

Oscillators :-

- capable of generating a variety of o/p wfs.
- Basically funⁿ of an oscillator is to generate alternating current or voltage wfs.
- an oscillator is a ckt that generates a repetitive wf of fixed amplitude & freqⁿ without any external i/p signal.

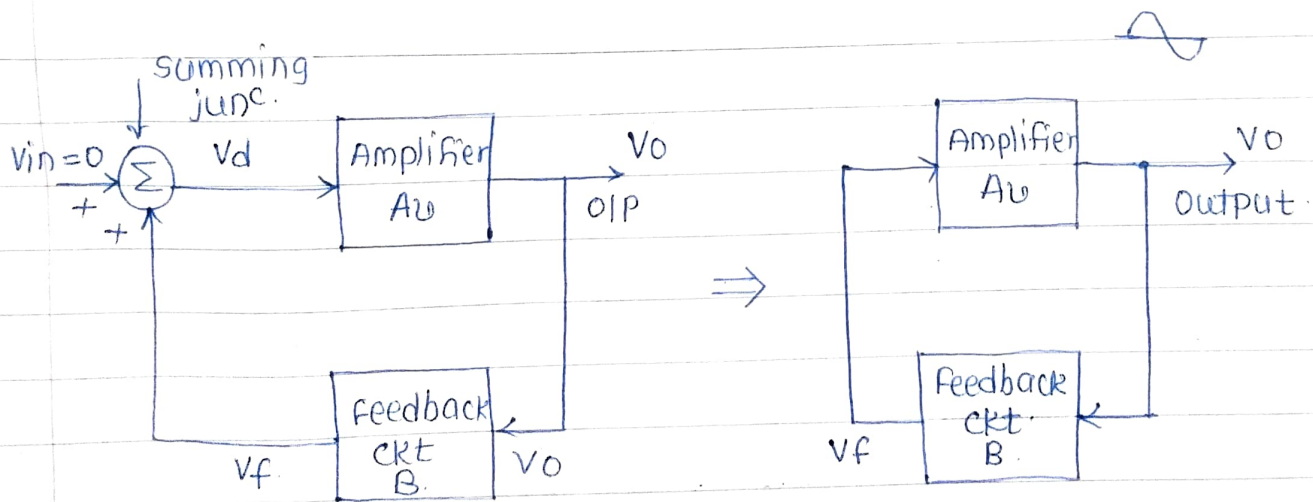
Applications:

- in radio, TV, computers & commⁿ.

Oscillator Principles :-

- It is a type of flb amp^r in which part of the o/p is fed back to the i/p via a feedback ckt. If the signal fed back is of proper magnitude & phase, the ckt produces alternating currents or voltages.

oscillator Block diagram :-



→ Here $V_{in} = 0$ & the flb is +ve, because most oscillators use +ve flb. Finally, the closed-loop gain of the amp^r is denoted by A_v , rather than A_f .

From block diagram,

$$V_d = V_f + V_{in}$$

$$V_o = A_v \cdot V_d$$

$$v_f = B \cdot v_o$$

Using these relationships, the following eqⁿ is obtained.

$$\frac{v_o}{v_{in}} = \frac{A_v}{1 - A_v \cdot B}$$

However, $v_{in} = 0$ & $v_o \neq 0$ implies that,

$$A_v \cdot B = 1$$

Expressed in polar form,

$$A_v \cdot B = 1 \angle 0^\circ \text{ or } 360^\circ \quad \text{--- (1)}$$

Eqⁿ (1) gives the two requirements for oscillation:

- 1) magnitude of the loop gain $A_v B$ must be at least 1 &
- 2) total phase shift of the loop gain $A_v B$ must be equal to 0° or 360° .

— The type of wlf generated by oscillator depends on the components in the ckt & hence may be sinusoidal, square or triangular.

— Freqⁿ of oscillation is determined by the components in the $A_v B$ ckt.

