



# Diodes

Perry L Heedley, Ph.D.

© 2014\*

- \* Most figures and examples are from the course textbook “Microelectronic Circuits” by Adel S. Sedra and Kenneth C. Smith, 6<sup>th</sup> Edition, © 2010 by Oxford University Press, Inc.

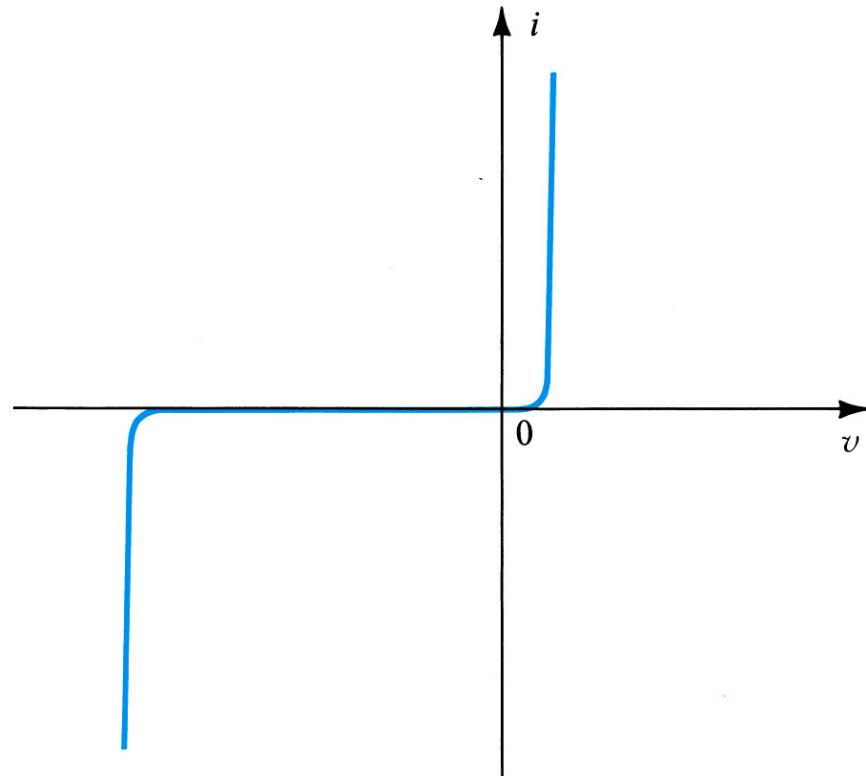


# Outline

- Large-signal models & analysis of forward-biased diodes
  - Exponential, Ideal and Constant Voltage-Drop Diode Models
  - Solving by Iteration, or by Graphical Analysis using Load Lines
- Small-signal analysis & the Small-signal Diode Model
- Models for reverse-biased Zener diodes
- Applications of Diodes
  - Voltage Regulation
  - Diode Logic Circuits
  - Limiting & Clamping Circuits
  - DC Restorer and Voltage Doubler Circuits
- Power Supplies
  - Diode rectifiers, Filters, Voltage regulation
- Summary of key concepts



# I-V Characteristics of PN Diodes

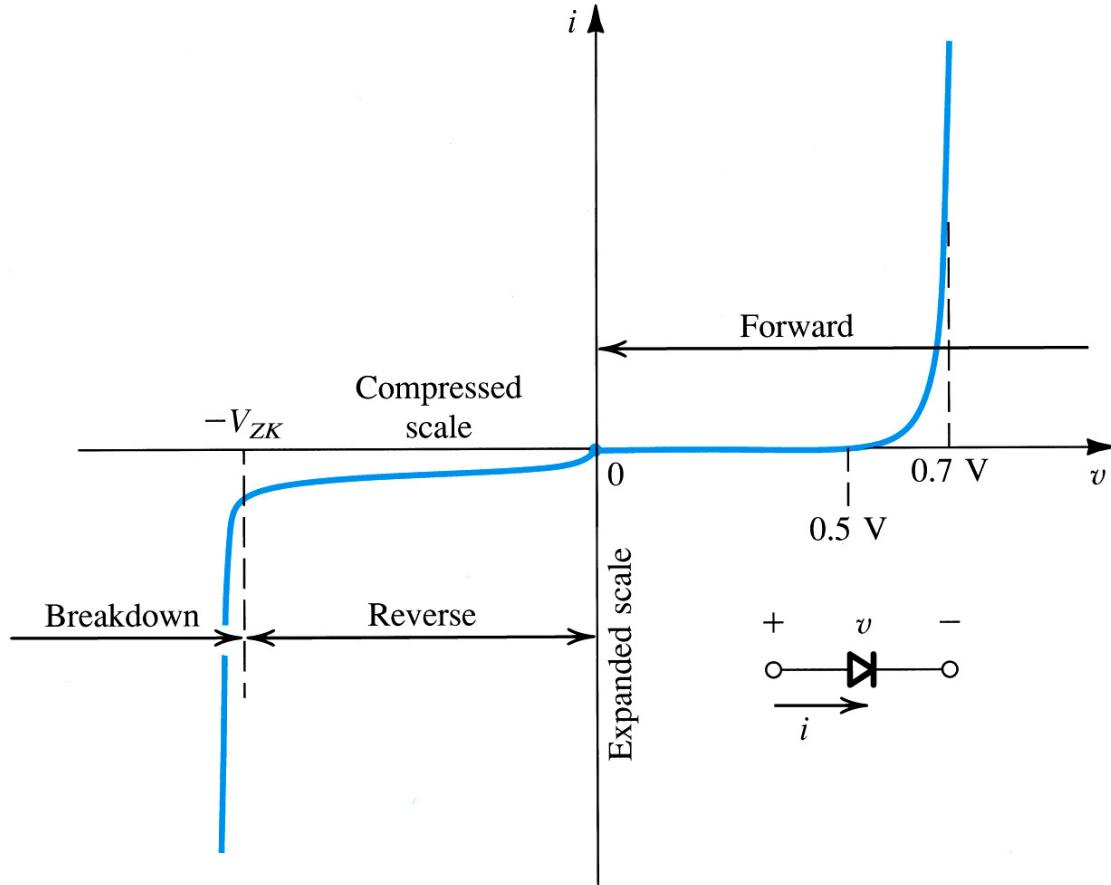


$$I = I_s (e^{V/V_T} - 1) \text{ where: } V_T = \frac{kT}{q}$$

- As discussed previously, PN junction **Diodes** conduct current when the junction is forward-biased (Voltage applied on the P-side is > on N-side)
- When reverse-biased, a diode only conducts a small current called the **saturation current,  $I_s$**
- If the reverse bias voltage exceeds the **breakdown voltage**, then current flow increases sharply



# I-V Characteristics of PN Diodes

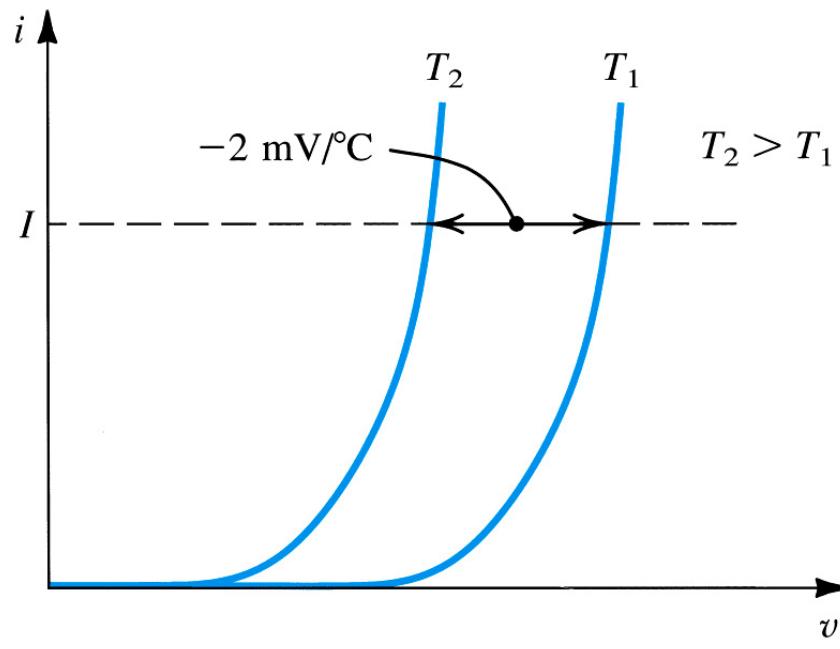


Note the use of expanded & compressed scales here to better show important details

- Silicon diodes “turn on” and start to carry a significant amount of current at a forward bias of ~ 0.5V at 300°K (room temperature)
- As  $I$  increases, so does  $V$ , but slowly ~60mV/decade of  $I$
- $V$  across a diode only varies slightly as  $I$  increases exponentially!



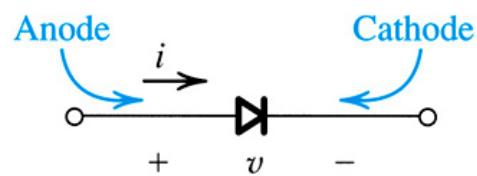
# Temperature Dependence



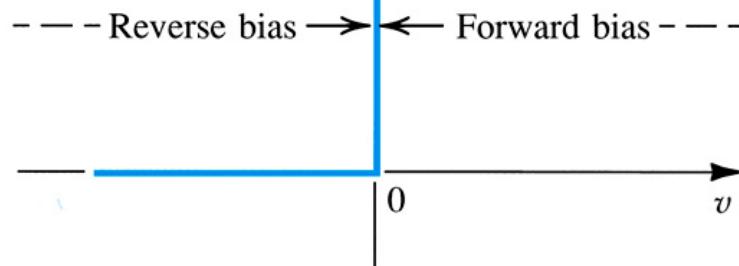
- The bias voltage across a diode which is carrying a constant current drops as temperature goes up!
- $V$  drops by  $\sim -2\text{mV}/^\circ\text{C}$  as temperature increases
- In some applications, this can cause problems with “thermal runaway”
- To avoid these problems, diodes are usually biased with a constant current, not at a constant voltage.



