

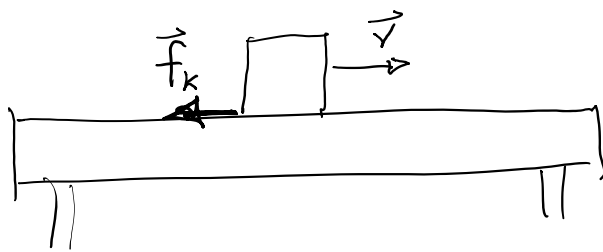
Last week: Newton's Laws

1. inertia - objects will keep moving at constant speed unless acted upon by an external force.
2. $F_{\text{net}} = ma$
3. every action has an equal + opposite reaction.

today: some more common forces

5.1 friction - the force that opposes ^{relative} motion between two surfaces in contact.

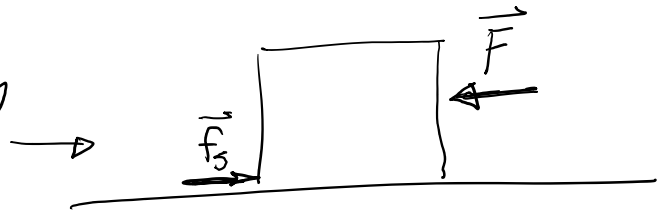
kinetic friction



moving box slowed down by friction with the table

static friction

friction prevents a weak force from moving a stationary box



- both cases: friction is proportional to the normal force.

- kinetic friction:

$$f_k = \mu_k N$$

magnitude of kinetic friction \nearrow f_k \nwarrow magnitude of normal force N
 \nearrow coefficient of kinetic friction μ_k

table 5.1 in book lists values of μ_k

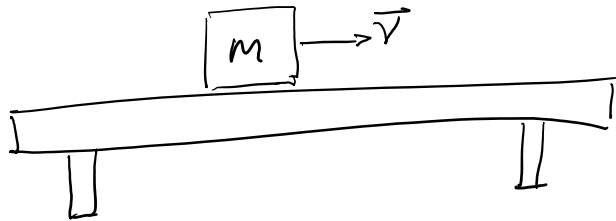
table 5.1 in book lists values of μ_k

e.g. wooden box sliding on wooden table

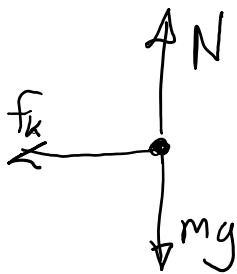
$$m = 1.0 \text{ kg}$$

$$v_0 = 2 \text{ m/s}$$

how much is it decelerating?



free body diagram



$$F_{\text{net},y} = N - mg = ma_y = 0$$

$$F_{\text{net},x} = -f_k = ma_x$$

$$N - mg = 0$$

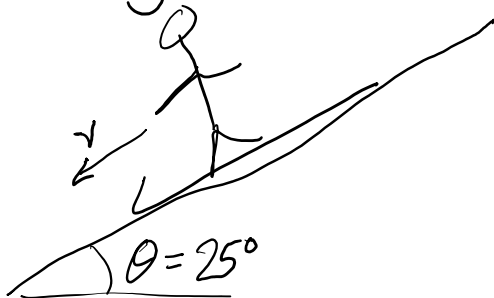
$$N = mg$$

$$ma_x = -\mu_k N$$

$$ma_x = -\mu_k mg$$

$$a_x = -\mu_k g = -(0.3)(9.81 \text{ m/s}^2) = \boxed{-2.94 \text{ m/s}^2}$$

e.g. skiing down a slope

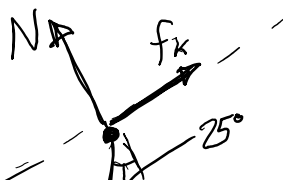


$$m = 62 \text{ kg}$$

$$f_k = 45 \text{ N}$$

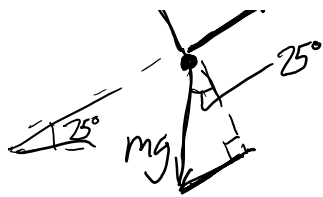
what is μ_k ?

