

CS 245: Database System Principles

Notes 6: Query Processing

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Query Processing

$Q \rightarrow \text{Query Plan}$

Query Processing

$Q \rightarrow \text{Query Plan}$

Focus: Relational System

- Others?

Example

Select B,D

From R,S

Where R.A = "c" \wedge S.E = 2 \wedge R.C=S.C

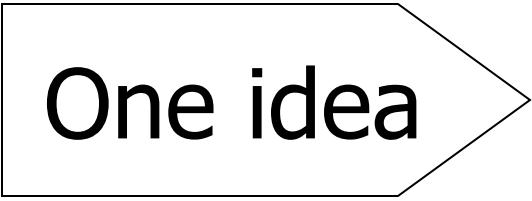
R	A	B	C	S	C	D	E
a	1	10		10	x	2	
b	1	20		20	y	2	
c	2	10		30	z	2	
d	2	35		40	x	1	
e	3	45		50	y	3	

R	A	B	C	S	C	D	E
a	1	10		10	x	2	
b	1	20		20	y	2	
c	2	10		30	z	2	
d	2	35		40	x	1	
e	3	45		50	y	3	

Answer

B	D
2	x

- How do we execute query?



One idea

- Do Cartesian product
- Select tuples
- Do projection

RXS

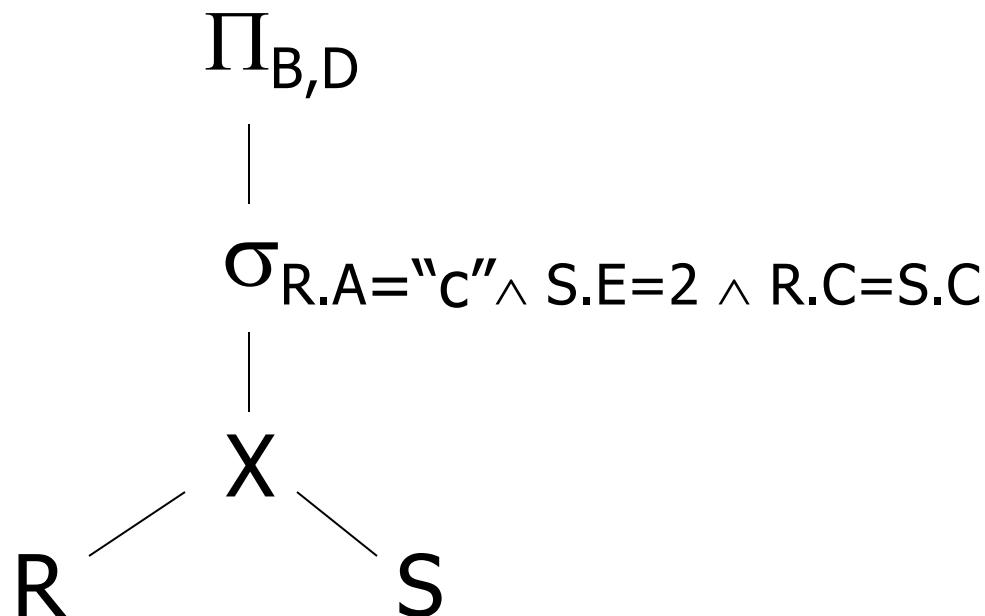
	R.A	R.B	R.C	S.C	S.D	S.E
a	1	10	10	x	2	
a	1	10	20	y	2	
.						
.						
C	2	10	10	x	2	
.						
.						

RXS

	R.A	R.B	R.C	S.C	S.D	S.E
a	1	10	10	x	2	
a	1	10	20	y	2	
.						
.						
Bingo!	C	2	10	10	x	2
Got one...		

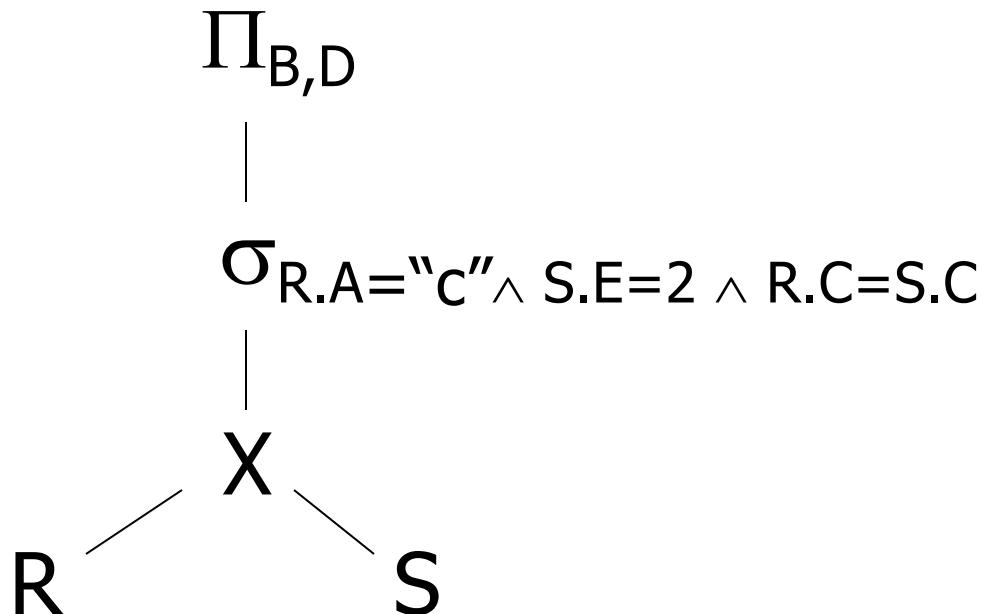
Relational Algebra - can be used to
describe plans...

Ex: Plan I



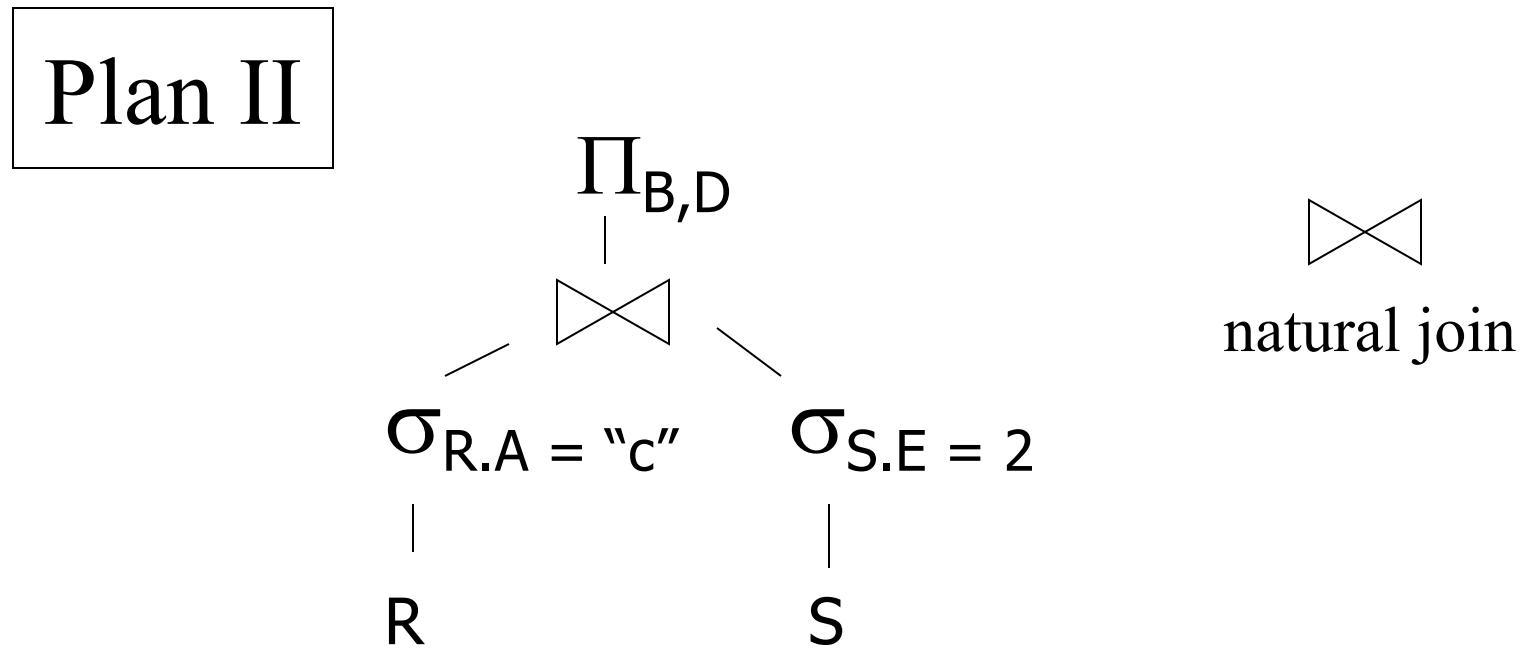
Relational Algebra - can be used to
describe plans...

Ex: Plan I



OR: $\Pi_{B,D} [\sigma_{R.A='c' \wedge S.E=2 \wedge R.C = S.C} (R \times S)]$

Another idea:



R

A	B	C
a	1	10
b	1	20
c	2	10
d	2	35
e	3	45

$\sigma(R)$

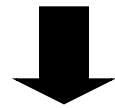
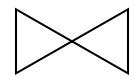
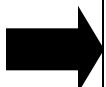
A	B	C
c	2	10

$\sigma(S)$

C	D	E
10	x	2
20	y	2
30	z	2

S

C	D	E
10	x	2
20	y	2
30	z	2
40	x	1
50	y	3



Plan III

Use R.A and S.C Indexes

- (1) Use R.A index to select R tuples
with R.A = "c"
- (2) For each R.C value found, use S.C
index to find matching tuples

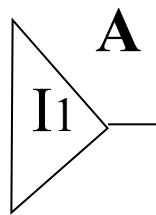
Plan III

Use R.A and S.C Indexes

- (1) Use R.A index to select R tuples
with R.A = "c"
- (2) For each R.C value found, use S.C
index to find matching tuples
- (3) Eliminate S tuples S.E \neq 2
- (4) Join matching R,S tuples, project
B,D attributes and place in result

R

A	B	C
a	1	10
b	1	20
c	2	10
d	2	35
e	3	45



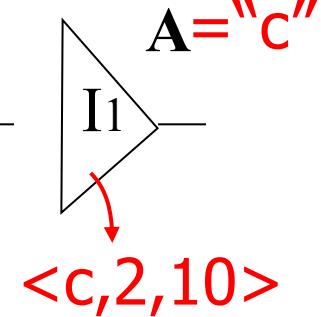
S

C	D	E
10	x	2
20	y	2
30	z	2
40	x	1
50	y	3

R

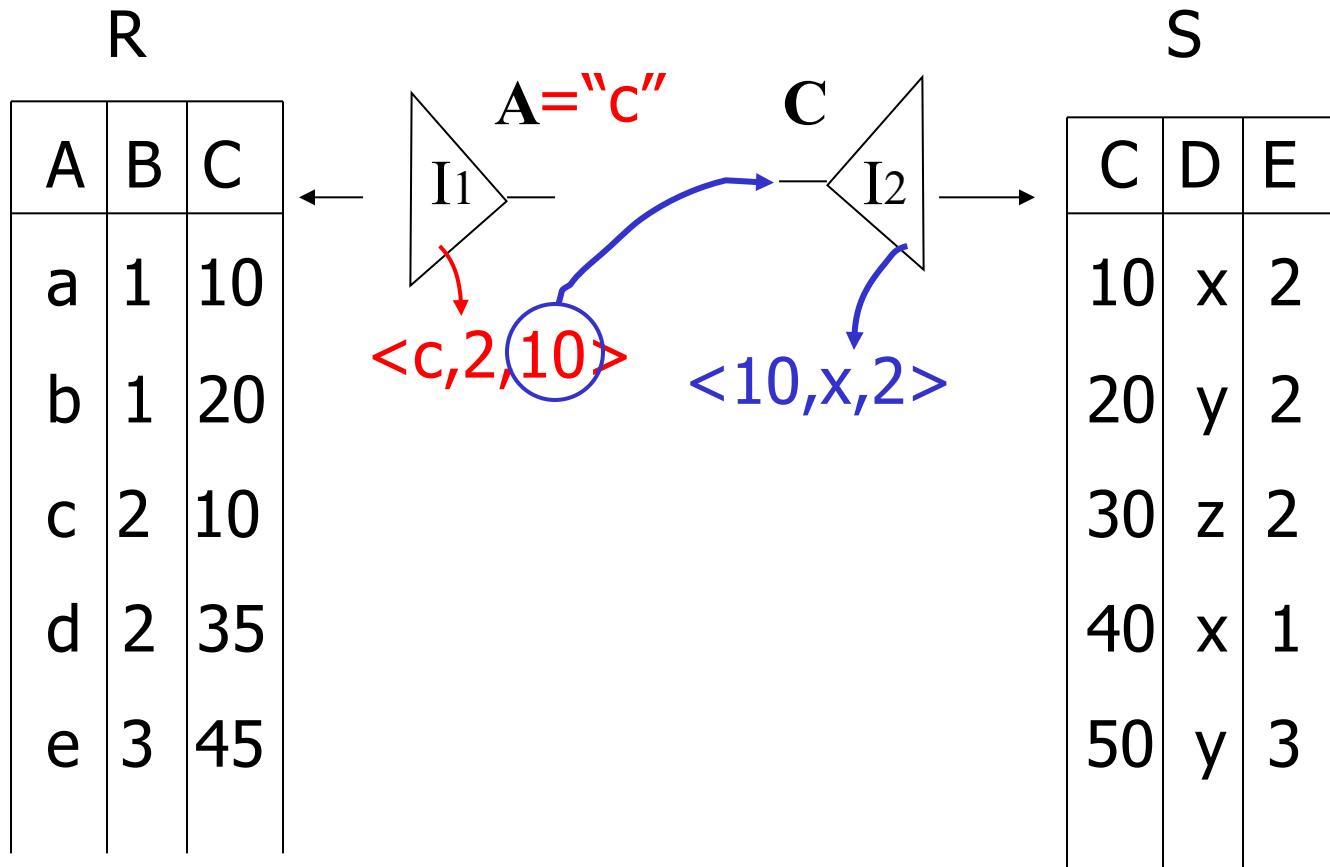
A	B	C
a	1	10
b	1	20
c	2	10
d	2	35
e	3	45

