

# Stack

## Concept - 1

1. Nearest number to left / right
2. " " " " " "

3. Stock span problem
4. maximum area of Histogram

5. maximum area of rectangle in Binary search

6. Rain water trapping
7. implementing a main stack
8. implementing stack using heap
9. the celebrity problem
10. longest valid parentheses
11. Iterative TOH.

## Concept II

### Identification

I. Array  $\leftarrow$  Heap  
 Stack

II  $O(n^2)$

```
for (int i=0; i<n; i++)
    for (int j=0; j<n; j++)
```

for i, j depend on each other

but in stack question.

i, j depend on each other

ex.

```
for (int i=0; i<n; i++)
    for (int j=0; j<i; j++)
```

P Nearest greater to Right.

arr[] : 1 3 2 4

o/p : 3 2 4 -1

Identification of stack.

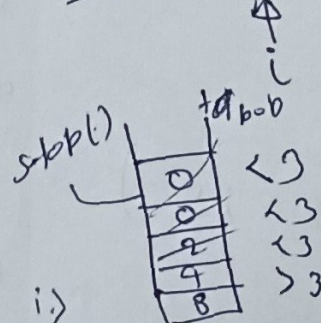
1 3 0 0 1 2 4

i j  
 compare to see h.

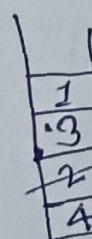
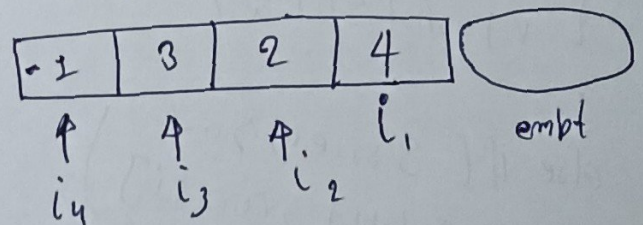
```
for (int i=0; i<n-1; i++)
    for (int j=i+1; j<n; j++)
        j depends on i.
```

approach.

eg 1 3 0 0 2 4 8



arr[] : 1 3 2 4 o/p = 3 4 4 -1



Stack

vector v : 1 4 4 9

stop() < arr[i] if pop() < arr[i]  
 stop() > arr[i] vector & push



vector[]: ~~1~~ -1 4 4 9

OP: 3 4 4 -1

we reverse(v.begin(), v.end())

~~reverse~~  
return v;

three step.

vector n push

Stack empty -1

s.top() > arr[i] → s.top()

s.top() <= arr[i] → pop stack

until i) stack empty

check ii) s.top() greater than arr[i].

code

vector<int> v;

stack<int> s;

for(int i = size-1; i >= 0; i--)

{ if (s.size() == 0)  
{ v.push\_back(-1);

} else if (s.size() > 0 &&  
s.top() > arr[i])

v.push\_back(s.top())

else if (s.size() > 0 &&  
s.top() <= arr[i])

{ while (s.size() > 0 &&  
s.top() <= arr[i])

~~v.push~~ s.pop()

~~s.top~~

} if (s.size() == 0) {  
v.push\_back(-1);

} else {  
v.push\_back(s.top());

} s.push\_back(arr[i]);

} return reverse(v.begin(),  
v.end());

Nearest Greater to Left.

arr[]: 1 3 2 4

op -1 -1 3 -1

code

vector<int> v;

stack<int> s;

for(int i = 0; i < arr.size(); i++)

{ while (s.size() > 0 &&  
s.top() >= arr[i])  
{ s.pop();

} if (s.isEmpty())  
v.push\_back(-1);

} else  
s.push(arr[i]); v.push\_back(arr[i])



# Nearest smaller to left

arr[]: 

4	5	2	10	8
---	---	---	----	---

o/p : -1 4 -1 2 2

Identification

```
for(int i=0; i<n; i++)
    for(int j=i-1; j>=0; j--)
```

4	5	2	10	8
---	---	---	----	---

/   \

i-1   j

code

```
vector<int> v;
stack<int> s;

for(int i=0; i<n; i++)
{
    while(s.size() > 0 && s.top() > arr[i])
    {
        s.pop();
    }
    if(s.empty())
        v.push_back(-1);
    else
        v.push_back(s.top());
    s.push(arr[i]);
}

return v;
```

Nearest smaller to right

arr[]: 4 5 2 10 8

op: 2 2 -1 8 -1

4	5	2	10	8
---	---	---	----	---

$O(n)$

Approach

s: 

4	5	2	10	8
---	---	---	----	---

↑   ↑   ↑   ↑   ↑

i

v: 

-1	8	-1	2	2
----	---	----	---	---

reverse(v): 

2	2	-1	8	-1
---	---	----	---	----

6 Stock Span Problem

arr: 

100	80	60	70	60	75	85
-----	----	----	----	----	----	----

op: 

1	1	1	2	1	4	6
---	---	---	---	---	---	---

see consecutive smaller or equal to arr[i].

arr: 

100	80	60	70	60	75	85
-----	----	----	----	----	----	----

arr in index

v: 

