>
$$ec1 := diff(x(t), t) = x(t) + 4y(t);$$

 $ec1 := \frac{d}{dt} x(t) = x(t) + 4y(t)$ (1)

 \rightleftharpoons ec2 := diff(y(t), t) = x(t) + y(t);

$$ec2 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = x(t) + y(t)$$
 (2)

 \rightarrow sist := ec1, ec2;

$$sist := \frac{d}{dt} x(t) = x(t) + 4 y(t), \frac{d}{dt} y(t) = x(t) + y(t)$$
 (3)

 \blacktriangleright with(DEtools):

 \rightarrow dsolve({sist}, {x(t), y(t)});

$$\left\{ x(t) = _C1 \, e^{3t} + _C2 \, e^{-t}, y(t) = \frac{_C1 \, e^{3t}}{2} - \frac{_C2 \, e^{-t}}{2} \right\}$$
 (4)

$$ec1 := \frac{\mathrm{d}}{\mathrm{d}t} x(t) = 2x(t) - y(t)$$
 (5)

= ec2 := diff(y(t), t) = x(t) + 2y(t);

$$ec2 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = x(t) + 2 \ y(t)$$
 (6)

 $\overline{}$ > sist := ec1, ec2;

$$sist := \frac{d}{dt} x(t) = 2 x(t) - y(t), \frac{d}{dt} y(t) = x(t) + 2 y(t)$$
 (7)

| with(DEtools):
| dsolve({sist}, {x(t), y(t)});
|
$$\{x(t) = e^{2t} (_C1 \sin(t) + _C2 \cos(t)), y(t) = e^{2t} (\sin(t) _C2 - \cos(t) _C1)\}$$
 (8)

> restart;

> ec1 := diff(x(t), t) = x(t) - y(t) + z(t);

$$ec1 := \frac{\mathrm{d}}{\mathrm{d}t} x(t) = x(t) - y(t) + z(t)$$
(9)

> ec2 := diff(y(t), t) = x(t) + y(t) - z(t);

$$ec2 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = x(t) + y(t) - z(t)$$
 (10)

> ec3 := diff(z(t), t) = -y(t) + 2z(t);

$$ec3 := \frac{\mathrm{d}}{\mathrm{d}t} \ z(t) = -y(t) + 2 \, z(t) \tag{11}$$

 \rightarrow sist := ec1, ec2, ec3;

$$sist := \frac{d}{dt} x(t) = x(t) - y(t) + z(t), \frac{d}{dt} y(t) = x(t) + y(t) - z(t), \frac{d}{dt} z(t) = -y(t) + 2 z(t)$$
 (12)

>
$$ec1 := diff(x(t), t) = 5 x(t) + 3 y(t) + 1;$$

$$ec1 := \frac{d}{dt} x(t) = 5 x(t) + 3 y(t) + 1$$
 (14)

> $ec2 := diff(y(t), t) = -6x(t) - 4y(t) + \exp(t);$

$$ec2 := \frac{d}{dt} y(t) = -6 x(t) - 4 y(t) + e^t$$
 (15)

 \Rightarrow sist := ec1, ec2;

$$sist := \frac{d}{dt} x(t) = 5 x(t) + 3 y(t) + 1, \frac{d}{dt} y(t) = -6 x(t) - 4 y(t) + e^{t}$$
 (16)

with(DEtools):dsolve({sist}, {x(t), y(t)});

$$\left\{ x(t) = e^{2t} C2 + e^{-t} C1 - \frac{3 e^{t}}{2} - 2, y(t) = -e^{2t} C2 - 2 e^{-t} C1 + 2 e^{t} + 3 \right\}$$
 (17)

restart; ec1 := diff(x(t), t) = -x(t) + 3y(t) - 4z(t) + 25t;

$$ec1 := \frac{d}{dt} x(t) = -x(t) + 3 y(t) - 4 z(t) + 25 t$$
 (18)

$$ec2 := diff(y(t), t) = -2 x(t) - 6 z(t) + 12 \exp(t);$$

$$ec2 := \frac{d}{dt} y(t) = -2 x(t) - 6 z(t) + 12 e^{t}$$
(19)

> ec3 := diff(z(t), t) = -2x(t) - 6y(t) + 6z(t) + 12;

$$ec3 := \frac{d}{dt} z(t) = -2 x(t) - 6 y(t) + 6 z(t) + 12$$
 (20)