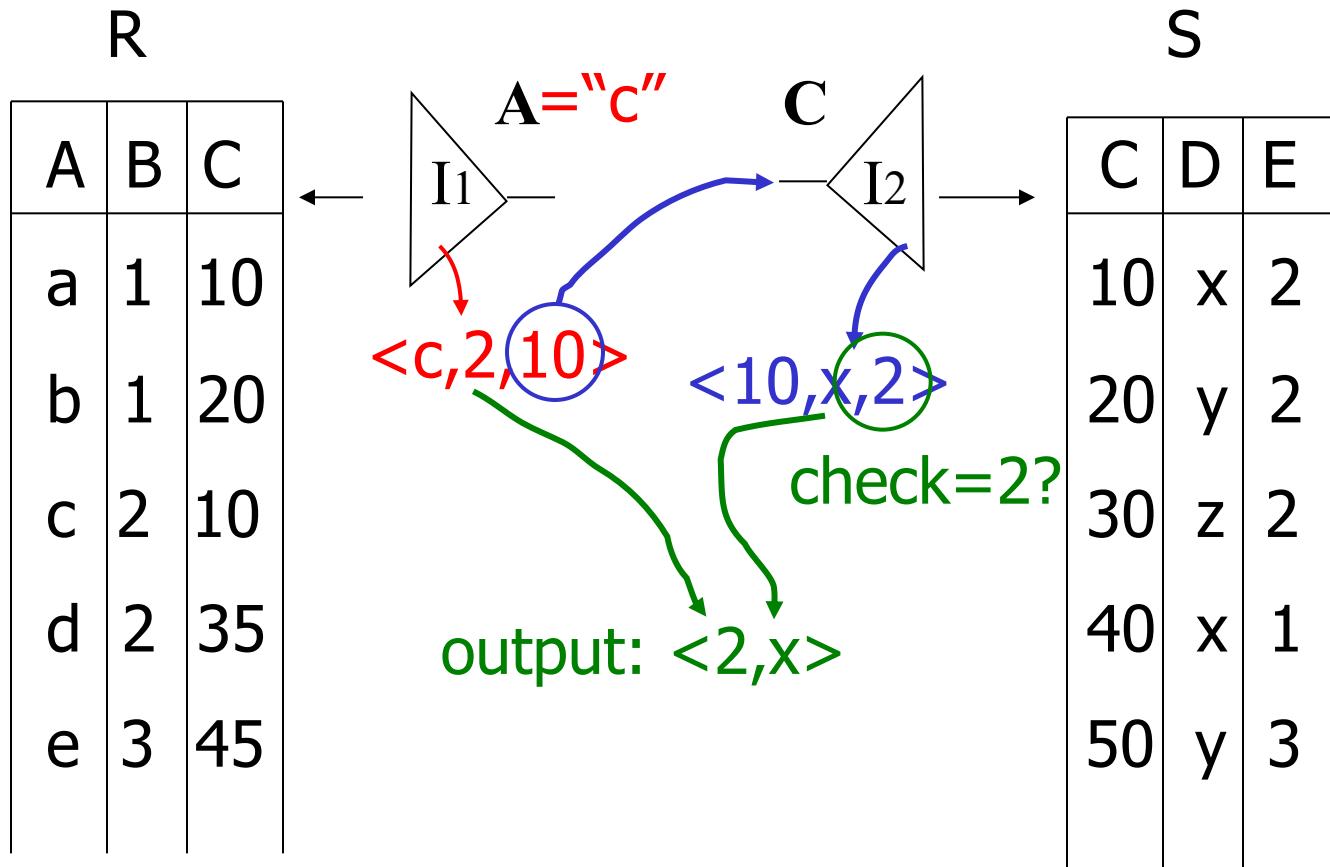
A="C"

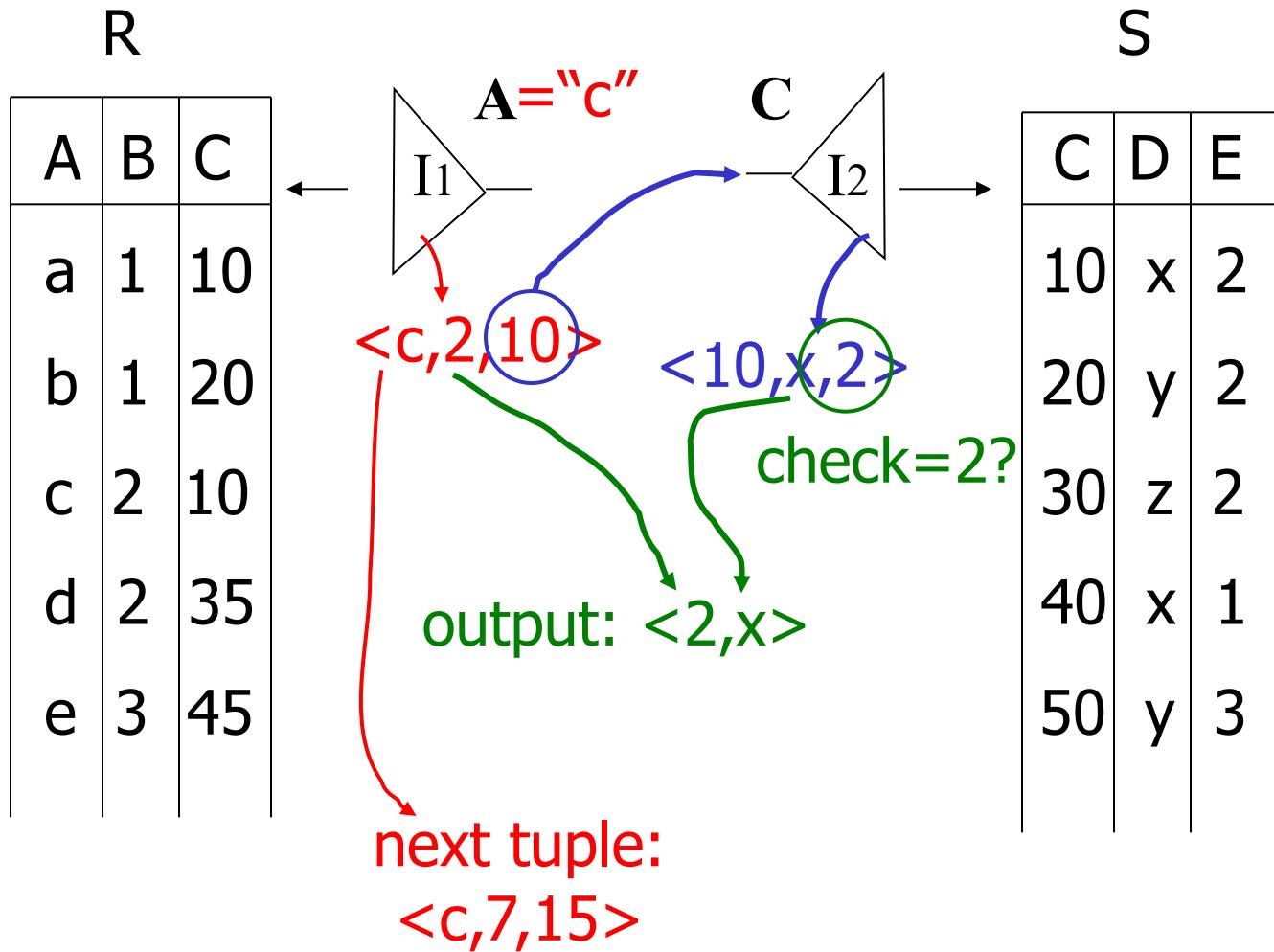


S

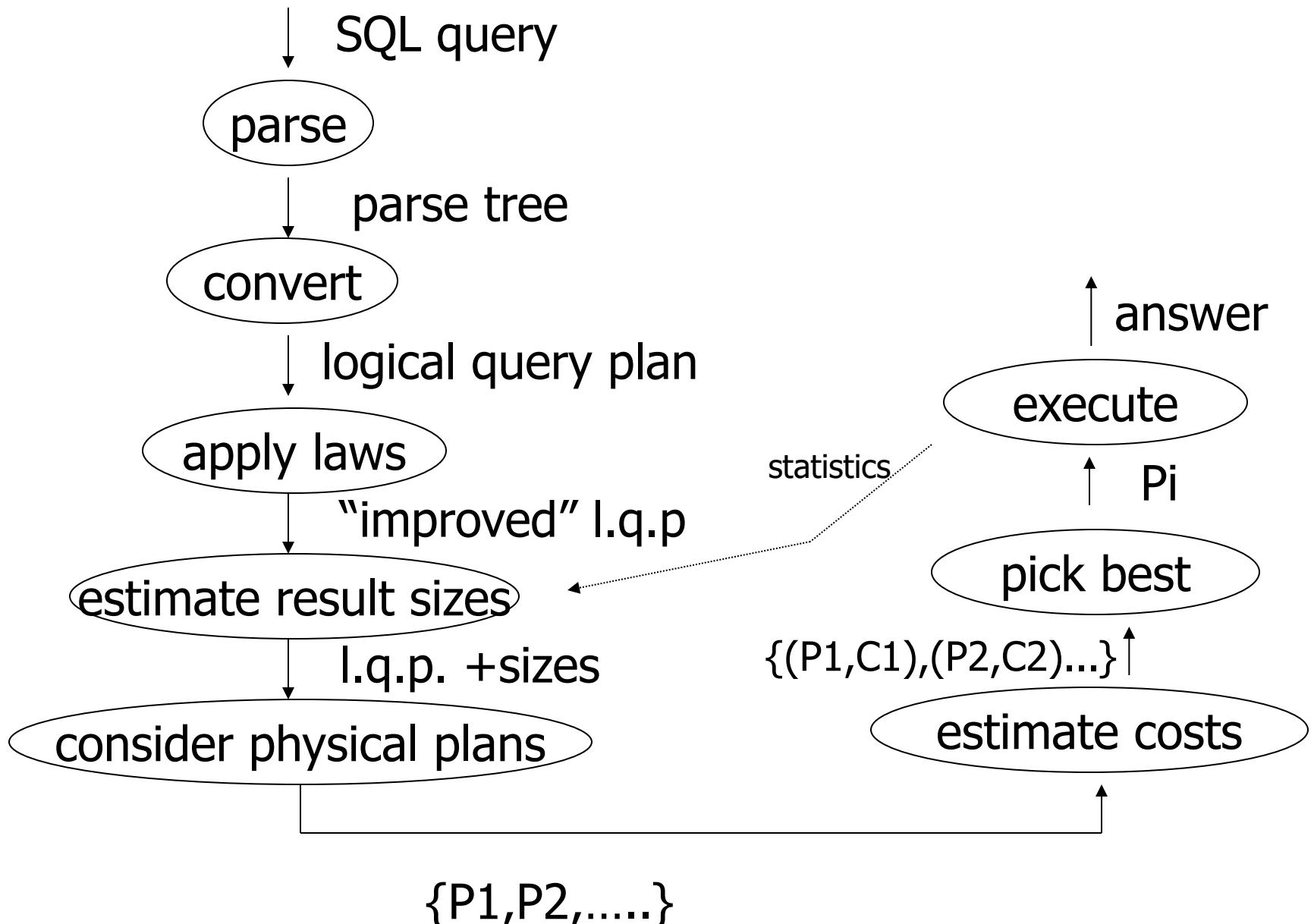
C	D	E
10	x	2
20	y	2
30	z	2
40	x	1
50	y	3