free body diagram



$$F_{\text{net},\parallel} = mg \sin 25^\circ - f_k = ma_{\parallel}$$

$$F_{\text{net},\perp} = N - mg \cos 25^\circ = 0$$



$$F_{\text{net}, \perp} = N - mg \cos 25^\circ = 0$$

$$N = mg \cos 25^\circ$$

$$f_k = \mu_k N$$

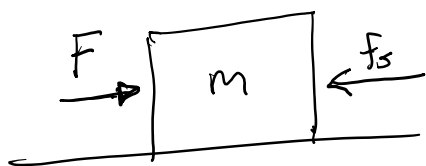
$$f_k = \mu_k mg \cos 25^\circ$$

$$\mu_k = \frac{f_k}{mg \cos 25^\circ} = \frac{45 \text{ N}}{(62 \text{ kg})(9.8 \text{ m/s}^2) \cos 25^\circ} = \boxed{0.082}$$

- static friction: $f_s \leq \mu_s N$ \leftarrow normal force

\nwarrow static friction
 \uparrow coefficient of static friction

static friction will match the strength of the applied force until the applied force becomes too big.



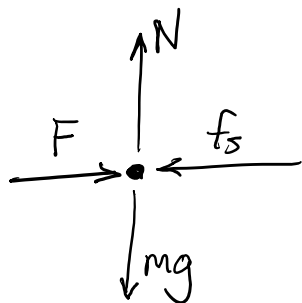
this force F is opposed by f_s .

if $F < \mu_s N$ then it stays still.

if $F \geq \mu_s N$ then it will start to move.

e.g. wood box on wood table. $m = 1.0 \text{ kg}$

how much force needs to be applied for it to move.



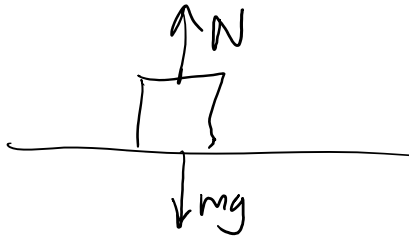
$$F_{\text{net}, x} = N - mg = ma = 0$$

$$N = mg$$

$$F \geq \mu_s N = (0.5)(1 \text{ kg})(9.8 \text{ m/s}^2) = \boxed{4.9 \text{ N}}$$

- generally $\mu_s > \mu_k$. this means it is harder to start

- generally $\mu_s > \mu_k$. This means it is harder to start something moving than to keep it moving.
- proportional to N . This means that heavier objects are slowed fastest. also means easier to move things on a slope.



large $N \rightarrow$ large f



$$N = mg \cos \theta$$

smaller $N \rightarrow$ smaller f

5.2 drag - the force that opposes motion through a fluid.

\hookrightarrow liquid or gas

$$F_D = \frac{1}{2} C \rho A v^2$$

force of drag.

drag coefficient depends on the shape of the object.

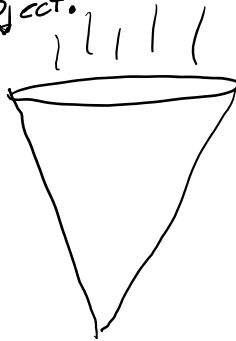
velocity of the object.

cross-sectional area of the object.

(mass) density of the fluid.
(unit: kg/m^3)



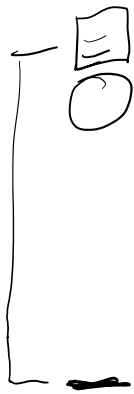
high drag



lower drag

table 5.2 lists some drag coefficients

terminal velocity - fastest speed an object can fall.



time how long it takes the sphere to fall.
want large height so more accurate measurements are easier.



