

q6

Thursday, May 02, 2024 9:09 PM

6) Write a program to apply various 2D transformations on a 2D object (use homogenous coordinates).

===== reflection about an arbitrary axis=====

```
#include <iostream>
#include <conio.h>
#include <math.h>
```

```
#include "dda.cpp"
#include <graphics.h>
```

```
using namespace std;
```

```
void matrixMultiplication(double **mat1, int rows1, int cols1,
                          double **mat2, int rows2, int cols2,
                          double **result) {
```

```
    if (cols1 != rows2) {
        std::cerr << "Error: Matrix dimensions \n";
        return;
    }
```

```
    for (int i = 0; i < rows1; ++i) {
        for (int j = 0; j < cols2; ++j) {
            result[i][j] = 0;
            for (int k = 0; k < cols1; ++k) {
                result[i][j] += mat1[i][k] * mat2[k][j];
            }
        }
    }
}
```

```
void print_sq_arr(double **arr ,int row, int col){
```

```
    for(int i=0;i<row;i++){
        for(int j=0;j<col;j++){
            cout<<arr[i][j]<<" , ";
        }
        cout<<endl;
    }
```

```
}
```

```
double **make_hom_2d_array_zero(int row,int col){
    double **arr = new double*[row];
```

```
    for(int i=0;i<row;i++){
        arr[i] = new double[col];
    }
    for(int i=0;i<row;i++){
```

```

        for(int j=0;j<col;j++){
            arr[i][j]=0.0;
        }
    }
    return &*arr;
}

```

```

double **make_hom_2d_array_ones(int row,int col){
    double **arr = new double*[row];

```

```

        for(int i=0;i<row;i++){
            arr[i] = new double[col];
        }
    for(int i=0;i<row;i++){
        for(int j=0;j<col;j++){
            arr[i][j]=1.0;
        }
    }
    return &*arr;
}

```

```

void fill_composite_matrix(double **arr,double m, double c){

```

```

    arr[0][0] = (1 - pow(m,2)) / (1 + pow(m,2));
    arr[1][0] = (2*m) / (1 + pow(m,2));
    arr[2][0] = (-2*c*m) / (1 + pow(m,2));

```

```

    arr[0][1] = (2*m) / (1 + pow(m,2));
    arr[1][1] = (pow(m,2) - 1) / (1 + pow(m,2));
    arr[2][1] = (2*c) / (1 + pow(m,2));

```

```

    arr[2][2] = 1;

```

```

}

```

```

void draw_square(double **arr,int r,int c,int colorr){
    dda(arr[0][0], arr[0][1], arr[1][0], arr[1][1],colorr);
    dda( arr[2][0], arr[2][1],arr[1][0], arr[1][1],colorr); //200, 100 200, 0
    dda(arr[2][0], arr[2][1], arr[3][0], arr[3][1],colorr);
    dda( arr[0][0], arr[0][1],arr[3][0], arr[3][1],colorr);
}

```

```

void draw_mirror(double m, double c){ // bcoz it fails at vertical line

```

```

    double y1=0, x1=0, y2=0, x2=0;

```

```

    if(m !=0){
        y1 = m*(0) + c;
        y2 = m*(getmaxx()) + c;
        x1 = (y1 - c)/m;
        x2 = (y2 - c)/m;
    }else{

```

```

        x1 = 0;
        x2 = getmaxx();
        y1 = c;
        y2 = c;

```

```

    }
    dda(x1,y1,x2,y2,GREEN);

