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import math
import sys
import random
import matplotlib.pyplot as plt
import numpy as np
recursion counter = [0]
def generate_random_number(min: int, max: int):
    Accepts min and max integer value as range to return a random
number within that range
    return random.randint(min, max)
def get_random_list(length: int):
    Accepts length integer and return a random list of numbers of the
specified length
    .....
    arr = []
    for i in range(0, length):
        arr.append(generate_random_number(-999, 999))
    return arr
def max_sub_array_using_brute_force(arr):
    Accepts a random array and returns the maximum sum, beginning
index and last index of the sub using brute-force method
    counter = 0
    # Initialize the max as the first element of the array
    max\_sum = -sys\_maxsize
    left_index = right_index = 0
    for i in range(0, len(arr)):
        counter += 1
        # Initialize current sum with every iteration of the outer-
loop
        current_sum = 0
        for j in range(i, len(arr)):
            counter += 1
            # Add array elements to current-sum to maintain
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current sum += arr[i]
            # Replace the max, left_index and right_index if current-
sum is greater than max
            if current_sum > max_sum:
                counter += 1
                max sum = current sum
                left index = i
                right index = j
    return max_sum, left_index, right_index, counter
def max_crossing_sub_array_sum(arr, left_index, mid_index,
right_index):
    111111
    Accepts the array, left index, mid index and right index and
returns the max sum of a sub array and it's indices
    current_sum = 0
    left_max_sum = -sys.maxsize
    left_max_begin_index = mid_index
    # Iterate from the mid to left index and find the max left sum
(Iterating back)
    for i in range(mid_index, left_index - 1, -1):
        current_sum = current_sum + arr[i]
        if current sum > left max sum:
            recursion counter[0] += 1
            left_max_sum = current_sum
            left max begin index = i
    current_sum = 0
    right max sum = -sys.maxsize
    right_max_end_index = mid_index
    # Iterate from the mid to right index and find the max right sum
(Iterating forward)
    for j in range(mid_index, right_index + 1):
        current sum = current sum + arr[j]
        if current_sum > right_max_sum:
            recursion counter[0] += 1
            right_max_sum = current_sum
            right_max_end_index = j
    # Calcuate the crossing sum by adding the left max sum, right max
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sum

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# Subtracting the mid-index because it is getting added twice
(both in left max sum and right max sum)
    crossing_sum = left_max_sum + right_max_sum - arr[mid_index]
    # Return the max sum from crossing sum, left sum and right sum
    if crossing sum > left max sum and crossing sum > right max sum:
        return crossing sum, left max begin index, right max end index
    elif left max sum > crossing sum and left max sum > right max sum:
        return left_max_sum, left_max_begin_index, mid_index
    else:
        return right max sum, mid index, right max end index
def max_sub_array_using_recursion(arr, left_index, right_index):
    Accepts and array, the left index(begin) of the array and the
right index (end) of the array and returns
    the maximum sum of a subarray and the beginning index and the
final index of the subarray
    if left_index >= right_index:
        return arr[left_index], left_index, right_index
    mid_index = (left_index + right_index) // 2
    left_sub_array_sum, left_begin_index, left_end_index =
max_sub_array_using_recursion(arr, left_index, mid_index)
    right_sub_array_sum, right_begin_index, right_end_index =
max_sub_array_using_recursion(arr, mid_index+1, right_index)
    crossing_sub_array_sum, crossing_begin_index, crossing_end_index =
max_crossing_sub_array_sum(arr, left_index, mid_index, right_index)
    # Return the max sum from crossing sum, left sum and right sum
    if left_sub_array_sum > right_sub_array_sum and
left sub array sum > crossing sub array sum:
        return left_sub_array_sum, left_begin_index, left_end_index
    elif right_sub_array_sum > left_sub_array_sum and
right sub array sum > crossing_sub_array_sum:
        return right sub array sum, right begin index, right end index
        return crossing sub array sum, crossing begin index,
crossing end index
def __init__():
    min_number_of_sets = 6
    max_number_of_sets = 10
    total_number_of_sets = generate_random_number(min_number_of_sets,
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max number of sets)
   brute_force_input_to_counter_dict = dict()
   recursion input to counter dict = dict()
   for num in range(0, total number of sets):
       array length = generate random number(50, 70)
       array = get random list(array length)
print(f'\n0riginal array: {array}')
       max sum brute force, left index, right index,
brute_force_counter = max_sub_array_using_brute_force(array)
       brute_force_input_to_counter_dict[array_length] =
brute force counter
       print('\nMax subarray sum using brute-force')
       print(f'Max Sum: {max_sum_brute_force}, left index:
{left_index + 1}, right index: {right_index + 1}')
       print(f'Sub-array: {array[left_index: right_index + 1]}')
       print(f'Number of inputs: {array_length}, Counter:
{brute_force_counter}, Worst case: {array_length * array_length}')
       recursion counter[0] = 0
       print('\nMax subarray sum using recursion')
       max sum recursion, left index, right index =
max sub array using recursion(array, 0, array length - 1)
       recursion_input_to_counter_dict[array_length] =
recursion counter[0]
       print(f'Max Sum: {max_sum_recursion}, left index: {left_index
+ 1}, right index: {right index + 1}')
       print(f'Sub-array: {array[left index: right index + 1]}')
       print(f'Number of inputs: {array_length}, Counter:
\{recursion counter[0]\}, Worst case: \{round((array length *
math.log(array_length, 2)), 2)}')
   input_length_array = []
   counter_array = []
   theoretical_time_complexity_array = []
   for key in brute_force_input_to_counter_dict:
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input length array.append(key)
        counter_array.append(brute_force_input_to_counter_dict[key])
        theoretical_time_complexity_array.append(key * key)
    input length array.sort()
    counter array.sort()
    theoretical time complexity array.sort()
    x = np.array(input_length_array)
    y1 = np.array(counter array)
    y2 = np.array(theoretical time complexity array)
    plt.axis([50, 70, 1000, 5000])
    plt.xticks([50, 55, 60, 65, 70])
    plt.xlabel('Number of Inputs')
    plt.ylabel('Time Complexity')
    plt.title('Max Sub Array Time Complexity - Brute Force')
    plt.plot(x, y1, color='red')
    plt.plot(x, y2, color='blue')
    plt.legend(['Actual Count', 'Theoretical Time Complexity'])
    plt.show()
    recursion_counter_array = []
    recursion_theoretical_time_complexity_array = []
    for key in recursion_input_to_counter_dict:
recursion counter array.append(recursion input to counter dict[key])
        recursion theoretical time complexity array.append(round((key
* math.log(key, 2)), 2))
    recursion_counter_array.sort()
    recursion_theoretical_time_complexity_array.sort()
    y3 = np.array(recursion counter array)
    y4 = np.array(recursion_theoretical_time_complexity_array)
    plt.axis([50, 70, 1000, 5000])
    plt.xticks([50, 55, 60, 65, 70])
    plt.xlabel('Number of Inputs')
    plt.vlabel('Time Complexity')
    plt.title('Max Sub Array Time Complexity - Recursion (Divide &
```

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Conquer)')

plt.plot(x, y3, color='yellow')
plt.plot(x, y4, color='green')
plt.legend(['Actual Count', 'Theoretical Time Complexity'])

plt.show()

__init__()
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