l)}$



Source

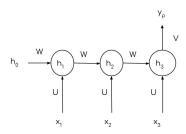
Backpropagation Through Time (BPT) product on the first transfer of the control o

① Consider a many-to-one variant RNN (e.g. sentiment analysis)



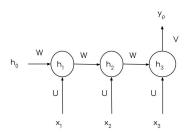
Backpropagation Through Time (BPT) under the training to the control of the contr

- Consider a many-to-one variant RNN (e.g. sentiment analysis)
- Let's separate the parameters into U, V, and W



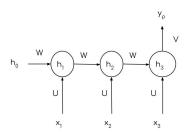
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① Let's now perform SGD (assume loss L is formulated on y_p)



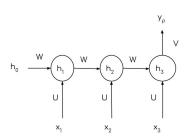
Backpropagation Through Time (BPT) under the training to the control of the contr

- ① Let's now perform SGD (assume loss L is formulated on y_p)
- ② \rightarrow we need to compute $\frac{\partial L}{\partial V}, \frac{\partial L}{\partial W}$, and $\frac{\partial L}{\partial U}$



Backpropagation Through Time (BPT) under the training tra

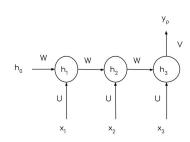
$$\begin{array}{cc} \textcircled{1} & \frac{\partial L}{\partial V} = \frac{\partial L}{\partial y_p} \frac{\partial y_p}{\partial V} = \\ & \frac{\partial L}{\partial y_p} \cdot \frac{\partial y_p}{\partial z_3} \cdot \frac{\partial z_3}{\partial V} \end{array}$$



Backpropagation Through Time (BPT) under the street of the colon local and a large decorption of the colon local a

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$$\frac{\partial L}{\partial V} = \frac{\partial L}{\partial y_p} \frac{\partial y_p}{\partial V} = \frac{\partial L}{\partial y_p} \cdot \frac{\partial y_p}{\partial z_3} \cdot \frac{\partial z_3}{\partial V}$$

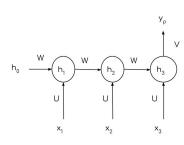
② $y_p = softmax(z_3)$ and $z_3 = V \cdot h_3 + b_y$



Backpropagation Through Time (BPT) under the training training the training training the training training

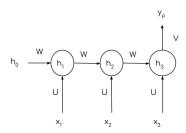
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- ② $y_p = softmax(z_3)$ and $z_3 = V \cdot h_3 + b_y$
- 3 Since we know that h_3, b_y are independent of V, we can compute $\frac{\partial L}{\partial V}$ in a single step



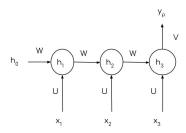
Backpropagation Through Time (BPT) or State Design 2 to 60 to 20 to 60 to 20 to 60 t

① Let's now consider $\frac{\partial L}{\partial W}$



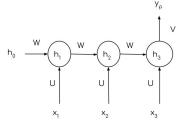
Backpropagation Through Time (BPT) under the treated to be a code to b

- **1** Let's now consider $\frac{\partial L}{\partial W}$
- There are multiple 'W's in the computational graph!

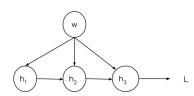


Backpropagation Through Time (BPTT)



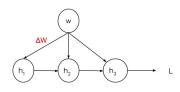


 For ease of understanding



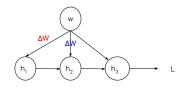
Backpropagation Through Time (BPT) Holden brillet between the trained and the latest the latest

①
$$\dfrac{\Delta w}{\partial w}$$
 change in $W o$ $\left(\dfrac{\partial h_1}{\partial W}\cdot \Delta w\right)$ change in h_1



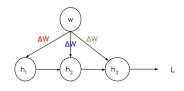
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- ② $rac{\Delta w}{\partial W}$ change in $W o \left(rac{\partial h_2}{\partial W}\cdot \Delta w
 ight)$ change in h_2