Overview of Query Optimization

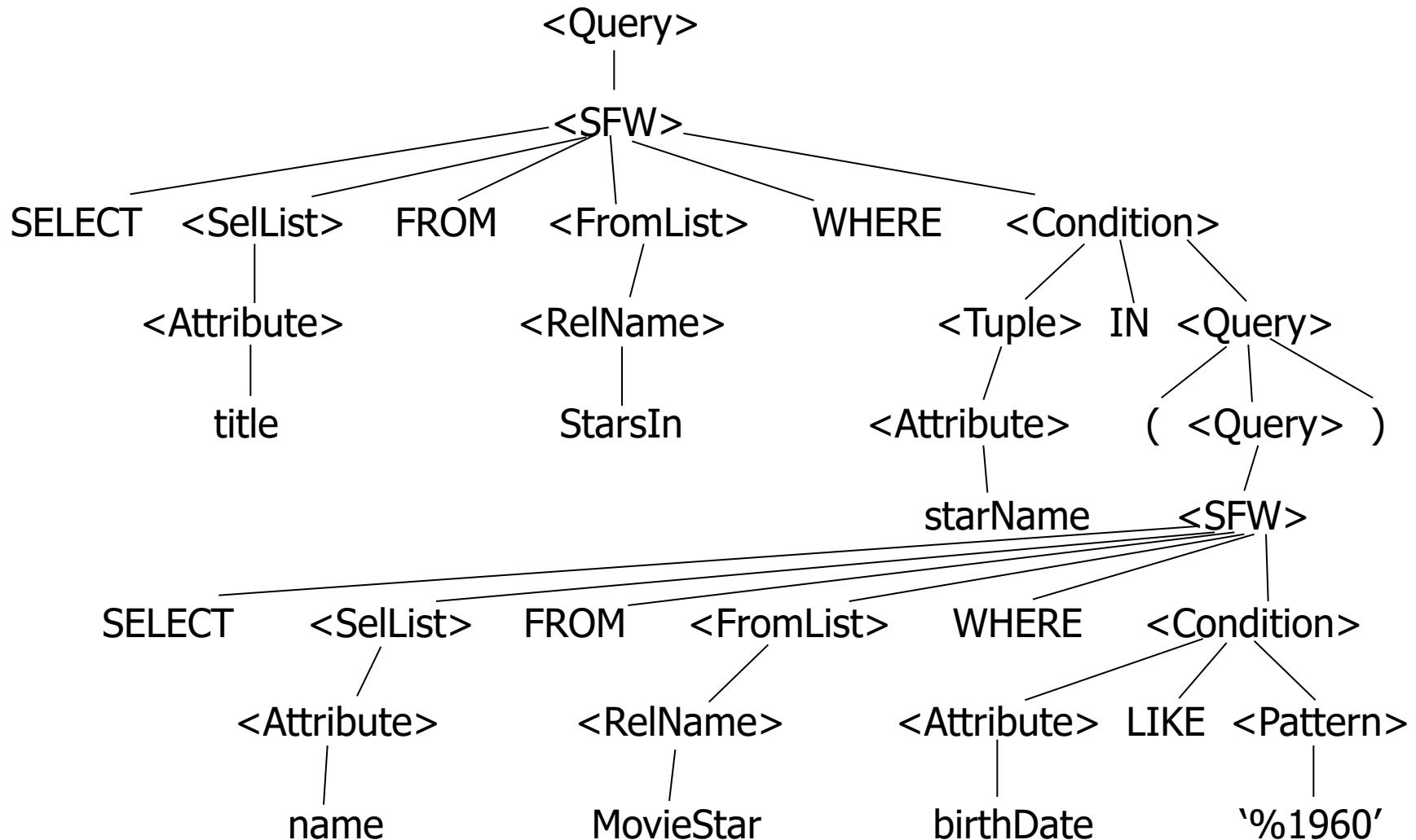


Example: SQL query

```
SELECT title  
FROM StarsIn  
WHERE starName IN (  
    SELECT name  
    FROM MovieStar  
    WHERE birthdate LIKE '%1960'  
);
```

(Find the movies with stars born in 1960)

Example: Parse Tree



Example: Generating Relational Algebra

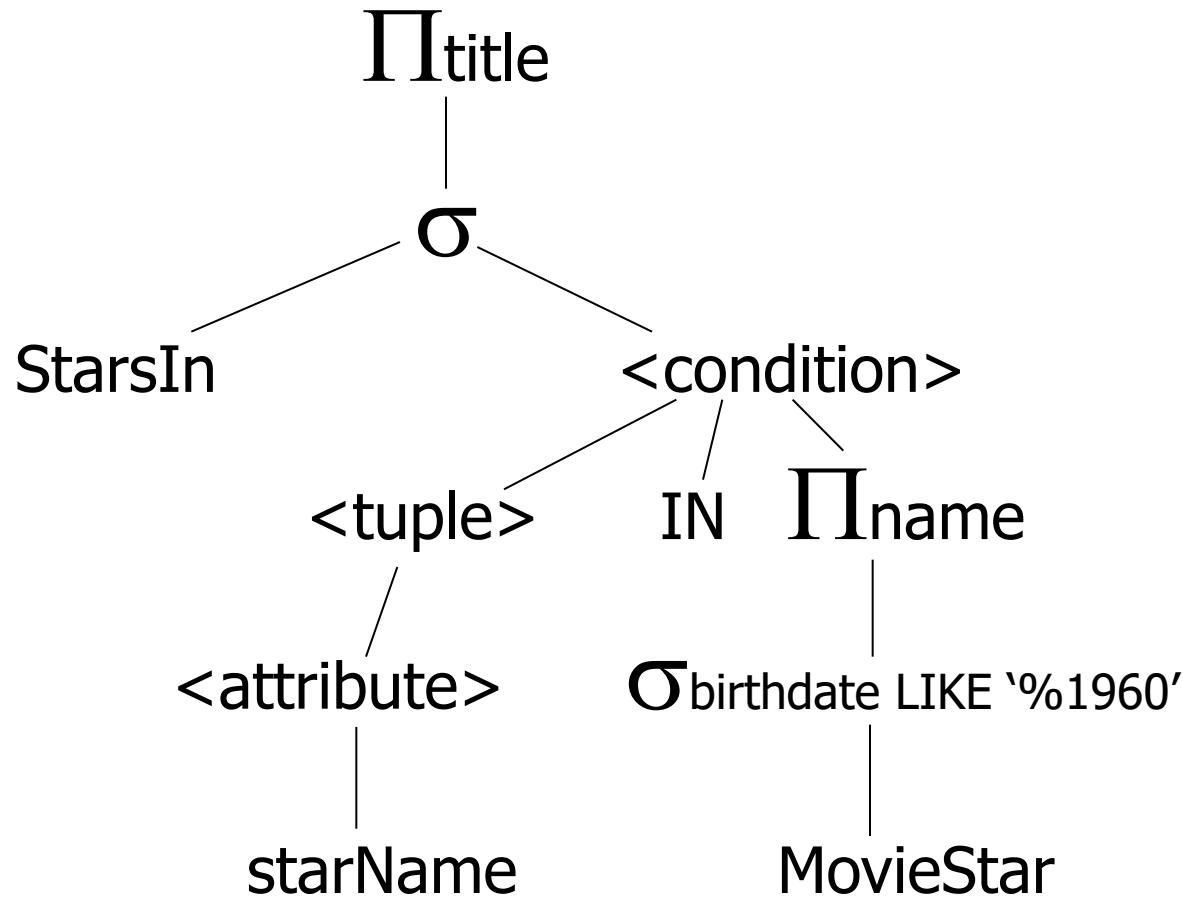


Fig. 7.15: An expression using a two-argument σ , midway between a parse tree and relational algebra

Example: Logical Query Plan

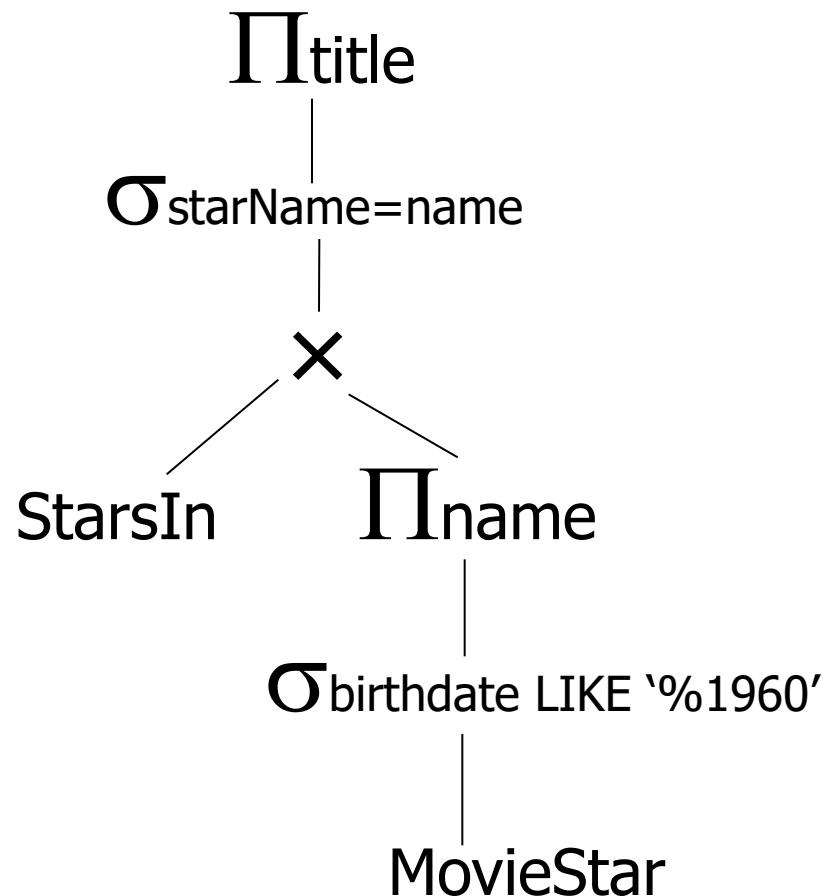
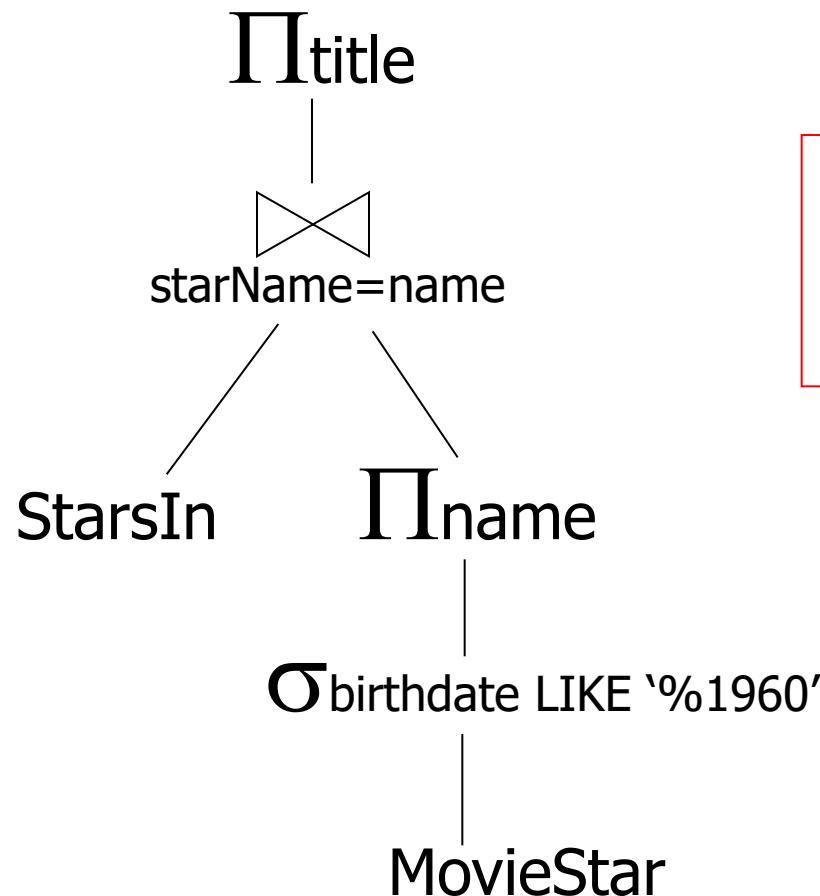


