Math 285: Exam	2
Spring 2020	
3/12/2020	

Name:	

## **Directions**

- 1. Do NOT open this exam booklet until you are instructed to do so!
- 2. You may use a TI-84/85 (or equivalent) calculator. Any other electronic devices or outside materials are not permitted.
- 3. This exam is 5 pages (including this cover page) and has 5 questions. Check that you have every page of the exam before handing it in.
- 4. Please write your answers in the space provided. If you need more space, continue on the back of a page (being sure to clearly label your work). Do <u>not</u> write any answers on scrap paper.
- 5. Work must be clearly written and organized. Please organize your work and write legibly! Circle your final answers.
- 6. If you have a question, please raise your hand.

## Good luck!

Do not write in the tables or on the line below.

Question	Points	Score
1	30	
2	30	
3	20	
4	10	
5	10	
Total:	100	

1. (30 points) Find the derivative of each function. You do  $\underline{not}$  need to simplify your answers.

(a) 
$$f(x) = 10x^6 + 4x^4 - 3x^3 + 2x - 7$$

(b) 
$$f(x) = x^{-3} - x^{1/3}$$

(c) 
$$f(x) = (x^2 + 3x + 1)(4x^2 - 3)$$

(d) 
$$f(x) = \frac{x^2 - 2x - 4}{2x^3 + 3}$$

(e) 
$$f(x) = (x^3 + 2x - 1)^3$$

2. (30 points) Find the derivative of each function. You do  $\underline{not}$  need to simplify your answers.

(a) 
$$f(x) = \ln(x^2 + \sin x)$$

(b) 
$$f(x) = \ln(10x + 1)e^{x^2+1}$$

(c) 
$$f(x) = \frac{\sin(x)}{\log_2(x)}$$

(d) 
$$f(x) = 5^{x^2+1}$$

(e) 
$$f(x) = \tan(\ln(x) + e^x)$$

- 3. (20 points) A function f has first derivative  $f'(x) = (x-3)^2(x+3)$  and second derivative f''(x) = 3(x-3)(x+1).
  - (a) For which intervals is *f* increasing? For which is it decreasing?

(b) For what values of x does f have a maximum? For which does it have a minimum?

(c) Over which intervals is f concave up? For which is it concave down?

(d) For what values of x does f have an inflection point?

4. (10 points) Find the equation of a tangent line to the function  $f(x) = \ln(x)$  when x = 5.

5. (10 points) Find the equation of a tangent line to the function  $f(x) = \sin(x)$  when  $x = \pi/2$ .