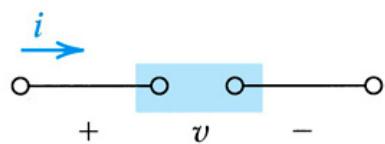
# Ideal Diode Model



(a)

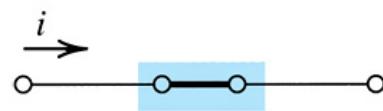


(b)



(c)

$$v < 0 \Rightarrow i = 0$$



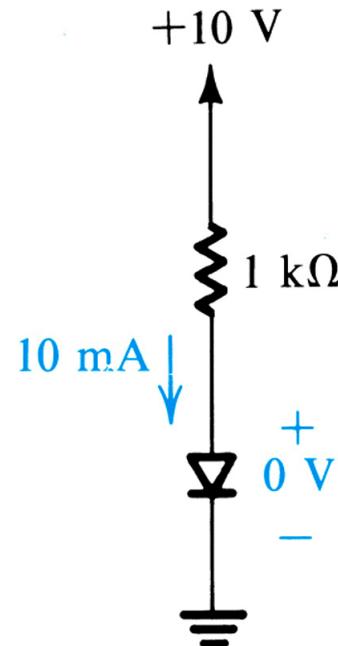
(d)

$$i > 0 \Rightarrow v = 0$$

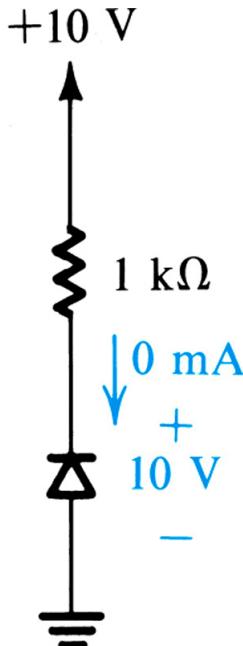
- The simplest model for a diode is the **Ideal Diode model**
- This models forward-biased diodes as short circuits ( $V = 0$ ), and reverse-biased diodes as open circuits ( $I = 0$ )



# Ideal Diode Model in Forward Bias



(a)



(b)

- For example, the circuit on the left has  $I = 10\text{mA}$ , since the voltage across the forward-biased diode is assumed to be 0 V so  $I = 10\text{V} / 1\text{k}\Omega$
- The circuit on the right has  $I = 0$ , since the reverse-biased diode is assumed to be an open circuit, and the full 10V appears across the reverse-biased diode

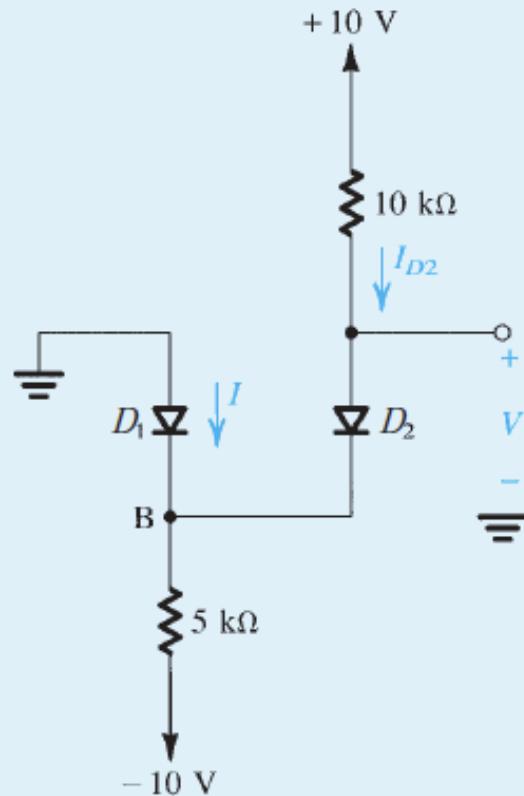
To solve these problems :

- 1<sup>st</sup> assume diodes are on or off,
- 2<sup>nd</sup> analyze the circuit, and
- 3<sup>rd</sup> check your assumptions

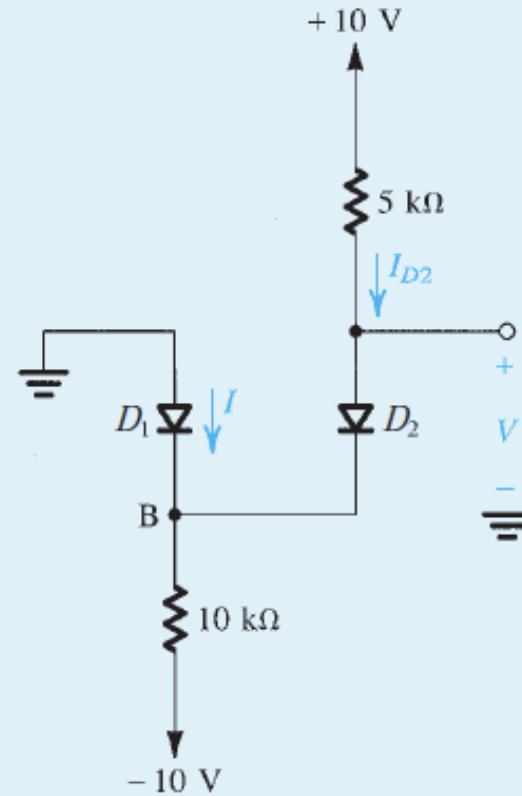


## Example 4.2

Assuming the diodes to be ideal, find the values of  $I$  and  $V$  in the circuits of Fig. 4.6.



(a)



(b)

Figure 4.6 Circuits for Example 4.2.



## Solution

In these circuits it might not be obvious at first sight whether none, one, or both diodes are conducting. In such a case, *we make a plausible assumption, proceed with the analysis, and then check whether we end up with a consistent solution*. For the circuit in Fig. 4.6(a), we shall assume that both diodes are conducting. It follows that  $V_B = 0$  and  $V = 0$ . The current through  $D_2$  can now be determined from

$$I_{D2} = \frac{10 - 0}{10} = 1 \text{ mA}$$

Writing a node equation at B,

$$I + 1 = \frac{0 - (-10)}{5}$$

results in  $I = 1$  mA. Thus  $D_1$  is conducting as originally assumed, and the final result is  $I = 1$  mA and  $V = 0$  V.

For the circuit in Fig. 4.6(b), if we assume that both diodes are conducting, then  $V_B = 0$  and  $V = 0$ . The current in  $D_2$  is obtained from

$$I_{D2} = \frac{10 - 0}{5} = 2 \text{ mA}$$

The node equation at B is

$$I + 2 = \frac{0 - (-10)}{10}$$

which yields  $I = -1$  mA. Since this is not possible, our original assumption is *not* correct. We start again, assuming that  $D_1$  is off and  $D_2$  is on. The current  $I_{D2}$  is given by

$$I_{D2} = \frac{10 - (-10)}{15} = 1.33 \text{ mA}$$

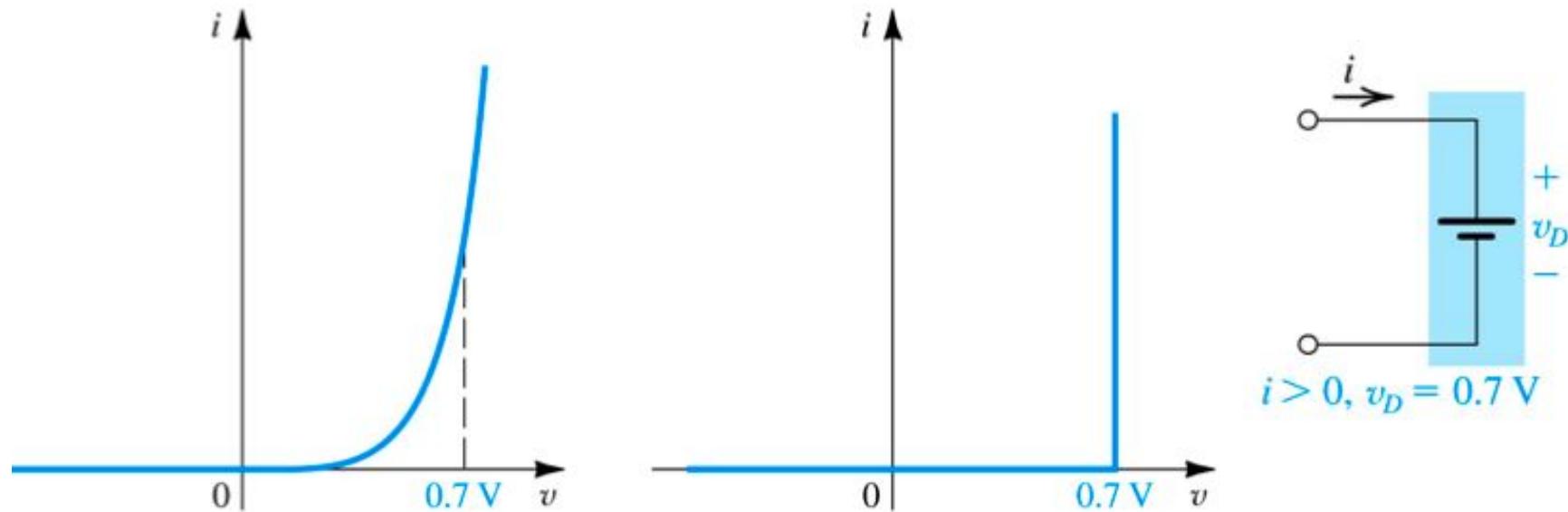
and the voltage at node B is

$$V_B = -10 + 10 \times 1.33 = +3.3 \text{ V}$$

Thus  $D_1$  is reverse biased as assumed, and the final result is  $I = 0$  and  $V = 3.3$  V.



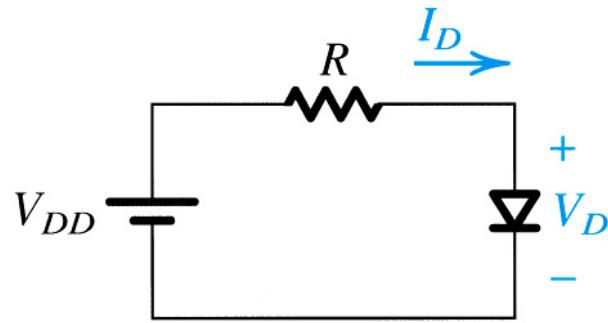
# Constant Voltage Model in Forward Bias



- A better diode model which typically gives more accurate results in circuit analysis is the **Constant Voltage Model**
- This model also assumes the diode is a short circuit when forward-biased, and an open circuit when reverse biased
- The diode is assumed to have  $V = 0.7V$  across it when on
  - $0.7V$  is a reasonable value to assume for most diodes



# Example using Diode models



For this example use :

$$V_{DD} = 5 \text{ V}$$

$$R = 1 \text{ k}\Omega$$

Then find  $I_D$  using :

$$I_D = (V_{DD} - V_D) / R$$

- Using the Ideal Diode model with  $V_D = 0\text{V}$  when the diode is turned on :

$$\rightarrow I_D = 5\text{V} / 1 \text{ k}\Omega = 5\text{mA}$$

- Using the Constant Voltage diode model with  $V_D = 0.7\text{V}$  when the diode is turned on :

$$\rightarrow I_D = 4.3\text{V} / 1 \text{ k}\Omega = 4.3\text{mA}$$

- To get the most accurate value, we must use the exponential equation for  $I_D$



# Solving by Iteration

## Example 4.4

Determine the current  $I_D$  and the diode voltage  $V_D$  for the circuit in Fig. 4.10 with  $V_{DD} = 5$  V and  $R = 1 \text{ k}\Omega$ . Assume that the diode has a current of 1 mA at a voltage of 0.7 V.

### Solution

To begin the iteration, we assume that  $V_D = 0.7$  V and use Eq. (4.7) to determine the current,

$$\begin{aligned} I_D &= \frac{V_{DD} - V_D}{R} \\ &= \frac{5 - 0.7}{1} = 4.3 \text{ mA} \end{aligned}$$

$$I_D = I_S (e^{V_D/V_T} - 1) \approx I_S e^{V_D/V_T} \Rightarrow V_D \approx V_T \ln(I_D/I_S) \text{ with : } V_T = \frac{kT}{q}$$

It was given that  $I_D = 1\text{mA}$  at  $V_D = 0.7\text{V}$ , so we can find  $I_S$ :

$$I_S \approx I_D e^{-V_D/V_T} \Rightarrow I_S \approx 10^{-3} e^{-0.7V/0.026V} = 2 \times 10^{-15} A = 2 fA$$



# Solving by Iteration

Procedure to solve for  $I_D$  by iteration :

1. “Guess” a value for  $I_D$
2. Solve for  $V_D$  using  $V_D = V_T \ln (I_D/I_S)$
3. Solve for  $I_D$  using  $I_D = (V_{DD} - V_D) / R$
4. Repeat Steps 1-3, using your new value of  $I_D$  as the next “guess”
5. Continue until the values for  $I_D$  converge

Example :

Guess 1:  $I_D = 4.3000000\text{mA} \rightarrow V_D = 738.309\text{mV} \rightarrow I_D = 4.2616913\text{mA}$

Guess 2:  $I_D = 4.2616913\text{mA} \rightarrow V_D = 738.076\text{mV} \rightarrow I_D = 4.2619240\text{mA}$

Guess 3:  $I_D = 4.2619240\text{mA} \rightarrow V_D = 738.077\text{mV} \rightarrow I_D = 4.2619225\text{mA}$

