

Homework-01

EEE 117

Due date 02/07/2022

Questions 1-5 2 points each

Questions 6-11 15 points each

Q-1 The rms value of $v(t) = V_{\max} \cos(\omega t + \delta)$ is given by
(a) V_{\max} (b) $V_{\max}/\sqrt{2}$ (c) $2 V_{\max}$ (d) $\sqrt{2} V_{\max}$

Q-2 If the rms phasor of a voltage is given by $V = 120/60^\circ$ volts, then the corresponding $v(t)$ is given by
(a) $120\sqrt{2} \cos(\omega t + 60^\circ)$ (b) $120 \cos(\omega t + 60^\circ)$
(c) $120\sqrt{2} \sin(\omega t + 60^\circ)$

Q-3 If a phasor representation of a current is given by $I = 70.7/45^\circ$ A, it is equivalent to
(a) $100 e^{j45^\circ}$ (b) $100 + j100$
(c) $50 + j50$

Q-4 With sinusoidal steady-state excitation, for a purely resistive circuit, the voltage and current phasors are
(a) in phase
(b) perpendicular with each other with V leading I
(c) perpendicular with each other with I leading V.

Q-5 For a purely inductive circuit, with sinusoidal steady-state excitation, the voltage and current phasors are
(a) in phase
(b) perpendicular to each other with V leading I
(c) perpendicular to each other with I leading V.

Q-6 Consider the sinusoidal voltage

$$v(t) = 25 \cos(400\pi t + 60^\circ) \text{ V.}$$

- What is the maximum amplitude of the voltage?
- What is the frequency in hertz?
- What is the frequency in radians per second?
- What is the phase angle in radians?
- What is the phase angle in degrees?
- What is the period in milliseconds?
- What is the first time after $t = 0$ that $v = 0$ V?

Q-7 Use the concept of the phasor to combine the following sinusoidal functions into a single trigonometric expression:

a) $y = 30 \cos(200t - 160^\circ) + 15 \cos(200t + 70^\circ)$,

b) $y = 90 \sin(50t - 20^\circ) + 60 \cos(50t - 70^\circ)$,

c) $y = 50 \cos(5000t - 60^\circ) + 25 \sin(5000t + 110^\circ) - 75 \cos(5000t - 30^\circ)$,

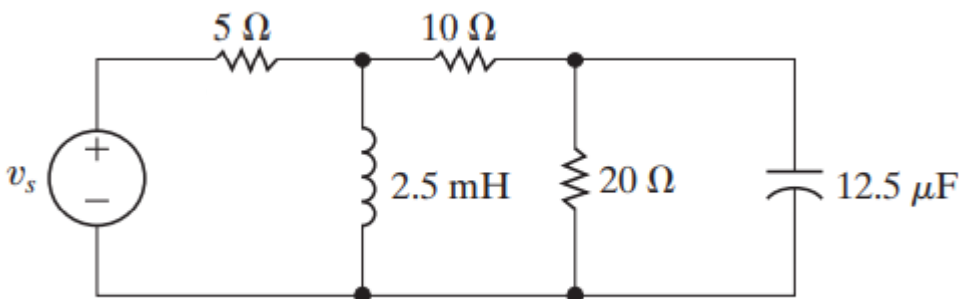
d) $y = 10 \cos(\omega t + 30^\circ) + 10 \sin \omega t + 10 \cos(\omega t + 150^\circ)$.

Q-8 A 25Ω resistor and a 10 mH inductor are connected in parallel. This parallel combination is also in parallel with the series combination of a 30Ω resistor and a $10 \mu\text{F}$ capacitor. These three parallel branches are driven by a sinusoidal current source whose current is $125 \sin(2500t + 60^\circ) \text{ A}$.

- a) Find total impedance.
- b) Analyze the circuit and find current and voltage for each component.