```

```

}

```

```
int main()
{

    int gd = DETECT, gm;
    char pathtodriver[] = "";
    initgraph(&gd, &gm, pathtodriver);

    double **mat = make_hom_2d_array_zero(3,3);

    double m = 1.0;
    double c = -20.0;

    draw_mirror(m,c); // 0 for horizontal , 1 for vertical , y = 200

    fill_composite_matrix(mat,m,c);

    int row = 4;
    double **arr = make_hom_2d_array_ones(row,3);

    //x
    arr[0][0] = 100;
    arr[1][0] = 200;
    arr[2][0] = 200;
    arr[3][0] = 100;

    //y
    arr[0][1] = 0;
    arr[1][1] = 0;
    arr[2][1] = 100;
    arr[3][1] = 100;

    draw_square(arr,row,3,GREEN);

    double **res = make_hom_2d_array_zero(row,3);

    matrixMultiplication(arr,row,3,mat,3,3,res);
    draw_square(res,row,3,BLUE);

    // will fail only for vertical line

    getch();
    closegraph();

    return 0;

}
```

```
//===== ROTATION. +
translation =====

#include <iostream>
#include <conio.h>
#include <math.h>
#include "dda.cpp"

#include <graphics.h>
using namespace std;

#define M_PI 3.14159265358979323846

class my_matrix{

public:

double** matrix ;
int row;
int col;

my_matrix(){

}

my_matrix(int r,int v){

row = r;
col = 3; // for homogeneous

matrix = new double*[r];

// Allocate memory for each row
for (int i = 0; i < r; ++i) {
    matrix[i] = new double[3]; // Create an array of integers for
each row
}

// Initialize each element to 1
for (int i = 0; i < r; ++i) {
    for (int j = 0; j < 3; ++j) {
        matrix[i][j] = v;
    }
}

}

void print_obj(){

cout<<"-----OBJECT-----\n";

for (int i = 0; i < row; ++i) {
    for (int j = 0; j < col; ++j) {
        std::cout << matrix[i][j] << " ";
    }
    std::cout << std::endl;
}

}
```

```

cout<<"-----\n";
}

void deallocate_matrix(){
    // Free dynamically allocated memory
    for (int i = 0; i < row; ++i) {
        delete[] matrix[i];
    }
    delete[] matrix;
}

};

double angle_to_radian(double degrees){
    return degrees * (M_PI / 180.0);
}

void draw_object(my_matrix *obj,int colorr){
    int x1=0;
    int y1=0;

    int x2=0;
    int y2=0;
    x1 = obj->matrix[0][0];
    y1 = obj->matrix[0][1];

    for (int i = 1; i < obj->row; ++i) {

        x2 = obj->matrix[i][0];
        y2 = obj->matrix[i][1];

        dda(x1,y1,x2,y2,colorr);

        x1 = x2;
        y1 = y2;

        // draw and switch
    }

    dda(x1,y1, obj->matrix[0][0], obj->matrix[0][1],colorr);
}

void create_rotation_matrix(double degrees, my_matrix *obj){ // angle is
in degree , can be used -90 degree

    obj->matrix[0][0] = round(cos(angle_to_radian(degrees)) * 10000) /
10000;
    obj->matrix[1][1] = round(cos(angle_to_radian(degrees)) * 10000) /
10000 ;
    obj->matrix[0][1] = round(sin(angle_to_radian(degrees))* 10000) /
10000 ;
    obj->matrix[1][0] = round(-sin(angle_to_radian(degrees)) * 10000) /
10000;
    obj->matrix[2][2] = 1;

}

```

```

void matrix_multiplication(my_matrix *obj , my_matrix *scaling ,
my_matrix *result){
    // Function to perform matrix multiplication
    if (obj->col != scaling->row) {
        std::cerr << "Error: Matrix dimensions mismatch for
multiplication." << std::endl;
        exit(1);
    }

    for (int i = 0; i < obj->row; ++i) {
        for (int j = 0; j < scaling ->col; ++j) {
            result -> matrix[i][j] = 0;

            for (int k = 0; k < obj -> col ; ++k) {
                result -> matrix[i][j] += obj->matrix[i][k] * scaling -> matrix[k]
[i];
            }

        }
    }
}

```

```

void create_translation_matrix(int tx,int ty, my_matrix *obj){
    obj->matrix[0][0] = 1;
    obj->matrix[1][1] = 1;
    obj->matrix[2][2] = 1;
    obj->matrix[2][0] = tx;
    obj->matrix[2][1] = ty;
}

```

```

int main(){

    int r = 4 ;
    // cout<<"\ngive the number of points : ";
    // cin>>r;
    my_matrix *obj;

    if(r>=1){
        cout<<"matrix made"<<endl;
        obj = new my_matrix(r,1);
        obj->print_obj();
    }else{
        cout<<"invalid input";
        return 0;
    }
}

```

```

// int temp =0;
// double x =0;
// double y = 0;

```

```

// while(temp < r){

```

```

//  cout<<"x , y : ";
//  cin>>x>>y;

```

```

//  obj->matrix[temp][0] = x;
//  obj->matrix[temp][1] = y;

