Import necessary library

```
1 import pandas as pd
2 import numpy as np
3 import torch
4 from torchvision import datasets
5 from torchvision.transforms import ToTensor
6 import torchvision.transforms as transforms
7 from torch.utils.data import DataLoader
8 import matplotlib.pyplot as plt
9 import torch.nn as nn
10 import torch.nn.functional as F
11 from torch import optim
12
13 from sklearn.metrics import confusion_matrix, recall_score, precision_score, f1_score, accura
14 from sklearn.metrics import classification_report, ConfusionMatrixDisplay
```

Dataset preparation

- · Acquire the MNIST dataset
- · Preprocess the data (normalizaon, reshaping, train/test split)

About Dataset ref: https://www.kaggle.com/datasets/oddrationale/mnist-in-csv

MNIST contains a collection of 70,000, 28 x 28 images of handwritten digits from 0 to 9.

The dataset consists of two files:

- · train: 60,000 training examples and labels
- · test: 10,000 test examples and labels

each set - label: a number from 0 to 9,image: the pixel values (a number from 0 to 255).

```
1 train_data = datasets.MNIST(
         root = 'data',
 3
         train = True,
 4
        transform = ToTensor(),
 5
        download = True,
 6)
 7 test_data = datasets.MNIST(
        root = 'data',
 8
 9
        train = False,
10
        transform = ToTensor(),
         download = True,
11
12)
 1 test_data
    Dataset MNIST
        Number of datapoints: 10000
        Root location: data
        Split: Test
        StandardTransform
    Transform: ToTensor()
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dtype=torch.uint8)
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Normalization

```
1 #Get mean and std of training data
   3 print('Min Pixel Value: {} \nMax Pixel Value: {}'.format(train_data.data.min(), train_data.data
   4 print('Mean Pixel Value {} \nPixel Values Std: {}'.format(train_data.float().mean(), train_data.float().mean(), train_data.float(), train_data.flo
   5 print('Scaled Mean Pixel Value {} \nScaled Pixel Values Std: {}'.format(train_data.data.float(

    Min Pixel Value: 0

         Max Pixel Value: 255
        Mean Pixel Value 33.31842041015625
         Pixel Values Std: 78.56748962402344
         Scaled Mean Pixel Value 0.13066047430038452
         Scaled Pixel Values Std: 0.30810779333114624
   1 #Get mean and std of testing data
   3 print('Min Pixel Value: {} \nMax Pixel Value: {}'.format(test_data.data.min(), test_data.data.u
   4 print('Mean Pixel Value {} \nPixel Values Std: {}'.format(test_data.data.float().mean(), test_u
   5 print('Scaled Mean Pixel Value {} \nScaled Pixel Values Std: {}'.format(test_data.data.float()
        Min Pixel Value: 0
        Max Pixel Value: 255
        Mean Pixel Value 33.79122543334961
         Pixel Values Std: 79.17247009277344
         Scaled Mean Pixel Value 0.1325146108865738
         Scaled Pixel Values Std: 0.3104802668094635
   1 transform_train=transforms.Compose([
   2
                             transforms.ToTensor(),
   3
                             transforms.Normalize((0.1307,), (0.3081,)) # divides by 255
   4
                             ])
   5 transform_test=transforms.Compose([
                             transforms.ToTensor(),
```

```
transforms.Normalize((0.1325,), (0.3105,)) # divides by 255
              1 train_data = datasets.MNIST(
                                                                                         root = 'data',
              3
                                                                                       train = True,
              4
                                                                                         transform = transform_train,
              5
                                                                                         download = True,
              6)
              7 test_data = datasets.MNIST(
                                                                                         root = 'data',
              9
                                                                                       train = False,
                                                                                       transform = transform_test,
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11
                                                                                         download = True,
12)
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dtype=torch.uint8)
```

Determine the appropriate hyperparameters

```
1 batch_size = 100
2 num_workers = 6
3 n_iters = 5000
4
5 #จำนวน epoch = จำนวน iteration/จำนวน batch (training set = 60000)
6 num_epochs = n_iters / (len(train_data) / batch_size)
7 num_epochs = int(num_epochs)
8 print(num_epochs)
9
10 learning_rate = 0.01
8
1 random_seed = 1
2 torch.backends.cudnn.enabled = False
3 torch.manual_seed(random_seed)
<torch._C.Generator at 0x7fc323795a30>
```

Dataloader

```
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                                                    project_NNdeep_learning - Colaboratory
           tiaii . tuitii.utits.uata.pataLuauci(tiaii_uata,
    ۷
    3
                                                     batch_size=batch_size,
    4
                                                     shuffle=True),
    5
           'test' : torch.utils.data.DataLoader(test_data,
    6
                                                     batch_size=batch_size,
                                                     shuffle=True)}
    8 loaders
       {'train': <torch.utils.data.dataloader.DataLoader at 0x7fc27e4fb2b0>,
        'test': <torch.utils.data.dataloader.DataLoader at 0x7fc27e4fb250>}
  Show sample data
    1 examples = enumerate(loaders['test'])
    2 batch_id, (example_data, example_targets) = next(examples)
    1 example_data.shape
      torch.Size([100, 1, 28, 28])
    1 fig = plt.figure()
```

plt.imshow(example_data[i][0], cmap='gray', interpolation='none')

plt.title("Ground Truth: {}".format(example_targets[i]))

3 for i in range(6):

plt.xticks([])
plt.yticks([])

5

10 fig

plt.subplot(2,3,i+1)

plt.tight_layout()

CNN model design

OUTPUT FORMULA FOR CONVOLUTION OUTPUT FORMULA FOR POOLING

•
$$O = \frac{W - K + 2P}{S} + 1$$

•
$$O = \frac{W-K}{S} + 1$$

- O: output height/length
- ullet W: input height/length
- K: filter size (kernel size)
- \bullet P: padding

•
$$P = \frac{K-1}{2}$$

• S: stride

Ref: https://www.run.ai/guides/deep-learning-for-computer-vision/pytorch-cnn

ดับเบิลคลิก (หรือกด Enter) เพื่อแก้ไข

Def for calculate next output