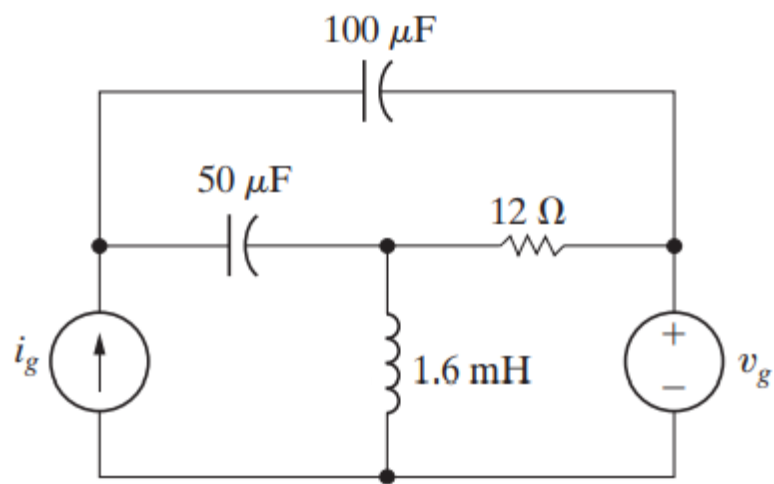
Q-9 For the circuit shown below.

- c) Find total impedance.
- d) Analyze the circuit and find current and voltage for each component. if $v_s = 25 \sin 4000t \text{ V}$.

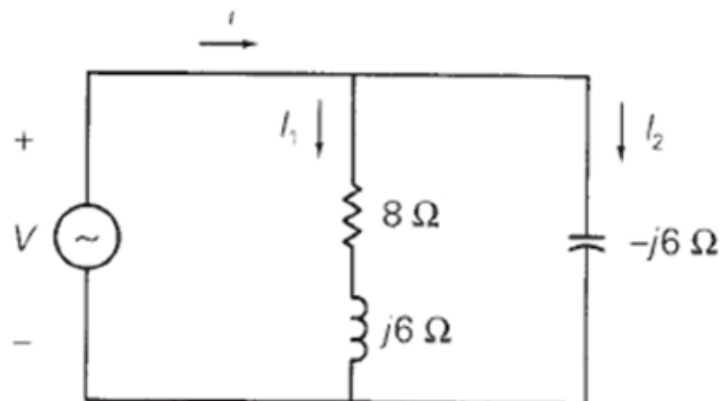


Q-10 Analyze the circuit and find current and voltage for each component.

if $i_g = 5 \cos 2500t$ A and $v_g = 20 \cos (2500t + 90^\circ)$ V.



Q-11 In the figure shown below, $\bar{I} = 10 \angle 0^\circ$ A, compute the phasors \bar{I}_1 , \bar{I}_2 and \bar{V} .



Q1 b.

Q2 b.

Q3 c.

Q4 a.

Q5 b.

Q6 $V(t) = V_m \cos(\omega t + \phi)$

(a) $V_m = 25 \text{ V}$

(b) $\omega = 2\pi f \rightarrow f = \frac{\omega}{2\pi} = \frac{400\pi}{2\pi} = 200 \text{ Hz}$

(c) $\omega = 400\pi$

(d) $\phi = 60^\circ = \pi/3 \text{ rad}$

(e) $\phi = 60^\circ$

(f) $\omega = 2\pi/T \rightarrow T = \frac{2\pi}{\omega} = \frac{2\pi}{400\pi} = 5 \times 10^{-3} \text{ s} \approx 5 \text{ ms}$

(g) @ $v = 0$: $0 = 25 \cos(400\pi t + 60^\circ)$ $\pi/6 = 400\pi t$
 $90^\circ = 400\pi t + 60^\circ$ $t = 4.17 \times 10^{-4} \text{ s} \approx 0.417 \text{ ms}$