 \rightarrow sist := ec1, ec2, ec3;

$$sist := \frac{d}{dt} x(t) = -x(t) + 3 y(t) - 4 z(t) + 25 t, \frac{d}{dt} y(t) = -2 x(t) - 6 z(t) + 12 e^{t}, \frac{d}{dt} z(t)$$

$$= -2 x(t) - 6 y(t) + 6 z(t) + 12$$
(21)

$$\left\{ x(t) = -e^{t} + 15 t - \frac{49}{10} + _{C}I e^{-3t} + _{C}2 e^{-2t} + _{C}3 e^{10t}, y(t) = -10 t - \frac{7 _{C}2 e^{-2t}}{5} + 2 e^{t} + 2 e^{t} + \frac{233}{30} + _{C}3 e^{10t} - \frac{10 _{C}I e^{-3t}}{3}, z(t) = -5 t - \frac{4 _{C}2 e^{-2t}}{5} + 2 e^{t} + \frac{33}{10} - 2 _{C}3 e^{10t} - 2 _{C}1 e^{-3t} \right\}$$

$$-2 _{C}I e^{-3t}$$

 \triangleright ec1 := diff (x(t), t) = x(t) + 4y(t);

$$ec1 := \frac{\mathrm{d}}{\mathrm{d}t} x(t) = x(t) + 4y(t)$$
 (23)

$$ec2 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = x(t) + y(t)$$
 (24)

 \Rightarrow sist := ec1, ec2;

$$sist := \frac{d}{dt} x(t) = x(t) + 4 y(t), \frac{d}{dt} y(t) = x(t) + y(t)$$
 (25)

> cond := x(0) = 1, y(0) = 2;

$$cond := x(0) = 1, y(0) = 2$$
 (26)

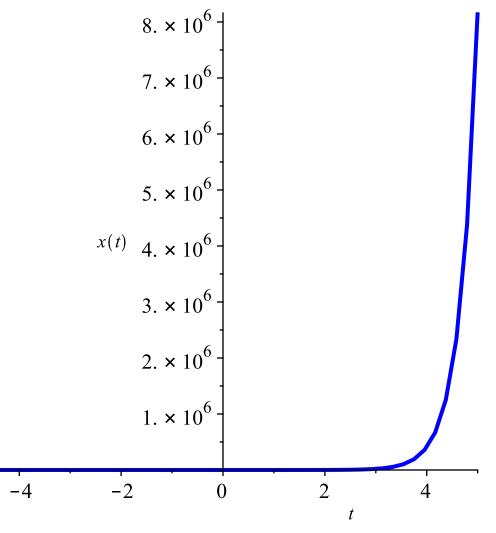
with(DEtools):

$$dsolve(\{sist, cond\}, \{x(t), y(t)\});$$

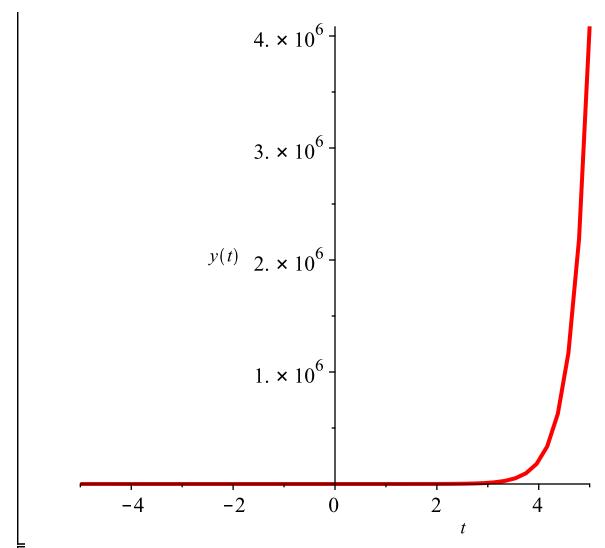
$$\left\{x(t) = -\frac{3e^{-t}}{2} + \frac{5e^{3t}}{2}, y(t) = \frac{3e^{-t}}{4} + \frac{5e^{3t}}{4}\right\}$$
(27)

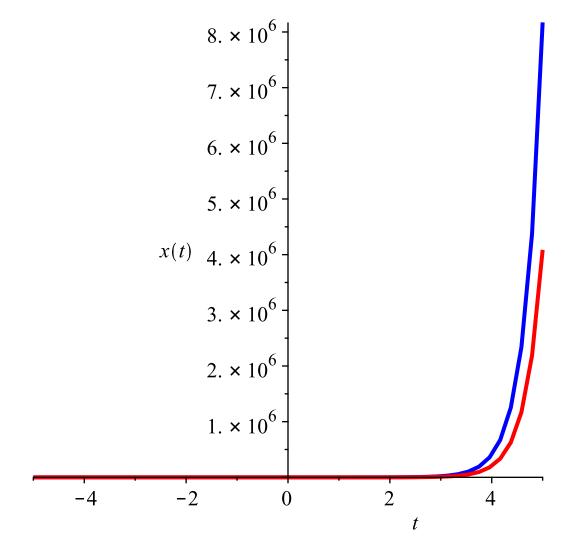
with(plots):

> xx := DEplot([sist], [x, y], t = -5..5, [[cond]], linecolor = blue, scene = [t, x(t)]);



> yy := DEplot([sist], [x, y], t = -5..5, [[cond]], linecolor = red, scene = [t, y(t)]);





•
$$ec1 := diff(x(t), t) = x(t) + 2y(t) + \exp(-t);$$

>
$$ec2 := diff(y(t), t) = -2x(t) + y(t) + 1;$$

$$ec2 := \frac{d}{dt} y(t) = -2 x(t) + y(t) + 1$$
 (29)