-1	0	1	1	3	1	0
----	---	---	---	---	---	---

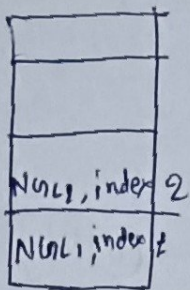
Next ?

o/p: 

1	1	1	2	1	4	6
---	---	---	---	---	---	---

arr in index - v[i]





100 80 60 70 60 75  
4 1

sum up

Stack space  
problem

NGL → (NGL index)  
→ created smaller

$i - NGL$

code

vector<int> v;

Stack

Stack<pair<int, int>> s;

for (int i = 0; i < n; i++) {

while (s.size() > 0 &&

s.top().first <= arr[i])

s.pop().first;

if (s.size() == 0)

v.push\_back(s.top().second);

else

v.push\_back(s.top().second);

s.push(arr[i], i);

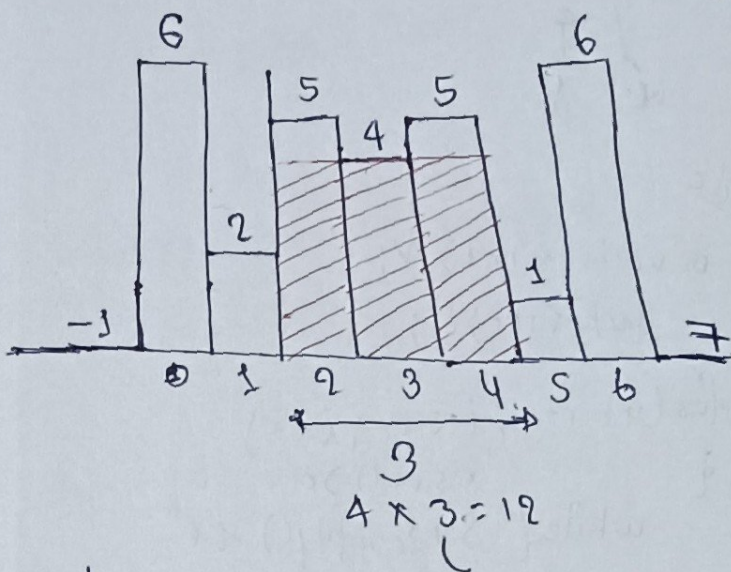
for (int i = 0; i < v.size(); i++)

v[i] = i - v[i];

return v;

#Maximum Area Histogram

arr: 6 2 5 4 5 1 6  
height



right  
(arr): 0 1 2 3 4 5 6  
NSR : 1 5 3 5 5 7 7  
(left)  
NSL : -1 -1 1 1 3 -1 5

width[i] = 5 - 1 = 4 - 1

= right - left - 1 = 3

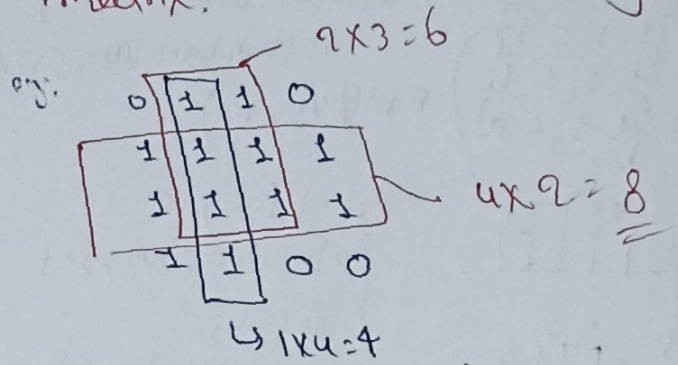
arr: 6 2 5 4 5 1 6  
width: 1 5 1 3 1 7 1

area[i] = arr[i] \* width[i]

area = 6 10 5 12 5 7 6



# max Area Rectangle in binary matrix.



MAH(int arr[], int size)  
 right[]  $\rightarrow$  NSR(arr, size)  
 left[]  $\rightarrow$  NSL(arr, size)  
 width[]  $\rightarrow$  right[i] - left[i] - 1  
 arr[]  $\rightarrow$  arr[i] \* width[i]  
 return max in arr[];

matching

MAH

d/p

given

MAH

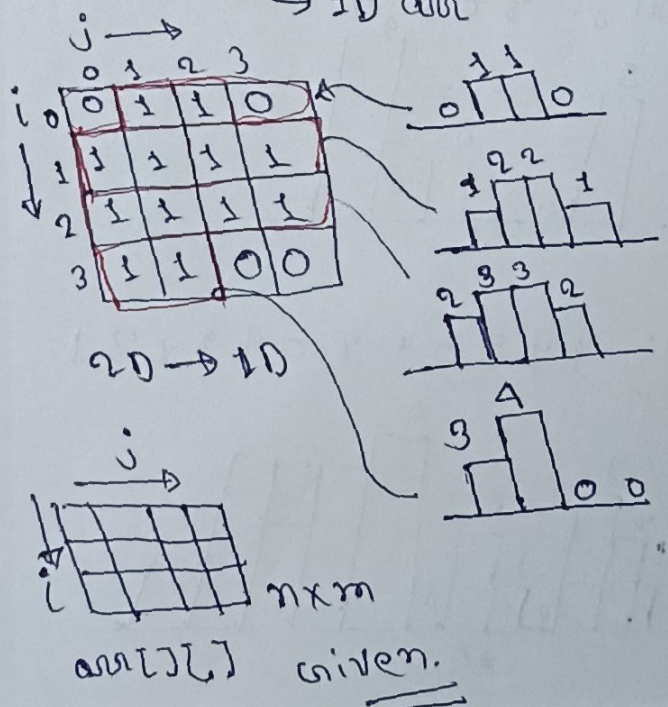
1D arr

Natural no.