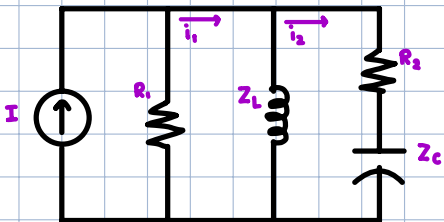
Q7 (a) $y = (30 \angle -160^\circ) + (15 \angle 70^\circ)$
 $= (-28.19 - j10.26) + (5.13 + j14.10)$
 $= -23.06 + j3.84$
 $= 23.38 \angle 170.55^\circ$
 $= 23.38 \cos(200t + 170.55^\circ)$

(c) $y = 50 \cos(5000t - 60^\circ) + 25 \cos(5000t + 20^\circ)$
 $= 50 \cos(5000t - 60^\circ) + 25 \cos(5000t + 20^\circ)$
 $y = (25 - j43.30) + (23.49 + j8.55) - (64.95 - j37.5)$
 $= -16.46 + j2.75$
 $= 16.67 \cos(5000t + 170.51^\circ)$

(b) $y = 90 \cos(50t - 110^\circ) + 60 \cos(50t - 70^\circ)$
 $= (-30.78 - j84.57) + (20.52 - j56.38)$
 $= -10.26 - j140.95$
 $= 141.32 \cos(50t - 94.16^\circ)$

(d) $y = (10 \angle 30^\circ) + (10 \angle -90^\circ) + (10 \angle 150^\circ)$
 $= (5\sqrt{3} + j5) + (0 - j10) + (-5\sqrt{3} + j5)$
 $= 0 + j0$
 $y = 0$

Q8



$I = 125 \sin(2500t + 60^\circ) \text{ A}$
 $= 125 \cos(2500t - 30^\circ) \text{ A}$
 $= 125 \angle -30^\circ \text{ A}$

$R1 = 25 \Omega$

$L = 10 \text{ mH} \approx 0.01 \text{ H}$

$R2 = 30 \Omega$

$C = 10 \mu\text{F} \approx 10 \times 10^{-6} \text{ F}$

$Z_L = j\omega L = j(2500)(0.01)$
 $= j25 \Omega$

$Z_C = \frac{-j}{\omega C} = \frac{-j}{(2500)(10 \times 10^{-6})}$
 $= -j40 \Omega$

(a) $\frac{1}{Z_{eq}} = \frac{1}{R1} + \frac{1}{Z_L} + \frac{1}{R2 + Z_C}$
 $= \frac{1}{25} + \frac{1}{j25} + \frac{1}{30 - j40}$
 $= \frac{1}{25} - \frac{j}{25} + \frac{3 + j4}{10(9 + 16)}$
 $= \frac{1 - j}{25} + \frac{3 + j4}{10(25)} = \frac{13 - j6}{250}$
 $Z_{eq} = \frac{250}{13 - j6} = \frac{250(13 + j6)}{205}$
 $= \frac{650}{41} + j \frac{300}{41} \Omega$
 $= 17.46 \angle 24.78^\circ \Omega$

$i_2 = \frac{V}{R2 + Z_C} = \frac{2182.5 \angle -5.22^\circ}{30 - j40}$
 $= \frac{2182.5 \angle -5.22^\circ}{50 \angle -53.13^\circ} = 43.65 \angle 47.91^\circ$

(b) $V = IZ$
 $= (125 \angle -30^\circ)(17.46 \angle 24.78^\circ)$
 $= 2182.5 \angle -5.22^\circ \text{ V}$

$I = 125 \angle -30^\circ \text{ A}$

$V_{R1} = V = 2182.5 \angle -5.22^\circ \text{ V}$

$I_{R1} = V/R1 = \frac{2182.5 \angle -5.22^\circ}{25 \angle 0^\circ} = 87.3 \angle -5.22^\circ \text{ A}$

$V_{Z_L} = V = 2182.5 \angle -5.22^\circ \text{ V}$

$I_{Z_L} = V/Z_L = \frac{2182.5 \angle -5.22^\circ}{25 \angle 90^\circ} = 87.3 \angle -95.22^\circ \text{ A}$