$$F_{net,y} = F_D - mg = ma_y = 0$$

$$F_D = \frac{1}{2} C \rho A v^2 = mg$$

$$v_t = \sqrt{\frac{2mg}{C\rho A}}$$

e.g. a skydiver falling head first



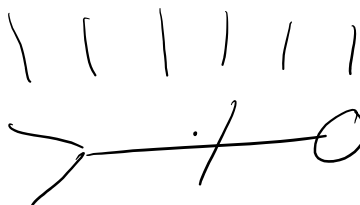
density of air: $\rho = 1.21 \text{ kg/m}^3$

mass of skydiver: $m = 75.0 \text{ kg}$

area of skydiver: $A = 0.18 \text{ m}^2$

drag coefficient: $C = 0.70$

$$v_t = \sqrt{\frac{2(75 \text{ kg})(9.8 \text{ m/s}^2)}{0.7(1.21 \text{ kg/m}^3)(0.18 \text{ m}^2)}} = \boxed{98 \text{ m/s}} = 350 \text{ km/hr}$$



$\sim 200 \text{ km/hr}$

the above only works for large, fast objects in less dense fluids.

if you are slow, small, or in a dense fluid you instead follow Stoke's law. (e.g. microorganisms, pollen, dust)

$$F_s = 6\pi r \eta v$$

radius of object
viscosity of the fluid
velocity of object.

water has low viscosity
honey has high viscosity
pitch has very high viscosity

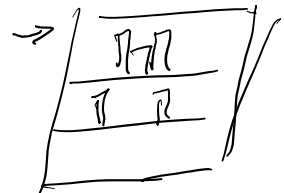
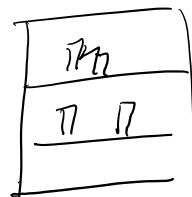
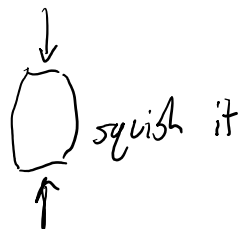
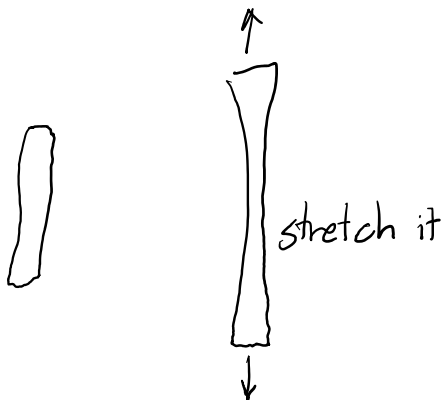
Why can a squirrel jump from a tree branch to the ground and be unharmed?

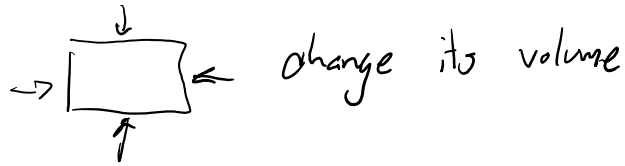
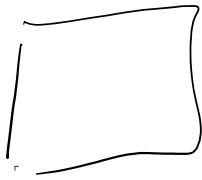
$$v_t = \sqrt{\frac{2mg}{\rho CA}}$$