Fig. 7.18: Applying the rule for IN conditions

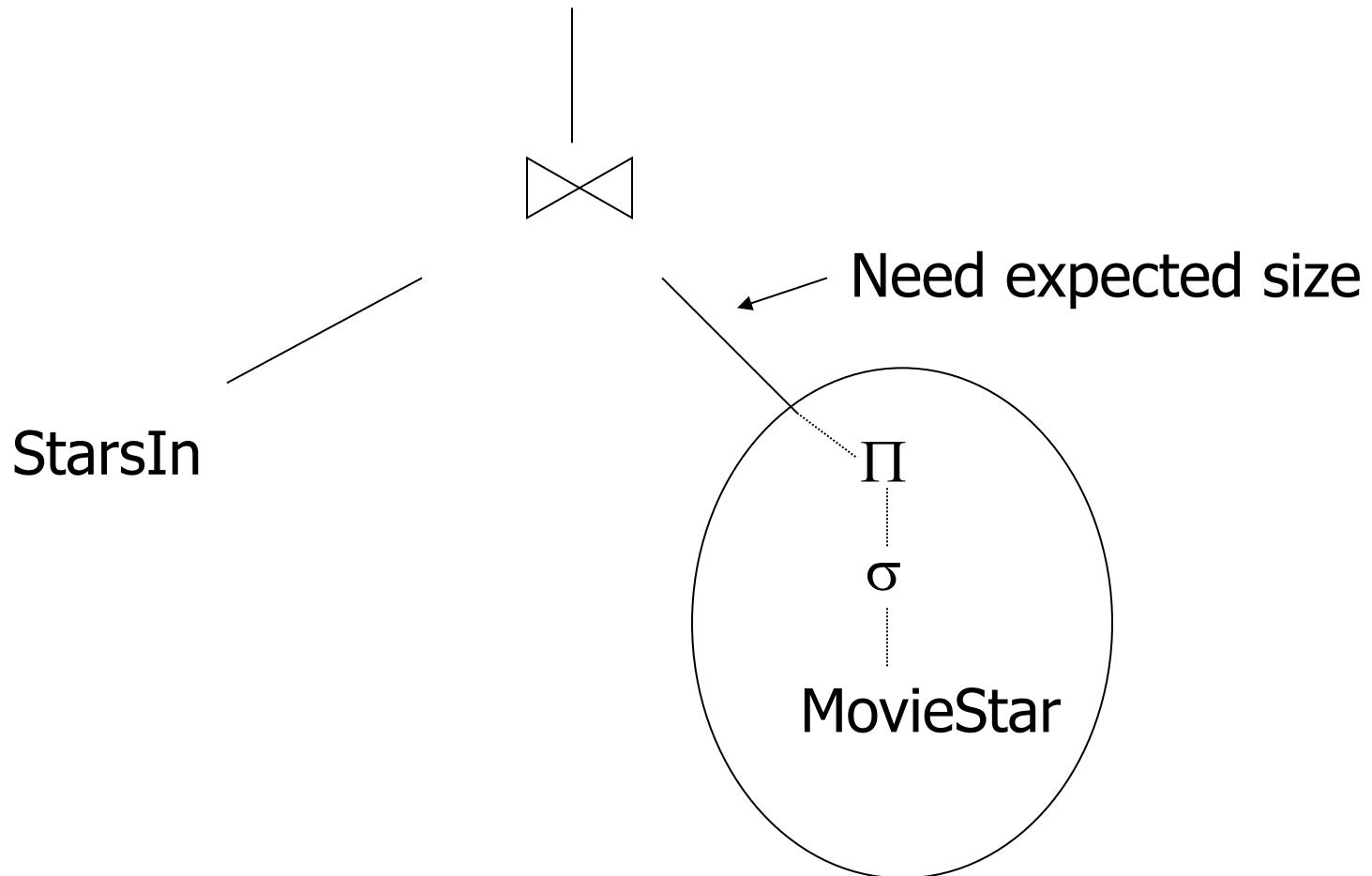
Example: Improved Logical Query Plan



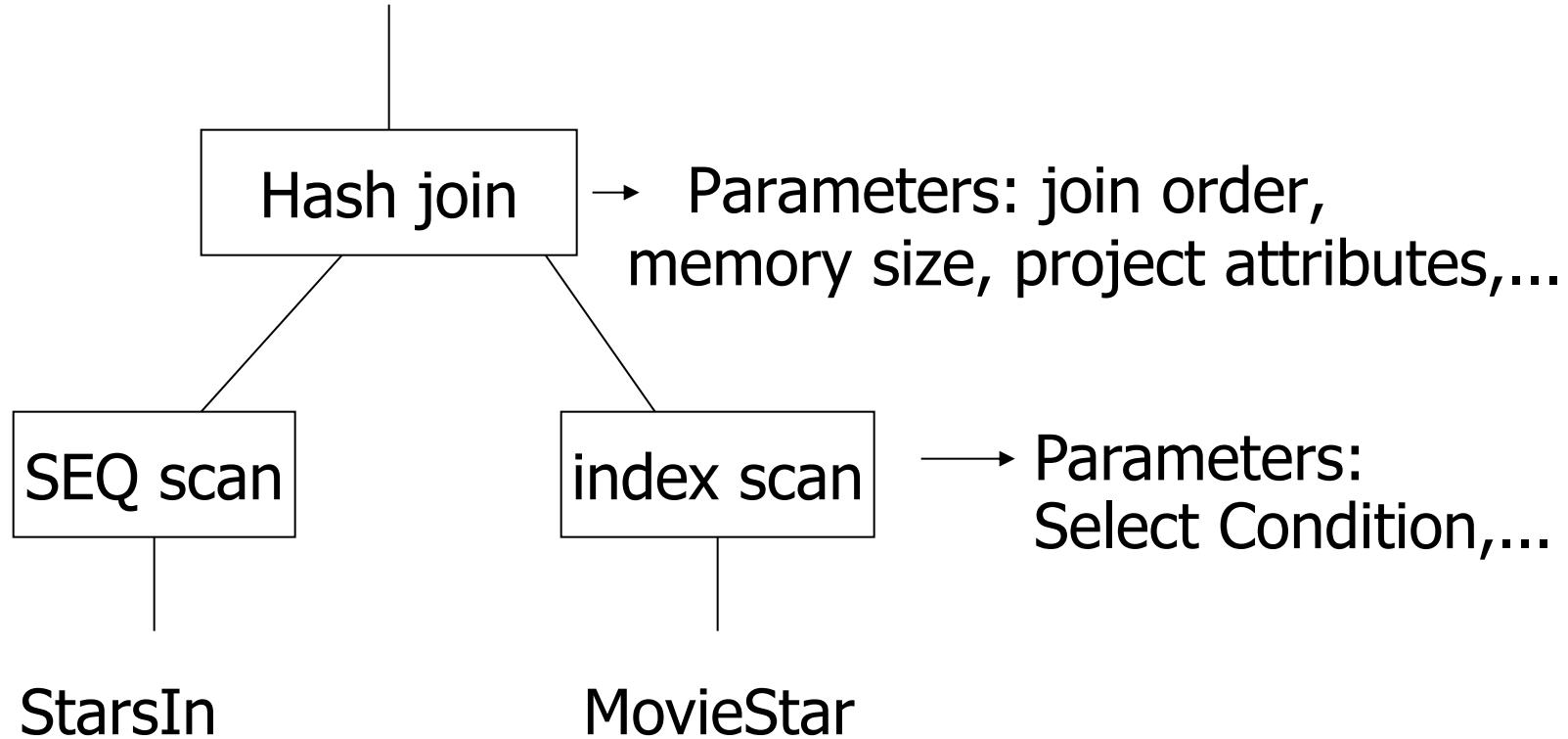
Question:
Push project to
StarsIn?

Fig. 7.20: An improvement on fig. 7.18.

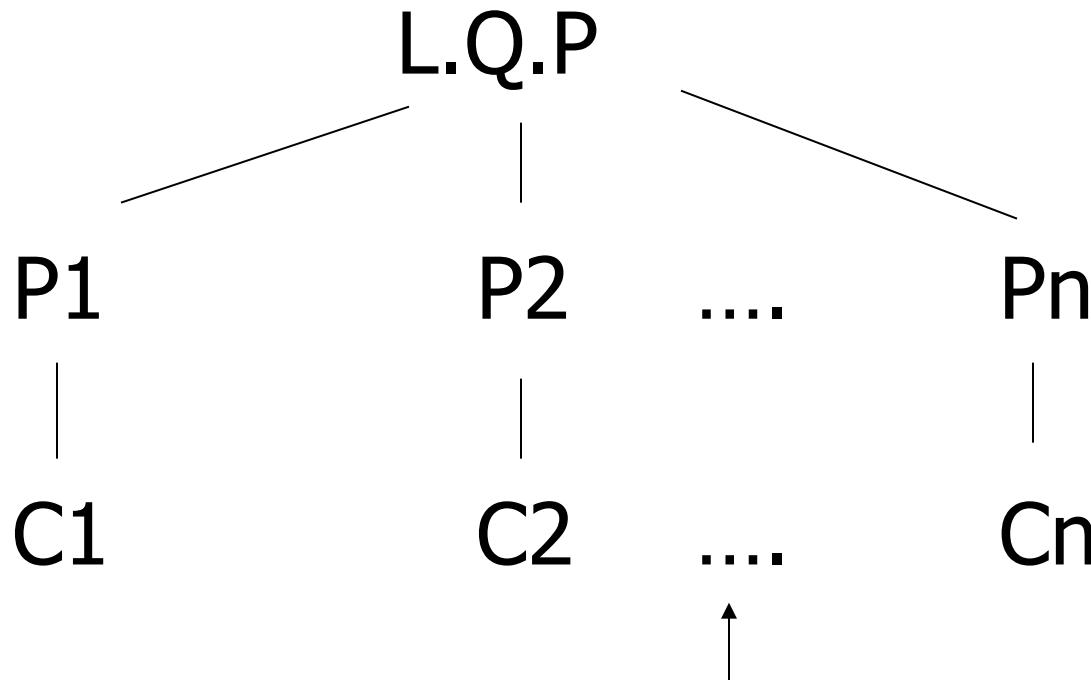
Example: Estimate Result Sizes



Example: One Physical Plan



Example: Estimate costs



Pick best!

Textbook outline

Chapter 15

5	Algebra for queries	[bags vs sets]
[Ch 5]	- Select, project, join,	[project list a,a+b->x,...]
	- Duplicate elimination, grouping, sorting	

15.1 Physical operators

[15.1]	- Scan, sort, ...
--------	-------------------

15.2 - 15.6 Implementing operators + [15.2-15.6] estimating their cost

Chapter 16

16.1[16.1]

Parsing

16.2[16.2]

Algebraic laws

16.3[16.3]

Parse tree -> logical query
plan

16.4[16.4]

Estimating result sizes

16.5-7[16.5-7]

Cost based optimization

Reading textbook - Chapters 15, 16

Optional:

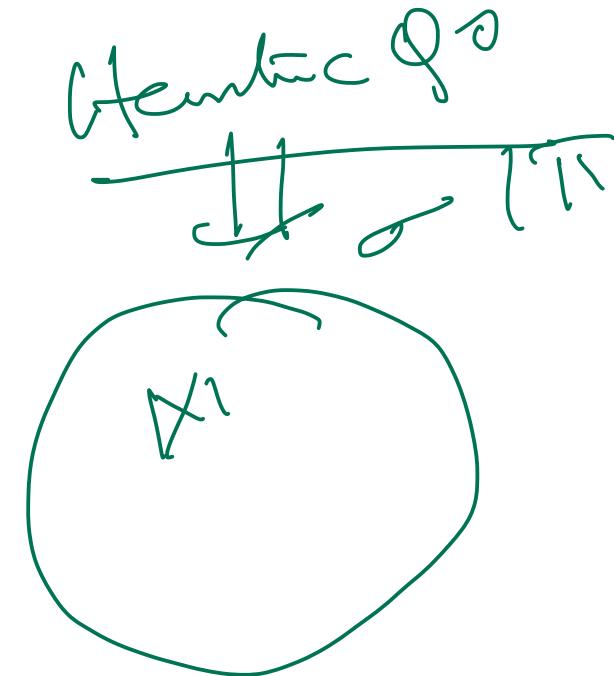
- Sections 15.7, 15.8, 15.9 [15.7, 15.8]
- Sections 16.6, 16.7 [16.6, 16.7]

Optional: Duplicate elimination operator
grouping, aggregation operators

Query Optimization - In class order

- Relational algebra level
- Detailed query plan level

Naive

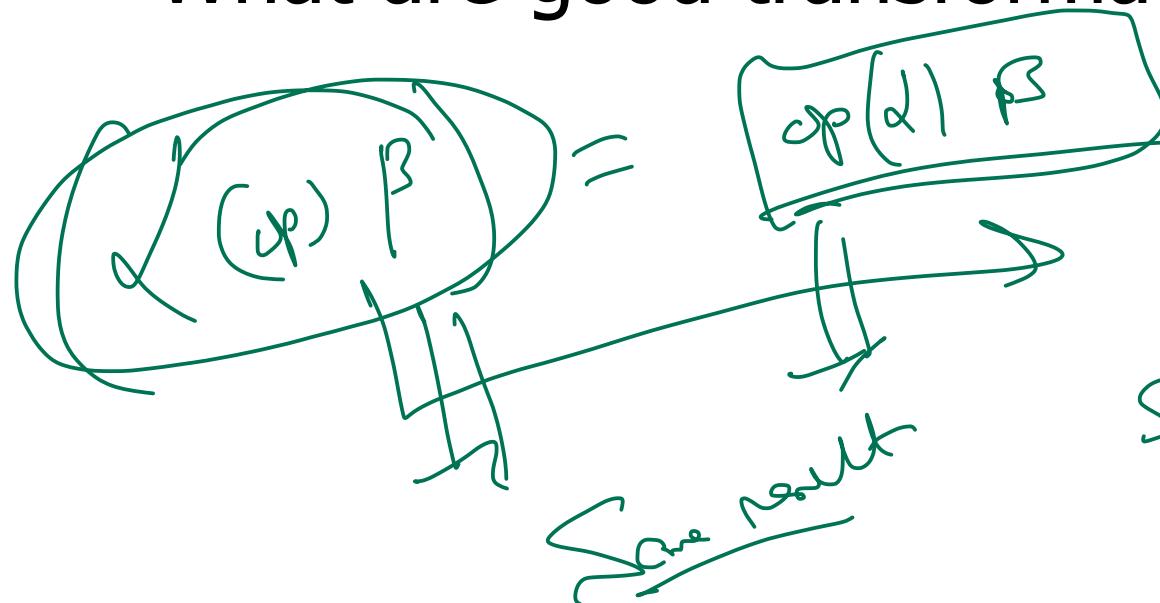


Query Optimization - In class order

- Relational algebra level
- Detailed query plan level
 - Estimate Costs
 - without indexes
 - with indexes
 - Generate and compare plans

Relational algebra optimization

- Transformation rules
(preserve equivalence)
- What are good transformations?



Rules: Natural joins & cross products & union

$$\begin{array}{c} R \bowtie S = S \bowtie R \\ (R \bowtie S) \bowtie T = R \bowtie (S \bowtie T) \end{array}$$

Diagram illustrating the commutativity and associativity of the natural join (\bowtie) operator. The first equation shows that the order of the two tables being joined does not matter. The second equation shows that the natural join is associative, allowing the grouping of multiple tables.