 $\sim cond := x(0) = 0, y(0) = 1;$

$$cond := x(0) = 0, y(0) = 1$$
 (30)

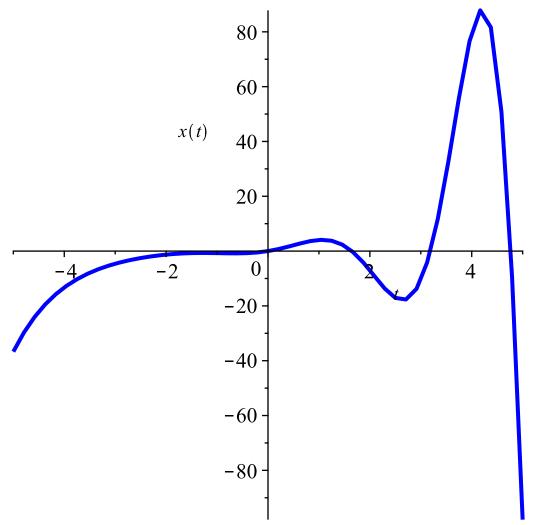
 \searrow with(DEtools): \searrow sist := ec1, ec2;

$$sist := \frac{d}{dt} x(t) = x(t) + 2 y(t) + e^{-t}, \frac{d}{dt} y(t) = -2 x(t) + y(t) + 1$$
 (31)

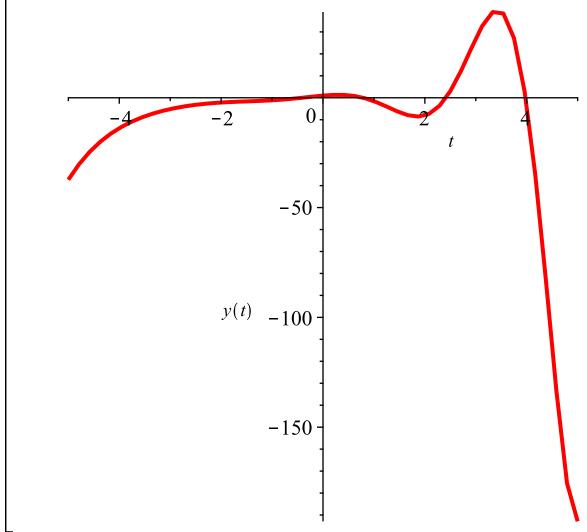
$$\begin{cases} solve(\{sist, cond\}, \{x(t), y(t)\}); \\ \left\{x(t) = -\frac{3 e^{t} \cos(2 t)}{20} + \frac{29 e^{t} \sin(2 t)}{20} - \frac{e^{-t}}{4} + \frac{2}{5}, y(t) = \frac{3 e^{t} \sin(2 t)}{20} + \frac{29 e^{t} \cos(2 t)}{20} - \frac{1}{5} - \frac{e^{-t}}{4} \right\} \end{cases}$$

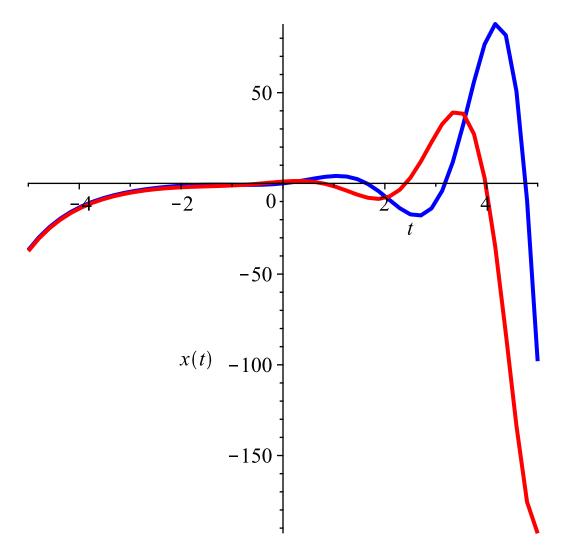
$$(32)$$

 $\begin{tabular}{ll} \begin{tabular}{ll} \beg$



> yy := DEplot([sist], [x, y], t = -5..5, [[cond]], linecolor = red, scene = [t, y(t)]);





> restart;

>
$$ec1 := diff(x(t), t) = -x(t) + 3y(t) + 3z(t) + 27t^2;$$

 $ec1 := \frac{d}{dt}x(t) = -x(t) + 3y(t) + 3z(t) + 27t^2$ (33)

>
$$ec2 := diff(y(t), t) = 2x(t) - 2y(t) - 5z(t) + 3t;$$

 $ec2 := \frac{d}{dt}y(t) = 2x(t) - 2y(t) - 5z(t) + 3t$
(34)

>
$$ec3 := diff(z(t), t) = -2x(t) + 3y(t) + 6z(t) + 3;$$

 $ec3 := \frac{d}{dt}z(t) = -2x(t) + 3y(t) + 6z(t) + 3$
(35)