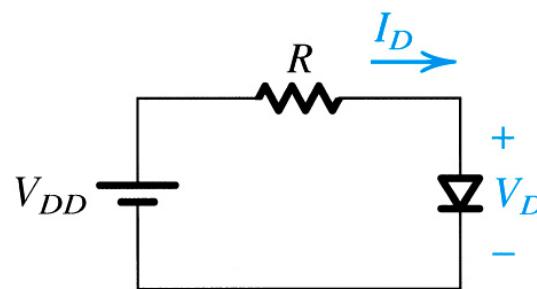
Guess 4:  $I_D = 4.2619225\text{mA} \rightarrow V_D = 738.077\text{mV} \rightarrow I_D = 4.2619225\text{mA}$

The result converged after only 4 iterations due to a good 1<sup>st</sup> guess. ☺

**Note the use of the slowly varying In function to aid convergence!**



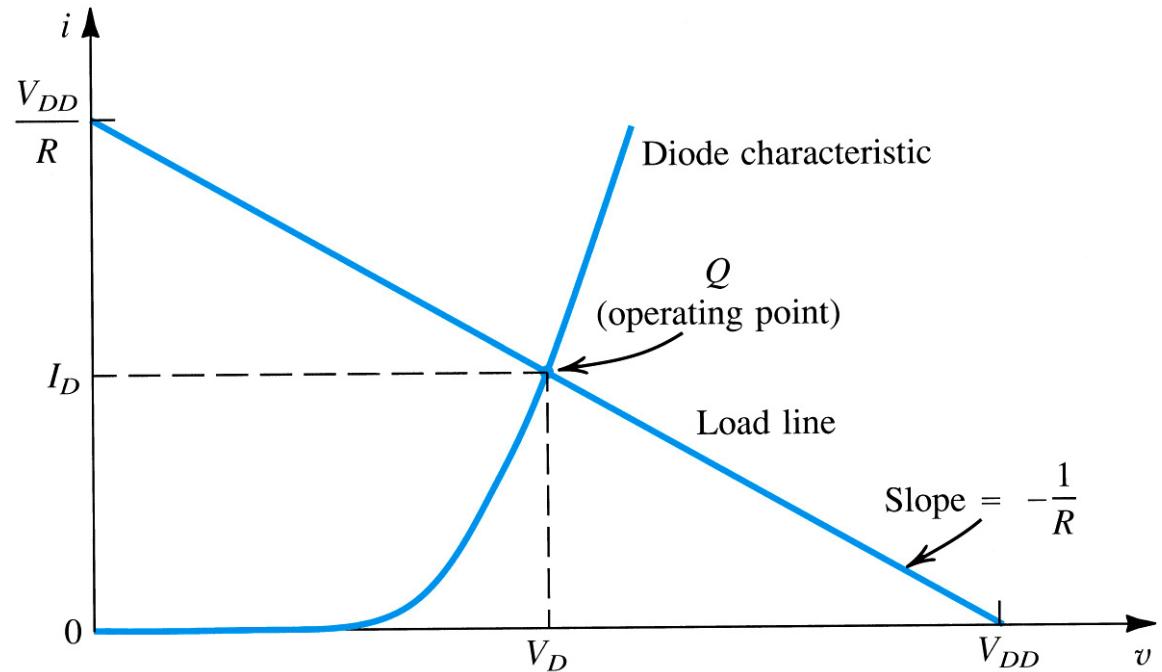
# Graphical Analysis using Load Lines



2 equations to solve :

$$I_D = (V_{DD} - V_D) / R$$

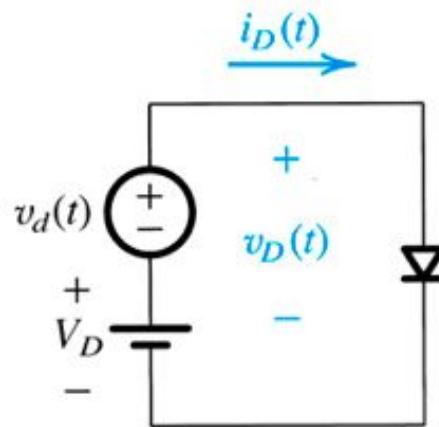
$$I_D = I_S (e^{V_D/V_T} - 1)$$



- Another way to solve this nonlinear set of simultaneous equations is graphically, by plotting a **Load line** for the circuit on a plot of the diode I-V characteristic curve
  - Where the 2 curves cross is the solution! Called the **Q-point**
  - Can use any 2 points to plot the Load line (Not just  $V_{DD}/R$  !)

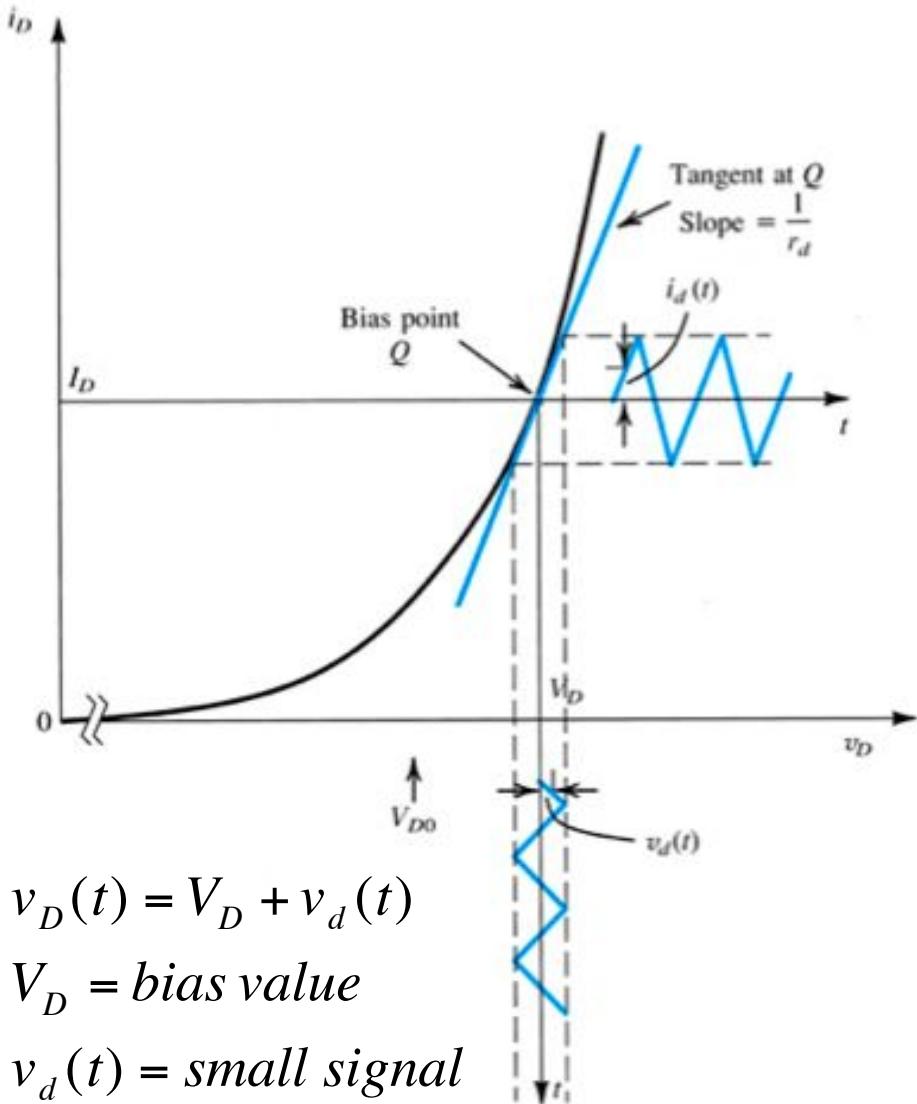


# Small-Signal Analysis



- Linear circuit analysis techniques such as superposition can be used for small variations around a bias point

***A small enough piece of anything nonlinear looks linear!***



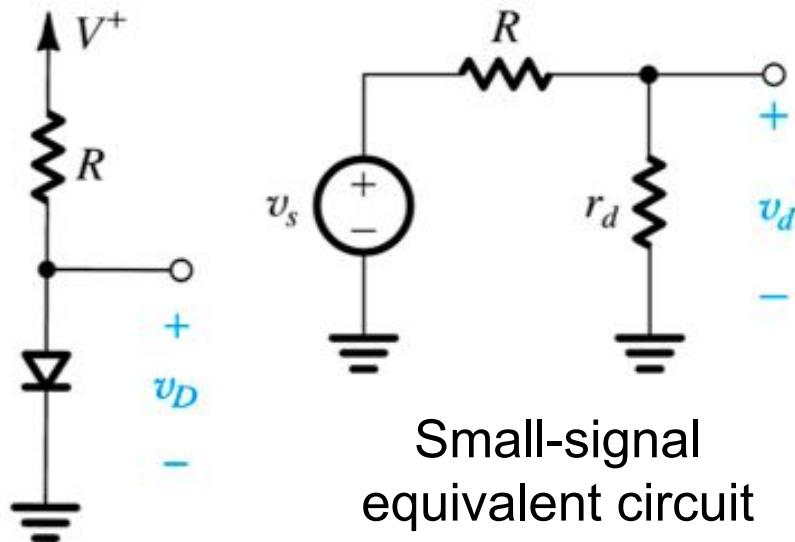
$$v_D(t) = V_D + v_d(t)$$

$V_D$  = bias value

$v_d(t)$  = small signal



# Small-Signal Diode Model



Small-signal diode resistance :

$$g_d = \frac{\partial i_D}{\partial v_D} \text{ at the bias point}$$

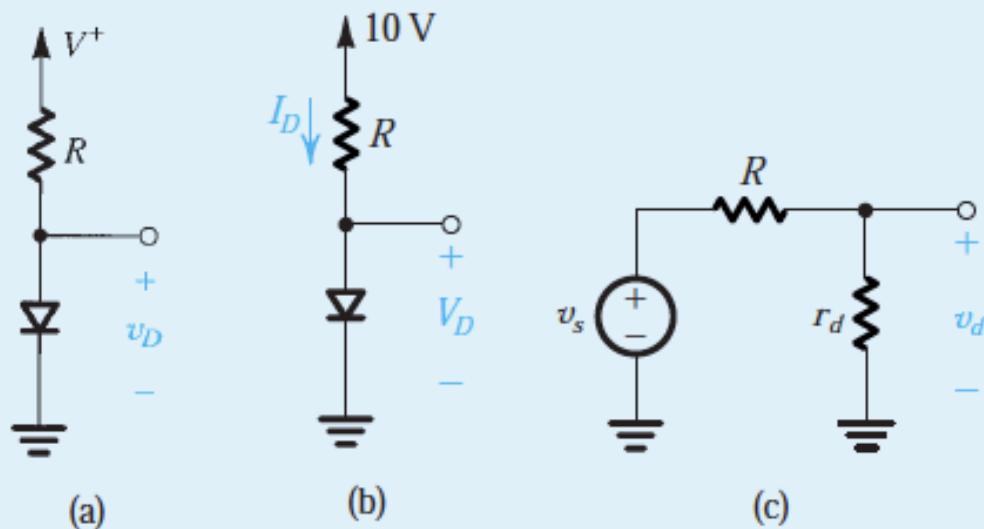
$$\Rightarrow r_d = \frac{1}{g_d} = \frac{V_T}{I_D}$$

- It is often convenient to analyze a nonlinear circuit for small variations around a bias point. (aka “Q-point”)
  - Can use linear circuit analysis methods, like voltage division
- To do this, we must first find  $r_d$ , **the small-signal resistance** of the diode
- Then we can draw the **small-signal equivalent circuit**, and analyze it using standard linear circuit analysis methods.