- squirrels weigh much less + thus have slower terminal velocity

5.3] elasticity

deformation - a change in shape due to an applied force

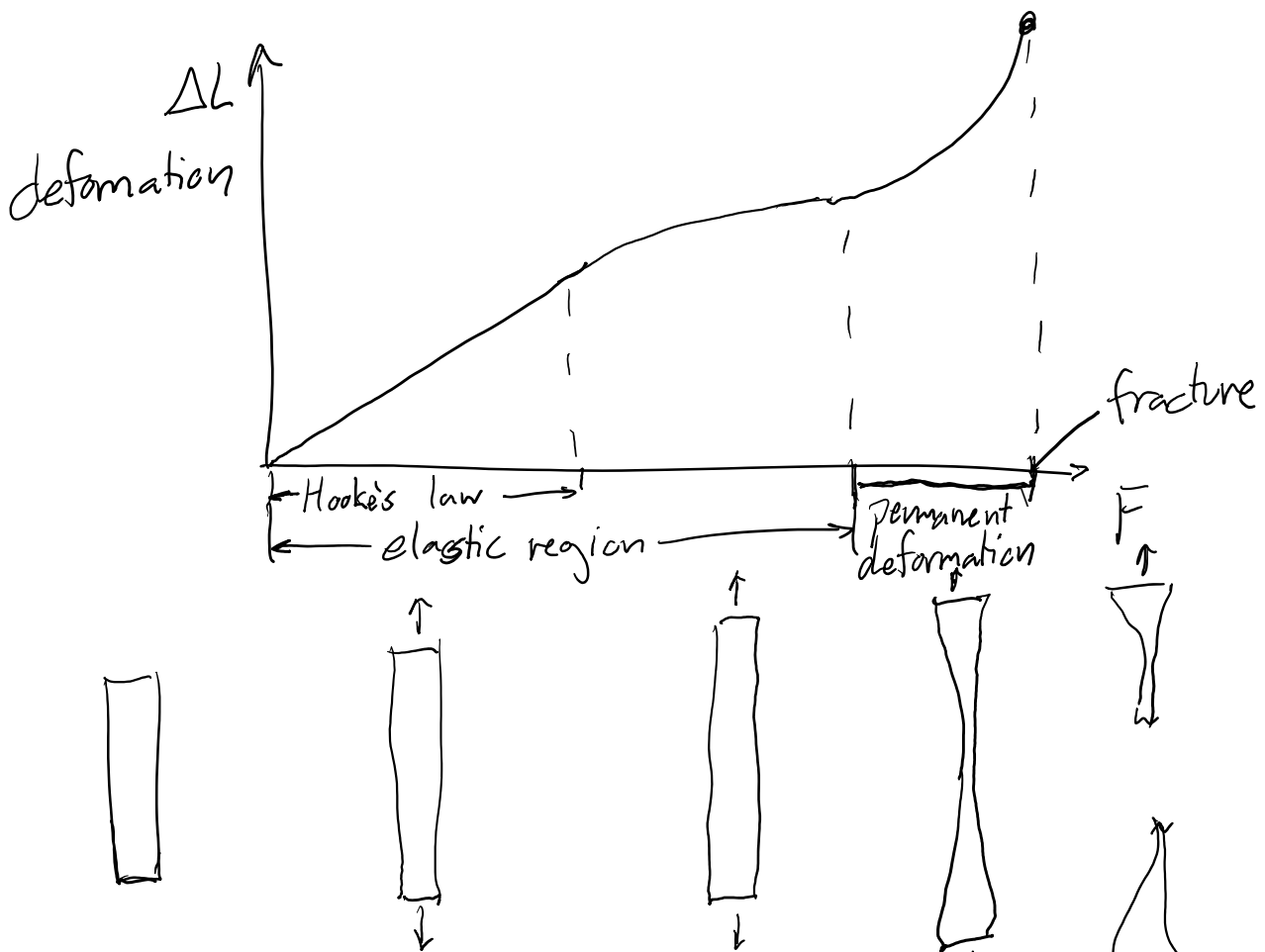




Hook's law - relates the amount of deformation to the force

$$F = k \Delta L$$

force constant amount of deformation (e.g. change in length)

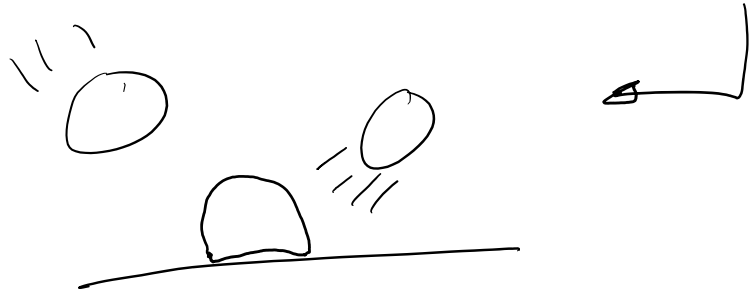


tensile strength - maximum amount of force that can be applied before permanent deformation

← for small forces + small deformations ($< \sim 0.1\%$) most materials will return to their initial state afterwards

(elastic region)