 \rightarrow sist := ec1, ec2, ec3;

$$sist := \frac{d}{dt} x(t) = -x(t) + 3 y(t) + 3 z(t) + 27 t^2, \frac{d}{dt} y(t) = 2 x(t) - 2 y(t) - 5 z(t) + 3 t,$$
 (36)

$$\frac{\mathrm{d}}{\mathrm{d}t} z(t) = -2 x(t) + 3 y(t) + 6 z(t) + 3$$

>
$$cond := x(0) = 50, y(0) = -30, z(0) = 26;$$

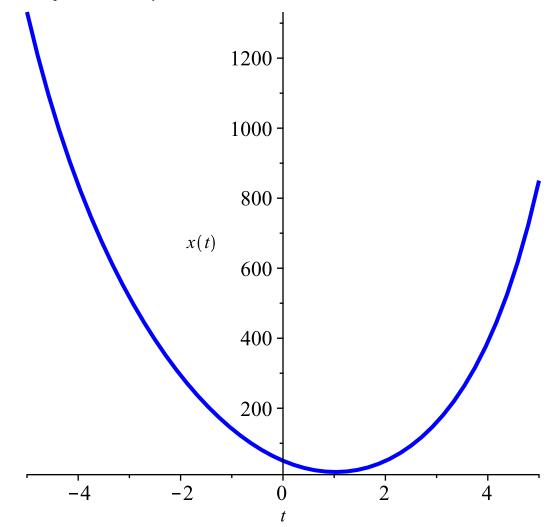
 $cond := x(0) = 50, y(0) = -30, z(0) = 26$
(37)

 \rightarrow with(DEtools):

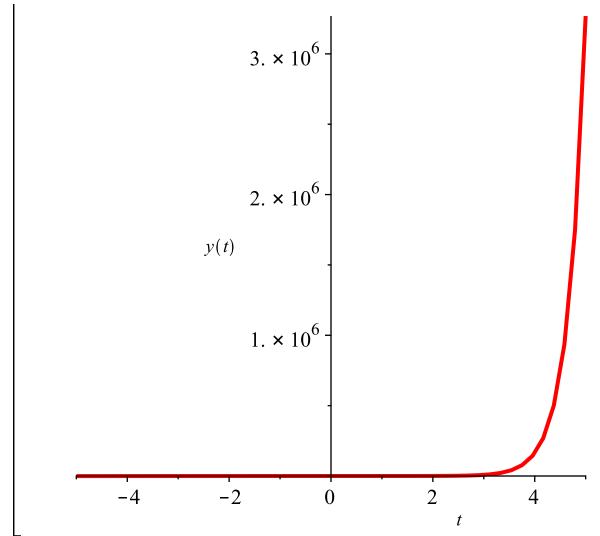
>
$$dsolve(\{sist, cond\}, \{x(t), y(t), z(t)\});$$

 $\{x(t) = 2 e^{-t} + 3 e^{t} + 27 t^{2} - 63 t + 45, y(t) = e^{3t} + 2 e^{t} - 18 t^{2} + 24 t - 32 - e^{-t}, z(t) = -e^{3t} - 27 t + 18 t^{2} + 26 + e^{-t}\}$
(38)

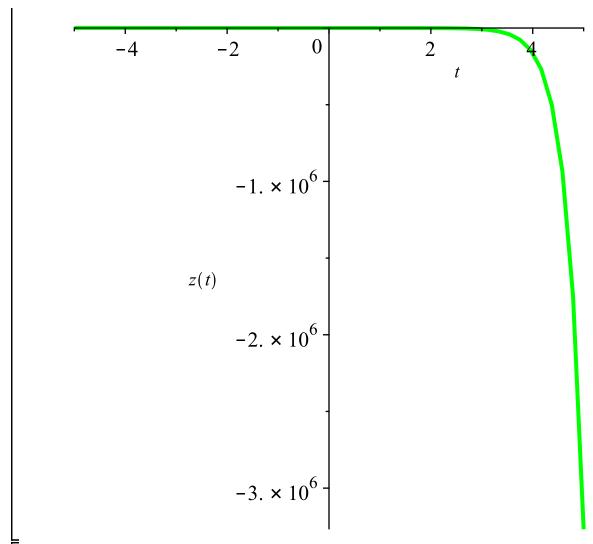
with(plots): xx := DEplot([sist], [x, y, z], t = -5..5, [[cond]], linecolor = blue, scene = [t, x(t)]);