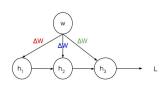
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- $oldsymbol{\Phi} rac{\Delta w}{\partial w}$ change in $W
 ightarrow \left(rac{\partial h_1}{\partial W} \cdot \Delta w
 ight)$ change in h_1
- $\begin{array}{ccc} \mathbf{3} & \Delta w \text{ change in W} \rightarrow \\ & \left(\frac{\partial h_3}{\partial W} \cdot \Delta w \right) \text{ change in } h_3 \end{array}$



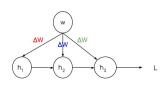
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①
$$\Delta L = \frac{\partial L}{\partial h_1} \cdot \Delta h_1 + \frac{\partial L}{\partial h_2} \cdot \Delta h_2 + \frac{\partial L}{\partial h_3} \cdot \Delta h_3$$



Backpropagation Through Time (BPTT) under the treated a transfer a few transfer and the tra

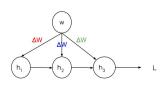
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Backpropagation Through Time (BPT) under the treated to be a code to b

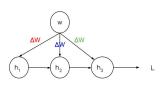
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$$\Delta L = \frac{\partial L}{\partial h_1} \cdot \Delta h_1 + \frac{\partial L}{\partial h_2} \cdot \Delta h_2 + \frac{\partial L}{\partial h_3} \cdot \Delta h_3$$

2
$$\frac{\partial L}{\partial W} = \frac{\partial L}{\partial h_1} \frac{\partial h_1}{\partial W} + \frac{\partial L}{\partial h_2} \frac{\partial h_2}{\partial W} + \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial W}$$



Backpropagation Through Time (BPT) under the treated to be a code to b

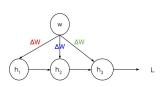
$$\begin{array}{ll} \mathbf{\Omega} & \Delta L = \\ & \frac{\partial L}{\partial h_1} \cdot \Delta h_1 + \frac{\partial L}{\partial h_2} \cdot \Delta h_2 + \frac{\partial L}{\partial h_3} \cdot \Delta h_3 \end{array}$$



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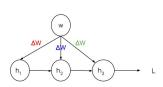
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\end{array}$$

$$\frac{\partial L}{\partial h_2} = ?$$



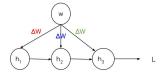
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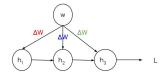
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$$\frac{\partial L}{\partial h_2} = \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial h_2}$$



Backpropagation Through Time (BPT) Indian Institute of Technology Mydrands

$$\frac{\partial L}{\partial W} = \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial h_2} \frac{\partial h_2}{\partial h_1} \frac{\partial h_1}{\partial W} + \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial h_2} \frac{\partial h_2}{\partial W} + \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial W} + \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial W}$$

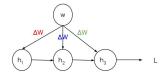


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5

$$\frac{\partial L}{\partial W} = \sum_{k=1}^{3} \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial h_k} \frac{\partial h_k}{\partial W}$$



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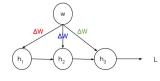
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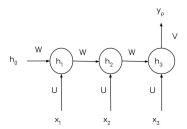


$$\frac{\partial L}{\partial W} = \sum_{k=1}^{3} \frac{\partial L}{\partial h_3} \left(\prod_{j=k+1}^{3} \frac{\partial h_j}{\partial h_{j-1}} \right) \frac{\partial h_k}{\partial W}$$



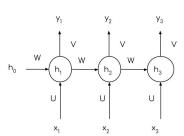
Backpropagation Through Time (BPT) And the least a long to lon

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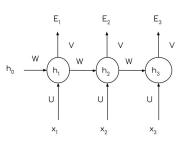
Backpropagation Through Time (BPT) Audian desilied a least a l

Consider a many-to-many variant RNN (e.g. PoS tagging)



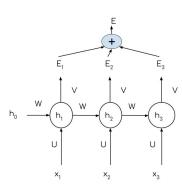
Backpropagation Through Time (BPT) produce the latest the first texture of texture of the challenger by the control of the challenger by t

- Consider a many-to-many variant RNN (e.g. PoS tagging)
- Full sequence is one training example (although there is an error computed at each time step)



Backpropagation Through Time (BPT) under the treated to be a large of the property of the control of the contro

- Consider a many-to-many variant RNN (e.g. PoS tagging)
- 2 Total error is the sum of errors at each time step



Backpropagation Through Time (BPT) under the state of the change of the company to the company that the company the company that the company t

At times, sequences can be quite lengthy!