- how springs work, how rubber bands work, why balls bounce



tension + compression

stretching squeezing

$$\Delta L = \frac{1}{Y} \frac{F}{A} L_0$$

change in length force original length

elastic modulus or Young's modulus cross-sectional area

Note: $F = \frac{YA}{L_0} \Delta L$ ← Hooke's law with $k = \frac{YA}{L_0}$

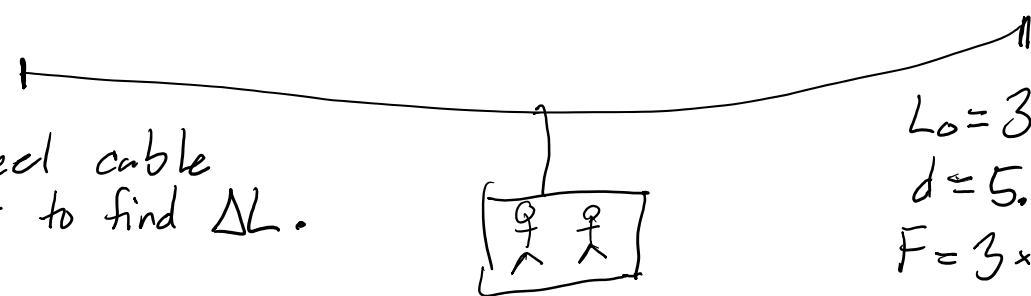
there is a list of values for Y in table 5.3

Note: often see this formula written as

$$\frac{F}{A} = Y \frac{\Delta L}{L_0}$$

"stress" (N/m^2) "strain" (unitless)

e.g.

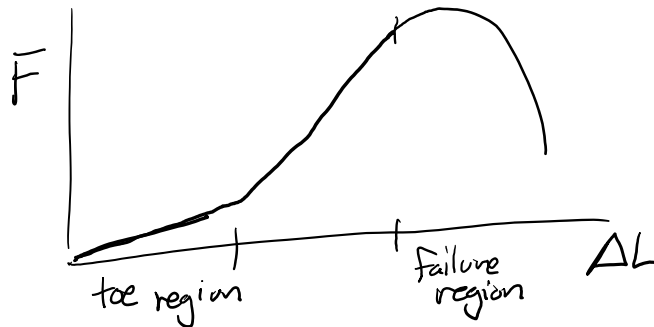
e.g.  steel cable
want to find ΔL .

$L_0 = 3020 \text{ m}$
 $d = 5.6 \text{ cm}$
 $F = 3 \times 10^6 \text{ N}$

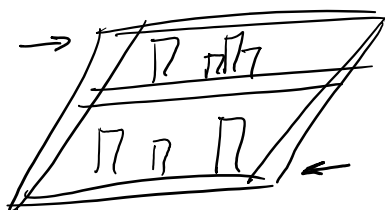
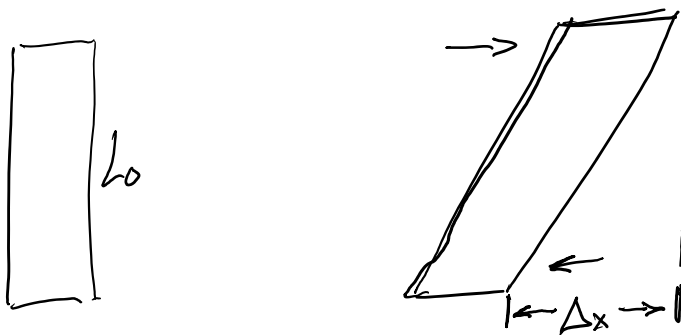
$$\Delta L = \frac{1}{Y} \frac{F}{A} L_0 = \frac{1}{(210 \times 10^9 \frac{\text{N}}{\text{m}^2})} \frac{3 \times 10^6 \text{ N}}{\underbrace{\pi \left(\frac{0.056 \text{ m}}{2} \right)^2}_{A = \pi r^2}} (3020 \text{ m})$$