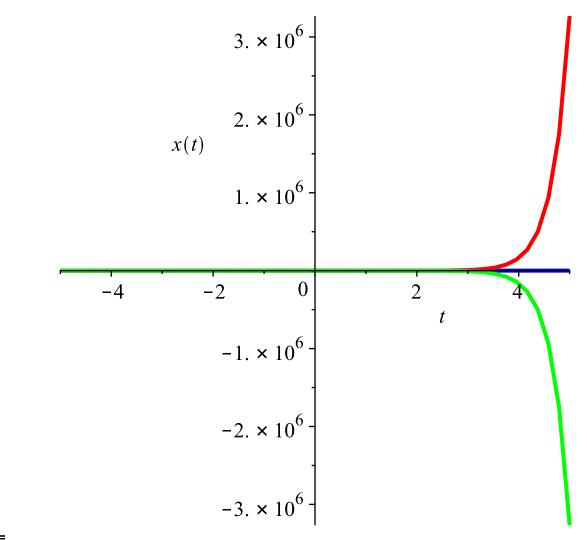


> yy := DEplot([sist], [x, y, z], t = -5..5, [[cond]], linecolor = red, scene = [t, y(t)]);



zz := DEplot([sist], [x, y, z], t=-5..5, [[cond]], linecolor = green, scene = [t, z(t)]);





> restart; > ec1 := diff(x(t), t) = x(t) + y(t);

$$ec1 := \frac{\mathrm{d}}{\mathrm{d}t} \ x(t) = x(t) + y(t)$$
 (39)

ec2 := diff(y(t), t) = -2x(t) + 4y(t);

$$ec2 := \frac{d}{dt} y(t) = -2 x(t) + 4 y(t)$$
 (40)

 \rightarrow sist := ec1, ec2;

$$sist := \frac{d}{dt} x(t) = x(t) + y(t), \frac{d}{dt} y(t) = -2 x(t) + 4 y(t)$$
 (41)

> cond := x(0) = 3, y(0) = 0;

$$cond := x(0) = 3, y(0) = 0$$
 (42)

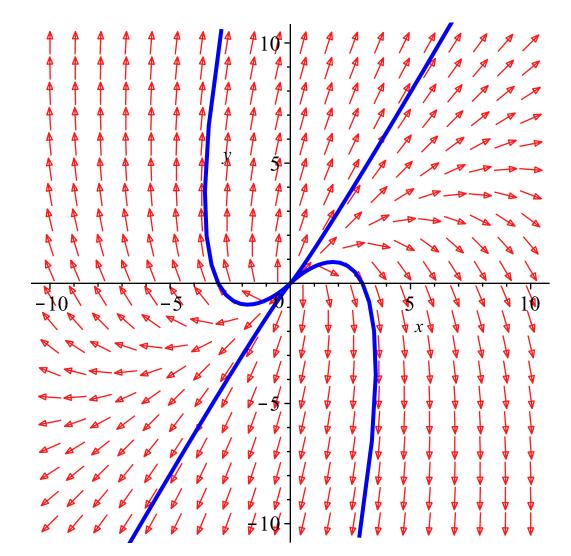
$$cond := x(0) = 3, y(0) = 0$$
| with(DEtools):
| sol := dsolve({sist, cond}, {x(t), y(t)});
| sol := {x(t) = 6 e^{2t} - 3 e^{3t}, y(t) = 6 e^{2t} - 6 e^{3t}}
| lim x(t) = -\infty
(42)

(42)

(43)

$$\lim_{t \to \infty} x(t) = -\infty \tag{44}$$

>
$$\lim_{t \to \infty} y(t) = -\infty$$
 (45)
> $\operatorname{cond2} := x(0) = 2, y(0) = 3;$ $\operatorname{cond2} := x(0) = 2, y(0) = 3$ (46)
> $\operatorname{sol2} := \operatorname{dsolve}(\{\operatorname{sist}, \operatorname{cond2}\}, \{x(t), y(t)\});$ $\operatorname{sol2} := \{x(t) = \operatorname{e}^{2t} + \operatorname{e}^{3t}, y(t) = \operatorname{e}^{2t} + 2\operatorname{e}^{3t}\}$ (47)
> $\lim_{t \to \infty} x(t) = \infty$ (48)
| $\lim_{t \to \infty} x(t) = \infty$ (49)
> $\operatorname{cond3} := x(0) = -3, y(0) = 0;$ $\operatorname{cond3} := x(0) = -3, y(0) = 0$ (50)
> $\operatorname{sol3} := \operatorname{dsolve}(\{\operatorname{sist}, \operatorname{cond3}\}, \{x(t), y(t)\});$ $\operatorname{sol3} := \{x(t) = -6\operatorname{e}^{2t} + 3\operatorname{e}^{3t}, y(t) = -6\operatorname{e}^{2t} + 6\operatorname{e}^{3t}\}$ (51)
> $\lim_{t \to \infty} x(t) = \infty$ (52)
| $\lim_{t \to \infty} x(t) = \infty$ (53)
> $\operatorname{cond4} := x(0) = -2, y(0) = -3;$ $\operatorname{cond4} := x(0) = -2, y(0) = -3$ (54)
> $\operatorname{sol4} := \operatorname{dsolve}(\{\operatorname{sist}, \operatorname{cond4}\}, \{x(t), y(t)\});$ $\operatorname{sol4} := \{x(t) = -\operatorname{e}^{2t} - \operatorname{e}^{3t}, y(t) = -\operatorname{e}^{2t} - 2\operatorname{e}^{3t}\}$ (55)
> $\operatorname{limit}(\operatorname{sol4}[1], t = \operatorname{infinity});$ $\lim_{t \to \infty} x(t) = -\infty$ (56)
| $\operatorname{limit}(\operatorname{sol4}[2], t = \operatorname{infinity});$ $\lim_{t \to \infty} x(t) = -\infty$ (57)
> $\operatorname{limit}(\operatorname{sol4}[2], t = \operatorname{infinity});$ $\lim_{t \to \infty} x(t) = -\infty$ (56)
> $\operatorname{limit}(\operatorname{sol4}[2], t = \operatorname{infinity});$ $\lim_{t \to \infty} x(t) = -\infty$ (57)
| $\operatorname{limit}(\operatorname{sol4}[2], t = \operatorname{infinity});$ $\lim_{t \to \infty} x(t) = -\infty$ (57)
> $\operatorname{limit}(\operatorname{sol4}[1], \operatorname{arrows} = \operatorname{medium}, \operatorname{linecolor} = \operatorname{blue}, \operatorname{stepsize} = 0.1);$