$V_{R2} = i_2 R2 = (43.65 \angle 47.91^\circ)(30 \angle 0^\circ)$
 $= 1309.5 \angle 47.91^\circ \text{ V}$

$I_{R2} = i_2 = 43.65 \angle 47.91^\circ \text{ A}$

$V_{Z_C} = i_2 Z_C = (43.65 \angle 47.91^\circ)(40 \angle -90^\circ)$
 $= 1746 \angle -42.09^\circ \text{ V}$

$I_{Z_C} = i_2 = 43.65 \angle 47.91^\circ \text{ A}$

Q9

$$Z_L = j\omega L = j(4000)(2.5 \times 10^{-3})$$

$$= j10 \Omega$$

$$Z_C = \frac{-j}{\omega C} = \frac{-j}{(4000)(12.5 \times 10^{-6})} = j20 \Omega$$

$$(c) \bullet 20 \Omega // 12.5 \mu F : \frac{1}{\frac{1}{20} + \frac{1}{j20}} = \frac{1}{\frac{1+j}{j20}} = \frac{j20}{1+j} = 10 + j10$$

$$\bullet 10 \Omega + (20 \Omega // 12.5 \mu F) : 10 + (10 + j10) = 20 + j10$$

$$\bullet 2.5 \text{ mH} // [10 \Omega + (20 \Omega // 12.5 \mu F)] : \frac{1}{\frac{1}{j10} + \frac{1}{20+j10}} = \frac{1}{\frac{3+j}{j25}} = 2.5 + j7.5$$

$$\bullet 5 \Omega + 2.5 \text{ mH} // [10 \Omega + (20 \Omega // 12.5 \mu F)] \quad Z_{eq} = 5 + (2.5 + j7.5) = 7.5 + j7.5$$

$$= 10.61 \angle 45^\circ$$

$$(d) \quad V = 12 \quad v_s = 25 \cos(4000t - 90^\circ) \text{ V} = 25 \angle -90^\circ \text{ V}$$

$$I = \frac{V}{Z} = \frac{25 \angle -90^\circ}{10.61 \angle 45^\circ} = 2.36 \angle -135^\circ$$

$$\text{NODE B: } \frac{V_B - V_A}{5} + \frac{V_B}{j10} + \frac{V_B - V_C}{10} = 0$$

$$V_B \left(\frac{1}{5} + \frac{1}{j10} + \frac{1}{10} \right) = \frac{-j25}{5} + \frac{V_C}{10}$$

$$V_B \left(\frac{3}{10} - j\frac{1}{10} \right) = -j5 + V_C/10$$

$$\text{NODE C: } \frac{V_C - V_B}{10} + \frac{V_C}{20} + \frac{V_C}{j20} = 0$$

$$V_C \left(\frac{1}{10} + \frac{1}{20} + \frac{1}{j20} \right) = \frac{V_B}{10}$$

$$V_C \left(\frac{3}{20} - j\frac{1}{20} \right) = V_B/10$$

$$V_C \left(\frac{3}{2} - j\frac{1}{2} \right) = V_B$$

$$V_B \left(\frac{3}{10} - j\frac{1}{10} \right) = -j5 + V_C/10$$

$$V_C \left(\frac{3}{2} - j\frac{1}{2} \right) \left(\frac{3}{10} - j\frac{1}{10} \right) = -j5 + V_C/10$$

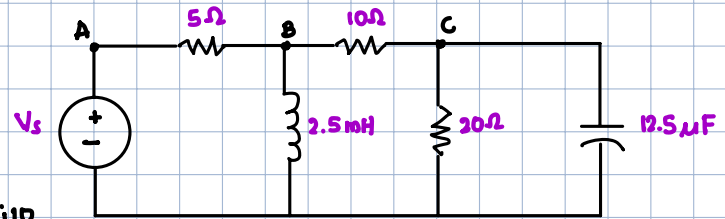
$$V_C \left(\frac{2}{5} - j\frac{3}{10} \right) - V_C/10 = -j5$$