⇒ Oscillator Types :-

	Types of components used.	Freq ⁿ of oscillation	Type of wlf generated.
1.	RC oscillator	Audio Freq ⁿ (AF)	Sinusoidal
2.	LC oscillator	Radio Freq ⁿ (RF)	Square wave
3.	Crystal oscillator		Triangular wave sawtooth wave, etc.

⇒ Freqⁿ stability :-

- Ability of the oscillator ckt to oscillate at one exact freqⁿ is called Freqⁿ stability.
- no. of factors may cause changes in oscillator freqⁿ.
- Primary factors are temp. changes & changes in the DC power supply.

- Temp & power supply changes cause variations in the op-amp's gain, in junction capacitances & resistances of the transistors in an op-amp & in external ckt. components.
- Another imp. factor that determines freqⁿ stability is the figure of merit Q of the ckt. Q is defined as $Q = \frac{\text{resonant freq}}{\text{bandwidth}}$.
- Higher the Q , the greater the stability.

Hence crystal oscillators are far more stable than RC or LC, especially at higher frequencies.

- LC ckt's & crystals are generally used for the generation of high freqⁿ signals, while RC components are most suitable for audio freqⁿ applications.
- We will see audio-freqⁿ RC oscillators only.

1. phase shift oscillator.

2. Wein bridge oscillator

3. Quadrature oscillator:

Wein Bridge Oscillator :-

It is simple & stable. Hence one of the most commonly used audio freqⁿ oscillators is the Wein bridge.

Fig. shows Wein Bridge oscillator in which the Wein bridge ckt is connected betⁿ the amp^r. I/P terminals & the O/P terminals.

The bridge has a series RC n/w in one arm & a parallel RC n/w in the adjoining arm.

In the remaining two arms of the bridge resistors R_1 & R_F are connected.

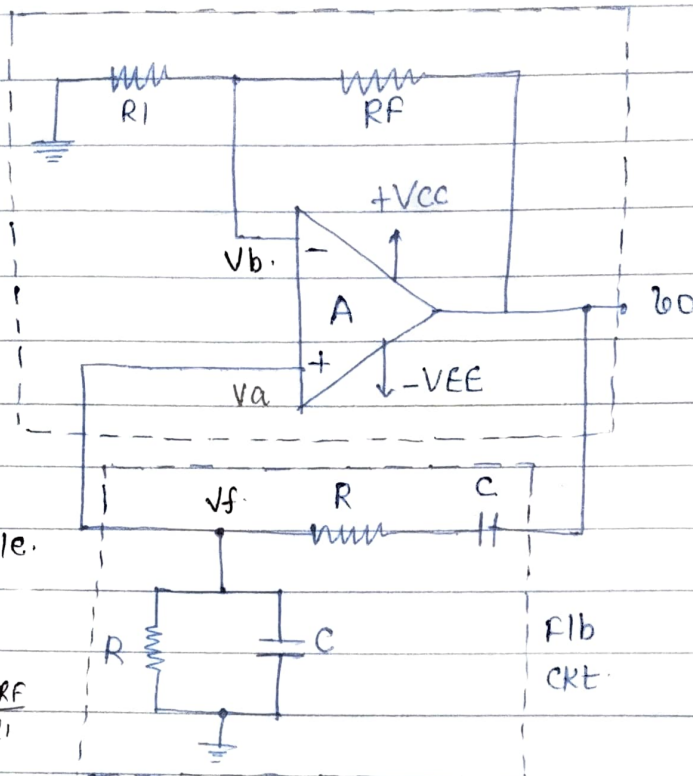
The phase angle criterion for oscillation is that the total phase shift around the ckt. must be 0° . This condition occurs only when the bridge is balanced, i.e. at resonance. The freqⁿ of oscillation f_0 is exactly the resonant freqⁿ of the balanced Wein bridge & is given by,

$$f_0 = \frac{1}{2\pi RC} = \frac{0.159}{RC}$$

Assuming that the resistors are equal in value & the capacitors are equal in value in the reactive leg of the wein bridge. At this freqⁿ the gain required for sustained oscillations is given by,

$$A_v = \frac{1}{\beta} = 3$$

Amplifier.