```

```
// temp +=1;

// }

//x
obj->matrix[0][0] = 100;
obj->matrix[1][0] = 200;
obj->matrix[2][0] = 200;
obj->matrix[3][0] = 100;

//y
obj->matrix[0][1] =0;
obj->matrix[1][1] =0;
obj->matrix[2][1] =100;
obj->matrix[3][1] =100;

double degrees = 45.0 ;
// cout<<"\nrotation factor in x : ";
// cin>>degrees;

my_matrix *rotation_matrix = new my_matrix(3,0);
create_rotation_matrix(degrees, rotation_matrix);

// 4 x 3    3 x 3 --> 4 x 3

// before rotation translate centroid to center
double x_centroid = 0;
double y_centroid= 0;

for(int i =0;i<obj->row;i++){
    x_centroid += obj->matrix[i][0];
    y_centroid += obj->matrix[i][1];
}

x_centroid = -1*(x_centroid / obj->row);
y_centroid = -1*(y_centroid / obj->row);

my_matrix *translation_mat = new my_matrix(3,0);

// translation
my_matrix *result1 = new my_matrix(r,0);
create_translation_matrix(x_centroid , y_centroid,translation_mat);
matrix_multiplication(obj,translation_mat,result1);

//rotation
my_matrix *result2 = new my_matrix(r,0);
matrix_multiplication(result1,rotation_matrix, result2);

my_matrix *translation_mat_inv = new my_matrix(3,0);
```

```
create_translation_matrix(-1*x_centroid , -1*y_centroid,
translation_mat_inv);
```

```
// inverse translation
```

```
my_matrix *result3 = new my_matrix(r,0);
```

```
matrix_multiplication(result2 , translation_mat_inv, result3);
```

```
int gd = DETECT, gm;
```

```
char pathtodriver[] = "";
```

```
initgraph(&gd, &gm, pathtodriver);
```

```
draw_object(obj, GREEN);
```

```
draw_object(result3, RED);
```

```
getch();
```

```
closegraph();
```

```
return 0;
```

```
}
```

```
//=====.
```

```
SCALING=====
```

```
#include <iostream>
```

```
#include <conio.h>
```

```
#include <math.h>
```

```
#include "dda.cpp"
```

```
#include <graphics.h>
```

```
using namespace std;
```

```
class my_matrix{ // 6 x 3 {object , triangle , square , polygon} 3 x 3 {
scaling matrix, scaling} --> 6 x 3
```

```
public:
```

```
int** matrix ;
```

```
int row;
```

```
int col;
```

```
my_matrix(){
```

```
}
```

```
my_matrix(int r,int v){ // 0, 1 object ,,1 transfo 0
```

```
row = r;
```

```
col = 3; // for homogeneous
```

```
matrix = new int*[r];
```

```
// Allocate memory for each row
```

```
for (int i = 0; i < r; ++i) {
```

```
matrix[i] = new int[3]; // Create an array of integers for each
```

```
row
```

```
}
```

```
// Initialize each element to 1
```



```

        for (int i = 0; i < r; ++i) {
            for (int j = 0; j < 3; ++j) {
                matrix[i][j] = v;
            }
        }
    }

void print_obj(){

cout<<"-----OBJECT-----"
-----\n";
    for (int i = 0; i < row; ++i) {
        for (int j = 0; j < col; ++j) {
            std::cout << matrix[i][j] << " ";
        }
        std::cout << std::endl;
    }

    cout<<"-----"
-----\n";
}

void deallocate_matrix(){
    // Free dynamically allocated memory
    for (int i = 0; i < row; ++i) {
        delete[] matrix[i];
    }
    delete[] matrix;
}

};

void create_scaling_matrix(int sx,int sy, my_matrix *obj){
    obj->matrix[0][0] = sx;
    obj->matrix[1][1] = sy;
    obj->matrix[2][2] = 1;
}

// object x scaling matrix - -> result
void matrix_multiplication(my_matrix *obj , my_matrix *scaling ,
my_matrix *result){
    // Function to perform matrix multiplication

    if (obj->col != scaling->row) {
        std::cerr << "Error: Matrix dimensions mismatch for
multiplication." << std::endl;
        exit(1);
    }

    for (int i = 0; i < obj->row; ++i) {
        for (int j = 0; j < scaling ->col; ++j) {
            result -> matrix[i][j] = 0;

            for (int k = 0; k < obj -> col ; ++k) {
                result -> matrix[i][j] += obj->matrix[i][k] * scaling -> matrix[k]
[i];
            }

        }
    }
}