$$ec1 := \frac{\mathrm{d}}{\mathrm{d}t} \ x(t) = y(t)$$
 (58)

> ec2 := diff(y(t), t) = -x(t) - 2y(t);

$$ec2 := \frac{d}{dt} y(t) = -x(t) - 2 y(t)$$
 (59)

 \rightarrow sist := ec1, ec2;

$$sist := \frac{d}{dt} x(t) = y(t), \frac{d}{dt} y(t) = -x(t) - 2 y(t)$$
 (60)

> with(DEtools):

> $sol := dsolve(\{sist\}, \{x(t), y(t)\});$

$$sol := \{x(t) = e^{-t} (_C2 t + _C1), y(t) = -e^{-t} (_C2 t + _C1 - _C2)\}$$
 (61)

> limit(sol[1], t = infinity);

$$\lim_{t \to \infty} x(t) = 0 \tag{62}$$

 \rightarrow limit(sol[2], t = infinity);

$$\lim_{t \to \infty} y(t) = 0 \tag{63}$$

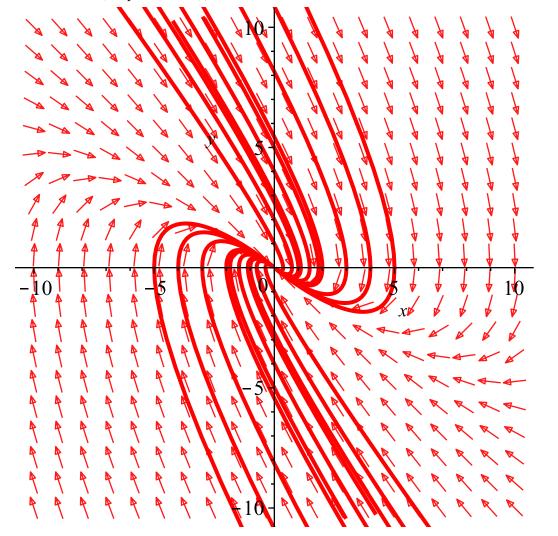
>
$$cond := [x(0) = 0, y(0) = i] \$i = 1 ...5, [x(0) = 0, y(0) = -i] \$i = 1 ...5, [x(0) = i, y(0) = 0] \$i = 1 ...5, [x(0) = -i, y(0) = 0] \$i = 1 ...5;$$

$$[x(0) = i, y(0) = 0] \$i = 1 ...5, [x(0) = -i, y(0) = 0] \$i = 1 ...5;$$

$$cond := [x(0) = 0, y(0) = 1], [x(0) = 0, y(0) = 2], [x(0) = 0, y(0) = 3], [x(0) = 0, y(0) = 4], [x(0) = 0, y(0) = -1], [x(0) = 0, y(0) = -2], [x(0) = 0, y(0) = -2], [x(0) = 0, y(0) = -3], [x(0) = 0, y(0) = -4], [x(0) = 0, y(0) = -5], [x(0) = 1, y(0) = 0], [x(0) = 2, y(0) = 0], [x(0) = 3, y(0) = 0], [x(0) = 4, y(0) = 0], [x(0) = 5, y(0) = 0], [x(0) = -1, y(0) = 0], [x(0) = -2, y(0) = 0], [x(0) = -3, y(0) = 0], [x(0) = -4, y(0) = 0], [x(0) = -5, y(0) = 0]$$

→ *with*(*plots*):

> DEplot([sist], [x(t), y(t)], t=-5...5, x=-10...10, y=-10...10, [cond], arrows = medium, linecolor = red, stepsize = 0.1);



> restart;

> ec1 := diff(x(t), t) = 2x(t) + y(t);

$$ec1 := \frac{d}{dt} x(t) = 2 x(t) + y(t)$$
 (65)