Handwritten notes:

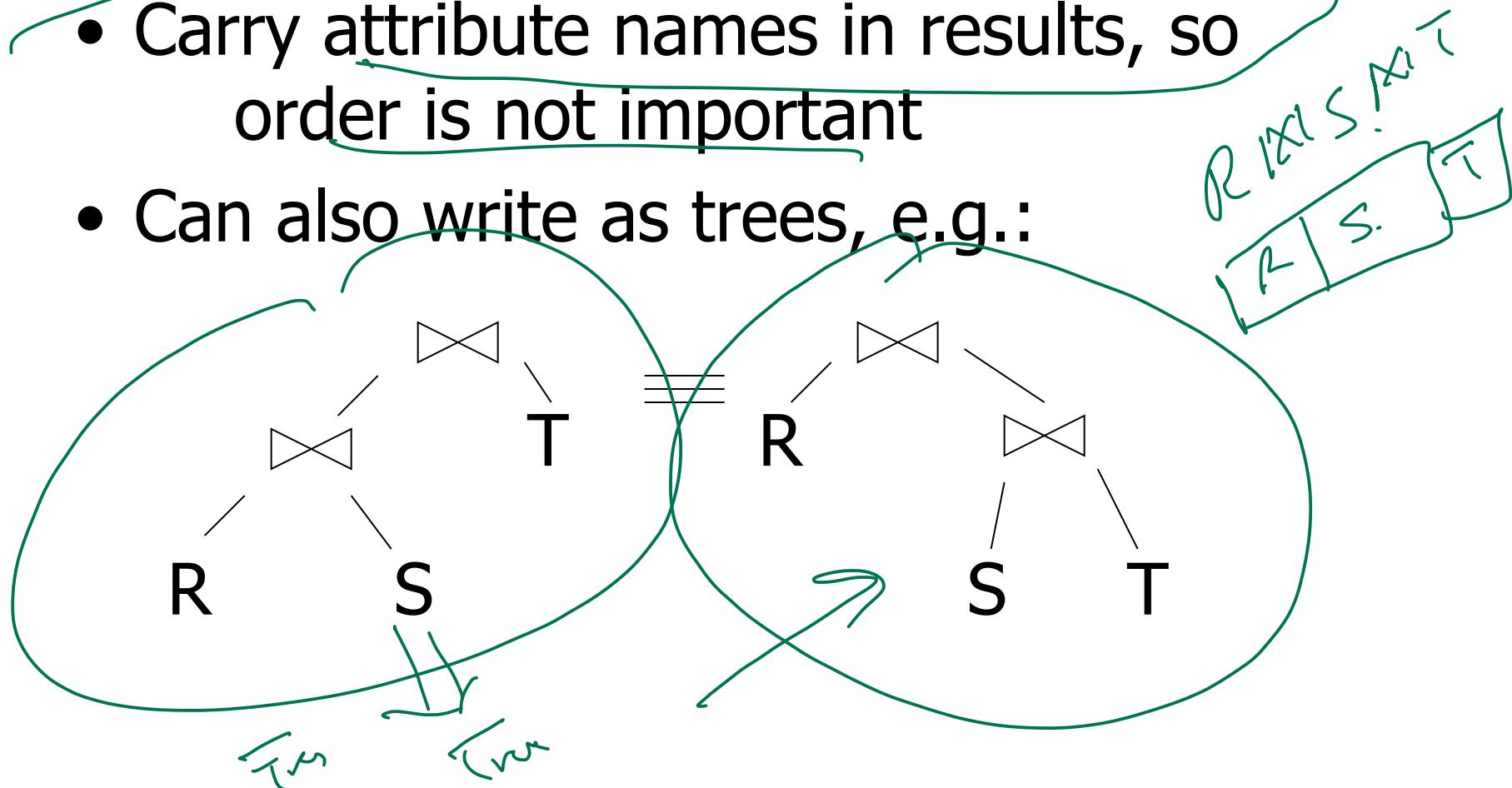
- Left side: $R \bowtie S$ is shown with a green oval around $(R \bowtie S)$ and $\bowtie T$. A green arrow points from $R \bowtie S$ to $(R \bowtie S) \bowtie T$, labeled "rc".
- Right side: $S \bowtie R$ is shown with a green oval around $R \bowtie (S \bowtie T)$. A green arrow points from $S \bowtie R$ to $R \bowtie (S \bowtie T)$.
- Bottom left: A tree diagram for $R \bowtie S$ with root R . It branches into R_A and R_B , which further branch into R_{A1}, R_{A2}, R_{A3} and R_{B1}, R_{B2} respectively. R_{A1} and R_{B1} both point to leaf node R_{AB} .
- Bottom right: A tree diagram for $S \bowtie R$ with root S . It branches into S_A and S_B , which further branch into S_{A1}, S_{A2}, S_{A3} and S_{B1}, S_{B2} respectively. S_{A1} and S_{B1} both point to leaf node S_{AB} .
- Bottom center: A tree diagram for $(R \bowtie S) \bowtie T$ with root $(R \bowtie S)$. It branches into $(R \bowtie S)_A$ and $(R \bowtie S)_B$, which further branch into $(R \bowtie S)_{A1}, (R \bowtie S)_{A2}, (R \bowtie S)_{A3}$ and $(R \bowtie S)_{B1}, (R \bowtie S)_{B2}$ respectively. $(R \bowtie S)_{A1}$ and $(R \bowtie S)_{B1}$ both point to leaf node $(R \bowtie S)_{AB}$.
- Bottom right: A tree diagram for $R \bowtie (S \bowtie T)$ with root R . It branches into R_A and R_B , which further branch into R_{A1}, R_{A2}, R_{A3} . R_{A1} and R_{B1} both point to leaf node $R_{(S \bowtie T)}$.

Commutative rule:

$$R \bowtie S = S \bowtie R$$

Note:

- Carry attribute names in results, so order is not important
- Can also write as trees, e.g.:



Rules: Natural joins & cross products & union

$$R \bowtie S = S \bowtie R$$

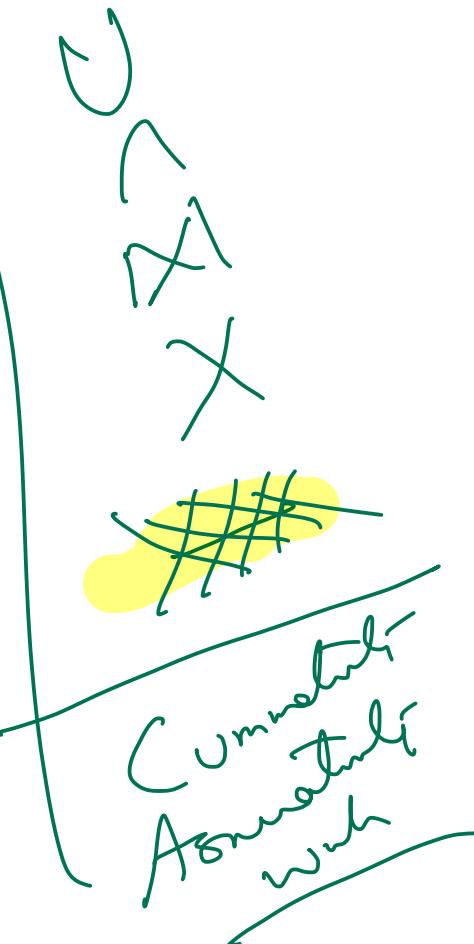
$$\underline{(R \bowtie S)} \bowtie T = R \bowtie \underline{(S \bowtie T)}$$

$$R \times S = S \times R$$

$$(R \times S) \times T = R \times (S \times T)$$

$$R \cup S = S \cup R$$

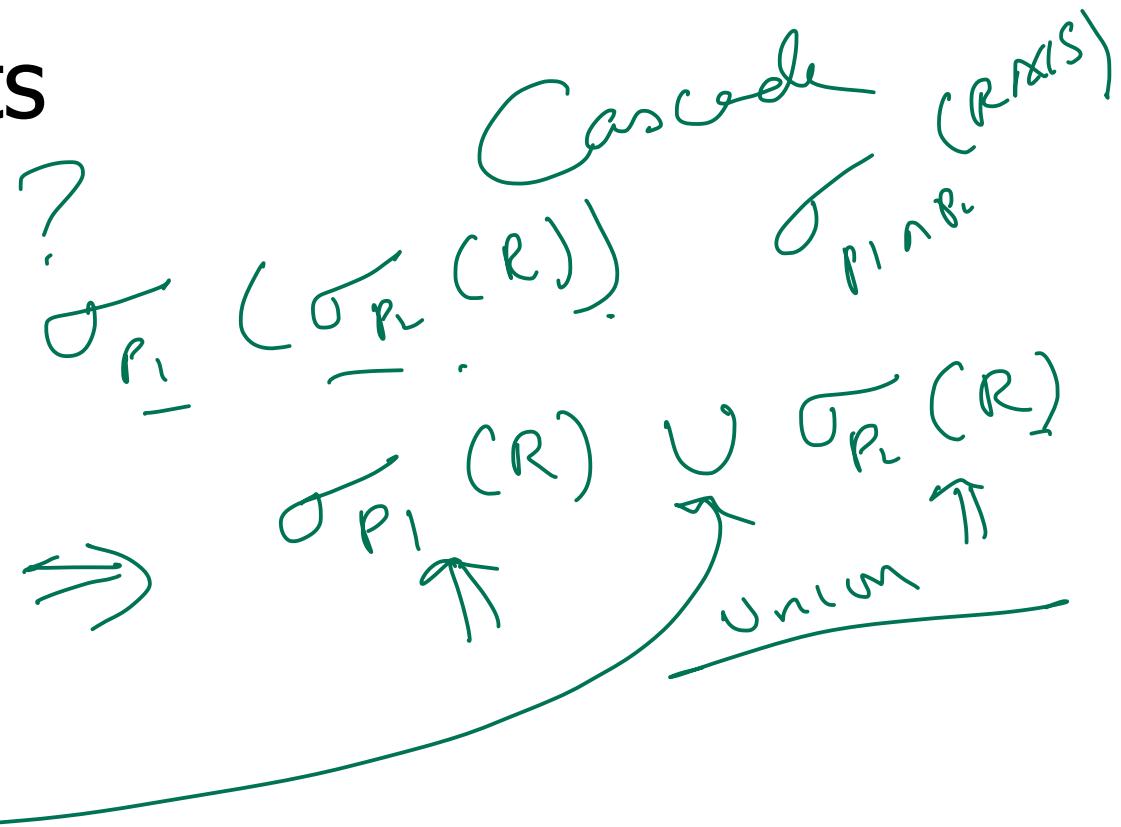
$$R \cup (S \cup T) = (R \cup S) \cup T$$



Rules: Selects

$$\sigma_{p_1 \wedge p_2}(R) =$$

$$\sigma_{p_1 \vee p_2}(R) =$$



Rules: Selects

$$\sigma_{p_1 \wedge p_2}(R) =$$

$$\sigma_{p_1 \vee p_2}(R) =$$

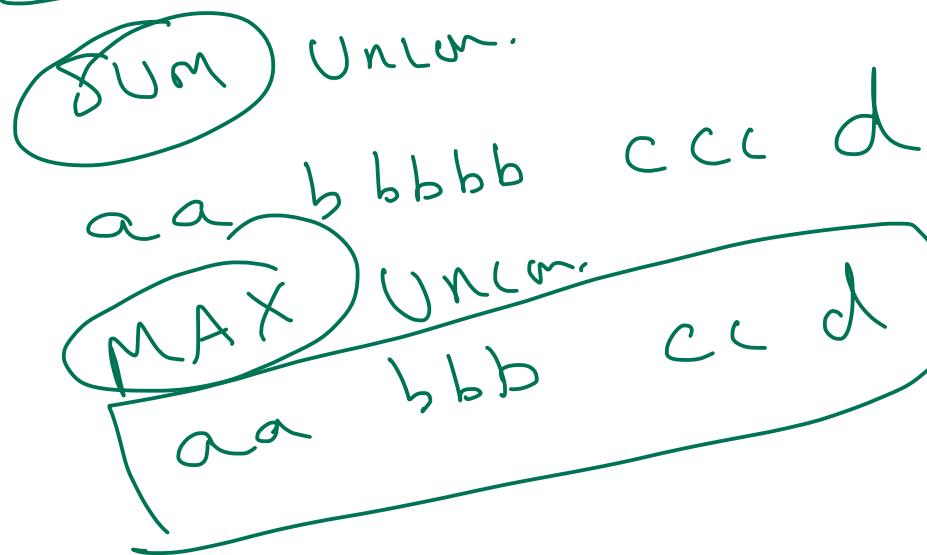
$$\sigma_{p_1} [\sigma_{p_2}(R)]$$
$$[\sigma_{p_1}(R)] \cup [\sigma_{p_2}(R)]$$

Bags vs. Sets

$$R = \{a, a, b, b, b, c\}$$

$$S = \{b, b, c, c, d\}$$

$$\underline{RUS} = ?$$



SQL DISTINCT

bag set
Sel \neq SSN
- - -

union
Sel \neq SSN
- - -
(bag)

Bags vs. Sets

$R = \{a, a, b, b, b, c\}$

$S = \{b, b, c, c, d\}$

$RUS = ?$

- Option 1 SUM

$RUS = \{a, a, b, b, b, b, b, c, c, c, d\}$ 

- Option 2 MAX

$RUS = \{a, a, b, b, b, c, c, d\}$ 

Option 2 (MAX) makes this rule work:

$$\underline{\sigma_{p1 \vee p2}(R)} = \underline{\sigma_{p1}(R)} \cup \underline{\sigma_{p2}(R)}$$

Example: $R=\{a,a,\underline{b},\underline{b},\underline{b},c\}$

P1 satisfied by a,b; P2 satisfied by b,c

Option 2 (MAX) makes this rule work:



$$\Sigma_{p1 \vee p2}(R) = \Sigma_{p1}(R) \cup \Sigma_{p2}(R)$$

Example: $R = \{a, a, b, b, b, c\}$

P1 satisfied by a,b; P2 satisfied by b,c

$$\Sigma_{p1 \vee p2}(R) = \{a, a, b, b, b, c\}$$

$$\underline{\Sigma_{p1}(R)} = \underline{\{a, a, b, b, b\}}$$

$$\underline{\Sigma_{p2}(R)} = \underline{\{b, b, b, c\}}$$

$$\Sigma_{p1}(R) \cup \Sigma_{p2}(R) = \{a, a, b, b, b, c\}$$

"Sum" option makes more sense:

LS
Senators (.....)