```

```
// [x1, y1, 1]
//[ x2, y2, 1]
//[ x3 , y3, 1]
//[x4, y4, 1]

void draw_object(my_matrix *obj,int colorr){
    int x1=0;
    int y1=0;

    int x2=0;
    int y2=0;

    x1 = obj->matrix[0][0];
    y1 = obj->matrix[0][1];

    for (int i = 1; i < obj->row; ++i) {

        x2 = obj->matrix[i][0];
        y2 = obj->matrix[i][1];

        dda(x1,y1,x2,y2,colorr);

        x1 = x2;
        y1 = y2;

        // draw and switch
    }

    dda(x1,y1, obj->matrix[0][0], obj->matrix[0][1],colorr);
}

int main(){

    int r = 4;
    // cout<<"\ngive the number of points : ";
    // cin>>r;
    my_matrix *obj;

    if(r>=1){
        cout<<"matrix made"<<endl;
        obj = new my_matrix(r,1);
        obj->print_obj();
    }else{
        cout<<"invalid input";
        return 0;
    }

    int temp =0;
    int x =0;
```

```

int y = 0;

// while(temp < r){

//   cout<<"x , y : ";
//   cin>>x>>y;

//   obj->matrix[temp][0] = x;
//   obj->matrix[temp][1] = y;

// temp +=1;

// }
//x
//x
obj->matrix[0][0] = 100;
obj->matrix[1][0] = 200;
obj->matrix[2][0] = 200;
obj->matrix[3][0] = 100;

//y
obj->matrix[0][1] =0;
obj->matrix[1][1] =0;
obj->matrix[2][1] =100;
obj->matrix[3][1] =100;

cout<<endl;

int sx = 2 ;
int sy = 2;
// cout<<"scaling factor in x : ";
// cin>>sx;

// cout<<"scaling factor in y : ";
// cin>>sy;

my_matrix *scaling_matrix = new my_matrix(3,0); // 3 x 3 , default 0
create_scaling_matrix(sx,sy,scaling_matrix);

cout<<"scaling matrix::"<<endl;
scaling_matrix->print_obj();

cout<<"\nyour input : "<<endl;
obj->print_obj();

my_matrix *result = new my_matrix(r,0); // 4 x 3   3 x 3 --> 4 x 3

matrix_multiplication(obj,scaling_matrix,result); // pre multiplication

cout<<"=====RESULT=====
=====\\n";
result->print_obj();

```

```
int gd = DETECT, gm;
char pathtodriver[] = "";
initgraph(&gd, &gm, pathtodriver);
```

```
draw_object(obj,BLUE);
draw_object(result,GREEN);
```

```
getch();
closegraph();
```

```
return 0;
}
```

```
//===== SHEAR
=====
```

```
#include <iostream>
#include <conio.h>
#include <math.h>
#include "dda.cpp"
```

```
#include <graphics.h>
using namespace std;
```

```
class my_matrix{
```

```
public:
```

```
int** matrix ;
int row;
int col;
```

```
my_matrix(){
```

```
}
```

```
my_matrix(int r,int v){
```

```
row = r;
col = 3; // for homogeneous
```

```
matrix = new int*[r];
```

```
// Allocate memory for each row
for (int i = 0; i < r; ++i) {
    matrix[i] = new int[3]; // Create an array of integers for each
row
}
```

```

        // Initialize each element to 1
        for (int i = 0; i < r; ++i) {
            for (int j = 0; j < 3; ++j) {
                matrix[i][j] = v;
            }
        }
    }

}

void print_obj(){

cout<<"-----OBJECT-----"
-----\n";
    for (int i = 0; i < row; ++i) {
        for (int j = 0; j < col; ++j) {
            std::cout << matrix[i][j] << " ";
        }
        std::cout << std::endl;
    }

    cout<<"-----"
-----\n";
}

void deallocate_matrix(){
    // Free dynamically allocated memory
    for (int i = 0; i < row; ++i) {
        delete[] matrix[i];
    }
    delete[] matrix;
}

};

void create_shear_matrix(int sx,int sy, my_matrix *obj){
    obj->matrix[0][0] = 1;
    obj->matrix[1][1] = 1;
    obj->matrix[2][2] = 1;

    obj->matrix[0][1] = sy;
    obj->matrix[1][0] = sx;

    // [1 sy 0]
    // [sx 1 0]
    // [0 0 1]

}

void matrix_multiplication(my_matrix *obj , my_matrix *shear_mat ,
my_matrix *result){
    // Function to perform matrix multiplication

    if (obj->col != shear_mat->row) {