```
1 def cal_out(input,k,s,p):
2    out = ((input-k+(2*p))/s)+1
3    return out
```

Model

```
1 class CNN(nn.Module):
      def __init__(self):
           super(CNN, self).__init__()
 3
           self.conv1 = nn.Conv2d(in_channels=1,out_channels=100,kernel_size=6,stride=2,padding=
 4
 5
           self.relu1 = nn.ReLU()
 6
           self.pool1 = nn.MaxPool2d(kernel_size=4,stride=2)
 7
           self.out1 = nn.Linear(100 * 6 * 6, 10)
           self.relu3 = nn.ReLU()
 8
 9
      def forward(self, x):
10
           x = self.conv1(x)
11
          x = self.relu1(x)
12
13
           x = self.pool1(x)
14
15
           # flatten the output of conv2
           x = x.view(x.size(0), -1)
17
           output = self.out1(x)
18
           return output
```

```
1 # class CNN(nn.Module):
 2 #
          def __init__(self):
              super(CNN, self).__init__()
 3 #
 4 #
              self.conv1 = nn.Conv2d(in_channels=1,out_channels=4,kernel_size=7,stride=1,padding=
 5 #
              self.relu1 = nn.ReLU()
              self.pool1 = nn.MaxPool2d(kernel_size=3)
 6 #
 7 #
              self.conv2 = nn.Conv2d(in_channels=4,out_channels=16,kernel_size=2,stride=1,padding
 8 #
              self.relu2 = nn.ReLU()
              self.out1 = nn.Linear(16 * 9 * 9, 10)
 9 #
10 #
              self.relu3 = nn.ReLU()
11
12 #
          def forward(self. x):
              x = self.conv1(x)
13 #
14 #
              x = self.relu1(x)
15 #
              x = self.pool1(x)
16 #
              x = self.conv2(x)
17 #
              x = self.relu2(x)
              # flatten the output of conv2
18 #
              x = x.view(x.size(0), -1)
19#
20 #
              output = self.out1(x)
21#
              return output
 1 \mod el = CNN()
 2 print(model)
    CNN (
      (conv1): Conv2d(1, 100, kernel_size=(6, 6), stride=(2, 2), padding=(2, 2))
      (relu1): ReLU()
      (pool1): MaxPool2d(kernel_size=4, stride=2, padding=0, dilation=1, ceil_mode=False)
      (out1): Linear(in_features=3600, out_features=10, bias=True)
      (relu3): ReLU()

    Define loss function, opmization algorithm
```

```
1 def call fuction(model):
      loss func = nn.CrossEntropyLoss()
3
      optimizer = optim.Adam(model.parameters(), lr = learning_rate, weight_decay=0.1)
4
      return loss_func,optimizer
1 loss_func,optimizer = call_fuction(model)
1 optimizer
  Adam (
  Parameter Group 0
     amsgrad: False
     betas: (0.9, 0.999)
     capturable: False
     differentiable: False
     eps: 1e-08
      foreach: None
     fused: None
     lr: 0.01
     maximize: False
     weight_decay: 0.1
```

Train model

```
1 print('Number of iterations in each epoch in train set =',(len(train_data) / batch_size))
2 print('Number of iterations in each epoch in test set =',(len(test_data) / batch_size))
3 print('Number of epochs =',num_epochs)
  Number of iterations in each epoch in train set = 600.0
  Number of iterations in each epoch in test set = 100.0
  Number of epochs = 8
```

```
1 def train(model,num epochs,optimizer,loss func):
 2
       iter = 0
 3
       correctImages = 0
 4
       totalImages = 0
 5
       trainingLoss = 0
 6
       model.train()
 7
       loss_each = []
 8
       acc_each = []
 9
       for epoch in range(num_epochs):
10
11
            for i, (images, labels) in enumerate(loaders['train']):
                images = images.requires_grad_()
12
                optimizer.zero grad()
13
14
                outputs = model(images)
15
                _, predicted = torch.max(outputs, 1)
                loss = loss_func(outputs, labels)
16
17
                loss.backward()
18
                optimizer.step()
                iter += 1
19
20
21
                correctImages += (predicted == labels).sum().item()
22
                totalImages += labels.size(0)
23
                trainingLoss += loss.item()
24
                accumulateAccuracy = round((correctImages/totalImages)*100,4)
25
26
                # Number of iterations in each epoch in train set
27
                if iter % 600 == 0:
28
                    print('Epoch [{}/{}] Iteration: {}'.format(epoch+1, num_epochs, iter))
                    print('Training accuracy: {} loss: {}'.format(accumulateAccuracy, round(loss.
29
30
                    loss each.append(round(loss.item(),4))
31
                    acc each.append(accumulateAccuracy)
32
                    pass
33
           pass
       pass
34
35
       return loss_each,acc_each
 1 trainloss,trainacc = train(model,num_epochs,optimizer,loss_func)
   Epoch [1/8] Iteration: 600
   Training accuracy: 89.1883 loss: 0.2394
   KeyboardInterrupt
                                        Traceback (most recent call last)
   <ipython-input-23-17480899683a> in <cell line: 1>()
      -> 1 trainloss,trainacc = train(model,num_epochs,optimizer,loss_func)
                            - 💲 6 frames
   /usr/local/lib/python3.10/dist-packages/torch/nn/functional.py in _max_pool2d(input, kernel_size, stride, padding, dilat:
       780
              if stride is None:
       781
                 stride = torch.jit.annotate(List[int], [])
     -> 782
              return torch.max_pool2d(input, kernel_size, stride, padding, dilation, ceil_mode)
```

KevboardInterrupt:

Model evaluation