RS
Rep (.....)

T1 = $\pi_{yr,state}$ Senators;

T1	Yr	State
	97	CA
	99	CA
	98	AZ

T2 = $\pi_{yr,state}$ Reps

T2	Yr	State
	99	CA
	99	CA
	98	CA



Sum)?
MAT

Union?

Same
Senators are diffnt

Executive Decision

- > Use "SUM" option for bag unions
- > Some rules cannot be used for bags

Evil
Sum
MA+

Rules: Project

Let: $X = \text{set of attributes}$

$Y = \text{set of attributes}$

$$XY = X \cup Y$$

$$\pi_{xy}(R) = \overbrace{\pi_X \pi_Y}^{\text{R}}(R)$$

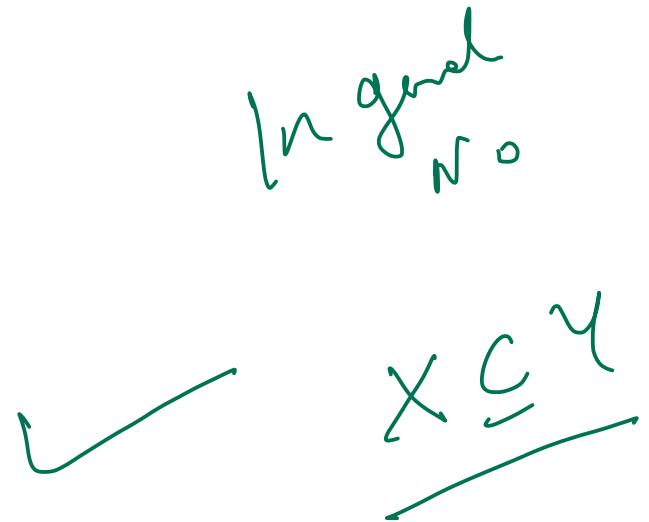
Rules: Project

Let: $X = \text{set of attributes}$

$Y = \text{set of attributes}$

$$XY = X \cup Y$$

$$\pi_{xy}(R) = \pi_x[\pi_y(R)]$$



Rules: Project

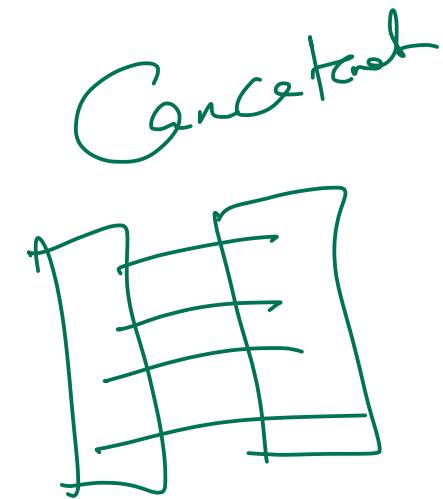
Let: $X = \text{set of attributes}$

$Y = \text{set of attributes}$

$$XY = X \cup Y$$

$$\pi_{xy}(R) = \pi_x[\pi_y(R)]$$

$$X \subseteq Y(R)$$

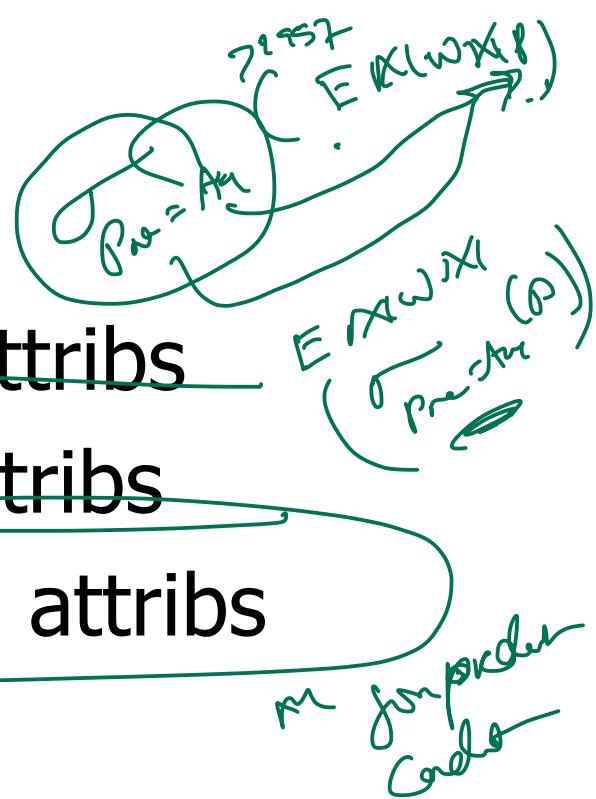


Rules: $\sigma + \bowtie$ combined

Let p = predicate with only R attrs

q = predicate with only S attrs

m = predicate with only R,S attrs



$$\sigma_p(R) \bowtie S =$$

$$\sigma_p(R) \bowtie S.$$

$$\sigma_q(R \bowtie S) =$$

$$R \bowtie \sigma_q(S).$$

Rules: $\sigma + \bowtie$ combined

Let p = predicate with only R attrs

q = predicate with only S attrs

m = predicate with only R, S attrs

$$\sigma_p (R \bowtie S) = [\sigma_p (R)] \bowtie S$$

$$\sigma_q (R \bowtie S) = R \bowtie [\sigma_q (S)]$$

Rules: $\sigma + \bowtie$ combined (continued)

Some Rules can be Derived:

$$\overline{\sigma_{p \wedge q}} (R \bowtie S) = \overline{\sigma_p(r) \bowtie \sigma_q(r)}$$

$$\overline{\sigma_{p \wedge q \wedge m}} (R \bowtie S) = \overline{\sigma_m(\sigma_p(r) \bowtie \sigma_q(r))}$$

$$\overline{\sigma_{p \vee q}} (R \bowtie S) =$$

Do one, others for homework:

$$\sigma_{p \wedge q} (R \bowtie S) = [\sigma_p(R)] \bowtie [\sigma_q(S)]$$

$$\sigma_{p \wedge q \wedge m} (R \bowtie S) =$$

$$\cancel{\sigma_m} [(\sigma_p R) \bowtie (\sigma_q S)]$$

$$\sigma_{p \vee q} (R \bowtie S) =$$

$$[(\sigma_p R) \bowtie S] \cup [R \bowtie (\sigma_q S)]$$

--> Derivation for first one:

$$\sigma_{p \wedge q} (R \bowtie S) =$$

$$\sigma_p [\sigma_q (R \bowtie S)] =$$

$$\sigma_p [R \bowtie \sigma_q (S)] =$$

$$[\sigma_p (R)] \bowtie [\sigma_q (S)]$$

Rules: π, σ combined

Let $x = \text{subset of } R \text{ attributes}$

$z = \text{attributes in predicate } P$

(subset of R attributes)

$R(a^-, b^-, c^-, d^-, e^-, f^-)$
 $\pi_x R$
 $\pi_z R$
 $z \subseteq x$
True

$$\pi_x[\sigma_P(R)] =$$

$$\sigma_P(\pi_x(R))$$

$$= \sigma_P(\pi_{x \cap z}(R))$$

$$x \cap z = \emptyset$$

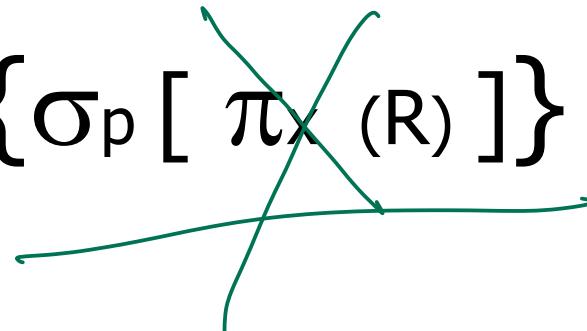
Rules: π, σ combined

Let x = subset of R attributes

z = attributes in predicate P
(subset of R attributes)

$$\pi_x[\sigma_p(R)] =$$

$$\{\sigma_p[\pi_x(R)]\}$$



Rules: π, σ combined

Let x = subset of R attributes

z = attributes in predicate P
(subset of R attributes)

$$\pi_x[\sigma_p(R)] = \{ \sigma_p [\pi_x(R)] \}$$

Handwritten annotations:

- A green box encloses the term π_x . A green bracket above it points to the expression π_{xz} .
- A green circle labeled "1" is connected by a green wavy line to the green box.
- A green circle labeled "2" is connected by a green wavy line to the green bracket above the expression π_{xz} .
- A green wavy line labeled "redacted" is drawn through the original expression $\pi_x(R)$.
- A green wavy line labeled "Later SSN" is drawn through the term σ_p .
- A green wavy line labeled "redacted" is drawn through the entire right side of the equation.

Rules: π , \bowtie combined

Let $x = \text{subset of } R \text{ attributes}$

$y = \text{subset of } S \text{ attributes}$

$\underline{z} = \text{intersection of } R, S \text{ attributes}$

$$\pi_{xy}(R \bowtie S) = \overbrace{\pi_{xz}(R) \bowtie \pi_{yz}(S)}^{\text{LARGE PAREN}} = \pi_{\text{large paren}}(E \bowtie P)$$

Annotations:

- $\pi_{xz}(R)$ is enclosed in a large green bracket.
- $\pi_{yz}(S)$ is enclosed in a large green bracket.
- A green arrow points from $\pi_{xz}(R)$ to E .
- A green arrow points from $\pi_{yz}(S)$ to P .
- $E \bowtie P$ is enclosed in a green oval.
- E is labeled $SSN = ESSN$.
- P is labeled $SSN = EMP$.
- $E \bowtie P$ is labeled (P) .