$$V_C = 25/3 - j25/3 = 11.79 \angle -45^\circ$$

$$V_B = V_C \left(\frac{3}{2} - j\frac{1}{2} \right)$$

$$= \left(\frac{25}{3} - j\frac{25}{3} \right) \left(\frac{3}{2} - j\frac{1}{2} \right)$$

$$= \frac{25}{3} - j\frac{50}{3} = 18.63 \angle -63.43^\circ$$



$$V_{5\Omega} = V_B - V_A = \left(\frac{25}{3} - j\frac{50}{3} \right) - (-j25)$$

$$= \frac{25}{3} + j\frac{25}{3} = 11.79 \angle 45^\circ \text{ V}$$

$$I_{5\Omega} = \frac{V_B - V_A}{5} = \frac{\frac{25}{3} + j\frac{25}{3}}{5} = \frac{5}{3} + j\frac{5}{3}$$

$$= 2.36 \angle 45^\circ \text{ A}$$

$$V_{2L} = V_B = 18.63 \angle -63.43^\circ \text{ V}$$

$$I_{2L} = \frac{V_B}{Z_L} = \frac{18.63 \angle -63.43^\circ}{10 \angle 90^\circ} = 1.86 \angle -153.43^\circ \text{ A}$$

$$V_{10\Omega} = V_B - V_C = \left(\frac{25}{3} - j\frac{50}{3} \right) - \left(\frac{25}{3} - j\frac{25}{3} \right)$$

$$= -j\frac{25}{3} = 8.33 \angle -90^\circ \text{ V}$$

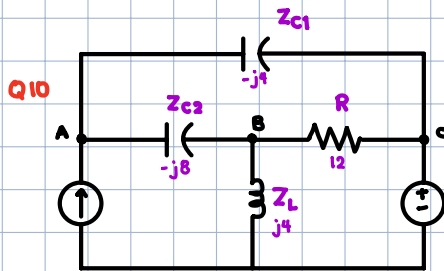
$$I_{10\Omega} = \frac{V_B - V_C}{10} = \frac{8.33 \angle -90^\circ}{10 \angle 0^\circ} = 0.83 \angle -90^\circ \text{ A}$$

$$V_{20\Omega} = V_C = 11.79 \angle -45^\circ \text{ V}$$

$$I_{20\Omega} = \frac{V_C}{20} = \frac{11.79 \angle -45^\circ}{20 \angle 0^\circ} = 0.59 \angle -45^\circ \text{ A}$$

$$V_{2C} = V_C = 11.79 \angle -45^\circ \text{ V}$$

$$I_{2C} = \frac{V_C}{Z_C} = \frac{11.79 \angle -45^\circ}{20 \angle 90^\circ} = 0.59 \angle -135^\circ \text{ A}$$



$$Z_{c1} = \frac{-j}{\omega C} = \frac{-j}{(2500)(100 \times 10^{-6})} = -j4$$

$$Z_{c2} = \frac{-j}{\omega C} = \frac{-j}{(2500)(50 \times 10^{-6})} = -j8$$

$$Z_L = j\omega L = j(2500)(1.6 \times 10^{-3}) = j4$$

NODE A: $\frac{V_A - V_C}{Z_{c1}} + \frac{V_A - V_B}{Z_{c2}} = 5 \angle 0^\circ$

$$V_A \left(\frac{1}{-j4} + \frac{1}{-j8} \right) = 5 + \frac{V_C}{-j4} + \frac{V_B}{-j8}$$

$$V_A \left(-\frac{3}{j8} \right) = 5 + \frac{j20}{-j4} + \frac{V_B}{-j8}$$

$$V_A \left(-\frac{3}{j8} \right) = 5 - 5 + \frac{V_B}{-j8}$$

$$V_A = V_B / 3 \rightarrow V_A = \frac{-8 + j4}{3} = -\frac{8}{3} + j\frac{4}{3}$$