V_f - using voltage divider rule.

$$\beta = \frac{V_f}{V_o}$$

$$A_v = \frac{V_o}{V_f} = 1 + \frac{R_F}{R_I}$$

$$A_v \cdot \beta = 3$$

$$R_F = 2R_I \text{ i.e.}$$

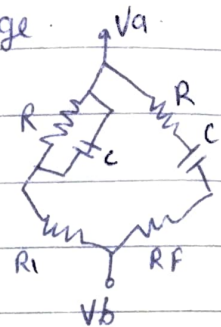
$$A_v = 3 = \frac{1}{\beta}$$

(53%)

$$\text{or } R_F = 2R_I$$

- simple & stable

- Bridge



when $V_a = V_b$, phase shift = 0

$$f_o = \frac{1}{2\pi R C} = 0.159$$

$$A_v = \frac{1}{\beta} = 3$$

wein bridge ckt \rightarrow ||el + series RC netw

$$1 + \frac{R_F}{R_I} = 3 \quad \therefore \frac{R_F}{R_I} = 2$$

Que: Design the wein bridge oscillator for $f_o = 965 \text{ Hz}$.

solⁿ: Let $C = 0.047 \mu\text{F}$.

$$\therefore R = 0.159$$

$$(0.047) \times 10^{-6} \times 965$$

$$R = \frac{0.159}{45.355 \times 10^{-6}} = 0.0035057 \times 10^6$$

$$R = 3.5 \text{ K}\Omega$$

Now, let $R_I = 12 \text{ K}\Omega$,

$$\therefore R_F = (2) \cdot (12 \text{ K}\Omega) = 24 \text{ K}\Omega$$

Use $R_F = 50 \text{ K}$ pot.

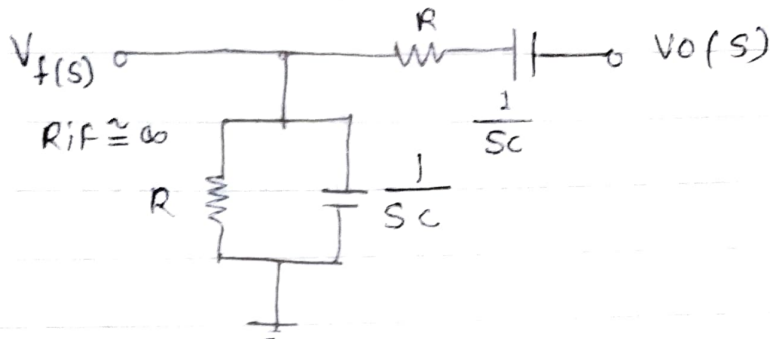
Derivation of Wein-bridge oscillator.

Prove that $f_0 = \frac{1}{2\pi RC}$... (1)

$R_F = 2R_1$... (2)

First consider the f/b ckt of wein bridge oscillator.

The s-domain representation is,



Applying voltage divider rule,

$$V_f(s) = \frac{Z_p(s) \cdot V_o(s)}{Z_p(s) + Z_s(s)} \quad \dots (3)$$

where $Z_p(s) = R \parallel \frac{1}{sC} = \frac{R}{sRC + 1}$

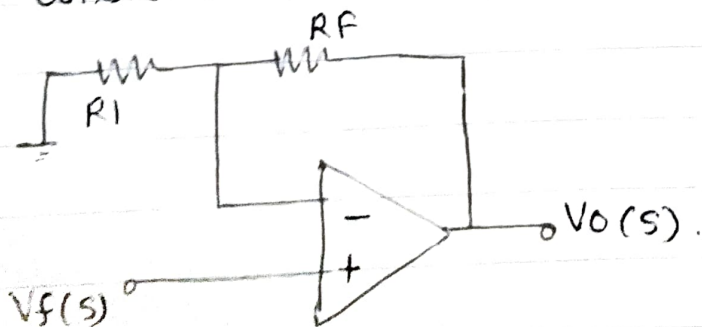
$$Z_s(s) = R + \frac{1}{sC} = \frac{R^2 sC + 1}{sC}$$