Rules: π , \bowtie combined

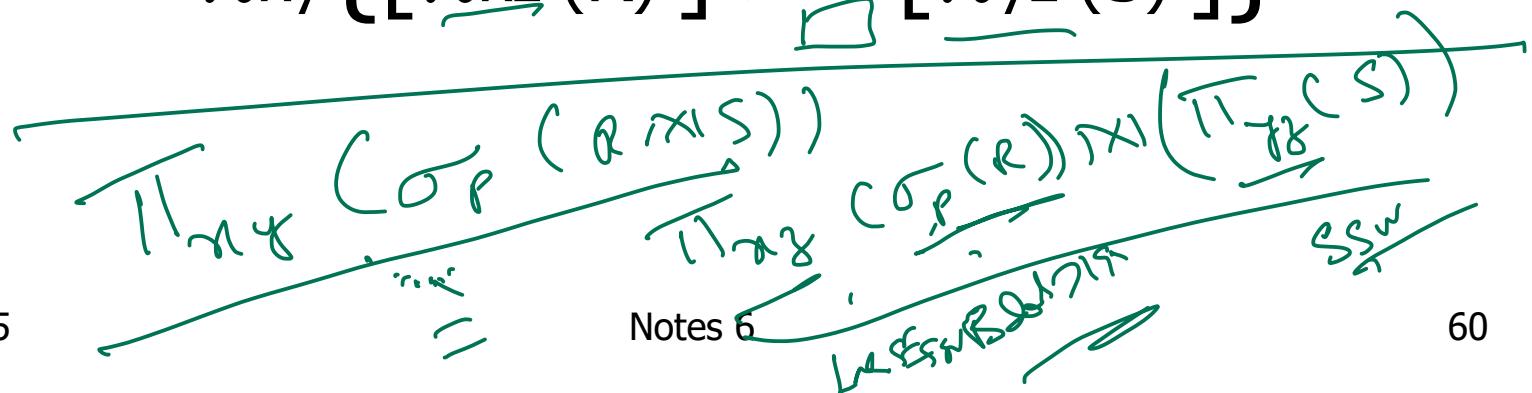
Let x = subset of R attributes

y = subset of S attributes

z = intersection of R, S attributes

$\pi_{xy} (R \bowtie S) =$

$$\pi_{xy} \{ [\pi_{xz} (R)] \bowtie [\pi_{yz} (S)] \}$$



$$\pi_{xy} \{ \sigma_p (R \bowtie S) \} =$$

$$\pi_{xy} \{ \sigma_p (R \bowtie S) \} =$$

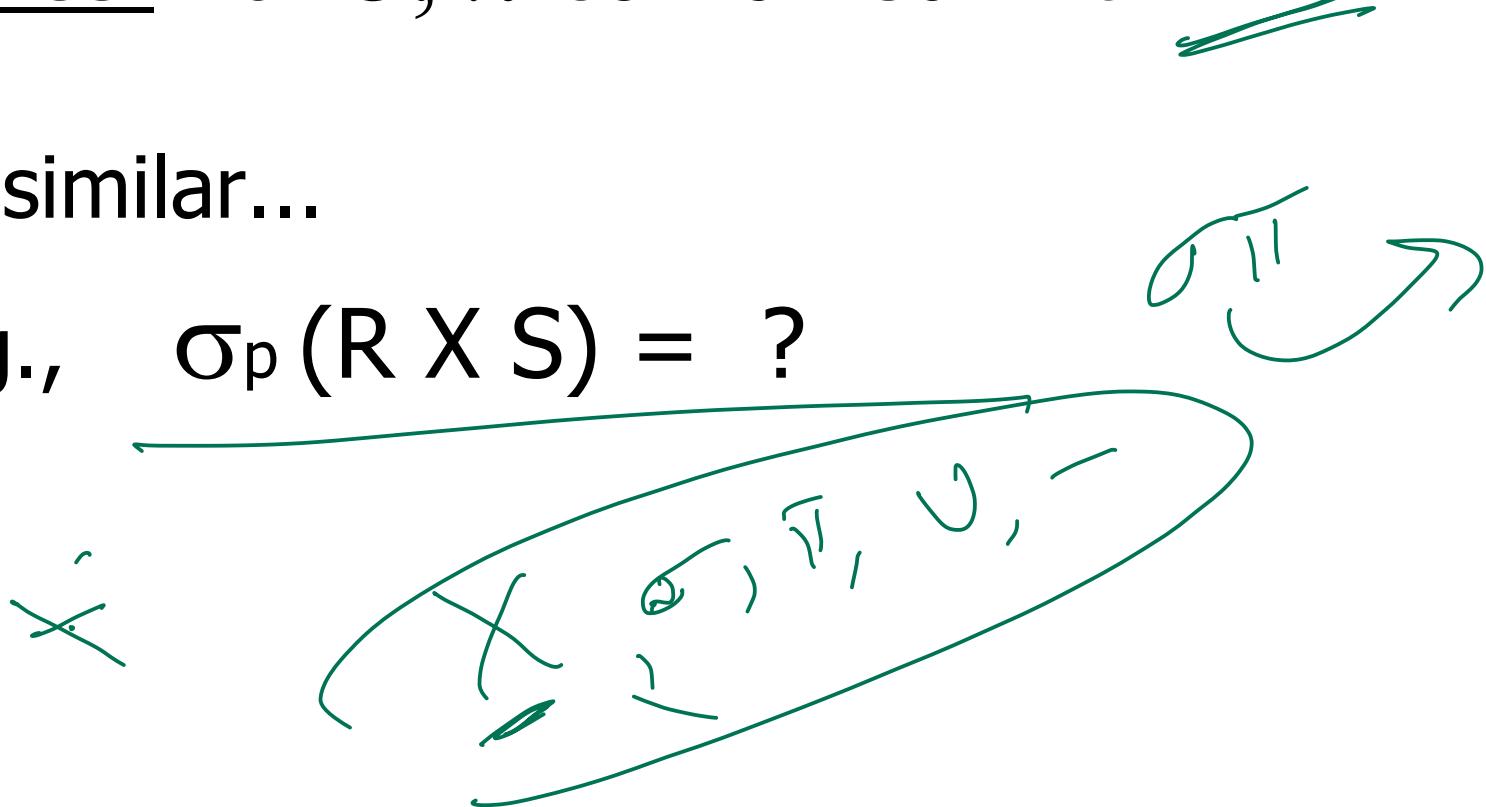
$$\pi_{xy} \{ \sigma_p [\pi_{xz'}(R) \bowtie \pi_{yz'}(S)] \}$$

$z' = z \cup \{ \text{attributes used in } P \}$

Rules for σ, π combined with X

similar...

e.g., $\sigma_p(R \times S) = ?$



Rules σ , U combined:

$$\sigma_p(R \cup S) = \sigma_p(R) \cup \sigma_p(S)$$

$$\sigma_p(R - S) = \sigma_p(R) - S = \sigma_p(R) - \sigma_p(S)$$

Which are “good” transformations?

- $\leftarrow \in R \leftarrow \leftarrow R \leftarrow t \leftarrow -$
- $\sigma_{p_1 \wedge p_2}(R) \rightarrow \sigma_{p_1}[\sigma_{p_2}(R)]$ ✓
 - $\sigma_p(R \bowtie S) \rightarrow [\sigma_p(R)] \bowtie S$ ✓
 - $R \bowtie S \rightarrow S \bowtie R$ (?)
 - $\pi_x[\sigma_p(R)] \rightarrow \pi_x\{\sigma_p[\pi_{xz}(R)]\}$ ✓

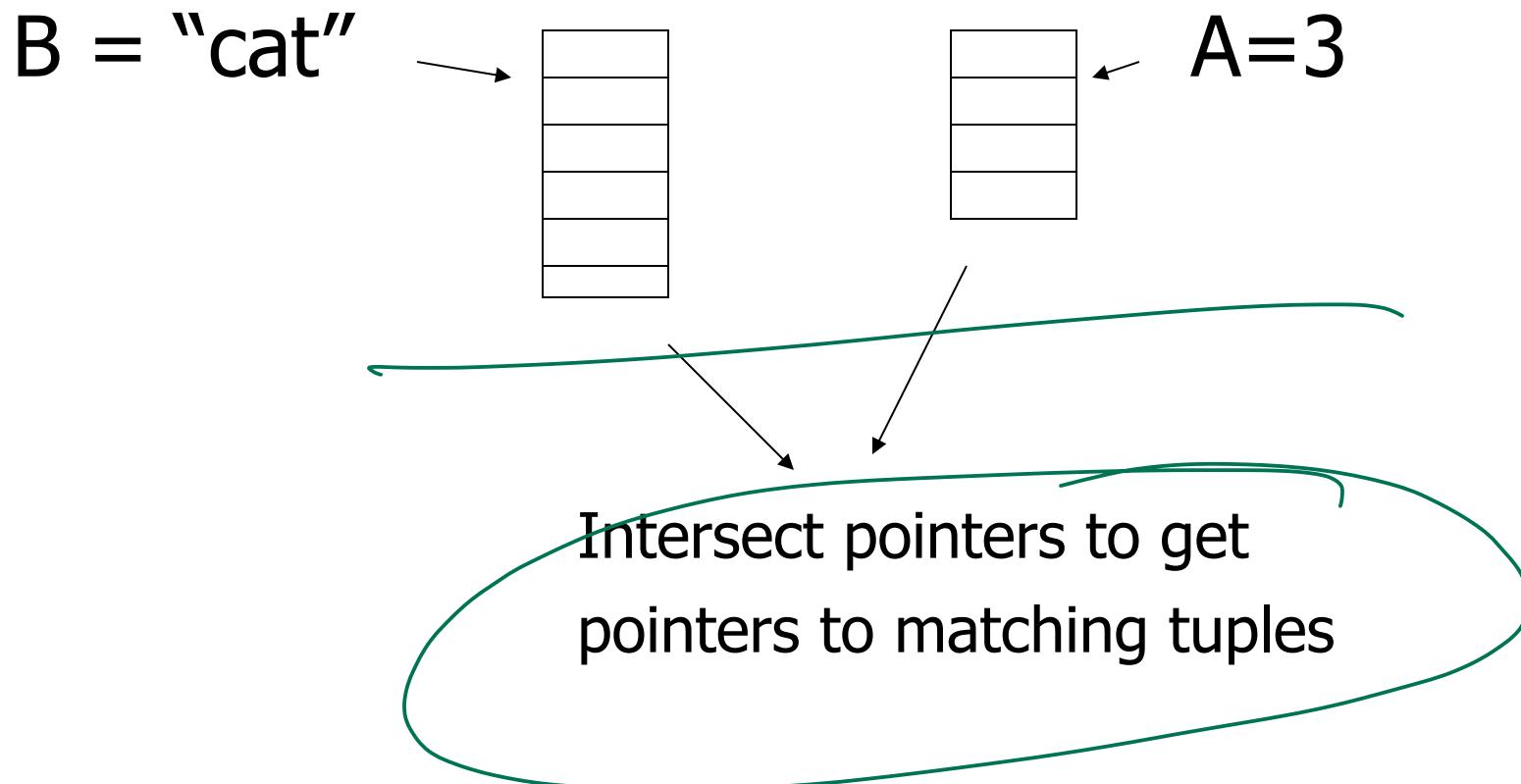
Conventional wisdom:
do projects early

Example: $R(A,B,C,D,E)$ $x=\{E\}$

$P: (A=3) \wedge (B=\text{"cat"})$

$\pi_x \{\sigma_p(R)\}$ vs. $\pi_E \{\sigma_p\{\pi_{ABE}(R)\}\}$

But what if we have A, B indexes?



Bottom line:

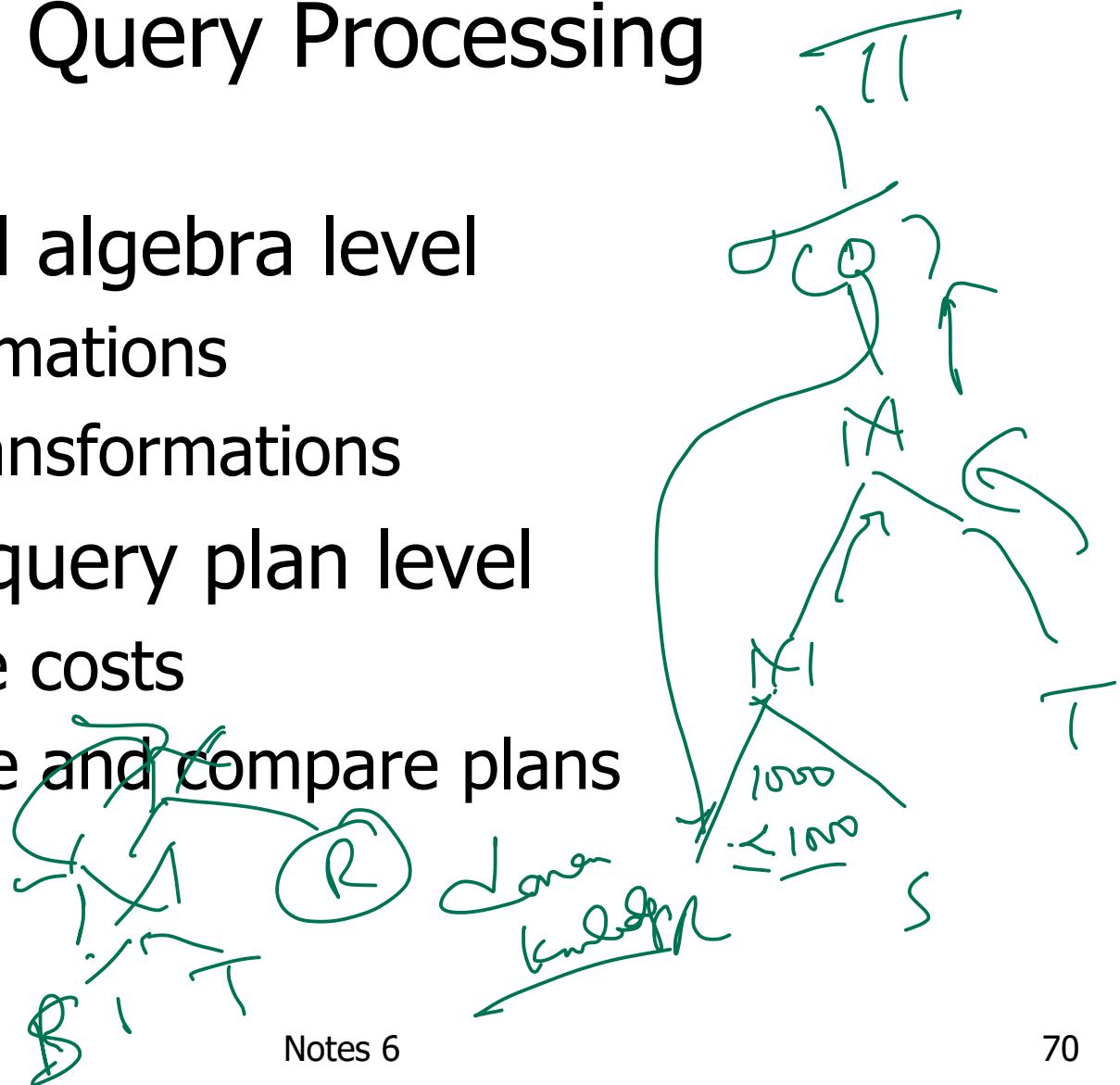
- No transformation is always good
- Usually good: early selections