$$\approx 2.98 \angle 153.43^\circ$$

NODE B: $\frac{V_B - V_A}{Z_{c2}} + \frac{V_B - V_C}{R} + \frac{V_B}{Z_L} = 0$

$$V_B \left(\frac{1}{-j8} + \frac{1}{12} + \frac{1}{j4} \right) - \frac{V_A}{-j8} = \frac{j20}{12}$$

$$V_B \left(\frac{1}{-j8} + \frac{1}{12} + \frac{1}{j4} \right) - \frac{V_B}{-j24} = \frac{j20}{12}$$

$$V_B \left(\frac{1}{12} - j\frac{1}{6} \right) = \frac{j20}{12}$$

$$V_B = -8 + j4 \approx 8.94 \angle 153.43^\circ$$

VOLTAGE ACROSS i_g : $V_A = 2.98 \angle 153.43^\circ \text{ V}$

$$V_{c1} = V_A - V_C = \left(-\frac{8}{3} + j\frac{4}{3} \right) - j20 = -\frac{8}{3} - j\frac{56}{3}$$

$$= 18.86 \angle -98.13^\circ \text{ V}$$

$$I_{c1} = \frac{V_A - V_C}{Z_{c1}} = \frac{-\frac{8}{3} - j\frac{56}{3}}{-j4} = \frac{14}{3} - j\frac{2}{3}$$

$$= 4.71 \angle -8.13^\circ \text{ A}$$

$$V_{c2} = V_A - V_B = \left(-\frac{8}{3} + j\frac{4}{3} \right) - (-8 + j4) = \frac{16}{3} - j\frac{8}{3}$$

$$= 5.96 \angle 153.43^\circ \text{ V}$$

$$I_{c2} = \frac{V_A - V_B}{Z_{c2}} = \frac{\frac{16}{3} - j\frac{8}{3}}{-j8} = \frac{1}{3} + j\frac{2}{3}$$

$$= 0.75 \angle 63.43^\circ \text{ A}$$

$$V_R = V_B - V_C = (-8 + j4) - j20 = -8 - j16$$

$$= 17.89 \angle -116.57^\circ \text{ V}$$

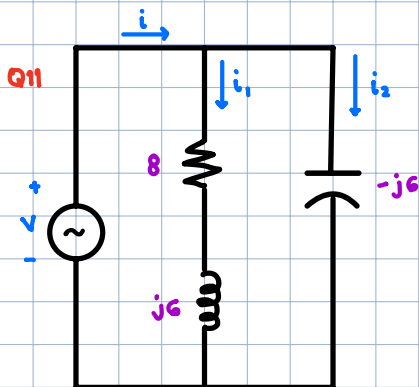
$$I_R = \frac{V_B - V_C}{R} = \frac{-8 - j16}{12} = -\frac{2}{3} - j\frac{4}{3}$$

$$= 1.49 \angle -116.57^\circ \text{ A}$$

$$V_L = V_B = 8.94 \angle 153.43^\circ \text{ V}$$

$$I_L = \frac{V_B}{Z_L} = \frac{-8 + j4}{-j4} = -1 - j2$$

$$= 2.24 \angle -116.57^\circ \text{ A}$$



$$I = 10 \angle 0^\circ \text{ A}$$

$$= 10$$

$$I_1 = I \left(\frac{-j6}{8 + j6 - j6} \right)$$

$$= 10 \left(\frac{-j6}{8} \right)$$

$$= -j7.5$$

$$\approx 7.5 \angle -90^\circ \text{ A}$$

$$I_2 = I \left(\frac{8 + j6}{8 + j6 - j6} \right)$$

$$= 10 \left(\frac{8 + j6}{8} \right)$$

$$= 10 + j7.5$$

$$\approx 12.5 \angle 36.87^\circ \text{ A}$$

$$V = I_2 Z_c$$

$$= (10 + j7.5)(-j6)$$

$$= 45 - j60$$

$$\approx 75 \angle -53.13^\circ \text{ V}$$