> ec2 := diff(y(t), t) = x(t) + 2y(t);

$$ec2 := \frac{d}{dt} y(t) = x(t) + 2 y(t)$$
 (66)

> sist := ec1, ec2; $sist := \frac{\mathrm{d}}{\mathrm{d}t} x(t) = 2 x(t) + y(t), \frac{\mathrm{d}}{\mathrm{d}t} y(t) = x(t) + 2 y(t)$ (67) $ule{ }$ with(plots): with(DEtools): > $dsolve(\{sist\}, \{x(t), y(t)\});$ ${x(t) = _C1 e^{3t} + _C2 e^{t}, y(t) = _C1 e^{3t} - _C2 e^{t}}$ (68)**>** DEplot([sist], [x(t), y(t)], t=-5...5, x=-10...10, y=-10...10, arrows = medium);> restart > ec1 := diff(x(t), t) = -x(t) - y(t);

$$ec1 := \frac{\mathrm{d}}{\mathrm{d}t} \ x(t) = -x(t) - y(t)$$
 (69)

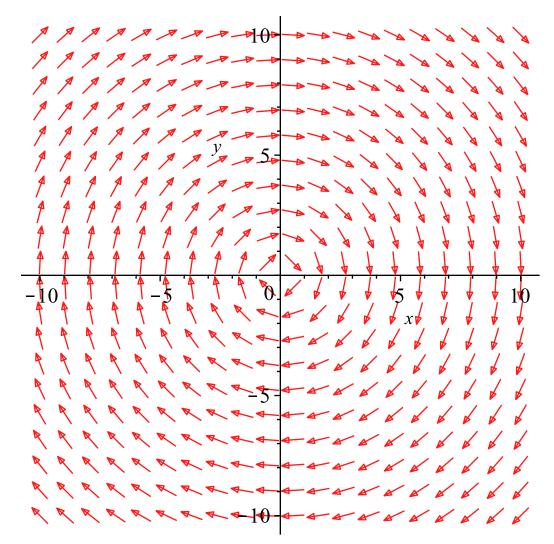
 $\rightarrow ec2 := diff(y(t), t) = x(t) - y(t);$

$$ec2 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = x(t) - y(t)$$
 (70)

> sist := ec1, ec2;

$$sist := \frac{d}{dt} x(t) = -x(t) - y(t), \frac{d}{dt} y(t) = x(t) - y(t)$$
 (71)

```
> dsolve(\{sist\}, \{x(t), y(t)\});
         \{x(t) = e^{-t} (C2 \cos(t) + C1 \sin(t)), y(t) = -e^{-t} (\cos(t) C1 - \sin(t) C2)\}
                                                                                                              (72)
\rightarrow with(DEtools) : with(plots) :
> DEplot([sist], [x(t), y(t)], t=-5...5, x=-10...10, y=-10...10, arrows=medium);
  ec1 := diff(x(t), t) = y(t);
                                        ec1 := \frac{\mathrm{d}}{\mathrm{d}t} x(t) = y(t)
                                                                                                              (73)
> ec2 := diff(y(t), t) = -x(t);
                                       ec2 := \frac{d}{dt} y(t) = -x(t)
                                                                                                              (74)
> sist := ec1, ec2;
                              sist := \frac{d}{dt} x(t) = y(t), \frac{d}{dt} y(t) = -x(t)
                                                                                                              (75)
> dsolve(\{sist\}, \{x(t), y(t)\});
                \{x(t) = CI\sin(t) + C2\cos(t), y(t) = CI\cos(t) - C2\sin(t)\}
                                                                                                              (76)
  with(DEtools) : with(plots) :
  DEplot([sist], [x(t), y(t)], t = -5...5, x = -10...10, y = -10...10, arrows = medium);
```



> restart

> ec1 := diff(x(t), t) = -2x(t);

$$ec1 := \frac{\mathrm{d}}{\mathrm{d}t} x(t) = -2 x(t) \tag{77}$$

> ec2 := diff(y(t), t) = -4x(t) - 2y(t);

$$ec2 := \frac{d}{dt} y(t) = -4 x(t) - 2 y(t)$$
 (78)

 \rightarrow sist := ec1, ec2;

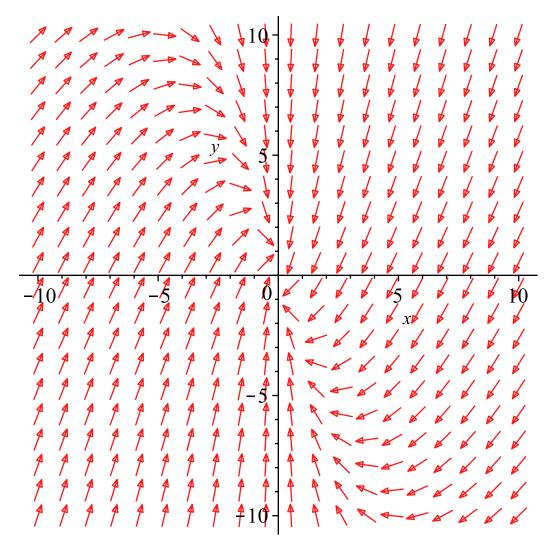
$$sist := \frac{d}{dt} x(t) = -2 x(t), \frac{d}{dt} y(t) = -4 x(t) - 2 y(t)$$
 (79)