\therefore substitute $Z_p(s)$ & $Z_s(s)$ in eqⁿ (3)

$$\therefore V_f(s) = \frac{(R^2 sC) \cdot V_o(s)}{(R^2 sC + 1)^2 + R^2 sC}$$

or $\beta = \frac{V_f(s)}{V_o(s)} = \frac{R^2 sC}{R^2 s^2 C^2 + 3R^2 sC + 1} \quad \dots (4)$

Let us consider op-amp part of wein bridge osc.



The vtg. gain of op-amp is ,

$$A_v = \frac{V_o(s)}{V_f(s)} = 1 + \frac{R_F}{R_1} \quad \dots (4)$$

Finally requirement for oscillator is,

$$A_v \cdot \beta = 1.$$

\therefore using eqⁿ (3) & (4)

$$\left(1 + \frac{R_F}{R_1}\right) \cdot \frac{RCS}{R^2C^2S^2 + 3RCS + 1} = 1.$$

substitute $s = j\omega$ & equate real & img. part.

$$\left(1 + \frac{R_F}{R_1}\right) jRC\omega = -R^2C^2\omega^2 + j3RC\omega + 1$$

Real part,

$$-R^2C^2\omega^2 + 1 = 0.$$

$$\therefore R^2C^2\omega^2 = 1.$$

$$\therefore \omega^2 = \frac{1}{R^2C^2} \quad \text{i.e. } \omega = \frac{1}{RC}.$$

$$\text{or } \boxed{f_0 = \frac{1}{2\pi RC}}$$

Img. part,

$$\left(1 + \frac{R_F}{R_1}\right) RC\omega = 3RC\omega.$$

$$\therefore 1 + \frac{R_F}{R_1} = 3.$$

$$\boxed{\therefore \text{i.e. } R_F = 2R_1}$$

phase shift Oscillator :-

It consists of an op-amp as the amplifying stage & three RC cascaded nlws as the ffb ckt.

ffb ckt provides feedback vltg. from the o/p back to the i/p of the amplifier.

op-amp is used in the inverting mode, therefore, any signal that appears at the inverting terminal is shifted by 180° at the o/p. An additional 180° phase shift required for the oscillation is provided by the cascaded RC nlws. Thus the total phase shift around the loop is 360° (or 0°).

At the some specific freqⁿ when the phase shift of the cascaded RC nlws is exactly 180° & the gain of the amp^r is sufficiently large, the ckt. will oscillate at that freqⁿ.

- This freqⁿ is called the freqⁿ of oscillation, f_o , & is given by

$$f_o = \frac{1}{2\pi\sqrt{6}RC} = \frac{0.065}{RC}$$

- At this freqⁿ, the gain A_v must be at least 29.