$$= \boxed{17.5 \text{ m}}$$

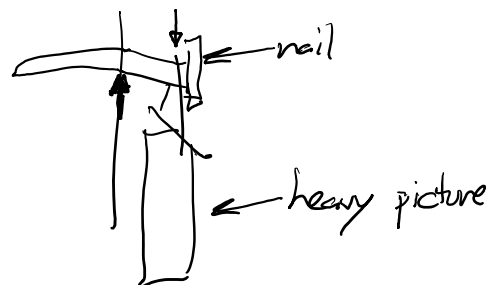
tendons



Shear - sideways deformation



$$\Delta x = \frac{1}{\tau} \frac{F}{A} L_0$$

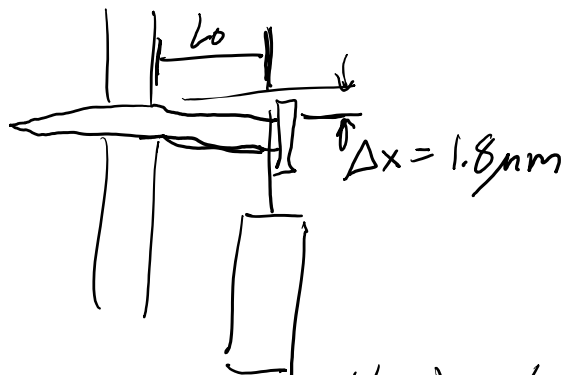


$$\Delta x = \frac{1}{S} \frac{F}{A} L_0$$

amount of shear
shear modulus

Usually: Shear modulus < Young's modulus
easier to bend a nail than stretch a nail

e.g. find the mass hanging from a nail if it shears $1.8 \mu\text{m}$
(its length is $L_0 = 5 \text{ mm}$, its radius is $r = 1.5 \text{ mm}$)



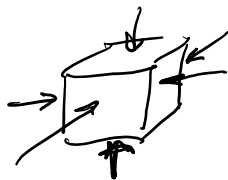
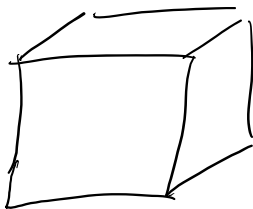
$$S = 80 \times 10^9 \text{ N/m}^2$$

$$F = \frac{SA}{L_0} \Delta x$$

$$F = \frac{(80 \times 10^9 \text{ N/m}^2) \pi (0.0015 \text{ m})^2}{0.005 \text{ m}} (1.8 \times 10^{-6} \text{ m}) = 51 \text{ N}$$

$$F = mg \rightarrow m = \frac{51 \text{ N}}{9.8 \text{ m/s}^2} = \boxed{5.2 \text{ kg}}$$

bulk deformation - change in volume



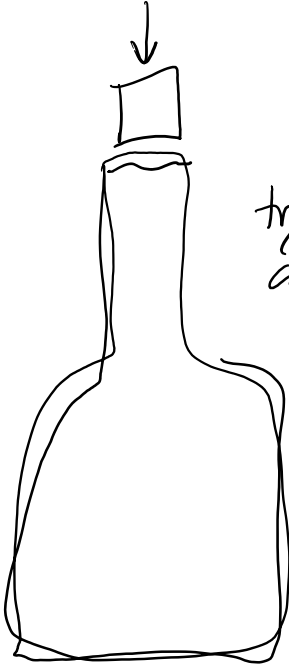
$$\Delta V = \frac{1}{B} \frac{F}{A} V_0$$

bulk modulus

e.g. how much is water compressed at the bottom of the ocean?

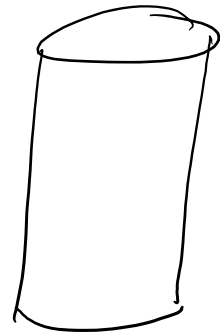
$$\frac{F}{A} = 5 \times 10^7 \frac{\text{N}}{\text{m}^2}$$

$$\frac{\Delta V}{V_0} = \frac{F/A}{B} = \frac{5 \times 10^7 \text{ N/m}^2}{2.2 \times 10^9 \text{ N/m}^2} = 0.023 = \boxed{2.3\%}$$



try to put a cork in
an overfull bottle

this takes way
too much force



Cool a full
can of water
past freezing

Volume of can stays constant
volume water wants to be
gets bigger