Backpropagation Through Time (BPT) under the treated to be a code to b

- At times, sequences can be quite lengthy!
- Need to perform BPTT through many layers

Backpropagation Through Time (BPT) reduce to cold \$2 laugh cold \$2 laugh

- ① At times, sequences can be quite lengthy!
- 2 Need to perform BPTT through many layers

$$\frac{\partial L}{\partial W} = \sum_{k=1}^{3} \frac{\partial L}{\partial h_3} \left(\prod_{j=k+1}^{3} \frac{\partial h_j}{\partial h_{j-1}} \right) \frac{\partial h_k}{\partial W}$$

Backpropagation Through Time (BPT) order bodded Dayle bod

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3

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4 Leads to Vanishing Gradient problem!

Backpropagation Through Time (BPT)

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$$\frac{\partial L}{\partial W} = \sum_{k=1}^{3} \frac{\partial L}{\partial h_3} \left(\prod_{j=k+1}^{3} \frac{\partial h_j}{\partial h_{j-1}} \right) \frac{\partial h_k}{\partial W}$$

- Leads to Vanishing Gradient problem!
- No impact of earlier time steps at later times (difficult to learn long-term dependencies!)

39 dl - 12/RNNs

Backpropagation Through Time (BPT) and the little of the color product o

We may move on from sigmoid/tanh (e.g. ReLU) and your gradients may not die

Backpropagation Through Time (BPT) under the state of the condition to th

- $\ \, \textcircled{\scriptsize 10} \,\,$ We may move on from sigmoid/tanh (e.g. ReLU) and your gradients may not die
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Backpropagation Through Time (BPT) or local to the local

- $\ensuremath{\text{\textcircled{1}}}$ We may move on from sigmoid/tanh (e.g. ReLU) and your gradients may not die
- 2 In some cases $\left(\prod_{j=k+1}^3 rac{\partial h_j}{\partial h_{j-1}}\right)$ may lead to exploding gradients
- 3 But, not much of an issue

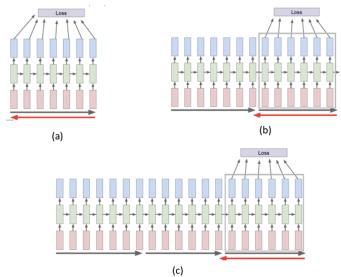
Backpropagation Through Time (BPT) acknowledge the control of the

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Backpropagation Through Time (BPT) urday bodde Daylo b

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- Better initialization, Regularization, short time sequences (Truncation)

Backpropagation Through Time (BPT) under the street the



Truncated BPTT (CS231n)

Handling long-term dependencies



Architectural modifications to RNNs

Handling long-term dependencies



- Architectural modifications to RNNs
 - LSTM (1997 by Sepp Hochreiter and Jürgen Schmidhuber; Improved by Gers et al. in 2000)

Handling long-term dependencies



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 - LSTM (1997 by Sepp Hochreiter and Jürgen Schmidhuber; Improved by Gers et al. in 2000)
 - GRU (Cho et al. 2014)



Long Short-Term Memory



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- $oldsymbol{2}$ At a time 't', hidden state $h^{(t)}$ and cell state $c^{(t)}$



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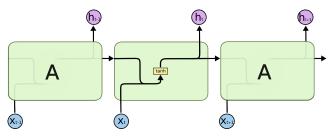


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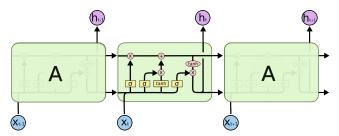
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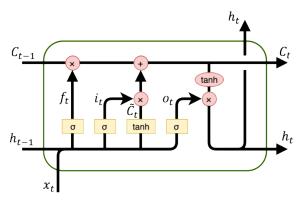
RNNs are chain of repeating moduels. Basic RNN (Colah's blog)





RNNs are chain of repeating moduels. LSTM (Colah's blog)