$$\text{i.e. } \left| \frac{R_F}{R_1} \right| = 29$$

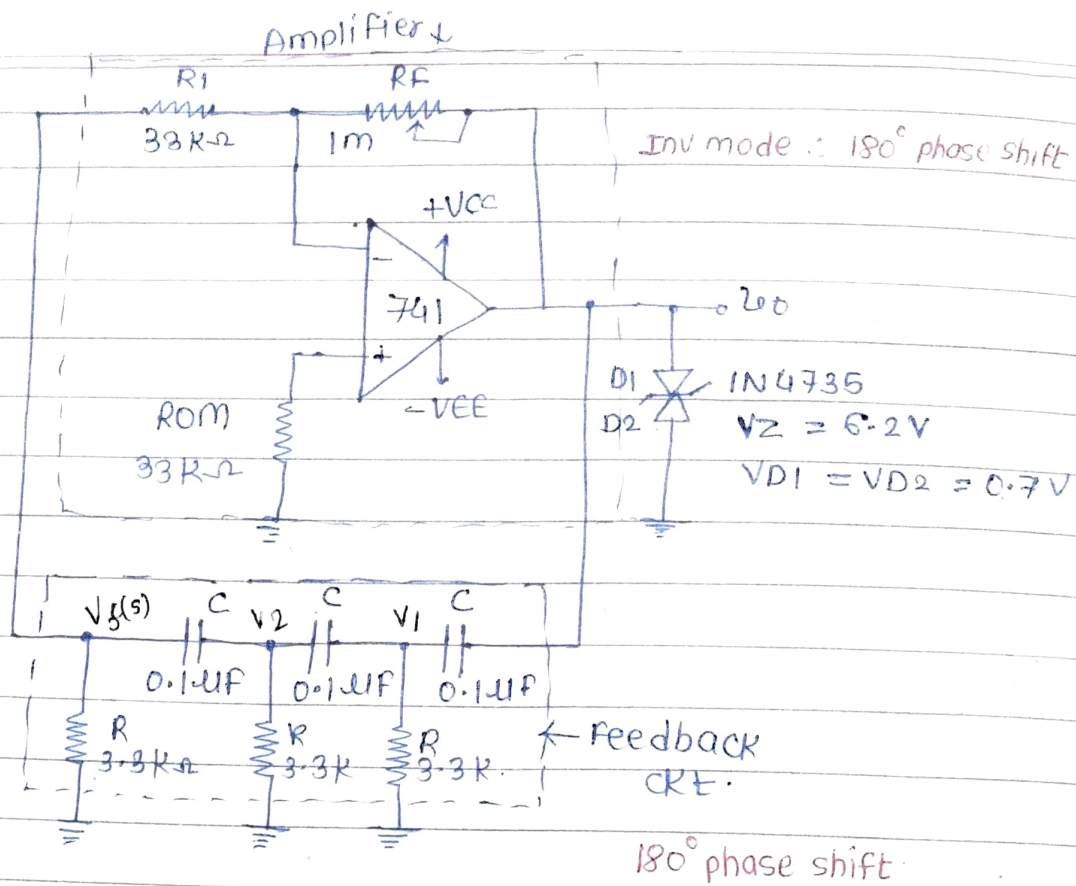
$$\text{or } R_F = 29 \cdot R_1$$

- This ckt. will produce a sine wave of freqⁿ f_o if the gain is 29 & the total phase shift around the ckt is exactly 360° .

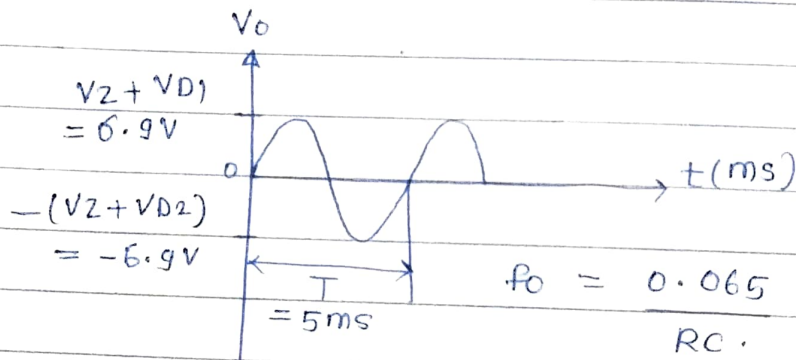
- For a desired freqⁿ of oscillation, choose a capacitor C & then calculate the value of R from eqⁿ,

$$f_o = \frac{1}{2\pi\sqrt{6}RC} = \frac{0.065}{RC}$$

- The desired o/p amplitude, however can be obtained with back to back zeners connected at the o/p terminal.



180° phase shift



∴ phase shift oscillator & its O/P w/f :

Que: Design the phase shift oscillator with $f_0 = 200Hz$.