## Example 4.5

Consider the circuit shown in Fig. 4.14(a) for the case in which  $R = 10 \text{ k}\Omega$ . The power supply  $V^+$  has a dc value of 10 V on which is superimposed a 60-Hz sinusoid of 1-V peak amplitude. (This “signal” component of the power-supply voltage is an imperfection in the power-supply design. It is known as the **power-supply ripple**. More on this later.) Calculate both the dc voltage of the diode and the amplitude of the sine-wave signal appearing across it. Assume the diode to have a 0.7-V drop at 1-mA current.



**Figure 4.14** (a) Circuit for Example 4.5. (b) Circuit for calculating the dc operating point. (c) Small-signal equivalent circuit.



## Solution

Considering dc quantities only, we assume  $V_D \approx 0.7$  V and calculate the diode dc current

$$I_D = \frac{10 - 0.7}{10} = 0.93 \text{ mA}$$

Since this value is very close to 1 mA, the diode voltage will be very close to the assumed value of 0.7 V. At this operating point, the diode incremental resistance  $r_d$  is

$$r_d = \frac{V_T}{I_D} = \frac{25}{0.93} = 26.9 \Omega$$

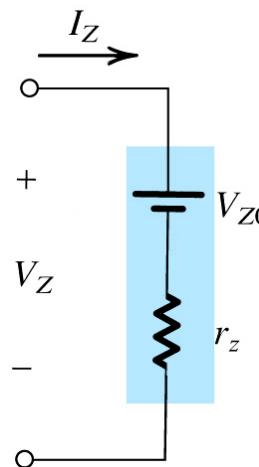
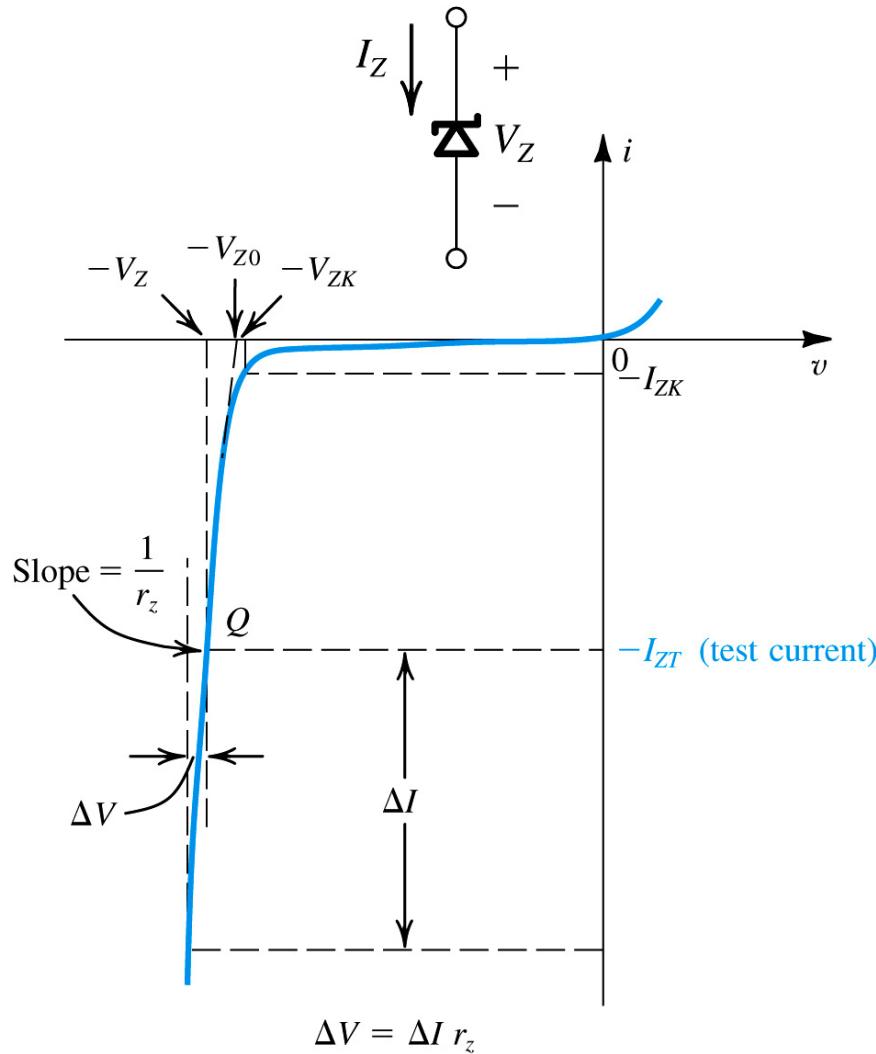
The signal voltage across the diode can be found from the small-signal equivalent circuit in Fig. 4.14(c). Here  $v_s$  denotes the 60-Hz 1-V peak sinusoidal component of  $V^+$ , and  $v_d$  is the corresponding signal across the diode. Using the voltage-divider rule provides the peak amplitude of  $v_d$  as follows:

$$\begin{aligned} v_d (\text{peak}) &= \hat{V}_s \frac{r_d}{R + r_d} \\ &= 1 \frac{0.0269}{10 + 0.0269} = 2.68 \text{ mV} \end{aligned}$$

Finally we note that since this value is quite small, our use of the small-signal model of the diode is justified.



# Reverse-biased Zener Diode Model



$g_z = \frac{\partial i_z}{\partial v_z}$  at the bias point

$$\Rightarrow r_z = \frac{1}{g_z} = \frac{1}{\text{Slope}}$$

$$\text{and } V_z = V_{z0} + I_z r_z$$

- Zener diodes are diodes intentionally operated in the reverse-breakdown region
- Used as voltage references
- Modeled as a DC battery in series with a small-signal **incremental resistance,  $r_z$**



# Voltage Regulation using Diodes

## Example 4.6

Consider the circuit shown in Fig. 4.15. A string of three diodes is used to provide a constant voltage of about 2.1 V. We want to calculate the percentage change in this regulated voltage caused by (a) a  $\pm 10\%$  change in the power-supply voltage and (b) connection of a  $1\text{-k}\Omega$  load resistance.

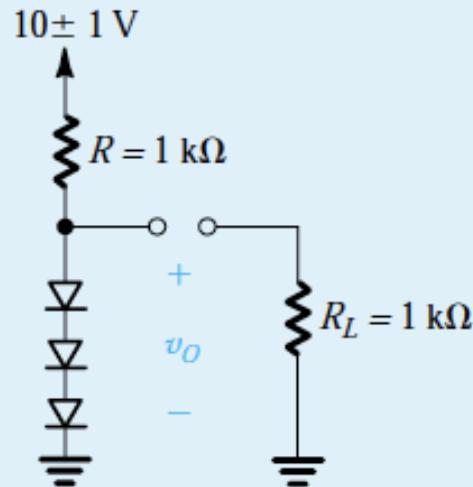


Figure 4.15 Circuit for Example 4.6.

### Solution

With no load, the nominal value of the current in the diode string is given by

$$I = \frac{10 - 2.1}{1} = 7.9 \text{ mA}$$



Thus each diode will have an incremental resistance of

$$r_d = \frac{V_T}{I}$$

Thus,

$$r_d = \frac{25}{7.9} = 3.2 \Omega$$

The three diodes in series will have a total incremental resistance of

$$r = 3r_d = 9.6 \Omega$$

This resistance, along with the resistance  $R$ , forms a voltage divider whose ratio can be used to calculate the change in output voltage due to a  $\pm 10\%$  (i.e.,  $\pm 1\text{-V}$ ) change in supply voltage. Thus the peak-to-peak change in output voltage will be

$$\Delta v_O = 2 \frac{r}{r+R} = 2 \frac{0.0096}{0.0096 + 1} = 19 \text{ mV peak-to-peak}$$

That is, corresponding to the  $\pm 1\text{-V}$  ( $\pm 10\%$ ) change in supply voltage, the output voltage will change by  $\pm 9.5 \text{ mV}$  or  $\pm 0.5\%$ . Since this implies a change of about  $\pm 3.2 \text{ mV}$  per diode, our use of the small-signal model is justified.

When a load resistance of  $1 \text{ k}\Omega$  is connected across the diode string, it draws a current of approximately  $2.1 \text{ mA}$ . Thus the current in the diodes decreases by  $2.1 \text{ mA}$ , resulting in a decrease in voltage across the diode string given by

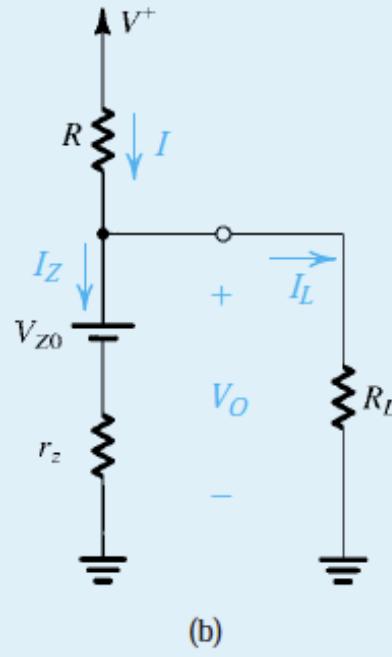
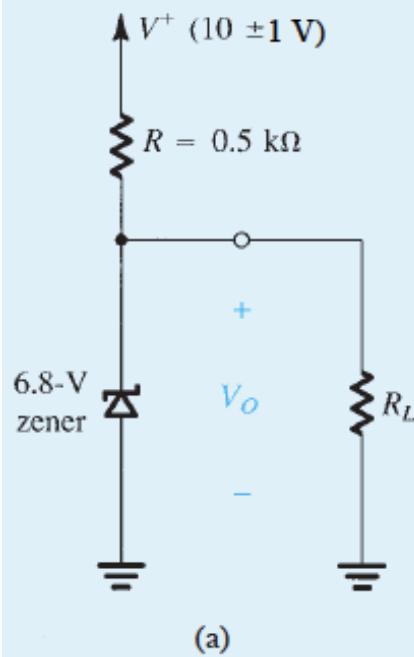
$$\Delta v_O = -2.1 \times r = -2.1 \times 9.6 = -20 \text{ mV}$$

Since this implies that the voltage across each diode decreases by about  $6.7 \text{ mV}$ , our use of the small-signal model is not entirely justified. Nevertheless, a detailed calculation of the voltage change using the exponential model results in  $\Delta v_O = -23 \text{ mV}$ , which is not too different from the approximate value obtained using the incremental model.



## Example 4.7

The 6.8-V zener diode in the circuit of Fig. 4.19(a) is specified to have  $V_Z = 6.8$  V at  $I_Z = 5$  mA,  $r_z = 20 \Omega$ , and  $I_{ZK} = 0.2$  mA. The supply voltage  $V^+$  is nominally 10 V but can vary by  $\pm 1$  V.



**Figure 4.19** (a) Circuit for Example 4.7. (b) The circuit with the zener diode replaced with its equivalent circuit model.

- Find  $V_O$  with no load and with  $V^+$  at its nominal value.
- Find the change in  $V_O$  resulting from the  $\pm 1$ -V change in  $V^+$ . Note that  $(\Delta V_O / \Delta V^+)$ , usually expressed in mV/V, is known as **line regulation**.
- Find the change in  $V_O$  resulting from connecting a load resistance  $R_L$  that draws a current  $I_L = 1$  mA, and hence find the **load regulation**  $(\Delta V_O / \Delta I_L)$  in mV/mA.



## Solution

First we must determine the value of the parameter  $V_{Z0}$  of the zener diode model. Substituting  $V_z = 6.8$  V,  $I_z = 5$  mA, and  $r_z = 20 \Omega$  in Eq. (4.20) yields  $V_{Z0} = 6.7$  V. Figure 4.19(b) shows the circuit with the zener diode replaced with its model.