```
1 def test(cnn):
 2
       # Test the model
 3
       cnn.eval()
 4
       loss_each = []
 5
       acc_each = []
 6
       y_trues = []
 7
       y_preds = []
 8
       with torch.no_grad():
 9
            iter = 0
10
            correctImages = 0
11
            totalImages = 0
12
            for epoch in range(num epochs):
13
14
                for images, labels in loaders['test']:
15
                    outputs = cnn(images)
16
                     _, predicted = torch.max(outputs, 1)
17
                    loss = loss_func(outputs, labels)
18
                    if epoch == (num epochs-1):
19
                         for i in labels.tolist():
20
                             y_trues.append(i)
21
                         for i in predicted.tolist():
                             y_preds.append(i)
22
23
                    correctImages += (predicted == labels).sum().item()
24
                    totalImages += labels.size(0)
25
                    accumulateAccuracy = round((correctImages/totalImages)*100,4)
26
                    iter += 1
27
28
                    # Number of iterations in each epoch in test set
29
                    if iter % 100 == 0:
30
                         print('Epoch [{}/{}] Iteration: {}'.format(epoch+1, num epochs, iter))
31
                         print('Testing accuracy: {} loss: {}'.format(accumulateAccuracy, round(lo
32
                         loss each.append(round(loss.item(),4))
33
                         acc each.append(accumulateAccuracy)
34
                         pass
35
                pass
36
            pass
37
       pass
38
39
        return y_trues, y_preds,loss_each,acc_each
40
 1 y trues, y preds, testloss, testacc = test(model)
Plot Loss and Accuracy
 1 def plot acc():
       epochs = range(1,num epochs+1)
       plt.plot(epochs, trainacc, 'ro', label='Accuracy of Train set')
 3
       plt.plot(epochs, testacc, 'bo', label='Accuracy of Test set')
 4
 5
       plt.title('Train Vs Test accuracy')
 6
       plt.xlabel('Epoch')
 7
       plt.ylabel('Accuracy')
 8
       plt.legend(loc=0)
 9
       plt.figure()
10
       plt.show()
 1 plot_acc()
 1 def plot_loss():
       epochs = range(1,num_epochs+1)
       plt.plot(epochs, trainloss, 'r', label='Loss of Train set')
plt.plot(epochs, testloss, 'b--', label='Loss of Test set')
 3
 4
 5
       plt.title('Train Vs Test Loss')
```

plt.xlabel('Epoch')
plt.ylabel('Loss')
plt.logond(loc-0)

6

```
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o ptt.tegenu(toc-v)

9 plt.figure()

10 plt.show()
```

Confusion Matrix

Result before Optimize

```
1 print('Accuracy:',accuracy_score(y_trues, y_preds))
 2 print('Precision:',precision_score(y_trues, y_preds, average='macro'))
 3 print('Recall:',recall_score(y_trues, y_preds, average='macro'))
 4 print('f1-Score:',f1_score(y_trues, y_preds, average='macro'))
 1 def plot_predict(model):
 2
      with torch.no_grad():
 3
           output = model(example_data)
 4
      fig = plt.figure()
 5
      for i in range(6):
 6
           plt.subplot(2,3,i+1)
 7
           plt.tight_layout()
 8
           plt.imshow(example data[i][0], cmap='gray', interpolation='none')
 9
           plt.title("Prediction: {}".format(
10
               output.data.max(1, keepdim=True)[1][i].item()))
11
           plt.xticks([])
          plt.yticks([])
12
13
      return(fig)
 1 plot_predict(model)
```

Model optimization

For repeatable experiments we have to set random seeds for anything using random number generation - this means numpy and random as well! It's also worth mentioning that cuDNN uses nondeterministic algorithms which can be disabled setting torch.backends.cudnn.enabled = False. (การสู่มเพื่อเทรน cnn แต่ละครั้งจะ nondeterministic หรือการที่มีความคล้ายกันแค้ไม่เหมือนกัน

```
1 def before_repeat():
2    random_seed = 1
3    torch.backends.cudnn.enabled = False
4    torch.manual_seed(random_seed)