> $dsolve(\{sist\}, \{x(t), y(t)\});$

$$\{x(t) = C2 e^{-2t}, y(t) = (-4 C2 t + C1) e^{-2t}\}$$
(80)

 \rightarrow with(DEtools) : with(plots) :

> DEplot([sist], [x(t), y(t)], t = -5...5, x = -10...10, y = -10...10, arrows = medium);



restart

> restart
>
$$ec1 := diff(x(t), t) = x(t) - 4y(t);$$

$$ec1 := \frac{d}{dt} x(t) = x(t) - 4 y(t)$$
 (81)

>
$$ec2 := diff(y(t), t) = 5 x(t) - 3 y(t);$$

$$ec2 := \frac{d}{dt} y(t) = 5 x(t) - 3 y(t)$$
 (82)

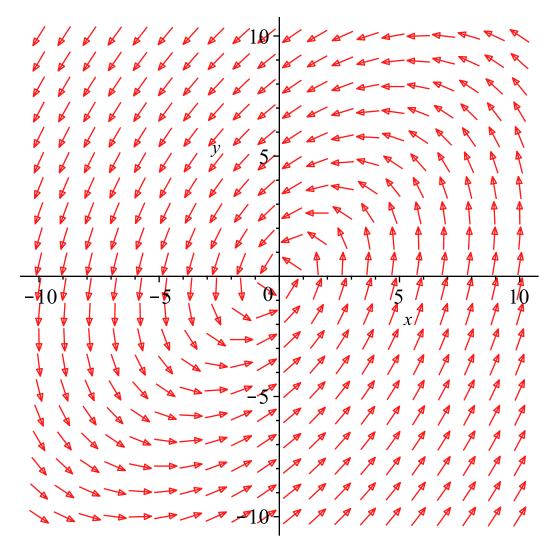
 \rightarrow sist := ec1, ec2;

$$sist := \frac{d}{dt} x(t) = x(t) - 4 y(t), \frac{d}{dt} y(t) = 5 x(t) - 3 y(t)$$
 (83)

> $dsolve(\{sist\}, \{x(t), y(t)\});$

$$\begin{cases} x(t) = e^{-t} \left(\sin(4t) \ _C1 + \cos(4t) \ _C2 \right), y(t) \end{cases}$$
 (84)

$$= \frac{e^{-t} \left(\sin(4 t) CI + 2 \sin(4 t) C2 - 2 \cos(4 t) CI + \cos(4 t) C2\right)}{2}$$



> restart

>
$$ec1 := diff(x(t), t) = 3 x(t) - y(t);$$

$$ec1 := \frac{d}{dt} x(t) = 3 x(t) - y(t)$$
 (85)

> ec2 := diff(y(t), t) = y(t);

$$ec2 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = y(t)$$
 (86)

 \rightarrow sist := ec1, ec2;

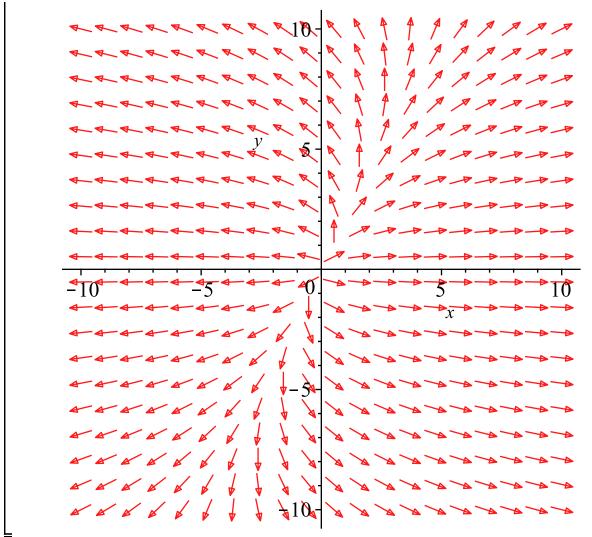
$$sist := \frac{d}{dt} x(t) = 3 x(t) - y(t), \frac{d}{dt} y(t) = y(t)$$
 (87)

> $dsolve(\{sist\}, \{x(t), y(t)\});$

$$\left\{ x(t) = \frac{-C2 e^{t}}{2} + e^{3t} CI, y(t) = -C2 e^{t} \right\}$$
 (88)

 \rightarrow with(DEtools) : with(plots) :

> DEplot([sist], [x(t), y(t)], t=-5...5, x=-10...10, y=-10...10, arrows=medium);



 $\#sistemele\ b,c,d,e\ au\ limitele\ x(t),y(t)\ egale\ cu\ 0$