(a) With no load connected, the current through the zener is given by

$$I_Z = I = \frac{V^+ - V_{Z0}}{R + r_z}$$
$$= \frac{10 - 6.7}{0.5 + 0.02} = 6.35 \text{ mA}$$
$$V_Z = V_{Z0} + r_z I_Z$$

Thus,

$$V_O = V_{Z0} + I_Z r_z$$
$$= 6.7 + 6.35 \times 0.02 = 6.83 \text{ V}$$

(b) For a  $\pm 1$ -V change in  $V^+$ , the change in output voltage can be found from

$$\Delta V_O = \Delta V^+ \frac{r_z}{R + r_z}$$
$$= \pm 1 \times \frac{20}{500 + 20} = \pm 38.5 \text{ mV}$$

Thus,

$$\text{Line regulation} = 38.5 \text{ mV/V}$$

Line regulation can also be expressed in percent

(c) When a load resistance  $R_L$  that draws a load current  $I_L = 1$  mA is connected, the zener current will decrease by 1 mA. The corresponding change in zener voltage can be found from

$$\Delta V_O = r_z \Delta I_Z$$
$$= 20 \times -1 = -20 \text{ mV}$$

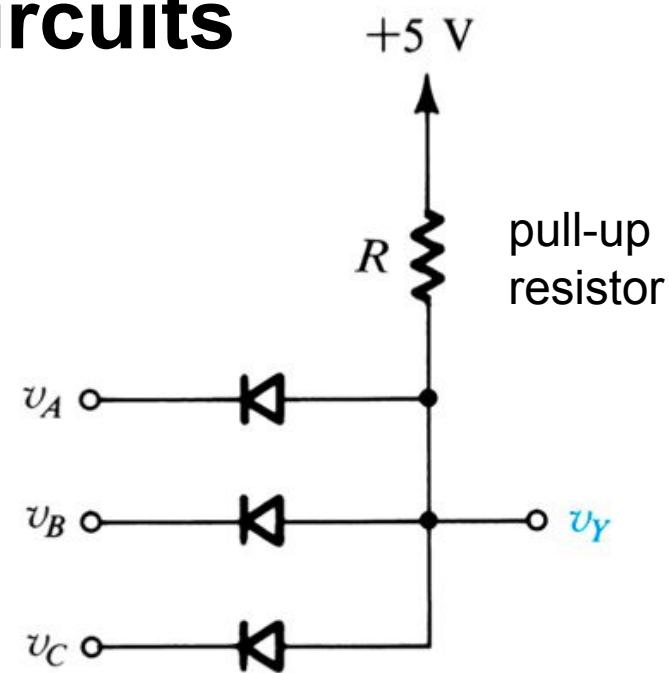
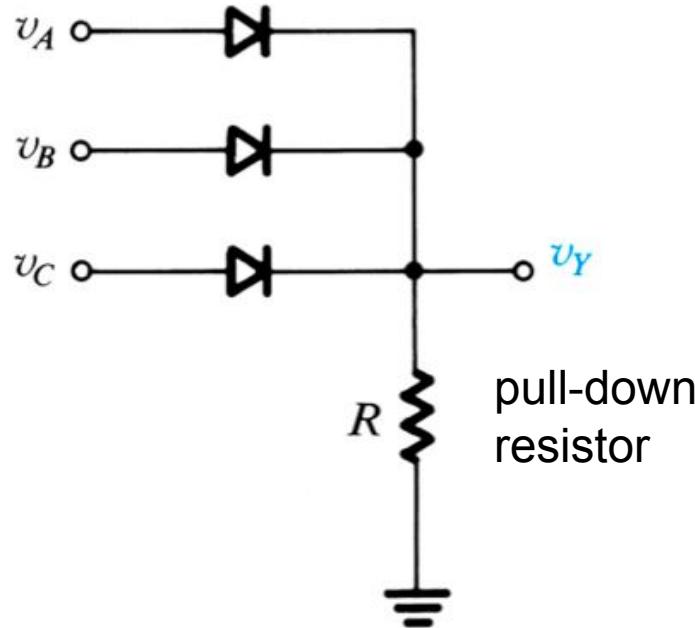
Thus the load regulation is

$$\text{Load regulation} \equiv \frac{\Delta V_O}{\Delta I_L} = -20 \text{ mV/mA}$$

Load regulation can also be expressed in percent



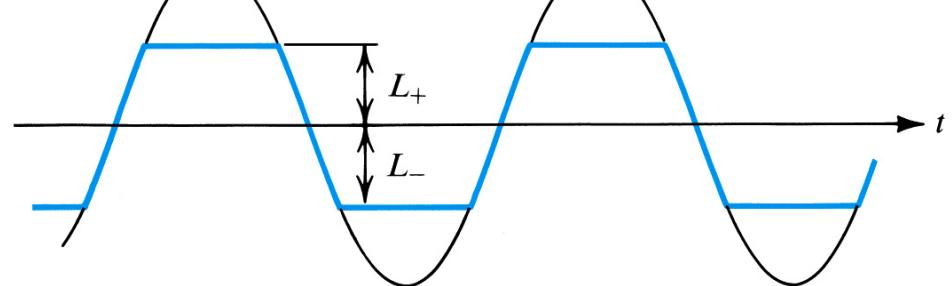
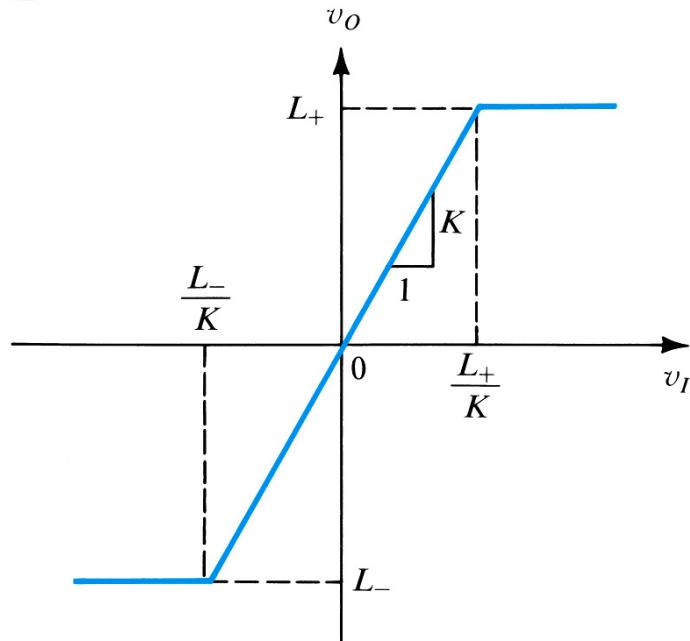
# Diode Logic Circuits



- Diodes can also be used to create simple logic circuits
  - **RDL = Resistor-Diode Logic**
- RDL is an old logic family, seldom used now since it doesn't amplify the signal
- The gate on the left is an OR gate, since the output is high when any input is high
- The gate on the left is an AND gate, since the output is low when any input is low



# Limiter Circuits

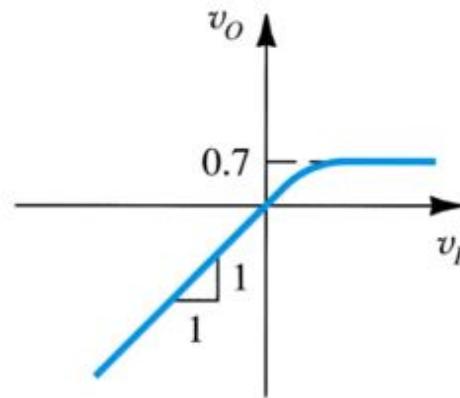
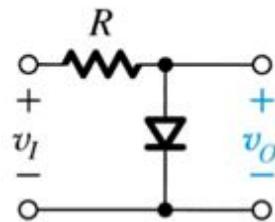


- Diodes can also be used to create **Limiter Circuits** which limit how high and how low a signal can go
  - The gain is set by the rest of the circuit (e.g., an opamp)

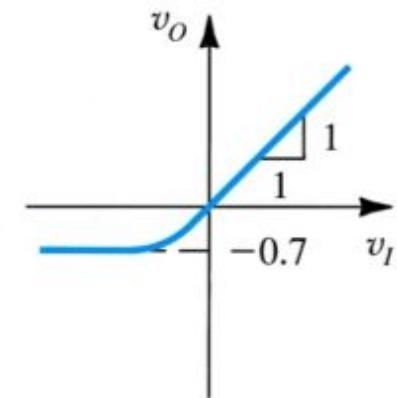
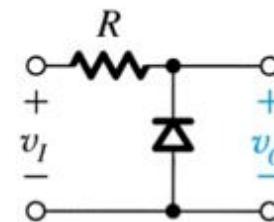
- Here a sine wave is limited by diodes to make it look more like a square wave
  - Useful in Phase-Locked Loops (PLLs) and communications circuits



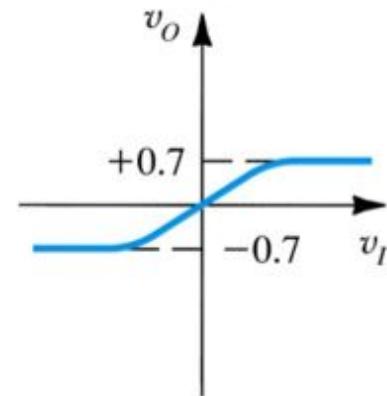
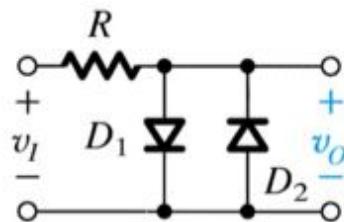
# Limiter Circuits



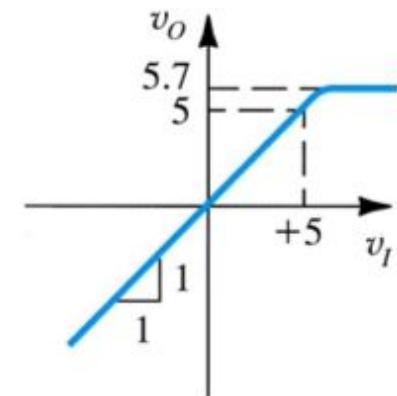
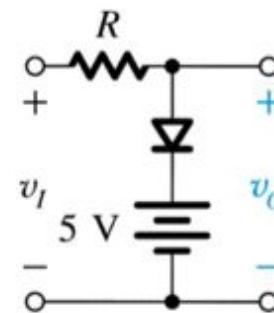
(a)



(b)



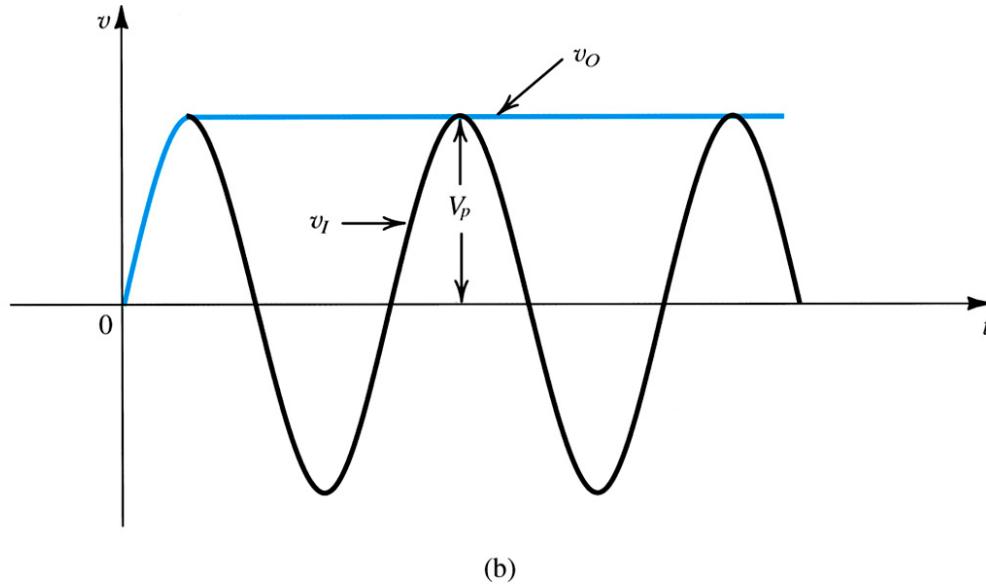
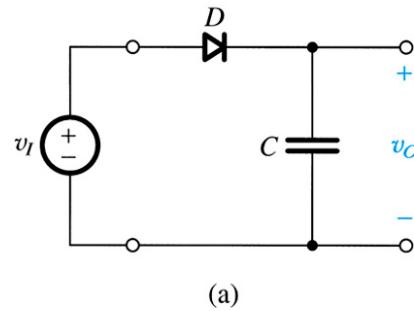
(c)



