Robotics Homework Assignment # 4

1) What are the rotation matrices ${}^{1}_{0}R$ for 60 degree rotations about
a) X-axis
b) Y-axis
c) Z-axis

2) A vector v with coordinates $v_0 = (1, 1, 1)$ is rotated by 45 degrees about the X_0 axis. What are the coordinates of the resulting vector?

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HOMEWORK 04a

1. What are the rotation matrices R_0^1 for 60 degree rotation about

(a) x-axis

$$R_1^0 = R_{x,\theta} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\theta & -\sin\theta \\ 0 & \sin\theta & \cos\theta \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0.5 & -0.866 \\ 0 & 0.866 & 0.5 \end{bmatrix}$$

$$R_0^1 = (R_1^0)^{-1} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0.5 & 0.866 \\ 0 & -0.866 & 0.5 \end{bmatrix}$$

(b) y-axis

$$R_1^0 = R_{y,\theta} = \begin{bmatrix} \cos\theta & 0 & \sin\theta \\ 0 & 1 & 0 \\ -\sin\theta & 0 & \cos\theta \end{bmatrix} = \begin{bmatrix} 0.5 & 0 & 0.866 \\ 0 & 1 & 0 \\ -0.866 & 0 & 0.5 \end{bmatrix}$$

$$R_0^1 = (R_1^0)^{-1} = \begin{bmatrix} 0.5 & 0 & -0.866 \\ 0 & 1 & 0 \\ 0.866 & 0 & 0.5 \end{bmatrix}$$

(c) z-axis

$$R_1^0 = R_{z,\theta} = \begin{bmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 0.5 & -0.866 & 0 \\ 0.866 & 0.5 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$R_0^1 = (R_1^0)^{-1} = \begin{bmatrix} 0.5 & 0.866 & 0 \\ -0.866 & 0.5 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

2. A vector v with coordinates $v_0 = (1,1,1)$ is rotated by 45 degrees about the X_0 axis. What are the coordinates of the resulting vector?

$$v_1^0 = R_{x,\pi/4} v^0 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\theta & -\sin\theta \\ 0 & \sin\theta & \cos\theta \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \sqrt{2}/2 & -\sqrt{2}/2 \\ 0 & \sqrt{2}/2 & \sqrt{2}/2 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ \sqrt{2} \end{bmatrix}$$

coordinates of resulting vector : $(1, 0, \sqrt{2})$