```

```

        std::cerr << "Error: Matrix dimensions mismatch for
multiplication." << std::endl;
        exit(1);
    }

    for (int i = 0; i < obj->row; ++i) {
        for (int j = 0; j < shear_mat->col; ++j) {
            result->matrix[i][j] = 0;

            for (int k = 0; k < obj->col ; ++k) {
                result->matrix[i][j] += obj->matrix[i][k] * shear_mat->
matrix[k][j];
            }
        }
    }
}

```

```

void draw_object(my_matrix *obj,int colorr){
    int x1=0;
    int y1=0;

    int x2=0;
    int y2=0;

```

```

    x1 = obj->matrix[0][0];
    y1 = obj->matrix[0][1];

```

```

    for (int i = 1; i < obj->row; ++i) {

```

```

        x2 = obj->matrix[i][0];
        y2 = obj->matrix[i][1];

```

```

        dda(x1,y1,x2,y2,colorr);

```

```

        x1 = x2;
        y1 = y2;

```

```

        // draw and switch
    }

```

```

    dda(x1,y1, obj->matrix[0][0], obj->matrix[0][1],colorr);
}

```

```

int main(){

```

```

    int r =4 ;
    // cout<<"ngive the number of points : ";

```

```

// cin>>r;
my_matrix *obj;

if(r>=1){
    cout<<"matrix made"<<endl;
    obj = new my_matrix(r,1);
    obj->print_obj();
}else{
    cout<<"invalid input";
    return 0;
}

int temp =0;
int x =0;
int y = 0;

// while(temp < r){

//     cout<<"x , y : ";
//     cin>>x>>y;

//     obj->matrix[temp][0] = x;
//     obj->matrix[temp][1] = y;

// temp +=1;

// }
//x
obj->matrix[0][0] = 100;
obj->matrix[1][0] = 200;
obj->matrix[2][0] = 200;
obj->matrix[3][0] = 100;

//y
obj->matrix[0][1] =0;
obj->matrix[1][1] =0;
obj->matrix[2][1] =100;
obj->matrix[3][1] =100;
cout<<endl;

int sx = 2 ;
int sy = 1;
// cout<<"shear factor in x : ";
// cin>>sx;

// cout<<"shear factor in y : ";
// cin>>sy;

my_matrix *shear_matrix = new my_matrix(3,0);;
create_shear_matrix(sx,sy,shear_matrix);

cout<<"\nyour input : "<<endl;
obj->print_obj();

my_matrix *result = new my_matrix(r,0); // 4 x 3    3 x 3 --> 4 x 3
matrix_multiplication(obj,shear_matrix,result);

```

```
int gd = DETECT, gm;  
char pathtodriver[] = "";  
initgraph(&gd, &gm, pathtodriver);
```

```
draw_object(obj,BLUE);  
draw_object(result,GREEN);
```

```
result->print_obj();
```

```
getch();  
closegraph();
```

```
return 0;  
}
```

```
//=====
```

```
//6) Write a program to apply various 2D transformations on a 2D object  
(use homogenous  
//coordinates).
```

```
#include <iostream>  
#include <conio.h>  
#include <math.h>  
#include "dda.cpp"
```

```
#include <graphics.h>
```

```
using namespace std;
```

```
class my_matrix{
```

```
public:
```

```
int** matrix ;  
int row;  
int col;
```

```
my_matrix(){
```

```
}
```

```
my_matrix(int r,int v){
```



```

row = r;
col = 3; // for homogeneous

matrix = new int*[r];

// Allocate memory for each row
for (int i = 0; i < r; ++i) {
    matrix[i] = new int[3]; // Create an array of integers for each
row
}

// Initialize each element to 1
for (int i = 0; i < r; ++i) {
    for (int j = 0; j < 3; ++j) {
        matrix[i][j] = v;
    }
}

}

void print_obj(){

cout<<"-----OBJECT-----"
-----\n";
for (int i = 0; i < row; ++i) {
    for (int j = 0; j < col; ++j) {
        std::cout << matrix[i][j] << " ";
    }
    std::cout << std::endl;
}

cout<<"-----"
-----\n";
}

void deallocate_matrix(){
    // Free dynamically allocated memory
    for (int i = 0; i < row; ++i) {
        delete[] matrix[i];
    }
    delete[] matrix;
}

};