Solⁿ:- let $C = 0.1 \mu F$

Then, $R = \frac{0.065}{(200)(10^{-7})} = 3.25K\Omega$

(use $R = 3.3K\Omega$)

To prevent the loading of the amp^t because of RC n/ws, it is necessary that $R_1 \geq 10R$.

\therefore let $R_1 = 10R = 33K\Omega$.

Then,

$$R_F = 29 (33K\Omega) = 957K\Omega.$$

(use $R_F = 1M\Omega$ pot).

when choosing an op-amp, 741 can be used at lower freq^{ns} ($< 1KHz$); however, at higher freq^{ns}, an op-amp such as the LM318 or LF351 is recommended because of its increased slew rate.

$$(1) \frac{V_f}{V_o}$$

Apply KCL at V_1, V_2 ,

$$V_f(s) =$$

$$V_2(s)$$

$$\frac{V_f}{V_o} = \beta$$

$$A_u = -\frac{R_F}{R_1}$$

$$A_u \cdot \beta = 1$$

$$f_c = \frac{1}{2\pi\sqrt{6}RC}$$

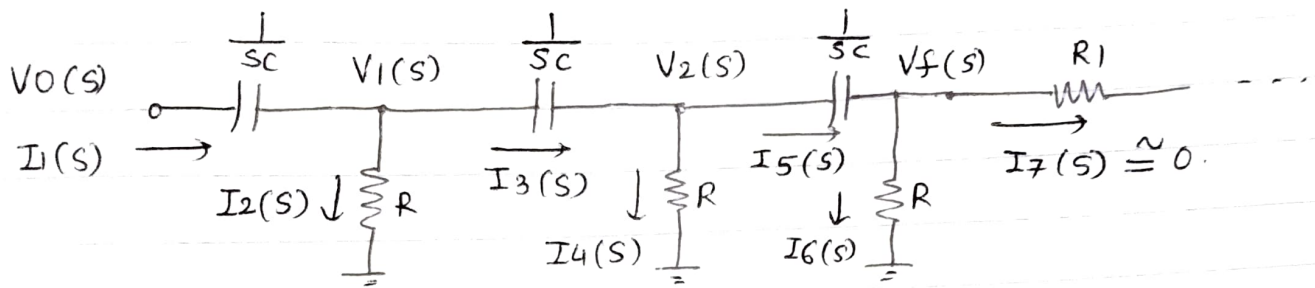
$$\frac{R_F}{R_1} = 29$$

derivation of phase shift oscillator,

To show: $f_o = \frac{1}{2\pi\sqrt{6}RC}$

$$\left| \frac{RF}{R1} \right| = 29.$$

First consider flb ckt consisting of RC combⁿ of phase shift OSC.
S-domain representation of flb ckt is,



Apply KCL at node $V_1(s)$

$$I_2(s) + I_3(s) = I_1(s).$$

$$\text{i.e. } \frac{V_0(s) - V_1(s)}{1/sC} = \frac{V_1(s)}{R} + \frac{V_1(s) - V_2(s)}{1/sC}.$$

solving for $V_1(s)$, we get.

$$V_1(s) = \frac{V_0(s) + V_2(s) \cdot RCS}{2RCS + 1} \quad \text{--- (1)}$$

writing KCL at node $V_2(s)$,

$$I_3(s) = I_4(s) + I_5(s)$$

$$\text{i.e. } \frac{V_1(s) - V_2(s)}{1/sC} = \frac{V_2(s)}{R} + \frac{V_2(s) - V_f(s)}{1/sC}$$

solving for $V_1(s)$,

$$V_1(s) = \frac{(2RCS + 1)V_2(s) - V_f(s)}{RCS} \quad \text{--- (2)}$$

If $R_1 \gg R$ in ckt, then $I_7(s) = 0$

$$\text{i.e. } I_5(s) = I_6(s).$$

\therefore using vtg divider rule,

$$V_f(s) = \frac{R}{R + (1/sC)} \cdot V_2(s)$$

$$\text{Or } V_2(s) = \frac{(RCs + 1) \cdot V_f(s)}{RCs}$$

substitute value of $V_2(s)$ in eqⁿ ①,

$$\therefore V_1(s) = \frac{RCs \cdot V_0(s)}{2RCs + 1} + \frac{(RCs + 1) \cdot V_f(s)}{2RCs + 1} \quad \dots (3)$$

substitute value of $V_2(s)$ in eqⁿ ②

$$\therefore V_1(s) = \frac{(RCs) \cdot V_0(s)}{2RCs + 1} + \frac{(RCs + 1) \cdot V_f(s)}{2RCs + 1}$$