(d)



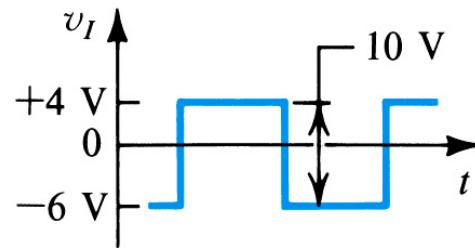
# Peak Detector Circuits



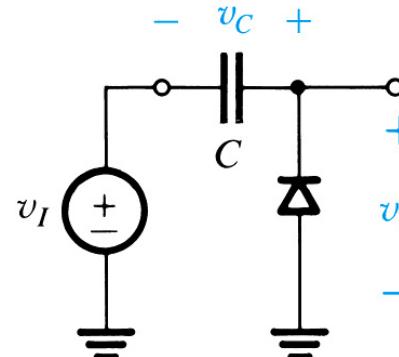
- Diodes are often used to create **Peak Detector** circuits, which output the max (peak) value of an input voltage
  - When  $V_I$  goes positive, the diode turns on and charges  $C$  to  $V_P$ , the peak value of  $V_I$  (Ideal diodes assumed here for simplicity)
  - When  $V_I$  drops from it's peak value, the diode turns off and  $C$  stays charged to  $V_P$  until a load or leakage current discharges it
- Useful in communications circuits, power supplies, etc.



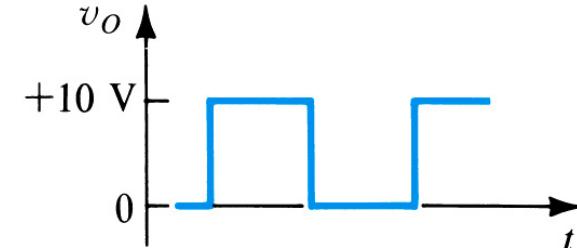
# DC Restorer Circuits



(a)



(b)

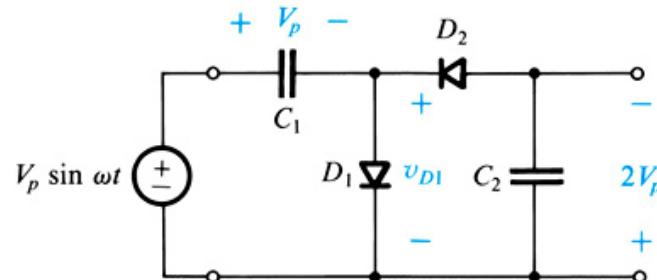


(c)

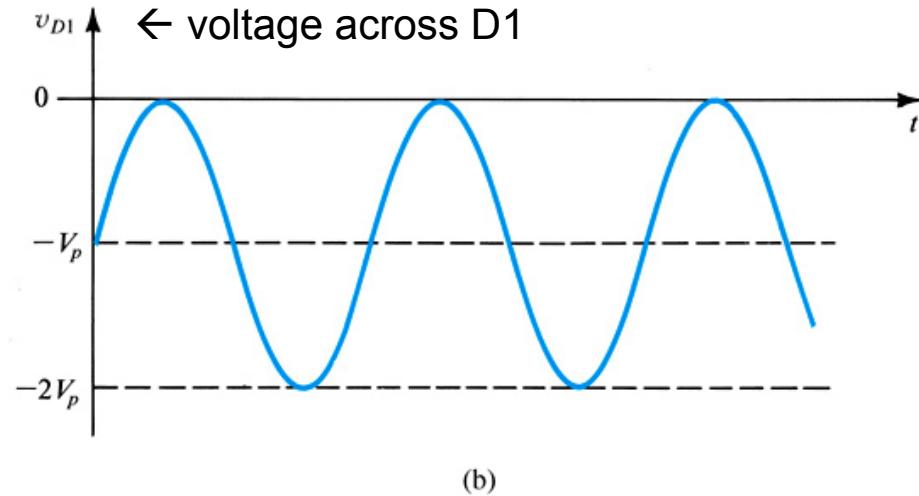
- Also referred to as a **Clamped Capacitor** circuit
- Since the diode turns on and prevents  $V_o < 0V$ , the capacitor charges up to the peak negative value of  $V_i$ 
  - In this example,  $V_C = +6V$  since the minimum  $V_i = -6V$
  - Ideal diodes were assumed here for ease of understanding
- Then when  $V_i$  rises the diode turns off and  $V_o$  goes up by the total change in voltage in  $V_i$
- Useful in restoring DC values to AC coupled signals, etc.



# Voltage Doubler Circuits



(a)

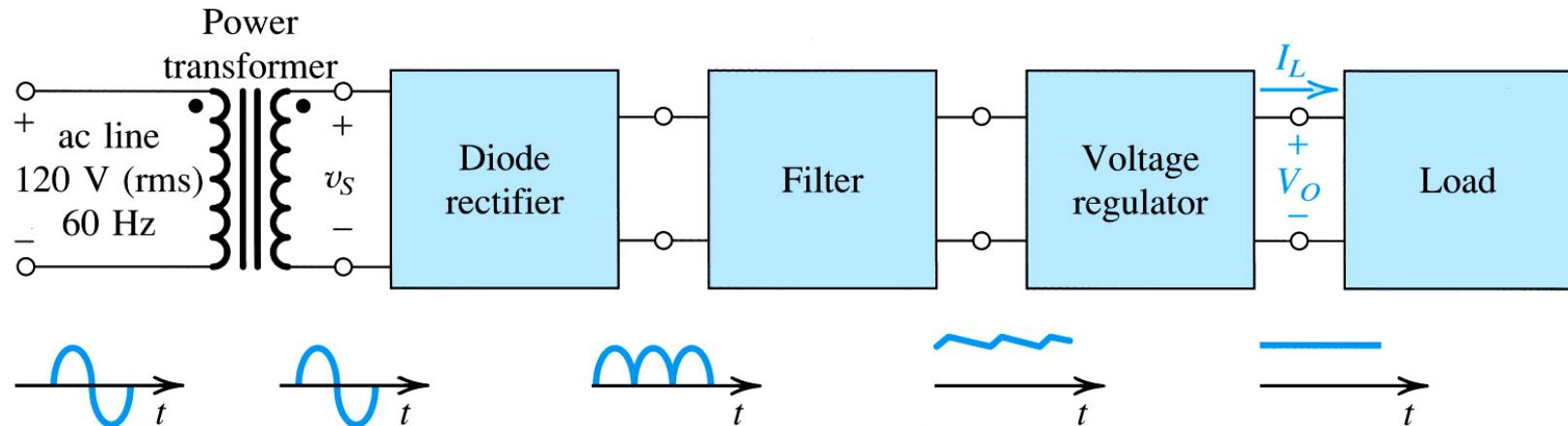


(b)

- By combining a clamped capacitor circuit and a peak detector circuit, we can build a **voltage doubler**
  - $C_1$  and  $D_1$  form the clamped capacitor circuit
  - $C_2$  and  $D_2$  form the peak detector circuit
- $D_1$  keeps  $V_{D1} < 0V$ , so  $C_1$  charges up to  $+V_P$
- $D_2$  turns on to charge  $C_2$  to  $-2V_P \rightarrow \underline{V_{out} = 2x \text{ the } V_{in}}$
- Useful to create voltages  $> V_{DD}$  (e.g., for flash memory)



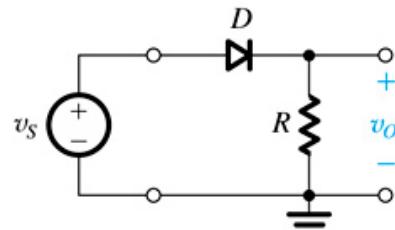
# Power Supplies



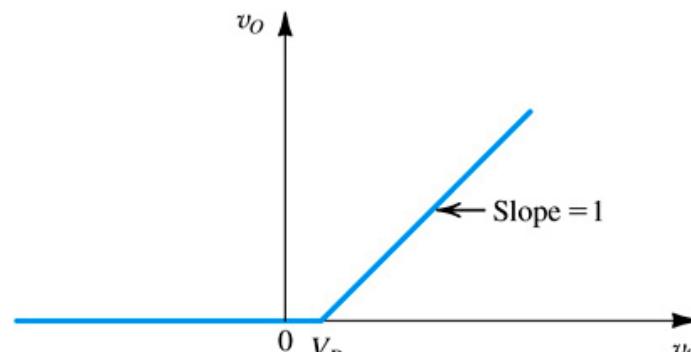
- One of the most useful applications of diodes is for DC Power Supplies, which convert AC  $V_{in}$  into DC  $V_{out}$ 
  - A transformer steps down the voltage to a useful value (e.g., 12V), and provides isolation between the user and the AC power grid
  - A diode rectifier converts the bipolar AC voltage into unipolar pulses
  - A filter smoothes out the pulses, leaving only small variations (ripple)
  - A voltage regulator keeps the output voltage constant, as both the input voltage and load current vary (e.g., Zener diode or IC regulator)



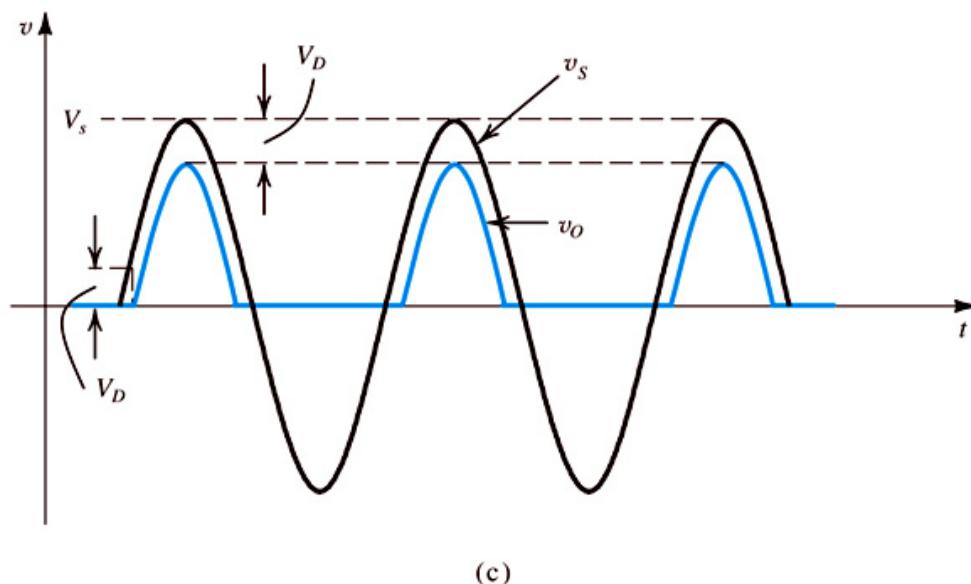
# Half Wave Rectifiers



(a)



(b)