1 before_repeat()
```

ก่อน train model ใหม่ต้องลบรันทาม และรัน def call_function(),train(),test() ก่อนด้วย

Different CNN architectures

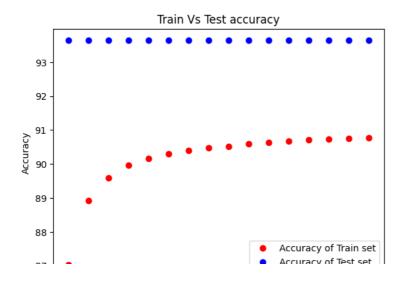
```
เพิ่ม drop out, fully-connected,ลด padding
```

```
1 # cal_out(7,5,1,2)
 1 batch_size = 100
 2 \text{ num workers} = 6
 3 n_{iters} = 10000
 5 #จำนวน epoch = จำนวน iteration/จำนวน batch (training set = 60000)
 6 num_epochs = n_iters / (len(train_data) / batch_size)
 7 num_epochs = int(num_epochs)
 8 print(num_epochs)
10 learning rate = 0.001
   16
 1 class CNN1(nn.Module):
       def __init__(self):
 3
           super(CNN1, self).__init__()
 4
           self.conv1 = nn.Conv2d(in_channels=1,out_channels=16,kernel_size=5,stride=1,padding=0
 5
           self.relu1 = nn.ReLU()
 6
           self.pool1 = nn.MaxPool2d(kernel_size=2)
 7
           self.conv2 = nn.Conv2d(16, 32, 5, 1, 0)
 8
           self.relu2 = nn.ReLU()
 9
           self.pool2 = nn.MaxPool2d(kernel_size=2)
10
           self.dropout = nn.Dropout(p=0.3)
11
12
           self.out1 = nn.Linear(32 * 4 * 4, 256)
13
           # self.out1 = nn.Linear(32 * 4 * 4, 10)
           self.relu3 = nn.ReLU()
14
15
           #fully connected layer, output 10 classes
16
17
           self.out2 = nn.Linear(256, 10)
18
19
20
       def forward(self, x):
21
           x = self.conv1(x)
22
           x = self.relu1(x)
23
           x = self.pool1(x)
24
25
           x = self_conv2(x)
26
           x = self.relu2(x)
27
           x = self.pool2(x)
28
29
           x = self.dropout(x)
30
31
           # # flatten the output of conv2
           x = x.view(x.size(0), -1)
33
           x = self.out1(x)
34
           x = self_relu3(x)
35
           x = self.dropout(x)
36
           output = self.out2(x)
37
           return output
 1 \mod 1 = CNN1()
 2 print(model1)
     (conv1): Conv2d(1, 16, kernel_size=(5, 5), stride=(1, 1))
     (relu1): ReLU()
     (pool1): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mode=False)
     (conv2): Conv2d(16, 32, kernel_size=(5, 5), stride=(1, 1))
     (relu2): ReLU()
     (pool2): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mode=False)
     (dropout): Dropout(p=0.3, inplace=False)
     (out1): Linear(in_features=512, out_features=256, bias=True)
```

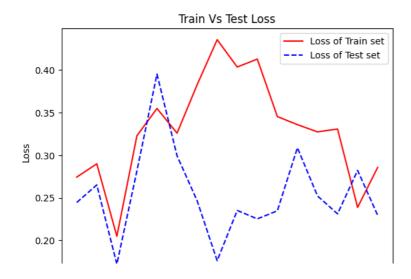
```
(relu3): ReLU()
    (out2): Linear(in_features=256, out_features=10, bias=True)
1 loss func,optimizer = call fuction(model1)
2 optimizer
  Adam (
  Parameter Group 0
      amsgrad: False
      betas: (0.9, 0.999)
      capturable: False
      differentiable: False
      eps: 1e-08
      foreach: None
       fused: None
      lr: 0.001
      maximize: False
      weight_decay: 0.1
1 trainloss,trainacc = train(model1,num epochs,optimizer,loss func)
  Epoch [1/16] Iteration: 600
  Training accuracy: 87.0333 loss: 0.2743
  Epoch [2/16] Iteration: 1200
  Training accuracy: 88.9292 loss: 0.2899
  Epoch [3/16] Iteration: 1800
  Training accuracy: 89.5906 loss: 0.2048
  Epoch [4/16] Iteration: 2400
  Training accuracy: 89.9567 loss: 0.3229
  Epoch [5/16] Iteration: 3000
  Training accuracy: 90.1717 loss: 0.3549
  Epoch [6/16] Iteration: 3600
  Training accuracy: 90.3083 loss: 0.3259
  Epoch [7/16] Iteration: 4200
  Training accuracy: 90.3957 loss: 0.3827
  Epoch [8/16] Iteration: 4800
  Training accuracy: 90.475 loss: 0.4357
  Epoch [9/16] Iteration: 5400
  Training accuracy: 90.5202 loss: 0.4036
  Epoch [10/16] Iteration: 6000
  Training accuracy: 90.589 loss: 0.4129
  Epoch [11/16] Iteration: 6600
  Training accuracy: 90.6445 loss: 0.3454
  Epoch [12/16] Iteration: 7200
  Training accuracy: 90.6831 loss: 0.3359
  Epoch [13/16] Iteration: 7800
  Training accuracy: 90.7206 loss: 0.3274
  Epoch [14/16] Iteration: 8400
  Training accuracy: 90.7415 loss: 0.3308
  Epoch [15/16] Iteration: 9000
  Training accuracy: 90.7627 loss: 0.2387
  Epoch [16/16] Iteration: 9600
  Training accuracy: 90.7754 loss: 0.2857
1 y_trues, y_preds, testloss, testacc = test(model1)
  Epoch [1/16] Iteration: 100
  Testing accuracy: 93.65 loss: 0.2445
  Epoch [2/16] Iteration: 200
  Testing accuracy: 93.65 loss: 0.2651
  Epoch [3/16] Iteration: 300
Testing accuracy: 93.65 loss: 0.172
Epoch [4/16] Iteration: 400
  Testing accuracy: 93.65 loss: 0.2816
  Epoch [5/16] Iteration: 500
  Testing accuracy: 93.65 loss: 0.3953
  Epoch [6/16] Iteration: 600
  Testing accuracy: 93.65 loss: 0.2993
  Epoch [7/16] Iteration: 700
  Testing accuracy: 93.65 loss: 0.2466 Epoch [8/16] Iteration: 800
  Testing accuracy: 93.65 loss: 0.1761
  Epoch [9/16] Iteration: 900
  Testing accuracy: 93.65 loss: 0.2351
  Epoch [10/16] Iteration: 1000
  Testing accuracy: 93.65 loss: 0.2252
  Epoch [11/16] Iteration: 1100
  Testing accuracy: 93.65 loss: 0.2347
  Epoch [12/16] Iteration: 1200
  Testing accuracy: 93.65 loss: 0.3088
  Epoch [13/16] Iteration: 1300
  Testing accuracy: 93.65 loss: 0.2522
  Epoch [14/16] Iteration: 1400
  Testing accuracy: 93.65 loss: 0.2311
```

Epoch [15/16] Iteration: 1500
Testing accuracy: 93.65 loss: 0.2822
Epoch [16/16] Iteration: 1600
Testing accuracy: 93.65 loss: 0.2294

1 plot_acc()



1 plot_loss()



1 disp_report_and_cm()

	prec	ision		recal	l	f1-sco	re	supp	ort	
0		0.97		0.9	6	0.	96		980	
1		0.96		0.9	9	0.	98	1	.135	
2		0.94		0.8	9	0.	92	1	.032	
3		0.88		0.9	7	0.	93	1	.010	
4		0.92		0.9	7	0.	95		982	
5		0.97		0.9	4	0.	96		892	
6		0.91		0.9	7	0.	94		958	
7		0.98		0.8	7	0.	92	1	.028	
8		0.92		0.9	1	0.	92		974	
9		0.91		0.9	0	0.	90	1	.009	
accuracy						0.	94	10	000	
macro avg		0.94		0.9	4	0.	94	10	000	
weighted avg		0.94		0.9	4	0.	94	10	000	
0 - 937 1	1	0	0	3	33	1	4	0		
1 - 0 <mark>112</mark>	0 2	3	2	0	4	0	3	1		1000

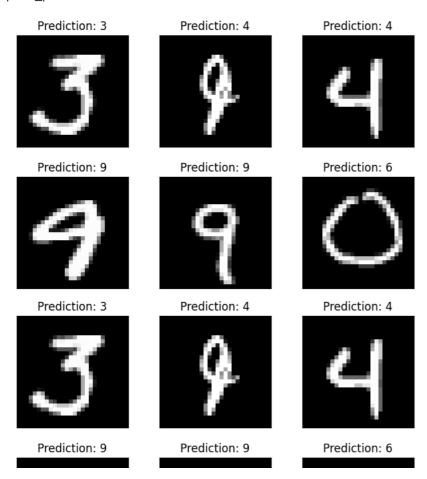
1 print('Accuracy:',accuracy_score(y_trues, y_preds))

2 print('Precision:',precision_score(y_trues, y_preds, average='macro'))

Accuracy: 0.9365

Precision: 0.9376093337555854 Recall: 0.9364077468081048 f1-Score: 0.9361741060721295

1 plot_predict(model1)



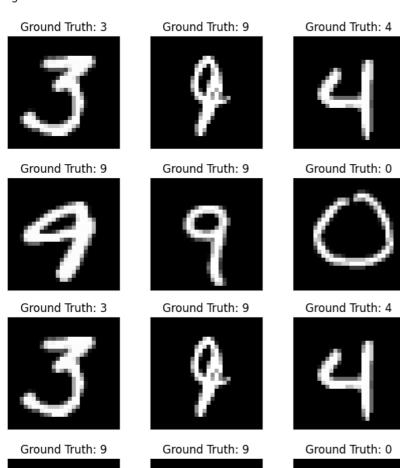
³ print('Recall:',recall_score(y_trues, y_preds, average='macro'))

⁴ print('f1-Score:',f1_score(y_trues, y_preds, average='macro'))

Data augmentation