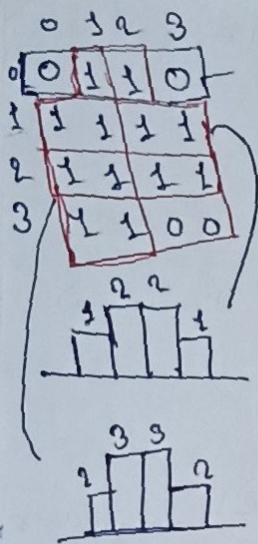
2D

2D arr.

binary no.  
0/1







for (int i = 0; i < m; i++)  
 $v_1 \text{ push\_back}(arr[0][i])$   
 $MAH_1(v_1, m)$

for (int i = 1; i < m; i++)  
 for (int j = 0; j < m; j++)  
 {  
 if (arr[i][j] == 0)  
 $v_2[j] = 0;$

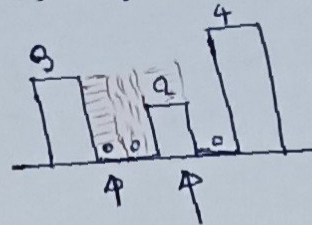
else  
 $v_2[j] = v_1[j] + arr[i][j]$   
 $MAH_2 = MAH(v_2, m)$

else  
 $v_3[i] = v_2[i] + arr[i][i];$

$MAH_3 = MAH(v_3, m)$

return max(MAH<sub>1</sub>, MAH<sub>2</sub>, MAH<sub>3</sub>, MAH<sub>4</sub>)

arr: 3 0 0 2 0 4



$$\min(3, 4) - 2 = 1 \times 2 = 2$$

water[i] = min(maxLeft - maxRight) - arr[i]

arr: 3 0 0 2 0 4

maxL: 3 3 3 3 3 4

maxR: 4 4 4 4 4 4

arr: 3 0 0 2 0 4

min(maxL: 3 3 3 3 3 4  
 maxR: 4 4 4 4 4 4)

minD: 3 3 3 3 3 4  
 arr: 3 0 0 2 0 4

water: 0 3 3 1 3 0

return sum of water

code

int maxL = arr[0]

for (int i = 1; i < n; i++)

maxL[i] = max(maxL[i-1], arr[i])

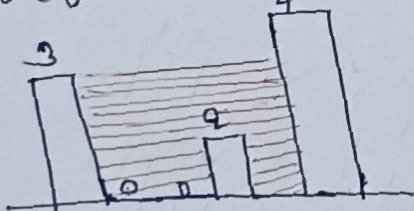
int maxR[n] = arr[n-1]

for (int i = n-2; i >= 0; i--)

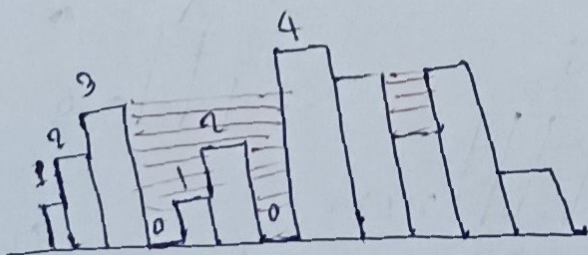
maxR[i] = max(maxR[i+1], arr[i])

## Rain water Trapping

arr: 3 0 0 2 0 4



eg2: 1 2 3 0 1 2 0 4 3 2 3 1

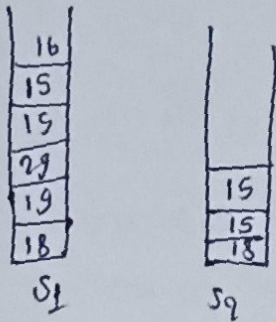




minimum element in stack  
with extra space.

arr 18 19 29 15 15 16

Approach.



code

```
stack <int> s1;
```

```
stack <int> s2;
```

```
int getmin ( )
```

```
{ if (s2.size() == 0)
```

```
    return -1;
```

```
    return s2.top();
```

```
}
```

```
void push (int a)
```

```
{ s1.push(a);
```

```
if (s2.size() == 0 || a <= s2.top())
```

```
    s2.push(a);
```

```
return;
```

```
int pop() {
```

```
if (s1.size() == 0)
```

```
    return -1;
```

```
int ans = s1.top();
```

```
s1.pop();
```

```
if (ans <= s2.top())
```

```
    s2.pop();
```

```
return ans;
```