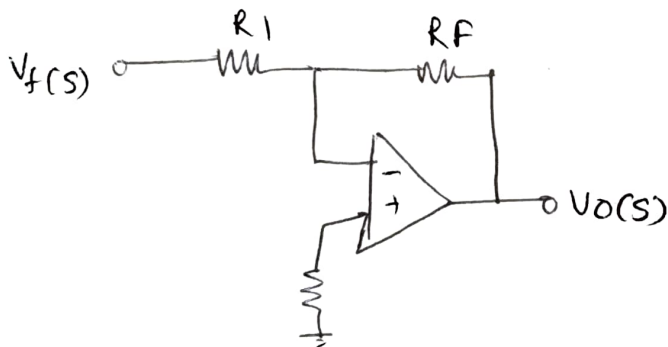
$$V_1(s) = \frac{(2RCs + 1)(RCs + 1) \cdot V_f(s)}{(RCs) \cdot (RCs)} - V_f(s) \quad \dots (4)$$

equate eqⁿ ③ & ④

$$\frac{V_f(s)}{V_0(s)} = \frac{R^3 C^3 S^3}{(R^3 C^3 S^3 + 6R^2 C^2 S^2 + 5RCs + 1)} = \beta \quad \dots (5)$$

Consider op-amp part of phase shift osc.

Vtg. gain of op-amp is



$$A_v = \frac{V_0(s)}{V_f(s)}$$

$$A_v = -\frac{R_F}{R_1} \quad \dots (6)$$

for an oscillator,

$$A_v \cdot \beta = 1. \quad \frac{-R_F}{R_1} \cdot \frac{R^3 C^3 S^3}{R^3 C^3 S^3 + 6R^2 C^2 S^2 + 5RCs + 1} = 1.$$

\therefore using above eqⁿ (5) & (6), & substitute $j\omega = s$.

$$-\frac{R_F}{R_1} (-jR^3 C^3 \omega^3) = (-jR^3 C^3 \omega^3) - (6R^2 C^2 \omega^2) + j5RC\omega + 1$$

compare real & img. parts,

$$-6R^2C^2\omega^2 + 1 = 0$$

$$\text{or } 6R^2C^2\omega^2 = 1 \quad \text{i.e. } \omega^2 = \frac{1}{6R^2C^2}$$

$$\therefore \omega = \frac{1}{\sqrt{6}RC}$$

$$\therefore f_0 = \frac{1}{2\pi\sqrt{6}RC}$$

img. part,

$$\left(-\frac{RF}{R_1}\right)(-jR^3C^3\omega^3) = (-jR^3C^3\omega^3) - (6R^2C^2\omega^2) + (j5RC\omega) + 1$$

$$0 =$$

$$-\frac{RF}{R_1}(-jR^3C^3\omega^3) = -jR^3C^3\omega^3 + j5RC\omega$$

$$\therefore \frac{-RF}{R_1} = \frac{1 - 5}{R^2C^2\omega^2}$$

substituting value of ω^2 .

$$\therefore \frac{-RF}{R_1} = 1 - \frac{5}{R^2C^2 \cdot 1/6R^2C^2}$$

$$= 1 - \frac{5 \times 6R^2C^2}{R^2C^2} = 1 - 30 = -29.$$

$$\therefore \frac{-RF}{R_1} = -29.$$

$$\therefore \frac{RF}{R_1} = 29$$