```
1 transform_train=transforms.Compose([
           transforms.RandomHorizontalFlip(),
 3
           transforms.RandomVerticalFlip(),
 4
           transforms.ToTensor(),
 5
           transforms.Normalize((0.1307,), (0.3081,)) # divides by 255
           1)
 6
 7 transform_test=transforms.Compose([
           transforms.ToTensor(),
           transforms.Normalize((0.1325,), (0.3105,)) # divides by 255
 9
10
 1 train_data = datasets.MNIST(
       root = 'data',
 2
 3
       train = True,
 4
       transform = transform train,
 5
       download = True,
 6)
 7 test_data = datasets.MNIST(
       root = 'data',
 8
 9
       train = False,
10
       transform = transform_test,
11
       download = True,
12)
 1 \, \text{batch\_size} = 100
 2 \text{ num workers} = 6
 3 \text{ n iters} = 10000
 5 #จำนวน epoch = จำนวน iteration/จำนวน batch (training set = 60000)
 6 num epochs = n iters / (len(train data) / batch size)
 7 num_epochs = int(num_epochs)
 8 print(num_epochs)
10 learning_rate = 0.001
   16
 1 loaders = {
       'train' : torch.utils.data.DataLoader(train_data,
 3
                                                batch size=batch size,
                                                shuffle=True),
 4
       'test' : torch.utils.data.DataLoader(test_data,
 5
 6
                                                batch_size=batch_size,
 7
                                                shuffle=True)}
 8 loaders
   {'train': <torch.utils.data.dataloader.DataLoader at 0x7fdb7e23fe80>,
     test': <torch.utils.data.dataloader.DataLoader at 0x7fdb7e23ef20>}
 1 examples = enumerate(loaders['test'])
 2 batch_id, (example_data, example_targets) = next(examples)
 1 example_data.shape
   torch.Size([100, 1, 28, 28])
```