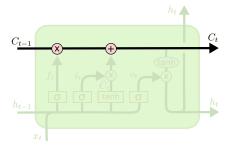




The LSTM node. (Colah's blog)

LSTM: The cell state



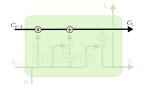


Cell state in LSTM (Colah's blog)

LSTM: The cell state



Info. can flow through unchanged

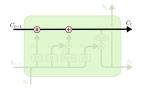


Cell state in LSTM (Colah's blog)

LSTM: The cell state



- Info. can flow through unchanged
- ② Gates can add/remove information to cell state

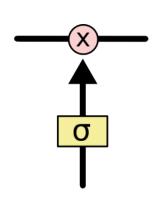


Cell state in LSTM (Colah's blog)

LSTM: The gates



Sigmoid neural nets (o/p numbers in [0, 1])

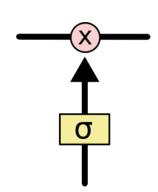


Cell state in LSTM (Colah's blog)

LSTM: The gates



- Sigmoid neural nets (o/p numbers in [0, 1])
- 2 Point-wise multiplication operation

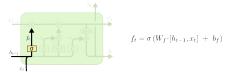


Cell state in LSTM (Colah's blog)

LSTM: The forget gate



 Decides what to throw away from cell state (e.g. forgetting the gender of old subject in light of a new one)

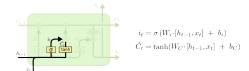


Forget gate in LSTM (Colah's blog)

LSTM: The input gate



 Next is to decide what new to store in cell state (e.g. add the gender of a new subject)

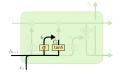


Input gate in LSTM (Colah's blog)

LSTM: The input gate



- Next is to decide what new to store in cell state (e.g. add the gender of a new subject)
- ② Done in two steps
 - input gate decides what to update
 - A tanh layer creates a candidate cell state

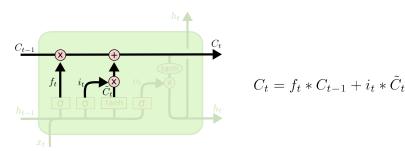


$$\begin{split} i_t &= \sigma\left(W_i {\cdot} [h_{t-1}, x_t] \ + \ b_i\right) \\ \hat{C}_t &= \tanh(W_C {\cdot} [h_{t-1}, x_t] \ + \ b_C) \end{split}$$

Input gate in LSTM (Colah's blog)

LSTM: The cell state update

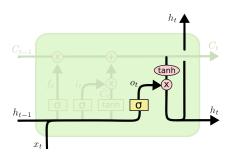




Cell state update in LSTM (Colah's blog)

LSTM: The output



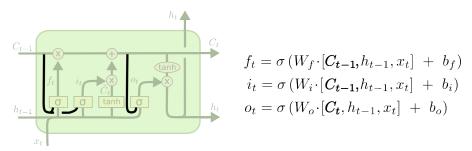


$$o_{t} = \sigma (W_{o} [h_{t-1}, x_{t}] + b_{o})$$
$$h_{t} = o_{t} * \tanh (C_{t})$$

Output computation in LSTM (Colah's blog) e.g. may be a verb that is coming next in case of a language model

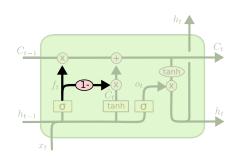
LSTM variant: Peephole connections





Variant with gates looking into the Cell state in LSTM by Ger et al. (Colah's blog)

LSTM variant: Coupled i/p and forget gates held the state of the state

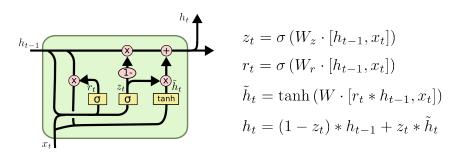


$$C_t = f_t * C_{t-1} + (\mathbf{1} - f_t) * \tilde{C}_t$$

Variant with coupled input and forget gates. (Colah's blog)

$\textbf{LSTM} \to \textbf{GRU}$





Gated Recurrent Unit (Colah's blog)



Use Via the gates!