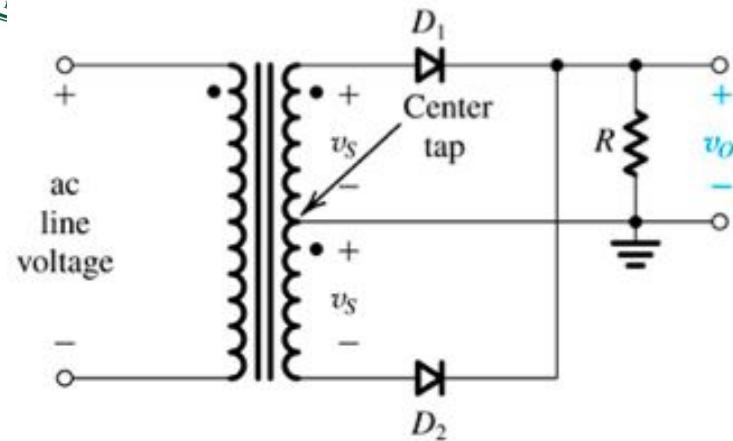


(c)

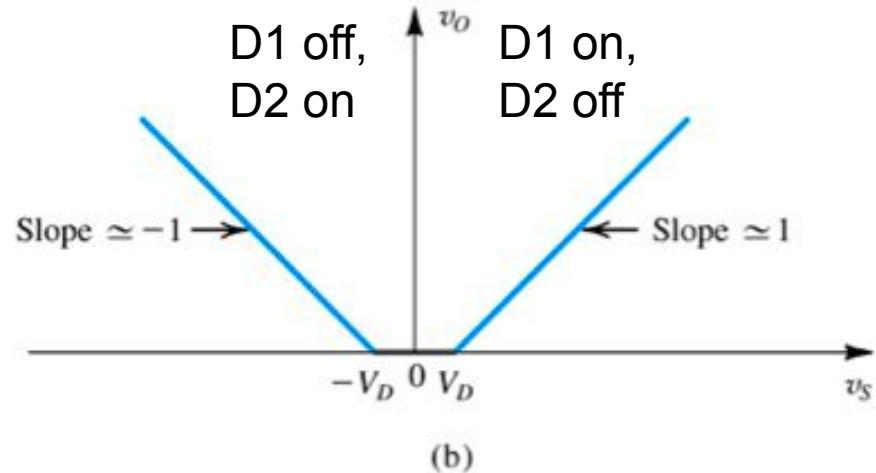
- **Half Wave Rectifiers** only allow the + or – parts of an input signal through
- Here the diode is on for  $V_S > 0.7V$ , off for  $V_S < 0.7V$
- Some input is lost across the diode
- Diode must handle the **Peak Inverse Voltage (PIV)** (Equal to  $V_S$  here)



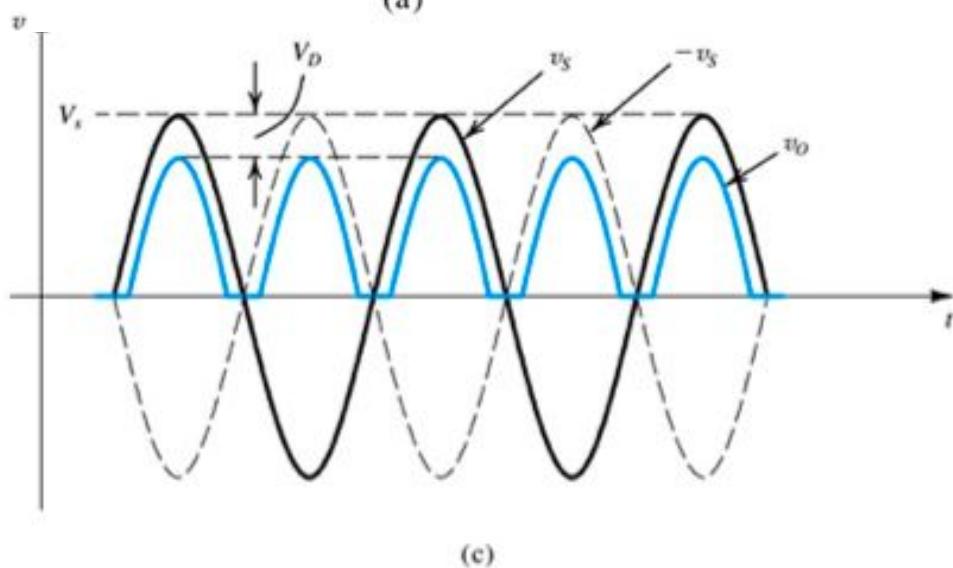
# Full Wave Rectifiers



(a)



(b)



(c)

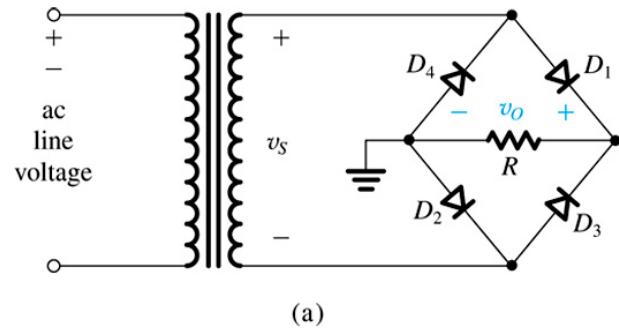
Here the PIV =  $2V_s - V_D$

- **Full Wave Rectifiers** allow both the + and – inputs through, but convert both to positive output voltage pulses
- Here a center-tapped transformer + 2 diodes are needed for this

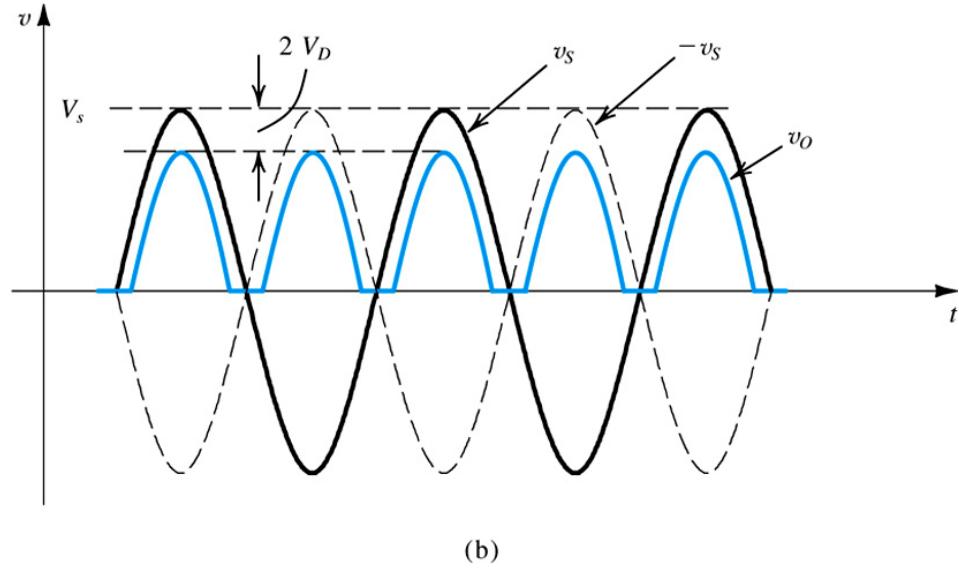


# Bridge Rectifiers

D1, D2 on and D3, D4 off  
on + peaks. On - peaks  
D1, D2 off and D3, D4 on



(a)

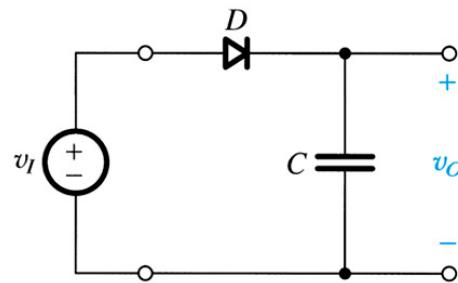


(b)

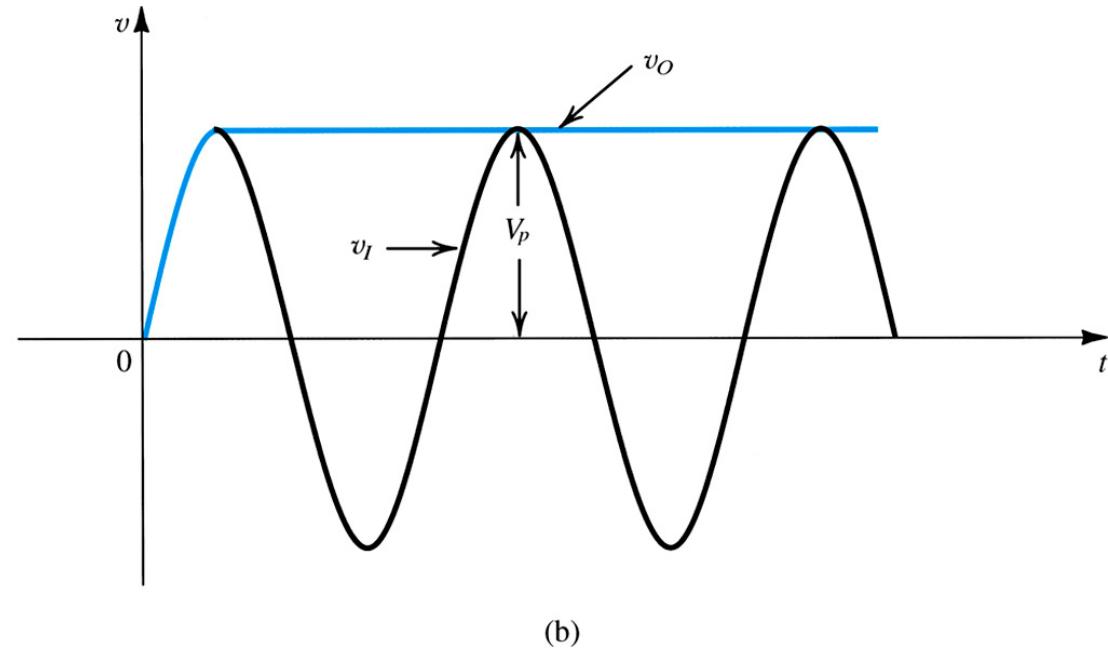
- **Bridge Rectifiers** perform full wave rectification without the need for a center-tapped transformer (lower cost)
  - Requires 4 diodes, but these cost less than the transformer
  - Output voltage peaks are slightly lower, at  $V_S - 2V_D$
  - Peak Inverse Voltage (PIV) is only  $V_S - V_D$ , since across 2 diodes
  - Most popular rectifier circuit used for power supplies



# Filter Capacitors



(a)



