

Q1h

Given $V_{in} = 10 \cos(20,000t)$.

What is the steady state output V_{out} ?

State your answer in the rectangular form Real + j Imaginary.

$V_{out} =$ ☒ + j ☒ V

$$Z_L = j\omega L = j(1)(20\,000) = j20K$$

$$10K\Omega // Z_L = \frac{(10K)(j20K)}{10K + j20K} = \frac{j200K}{10 + j20} \cdot \frac{10 - j20}{10 - j20} = \frac{4000K + j2000K}{500}$$

$$= 8K + j4K$$

$$\text{NODE } V_n: \frac{V_n^\circ - V_{in}}{10K} + \frac{V_n^\circ - V_o}{8K + j4K} = 0 \quad V_{in} = 10\angle 0^\circ = 10$$

$$-\frac{V_{in}}{10K} - \frac{V_o}{8K + j4K} = 0$$

$$V_o = -\frac{(10)(8K + j4K)}{10K} = -8 - j4$$

$$I_1 = 5A \approx 5 + j0 A$$

$$V = 20\angle 45^\circ \approx 10\sqrt{2} + j10\sqrt{2}$$

$$I_2: -50(I_2 - I_1) - 75(I_2 - I_3) - (10\sqrt{2} + j10\sqrt{2}) = 0$$

$$50I_1 - 125I_2 + 75I_3 = 10\sqrt{2} + j10\sqrt{2}$$

$$-125I_2 + 75I_3 = -250 + 10\sqrt{2} + j10\sqrt{2}$$

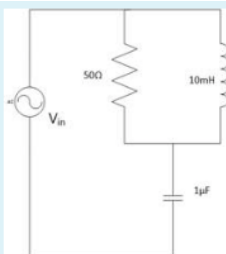
$$I_3: -j12I_3 - 75(I_3 - I_2) + j20(I_3 - I_1) = 0$$

$$-j20I_1 + 75I_2 + (-75 + j8)I_3 = 0$$

$$75I_2 + (-75 + j8)I_3 = j100$$

$$I_2 = \frac{j100}{75} + \left(\frac{75 - j8}{75}\right)I_3$$

$$\left. \begin{aligned} -125I_2 + 75I_3 &= -250 + 10\sqrt{2} + j10\sqrt{2} \\ 75I_2 + (-75 + j8)I_3 &= j100 \end{aligned} \right\} \begin{aligned} I_2 &= 8.069 - j1.434 \\ I_3 &= 5.304 - j2.202 \end{aligned}$$



Q3c

Given $V_{in} = 22 \cos(10,000 t)$

Find the steady state phasor current "through" the 1 μF (micro F) capacitor.

State your answer with the smallest appropriate positive angle.

$I_{1\mu F}$ (polar form) = Magnitude ☒ Phase ☒ ° (Degree) Amps

$$V_{in} = 22$$

$$Z_L = j\omega L = j(10K)(10 \times 10^{-3}) = j100$$

$$50\Omega // 10mH = \frac{(50)(j100)}{50 + j100} \cdot \frac{50 - j100}{50 - j100} = \frac{500\,000 + j250\,000}{12\,500} = 40 + j20$$

$$Z_C = \frac{-j}{\omega C} = \frac{-j}{(10\,000)(1 \times 10^{-6})} = -j100$$

$$V = IR \rightarrow I_{1\mu F} = \frac{22}{40 + j20 - j100} = \frac{22}{40 - j80} \cdot \frac{40 + j80}{40 + j80} = \frac{880 + j1760}{8000} = 0.11 + j0.22$$

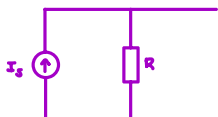
$$I_{1\mu F} = 0.11 + j0.22 \approx 0.25\angle 63.43^\circ$$

$$Z_C = \frac{-j}{\omega C} = \frac{-j}{(10\,000)(10 \times 10^{-6})} = -j10$$

$$Z_L = j\omega L = j(10\,000)(1 \times 10^{-3}) = j10$$

$$V = IR$$

$$I_s = \frac{V_{in}}{R} = \frac{30}{50 - j10 + j10} = 0.6$$



$$R // j10 = \frac{(50 - j10)(j10)}{50 - j10 + j10} = \frac{100 + j500}{50} = 2 + j10$$

$$Z_{TH} = R_{eq} = 20 + j10$$

$$V_{TH} = I_s R = (0.6)(j10) = j6$$

$$2.31 + j1.69$$

$$\begin{aligned}
 v &= 240 \cos [90 - (377t)] \\
 &= 240 \cos (377t - 90^\circ) \\
 &= 240 \angle -90^\circ
 \end{aligned}$$

$$i = 6 \angle -85^\circ$$

$$\begin{aligned}
 P &= V_{\text{eff}} I_{\text{eff}} \cos(\theta_v - \theta_i) \\
 &= (240)(6) \cos(-90^\circ + 85^\circ)
 \end{aligned}$$

$$\begin{aligned}
 Q &= V_{\text{eff}} I_{\text{eff}} \sin(\theta_v - \theta_i) \\
 &= (240)(6) \sin(-90^\circ + 85^\circ) =
 \end{aligned}$$

$$S = V_{\text{eff}} \cdot I_{\text{eff}}$$

$$v = 120 \angle -25^\circ$$

$$i = 7 \angle 25^\circ$$

$$\begin{aligned}
 pf &= \cos(\theta_v - \theta_i) \\
 &= \cos(-25 - 25) = 0.69
 \end{aligned}$$

$$(a) \quad I_{\text{rms}} = I_{\text{max}} / 1.414 = 200 / 1.414 = 141.42 \text{ mA}$$

$$P_{\text{avg}} = (I_{\text{rms}})^2 \cdot R = (141.42)^2 (5) =$$

$$I_{\text{rms}} = \frac{I_0}{\sqrt{2}} = \frac{200}{\sqrt{2}} = 141.42 \text{ mA}$$

$$P_{\text{avg}} = (I_{\text{rms}})^2 \cdot R = (141.42 \times 10^{-3})^2 (5000) = 66.67 \text{ W}$$