

NEWTON'S 2ND LAW:-

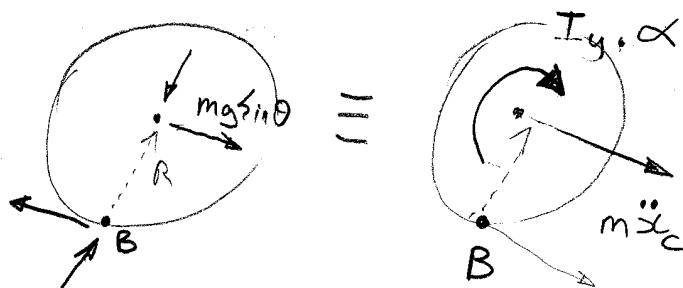
$$\sum F_z = m \ddot{z} = 0$$

$$\therefore N - mg \cos \theta = 0$$

$$\therefore \boxed{N = mg \cos \theta} \quad \text{--- (1)}$$

$$\sum F_x = m \ddot{x}_c$$

$$\therefore \boxed{mg \sin \theta - F_f = m \ddot{x}_c} \quad \text{--- (2)}$$



$$\sum M_B = mg R \sin \theta$$

and

$$\sum M_B = I_y \cdot \alpha + R \cdot m \ddot{x}_c$$

$$\therefore mg R \sin \theta = I_y \alpha + R m \ddot{x}_c$$

For NO-SLIP we have

$$\boxed{\ddot{x}_c = R \cdot \alpha} \quad \text{--- (3)}$$

$$\therefore mg R \sin \theta = \alpha (I_y + m R^2)$$

$$\therefore \alpha = \frac{R \cdot mg \sin \theta}{I_y + m R^2}$$

For a sphere we have

$$I_y = \frac{2}{5} m R^2$$

$$\therefore \alpha = \frac{mg \sin \theta \cdot R}{\frac{2}{5} m R^2 + m R^2}$$

$$\therefore \alpha = \frac{g \sin \theta \cdot R}{\frac{7}{5} R^2}$$

$$\boxed{\alpha = \frac{5g \sin \theta}{7 \cdot R}} \quad \text{--- (3)}$$

\therefore Sub (3) and (2b) into (2)

$$\boxed{F_f = mg \sin \theta - m R \alpha} \quad \text{--- (4)}$$