LSTM: handling the vanishing gradients







Computational graph at time k-1

LSTM: handling the vanishing gradients

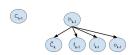




$$\tilde{C}_k = \\ \tanh(W_c[h_{t-1}, x_t] + b_c)$$

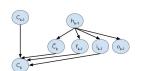
LSTM: handling the vanishing gradients





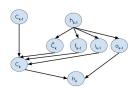
All the gates





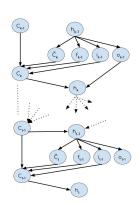
Next cell state





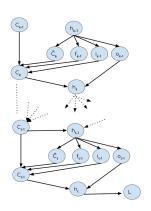
1 Next hidden state





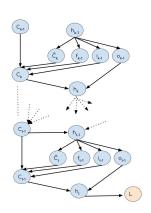
Running till time step 't'





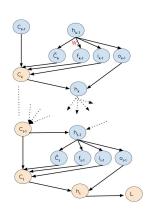
Consider loss computation





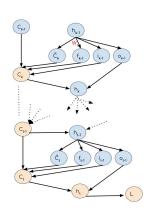
Let's know if the gradient flows to an arbitrary time step 'k'





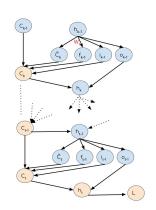
① Specifically, let's consider if gradient flows to W_f through C_k





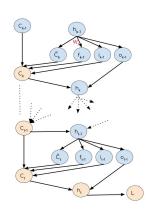
- $\textbf{①} \ \, \text{Specifically, let's} \\ \ \, \text{consider if gradient flows} \\ \ \, \text{to} \ \, W_f \ \, \text{through} \ \, C_k$
- ② Note that there are multiple paths between L and C_k (but, consider one such path as highlighted)





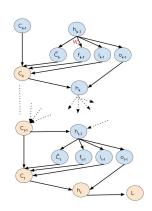
$$\begin{array}{ll} \textbf{0} & \mathsf{Grad} = \\ & \frac{\partial L}{\partial h_t} \frac{\partial h_t}{\partial C_t} \frac{\partial C_t}{\partial C_{t-1}} \dots \frac{\partial C_{k+1}}{\partial C_k} \end{array}$$





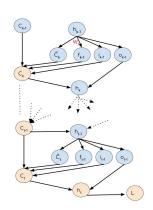
- 2 $\frac{\partial L}{\partial h_t}$ doesn't vanish (no intermediate nodes)





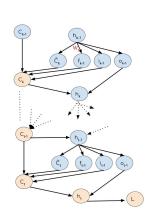
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- $b_t = o_t \odot \sigma(C_t)$



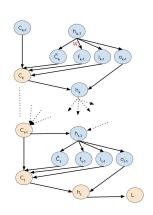


- 2 $\frac{\partial L}{\partial h_t}$ doesn't vanish (no intermediate nodes)
 - $h_t = o_t \odot \sigma(C_t)$
- $egin{array}{l} lacktriangledown & rac{\partial h_t}{\partial C_t} = \mathbb{D}(o_t \odot \sigma'(C_t)) \ ext{(diagonal matrix)} \end{array}$



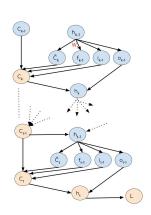






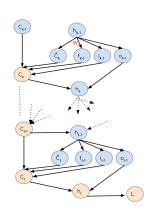
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- ② Note that \tilde{C}_t depends on C_{t-1} , and for simplicity assume the gradient from that term vanishes
- 3 Grad = $\frac{\partial L}{\partial h_t} \frac{\partial h_t}{\partial C_t} \frac{\partial C_t}{\partial C_{t-1}} \cdots \frac{\partial C_{k+1}}{\partial C_k}$





- $C_t = f_t \odot C_{t-1} + i_t \odot \tilde{C}_t$
- 2 Note that C_t depends on C_{t-1} , and for simplicity assume the gradient from that term vanishes





- ② Red term vanishes only if during the forward pass this product caused the information to vanish (by the time 't')!



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- That means, gradient will vanish only if dependency in the forward pass vanishes! (which makes sense)
- Gates do the same regulation in backward pass as they do in the forward

RNNs



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- Attention and Transformers are becoming more popular lately