```
1 fig = plt.figure()
2
3 for i in range(6):
4   plt.subplot(2,3,i+1)
5   plt.tight_layout()
6   plt.imshow(example_data[i][0], cmap='gray', interpolation='none')
7   plt.title("Ground Truth: {}".format(example_targets[i]))
8   plt.xticks([])
9   plt.yticks([])
10 fig
```



```
1 loss_func,optimizer = call_fuction(model1)
2 optimizer
  Adam (
  Parameter Group 0
      amsgrad: False
      betas: (0.9, 0.999)
capturable: False
      differentiable: False
      eps: 1e-08
      foreach: None
      fused: None
      lr: 0.001
      maximize: False
      weight_decay: 0.1
1 trainloss,trainacc = train(model1,num_epochs,optimizer,loss_func)
  Epoch [1/16] Iteration: 600
  Training accuracy: 68.955 loss: 0.6889
  Epoch [2/16] Iteration: 1200
  Training accuracy: 71.1675 loss: 0.6685
```

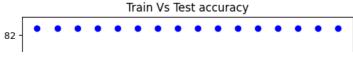
Epoch [3/16] Iteration: 1800

Training accuracy: 72.2644 loss: 0.8567 Epoch [4/16] Iteration: 2400 Training accuracy: 73.0175 loss: 0.7257 Epoch [5/16] Iteration: 3000 Training accuracy: 73.4433 loss: 0.6579 Epoch [6/16] Iteration: 3600 Training accuracy: 73.8172 loss: 0.7397 Epoch [7/16] Iteration: 4200 Training accuracy: 74.061 loss: 0.9463 Epoch [8/16] Iteration: 4800 Training accuracy: 74.2517 loss: 0.9383 Epoch [9/16] Iteration: 5400 Training accuracy: 74.3863 loss: 0.9362 Epoch [10/16] Iteration: 6000 Training accuracy: 74.542 loss: 0.6689 Epoch [11/16] Iteration: 6600 Training accuracy: 74.6724 loss: 0.7209 Epoch [12/16] Iteration: 7200 Training accuracy: 74.7761 loss: 0.7705 Epoch [13/16] Iteration: 7800 Training accuracy: 74.884 loss: 0.8183 Epoch [14/16] Iteration: 8400 Training accuracy: 74.9385 loss: 0.7529 Epoch [15/16] Iteration: 9000 Training accuracy: 75.0258 loss: 0.6349 Epoch [16/16] Iteration: 9600 Training accuracy: 75.0896 loss: 0.9992

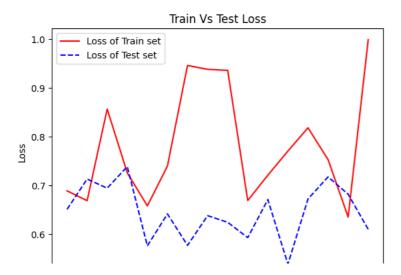
1 y_trues, y_preds, testloss, testacc = test(model1)

Epoch [1/16] Iteration: 100 Testing accuracy: 82.4 loss: 0.6508 Epoch [2/16] Iteration: 200 Testing accuracy: 82.4 loss: 0.713 Epoch [3/16] Iteration: 300 Testing accuracy: 82.4 loss: 0.6943 Epoch [4/16] Iteration: 400 Testing accuracy: 82.4 loss: 0.7386 Epoch [5/16] Iteration: 500 Testing accuracy: 82.4 loss: 0.5758 Epoch [6/16] Iteration: 600 Testing accuracy: 82.4 loss: 0.6414 Epoch [7/16] Iteration: 700 Testing accuracy: 82.4 loss: 0.5768 Epoch [8/16] Iteration: 800 Testing accuracy: 82.4 loss: 0.6378 Epoch [9/16] Iteration: 900 Testing accuracy: 82.4 loss: 0.6242 Epoch [10/16] Iteration: 1000 Testing accuracy: 82.4 loss: 0.5927 Epoch [11/16] Iteration: 1100 Testing accuracy: 82.4 loss: 0.6709 Epoch [12/16] Iteration: 1200 Testing accuracy: 82.4 loss: 0.5382 Epoch [13/16] Iteration: 1300 Testing accuracy: 82.4 loss: 0.672 Epoch [14/16] Iteration: 1400 Testing accuracy: 82.4 loss: 0.7175 Epoch [15/16] Iteration: 1500 Testing accuracy: 82.4 loss: 0.6818 Epoch [16/16] Iteration: 1600 Testing accuracy: 82.4 loss: 0.6097

1 plot_acc()

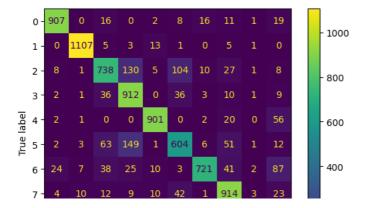






1 disp_report_and_cm()

	precision	recall	f1-score	support
0	0.94	0.93	0.93	980
1	0.97	0.98	0.97	1135
2	0.80	0.72	0.75	1032
3	0.62	0.90	0.74	1010
4	0.93	0.92	0.92	982
5	0.72	0.68	0.70	892
6	0.90	0.75	0.82	958
7	0.80	0.89	0.84	1028
8	0.98	0.58	0.73	974
9	0.74	0.86	0.80	1009
accuracy			0.82	10000
macro avg	0.84	0.82	0.82	10000
weighted avg	0.84	0.82	0.82	10000

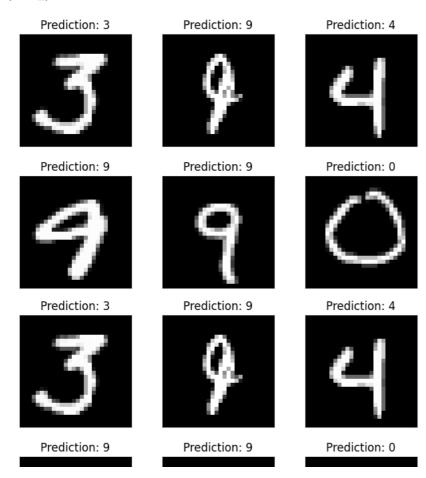