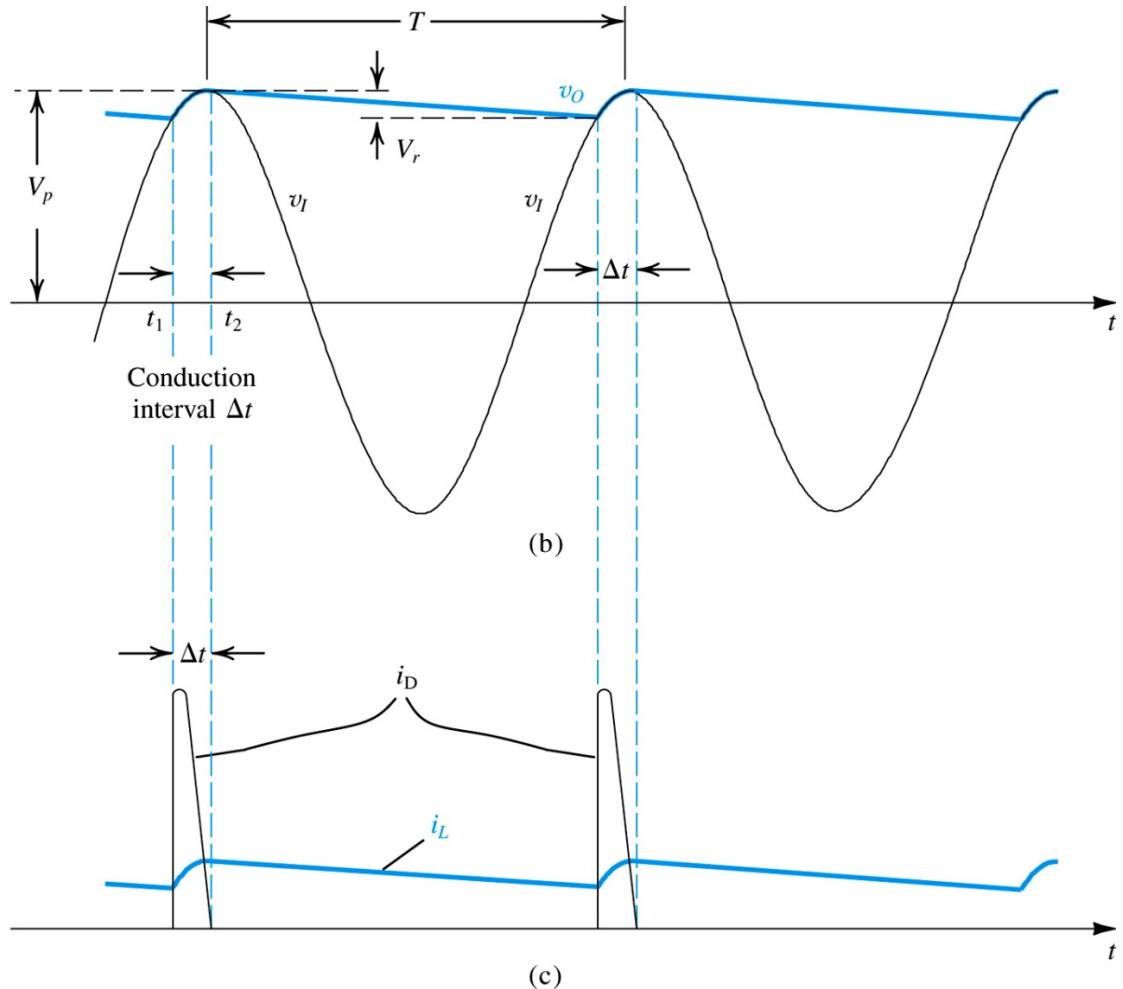
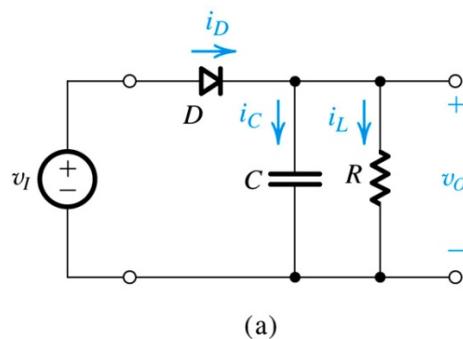
(b)

- To filter the pulses from the diode rectifier circuit, a large filter capacitor is used ( $100\text{-}1000\mu\text{F}$  or larger)
- Larger capacitors reduce ripple more, but also cost more (Shown here without a load current to discharge the cap)



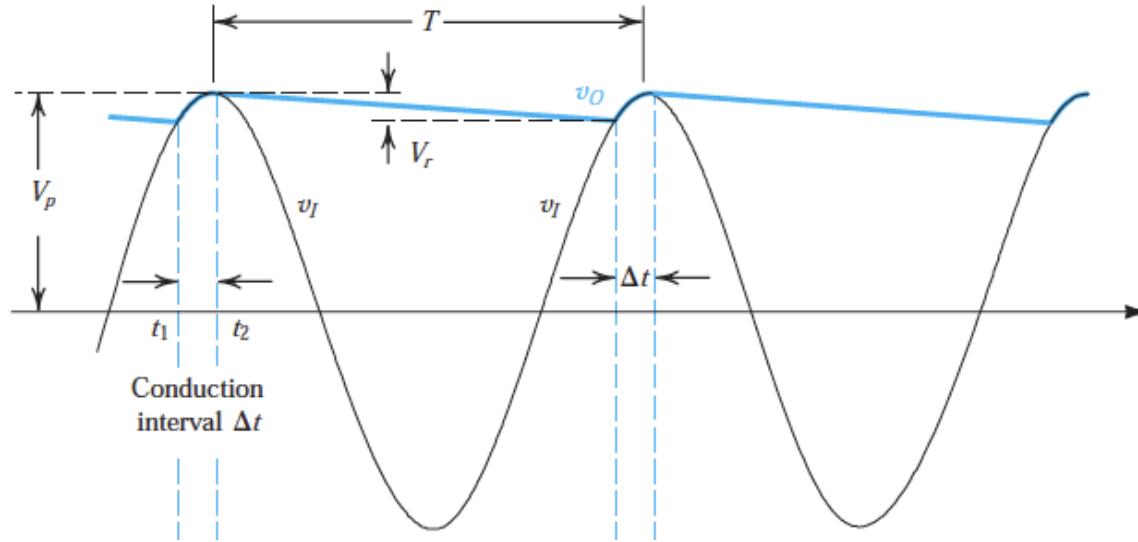
# Filter Capacitors

- With a load, the filter capacitor discharges when the diode is off  
**→ Ripple! ( $V_r$ )**
- The diode turns on every cycle to replace the lost charge to the cap





# Ripple Voltage



- The filter capacitor is chosen such that  $RC \gg T$ , so the normal exponential capacitor discharge appears linear

$$I = C \frac{dV}{dt} \approx C \frac{\Delta V}{\Delta t} \quad \text{and} \quad I_L \approx \frac{V_p}{R} \Rightarrow \frac{V_p}{R} \approx C \frac{V_r}{T}$$

or 
$$V_r \approx V_p \left( \frac{T}{RC} \right)$$

which can also be written as:

$$V_r \approx \frac{I_L}{fC}$$



# Average and Peak Diode Current

The charge supplied to the load by the capacitor during T is:

$$I = \frac{\Delta Q}{\Delta t} \Rightarrow \Delta Q = I \Delta t \Rightarrow Q_{lost} = I_L T$$

During  $\Delta t$  the diode must replace this charge lost from the capacitor, plus the load current,  $I_L$  :

$$Q_{supplied} = Q_{lost} + I_L \Delta t = I_L T + I_L \Delta t = I_L (T + \Delta t)$$

Therefore the average diode current is given by :

$$I_{Davg} = \frac{Q_{supplied}}{\Delta t} = I_L \left( 1 + \frac{T}{\Delta t} \right)$$



# Average and Peak Diode Current

To find the average diode current, we need to know the **conduction angle  $\omega\Delta t$**  and the **conduction interval  $\Delta t$**

$$V_P - V_r = V_P \cos(\omega\Delta t) \approx V_P \left(1 - \frac{1}{2}(\omega\Delta t)^2\right) \text{ for } \omega\Delta t \text{ small}$$

$$\Rightarrow \omega\Delta t \approx \sqrt{2V_r/V_P} \text{ and } \Delta t \approx \left(\frac{T}{2\pi}\right) \sqrt{\frac{2V_r}{V_P}}$$

Combining this result with the previous equation for  $I_{Davg}$  :

$$I_{Davg} = I_L \left(1 + \frac{T}{\Delta t}\right) = I_L \left(1 + \pi \sqrt{\frac{2V_P}{V_r}}\right)$$

Also, analyzing the differential equation for  $I_{Dmax}$  yields :

$$I_{Dmax} = I_L \left(1 + 2\pi \sqrt{\frac{2V_P}{V_r}}\right) \approx 2I_{Davg}$$



## Example 4.8

Consider a peak rectifier fed by a 60-Hz sinusoid having a peak value  $V_p = 100$  V. Let the load resistance  $R = 10$  k $\Omega$ . Find the value of the capacitance  $C$  that will result in a peak-to-peak ripple of 2 V. Also, calculate the fraction of the cycle during which the diode is conducting and the average and peak values of the diode current.

### Solution

From Eq. (4.29a) we obtain the value of  $C$  as

$$C = \frac{V_p}{V_r fR} = \frac{100}{2 \times 60 \times 10 \times 10^3} = 83.3 \text{ } \mu\text{F}$$

The conduction angle  $\omega \Delta t$  is found from Eq. (4.30) as

$$\omega \Delta t = \sqrt{2 \times 2/100} = 0.2 \text{ rad}$$

Thus the diode conducts for  $(0.2/2\pi) \times 100 = 3.18\%$  of the cycle. The average diode current is obtained from Eq. (4.31), where  $I_L = 100/10 = 10$  mA, as

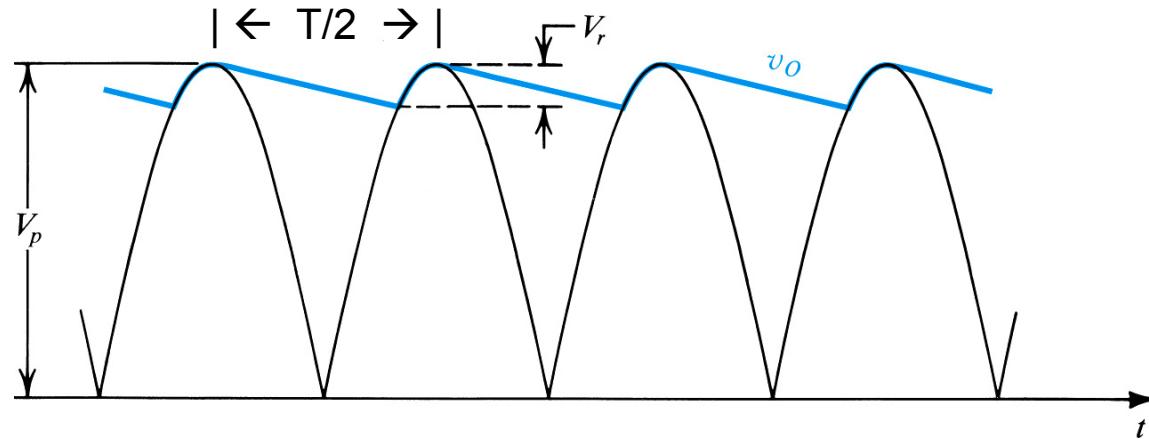
$$i_{Dav} = 10(1 + \pi\sqrt{2 \times 100/2}) = 324 \text{ mA}$$

The peak diode current is found using Eq. (4.32),

$$i_{Dmax} = 10(1 + 2\pi\sqrt{2 \times 100/2}) = 638 \text{ mA}$$



# Ripple, $I_{Davg}$ , $I_{Dmax}$ for Full Wave Rectifier



- The equations found for a Half Wave Rectifier can be modified for a Full Wave Rectifier by replacing T with T/2 :

$$V_r \approx V_P \left( \frac{T}{2RC} \right) \approx \frac{I_L}{2fC}$$

$$I_{Davg} = I_L \left( 1 + \frac{T}{2\Delta t} \right) = I_L \left( 1 + \pi \sqrt{\frac{V_P}{2V_r}} \right)$$

$$I_{Dmax} = I_L \left( 1 + 2\pi \sqrt{\frac{V_P}{2V_r}} \right) \approx 2I_{Davg}$$



# Summary of Key Concepts

- Large-signal models & analysis of forward-biased diodes
  - Exponential, Ideal and Constant Voltage-Drop Diode Models
  - Solving by Iteration, or by Graphical Analysis using Load Lines
- Small-signal analysis & the Small-signal Diode Model
- Models for reverse-biased Zener diodes
- Applications of Diodes
  - Voltage Regulation
  - Diode Logic Circuits
  - Limiting & Clamping Circuits
  - DC Restorer and Voltage Doubler Circuits
- Power Supplies
  - Diode rectifiers, Filters, Voltage regulation