```

```

void create_scaling_matrix(int tx,int ty, my_matrix *obj){
    obj->matrix[0][0] = 1;
    obj->matrix[1][1] = 1;
    obj->matrix[2][2] = 1;

    obj->matrix[2][0] = tx;
    obj->matrix[2][1] = ty;

```

```
// [ 1 0 0]
// [ 0 1 0]
// [tx ty 1]
```

```
}
```

```
void matrix_multiplication(my_matrix *obj , my_matrix *scaling ,
my_matrix *result){
```

```
// Function to perform matrix multiplication
```

```
    if (obj->col != scaling->row) {
        std::cerr << "Error: Matrix dimensions mismatch for
multiplication." << std::endl;
        exit(1);
    }
```

```
    for (int i = 0; i < obj->row; ++i) {
        for (int j = 0; j < scaling->col; ++j) {
            result->matrix[i][j] = 0;
```

```
            for (int k = 0; k < obj->col ; ++k) {
                result->matrix[i][j] += obj->matrix[i][k] * scaling->matrix[k]
[i];
            }
```

```
        }
    }
```

```
}
```

```
void draw_object(my_matrix *obj,int colorr){
```

```
    int x1=0;
    int y1=0;
```

```
    int x2=0;
    int y2=0;
```

```
    x1 = obj->matrix[0][0];
    y1 = obj->matrix[0][1];
```

```
    for (int i = 1; i < obj->row; ++i) {
```

```
        x2 = obj->matrix[i][0];
        y2 = obj->matrix[i][1];
```

```
        dda(x1,y1,x2,y2,colorr);
```

```
        x1 = x2;
        y1 = y2;
```

```
// draw and switch
}

dda(x1,y1, obj->matrix[0][0], obj->matrix[0][1],colorr);
}

int main(){

    int r = 4 ;
    cout<<"\ngive the number of points : ";
    // cin>>r;
    my_matrix *obj;

    if(r>=1){
        cout<<"matrix made"<<endl;
        obj = new my_matrix(r,1);
        obj->print_obj();
    }else{
        cout<<"invalid input";
        return 0;
    }

    int temp =0;
    int x =0;
    int y = 0;

    // while(temp < r){

    //     cout<<"x , y : ";
    //     cin>>x>>y;

    //     obj->matrix[temp][0] = x;
    //     obj->matrix[temp][1] = y;

    //     temp +=1;

    // }
    //x
    obj->matrix[0][0] = 100;
    obj->matrix[1][0] = 200;
    obj->matrix[2][0] = 200;
    obj->matrix[3][0] = 100;

    //y
    obj->matrix[0][1] =0;
    obj->matrix[1][1] =0;
    obj->matrix[2][1] =100;
    obj->matrix[3][1] =100;
    cout<<endl;

    int tx = 0 ;
    int ty = 0;
    cout<<"translation factor in x : ";
    cin>>tx;
```

```
cout<<"translation factor in y : ";
cin>>ty;
```

```
my_matrix *translation_matrix = new my_matrix(3,0);
```

```
create_scaling_matrix(tx,ty,translation_matrix);
```

```
cout<<"translation matrix::"<<endl;
translation_matrix->print_obj();
```

```
cout<<"\nyour input : "<<endl;
obj->print_obj();
```

```
my_matrix *result = new my_matrix(r,0); // 4 x 3   3 x 3 --> 4 x 3
```

```
matrix_multiplication(obj,translation_matrix,result);
```

```
cout<<"=====RESULT=====
=====\\n";
result->print_obj();
```

```
int gd = DETECT, gm;
char pathtodriver[] = "";
initgraph(&gd, &gm, pathtodriver);
```

```
draw_object(obj,RED);
draw_object(result,BLUE);
```

```
getch();
closegraph();
```

```
return 0;
}
```

```
//=====
```