```
1 print('Accuracy:',accuracy_score(y_trues, y_preds))
2 print('Precision:',precision_score(y_trues, y_preds, average='macro'))
3 print('Recall:',recall_score(y_trues, y_preds, average='macro'))
4 print('f1-Score:',f1_score(y_trues, y_preds, average='macro'))
```

Accuracy: 0.824

Precision: 0.839832031379148 Recall: 0.8198635829151002 f1-Score: 0.82055084290603

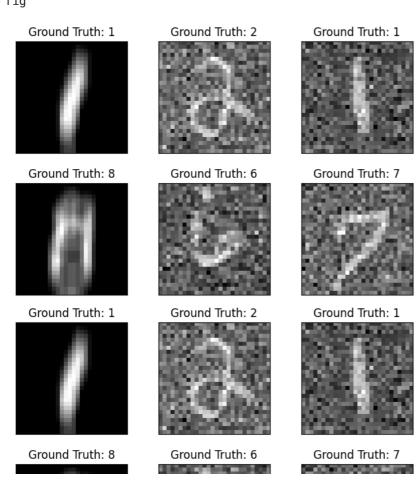
1 plot_predict(model1)



Test by testing dataset (50 images)

```
1 from google.colab import drive
2 drive.mount('/content/drive')
1 transform_test=transforms.Compose([
         transforms.Grayscale(),
3
         transforms.ToTensor(),
         transforms.Normalize((0.1325,), (0.3105,)) # divides by 255
4
5
         ])
1 from torchvision.datasets import ImageFolder
2 test_data_new = ImageFolder('/content/drive/MyDrive/Senior_Project/50images/testing/', transfe
1 print('New test images :', len(test_data_new))
1 loaders['test_new'] = torch.utils.data.DataLoader(test_data_new,
2
                                            batch_size=batch_size,
3
                                            shuffle=True)
```

```
1 examples = enumerate(loaders['test new'])
 2 batch_id, (example_data, example_targets) = next(examples)
 1 example data.shape
   torch.Size([100, 1, 28, 28])
 1 fig = plt.figure()
 3 for i in range(6):
    plt.subplot(2,3,i+1)
 5
    plt.tight_layout()
    plt.imshow(example_data[i][0], cmap='gray', interpolation='none')
    plt.title("Ground Truth: {}".format(example_targets[i]))
 7
    plt.xticks([])
9
    plt.yticks([])
10 fig
```



1 print('Number of iterations in each epoch in test set =',(len(test_data_new) / batch_size))
Number of iterations in each epoch in test set = 5.0

```
1 def test2(cnn):
      # Test the model
 2
 3
      cnn.eval()
 4
      loss each = []
 5
      acc_each = []
 6
      y_trues = []
 7
      y_preds = []
 8
      with torch.no_grad():
 9
           iter = 0
10
           correctImages = 0
11
           totalImages = 0
           for epoch in range(num epochs):
12
               for images, labels in loaders['test new']:
13
14
                   outputs = cnn(images)
15
                   _, predicted = torch.max(outputs, 1)
                   loss = loss_func(outputs, labels)
16
17
                   if epoch == (num_epochs-1):
                       for i in labels.tolist():
18
19
                           y_trues.append(i)
20
                       for i in predicted.tolist():
                           y_preds.append(i)
21
22
                   correctImages += (predicted == labels).sum().item()
23
                   totalImages += labels.size(0)
24
                   accumulateAccuracy = round((correctImages/totalImages)*100,4)
25
                   iter += 1
26
                   # Number of iterations in each epoch in test set
27
28
                   if iter % 5 == 0:
29
                       print('Epoch [{}/{}] Iteration: {}'.format(epoch+1, num_epochs, iter))
30
                       print('Testing accuracy: {} loss: {}'.format(accumulateAccuracy, round(lo
31
                       loss each.append(round(loss.item(),4))
32
                       acc each.append(accumulateAccuracy)
33
                       pass
34
               pass
          pass
35
36
      pass
37
               # print('Test Accuracy of the model on the 10000 test images: %.2f' % accuracy)
38
39
40
      return y_trues, y_preds,loss_each,acc_each
```

Base Model

```
1 y_trues, y_preds, testloss, testacc = test2(model)

1 plot_acc()

1 plot_loss()

1 disp_report_and_cm()

1 print('Accuracy:',accuracy_score(y_trues, y_preds))
2 print('Precision:',precision_score(y_trues, y_preds, average='macro'))
3 print('Recall:',recall_score(y_trues, y_preds, average='macro'))
4 print('f1-Score:',f1_score(y_trues, y_preds, average='macro'))

1 plot_predict(model)
```

> New Model

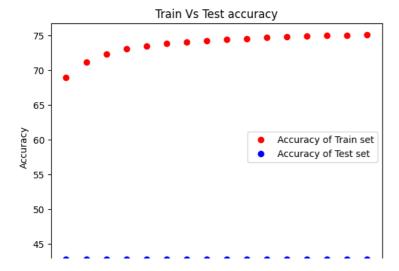
```
[] 🕁 ช่อน 6 เซลล์
```

New Model with augmentation

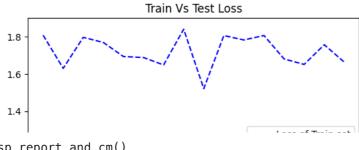
1 y_trues, y_preds, testloss, testacc = test2(model1)

Epoch [1/16] Iteration: 5 Testing accuracy: 42.8 loss: 1.8082 Epoch [2/16] Iteration: 10 Testing accuracy: 42.8 loss: 1.6302 Epoch [3/16] Iteration: 15 Testing accuracy: 42.8 loss: 1.7968 Epoch [4/16] Iteration: 20 Testing accuracy: 42.8 loss: 1.7691 Epoch [5/16] Iteration: 25 Testing accuracy: 42.8 loss: 1.6936 Epoch [6/16] Iteration: 30 Testing accuracy: 42.8 loss: 1.6883 Epoch [7/16] Iteration: 35 Testing accuracy: 42.8 loss: 1.6485 Epoch [8/16] Iteration: 40 Testing accuracy: 42.8 loss: 1.8405 Epoch [9/16] Iteration: 45 Testing accuracy: 42.8 loss: 1.5212 Epoch [10/16] Iteration: 50 Testing accuracy: 42.8 loss: 1.8063 Epoch [11/16] Iteration: 55 Testing accuracy: 42.8 loss: 1.7826 Epoch [12/16] Iteration: 60 Testing accuracy: 42.8 loss: 1.8067 Epoch [13/16] Iteration: 65 Testing accuracy: 42.8 loss: 1.6807 Epoch [14/16] Iteration: 70 Testing accuracy: 42.8 loss: 1.6512 Epoch [15/16] Iteration: 75 Testing accuracy: 42.8 loss: 1.757 Epoch [16/16] Iteration: 80 Testing accuracy: 42.8 loss: 1.6635

1 plot_acc()



1 plot_loss()



1 (disp	_re	oort	_and	_cm()	
-----	------	-----	------	------	------	---	--

	precision	recall	f1-score	support
0	0.76	0.78	0.77	50
1	0.36	0.34	0.35	50
2	0.62	0.42	0.50	50
3	0.40	0.48	0.44	50
4	0.26	0.60	0.36	50
5	1.00	0.02	0.04	50
6	0.61	0.44	0.51	50
7	0.94	0.30	0.45	50
8	0.31	0.54	0.39	50
9	0.36	0.36	0.36	50
accuracy			0.43	500
macro avg	0.56	0.43	0.42	500
weighted avg	0.56	0.43	0.42	500

0 -	39	0	2	0	5	0	0	0	3	1		
1 -	0	17	0	0	6	0	0	0	27	0		- 35
2 -	5	4	21		6	0		1	4	0	-	30
3 -		5	3	24	4	0	2	0	5	4	-	- 25
label	1	0	1	0	30	0	1	0				- 20
True -	1	7	1	22	5	1	2	0	2			20
6 -	0	0	1	1	22	0	22	0	2	2		- 15
7 -	0	6	5	2	10	0	5	15	3	4		- 10

```
1 print('Accuracy:',accuracy_score(y_trues, y_preds))
2 print('Precision:',precision_score(y_trues, y_preds, average='macro'))
3 print('Recall:',recall_score(y_trues, y_preds, average='macro'))
4 print('f1-Score:',f1_score(y_trues, y_preds, average='macro'))
```

Accuracy: 0.428

Precision: 0.5615894618175594 Recall: 0.428000000000000005 f1-Score: 0.4175131160752478

1 plot_predict(model1)