In textbook: more transformations

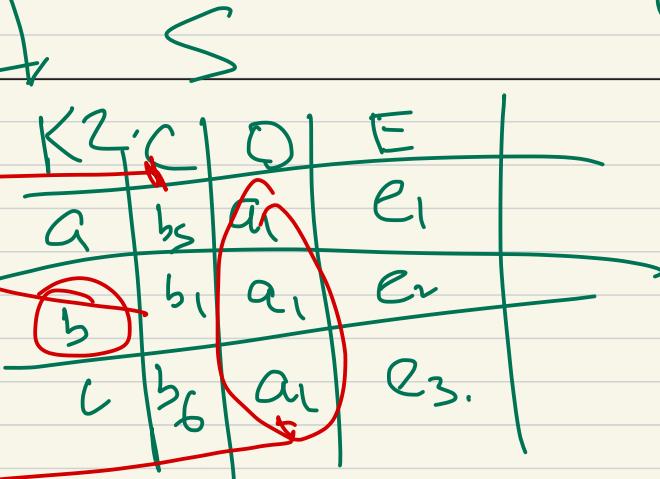
- Eliminate common sub-expressions
- Other operations: duplicate elimination

Outline - Query Processing

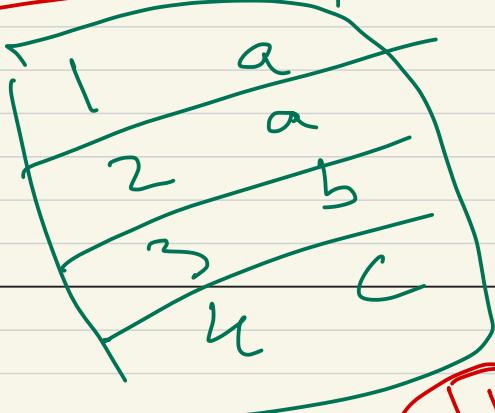
- Relational algebra level
 - transformations
 - good transformations
- Detailed query plan level
 - estimate costs
 - generate and compare plans



12



$$\Pi_{(K_1, K_2)}(R, T_1, S) \\ R - F_K = \\ R - K$$



$$R \leftarrow m \\ S \leftarrow m \\ \beta \leftarrow m$$

$$R \cdot B = S \cdot C$$

12
1m

12

$$R \cdot A = S \cdot D$$

6 ↗

Rows

1, 4, 6,

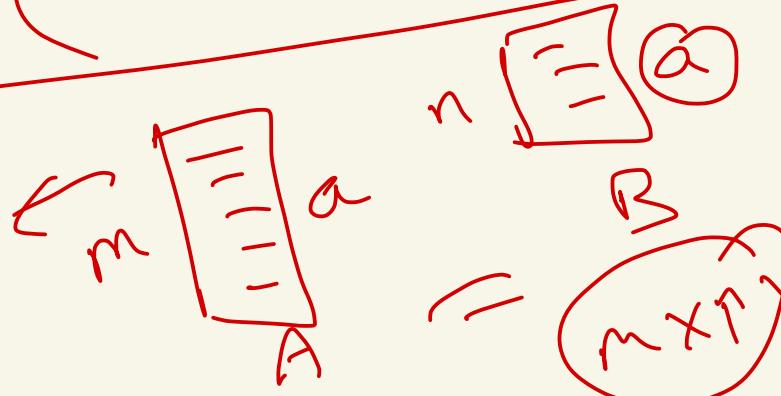
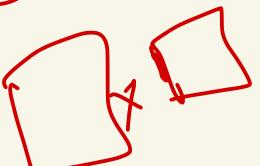
R \times 15
—

$(R \times S) \rightarrow$ No. rows in result is not
easy

(R), (S)

$(R \times S)$

Min. Col. prod.



$R \times S$

unless Σ event
contains

God ($R \times S$)

(Σ)

Man

(Σ)

S A. not R

not Σ

(Σ)

Effects of χ along op verschillende

$T(R)$

of types in a behavior

$$T(\overline{T}(R)) = \underline{T(R)} \leq T(R) \quad T(R).$$

$$T(C\circ C(R)) = ? - T(R)$$

Estimate the number of joins

$$T(\overline{\Pi}_A((\sigma_{C_1}(R) \times \sigma_{C_2}(S)) \times \sigma_{C_3}(T)))$$

?

$\sigma_{C_3}(T)$

$T(R) \quad T(S) \quad T(T)$

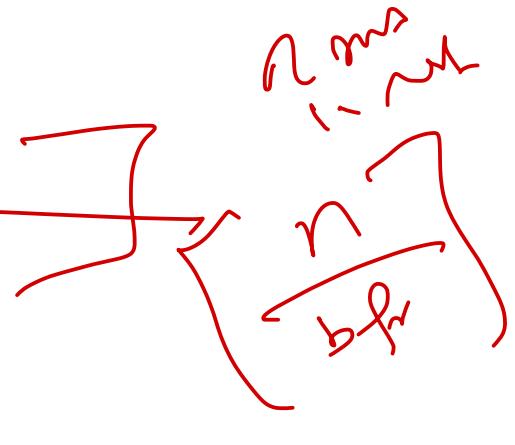
T *This is the useful end*

useful ←
Accurate

- Estimating cost of query plan

(1) Estimating size of results

(2) Estimating # of IOs



Estimating result size

- Keep statistics for relation R

- $T(R)$: # tuples in R

- $S(R)$: # of bytes in each R tuple

- $B(R)$: # of blocks to hold all R tuples

- $V(R, A)$: # distinct values in R

for attribute A

SDay number
 ~ 150

Notes 6

APs (~ 12 15
Query Proc time

Size of result

$A\text{-val}(R)$

Result
of query

$|R|$ (R)
 n k

$\sqrt{(\mathbb{R}, A)} \rightarrow$





$T(R)$



$V(R, A)$

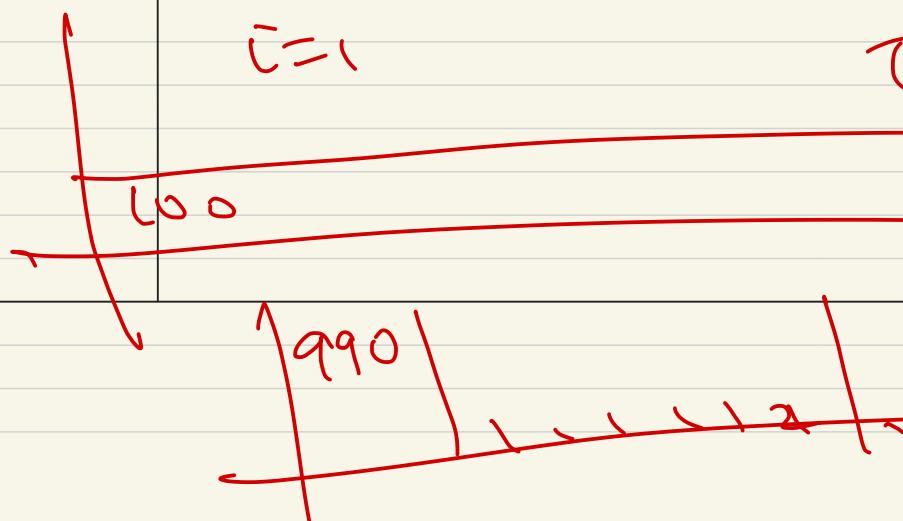
$$V(R, A) = \frac{10}{60,000}$$

~~$\frac{10}{60,000}$~~

~~$\frac{10}{60,000}$~~

$$1000 = \sum_{i=1}^{10} T(\sigma_{A=a_i}^{(R)})$$

~~$T(\sigma_{A=a_1}^{(R)})$~~ $(\sigma_{a_1}^{(R)})$ $(\sigma_{a_2}^{(R)})$



$T(\sigma_{A=a_n}^{(R)})$



$\sigma_{X=a_n | A=a_s}^{(R)}$

Example

R

R

	A	B	C	D
cat	1	10	a	
cat	1	20	b	
dog	1	30	a	
dog	1	40	c	
bat	1	50	d	

$T(R) \approx 5$

- A: 20 byte string
- B: 4 byte integer
- C: 8 byte date
- D: 5 byte string

Example

R

	A	B	C	D
cat	1	10	a	
cat	1	20	b	
dog	1	30	a	
dog	1	40	c	
bat	1	50	d	

A: 20 byte string

B: 4 byte integer

C: 8 byte date

D: 5 byte string

$$T(R) = 5$$

$$S(R) = 37$$

$$V(R,A) = 3$$

$$V(R,B) = 1$$

$$V(R,C) = 5$$

$$V(R,D) = 4$$

Storage
R

Size estimates for $W = R_1 \times R_2$

$$T(W) = \overbrace{T(R_1) \times T(R_2)}^{\text{R}(\times \text{R})}$$

Min Cost
rule

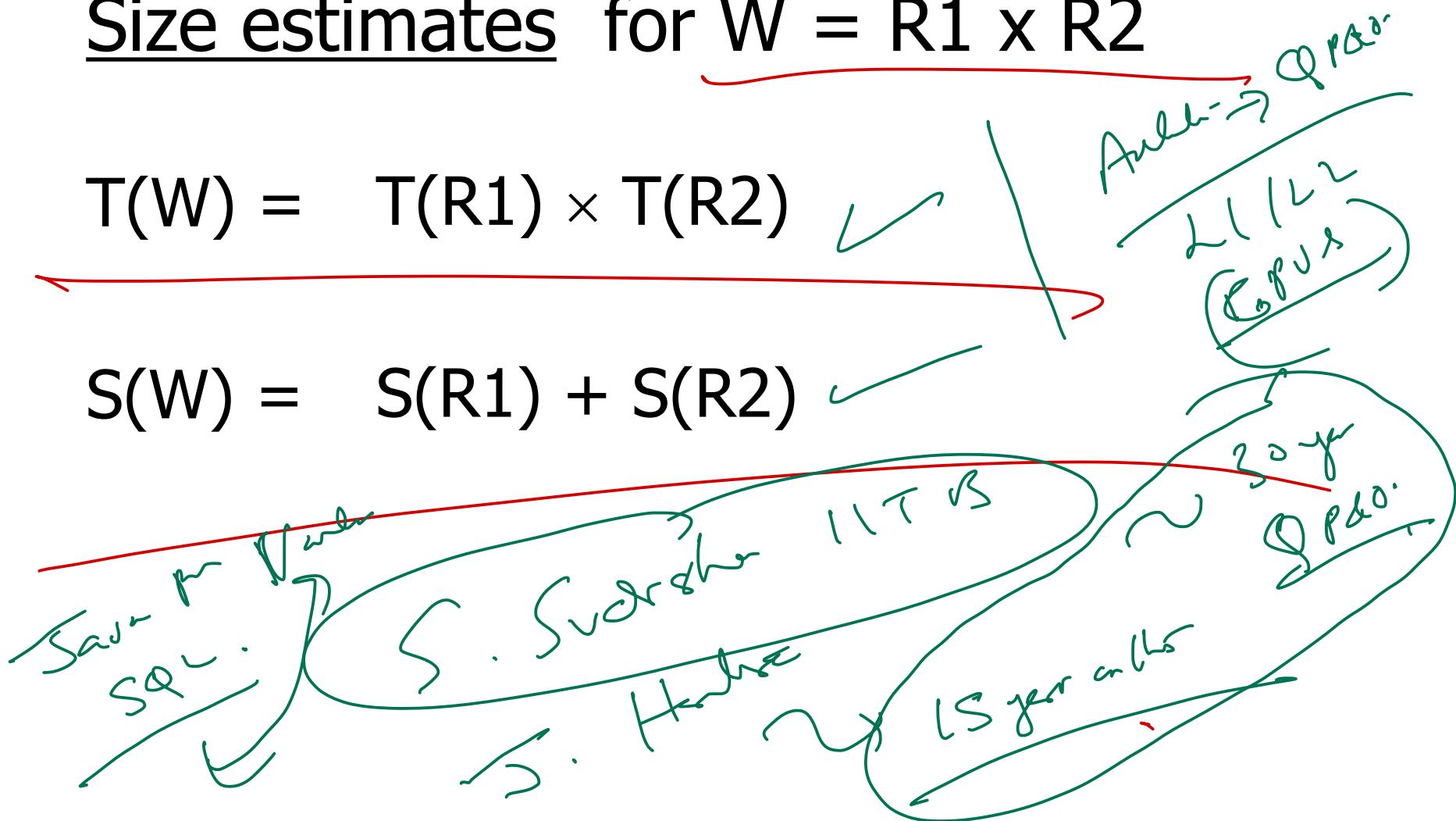
$$S(W) = \overbrace{-S(R_1) + S(R_2)}^{\text{Diagram showing overlapping regions A, B, C}}$$

$$\sigma_{\alpha=a} \cap \sigma_{\beta=b} \cap \sigma_{\gamma=c}$$

Size estimates for $W = R1 \times R2$

$$T(W) = T(R1) \times T(R2)$$

$$S(W) = S(R1) + S(R2)$$



Size estimate for $W = \sigma_{A=a}(R)$

$$S(W) = S(R)$$

$$T(W) = ?$$

$$\omega = \sigma_{A=a}(R)$$

$$T(\omega) = \frac{T(R)}{\text{Dom}(R, A)}$$

$V(R, A) \subseteq \text{Dom}(R, A)$

Consecutive estimate

$$\exists v \in \text{Dom}(R, A)$$

$$v \notin V(R, A)$$

will come \exists at least one row with $A=0$

$$\text{DOM}(R, A)$$

$$a \in \text{Dom}(A)$$

$$a \in V(R, A)$$

$$V(R, A)$$

in R A has

$$V(R, A)$$

distinct
values

$$A=0$$

More than one value
at $V(R, A)$

$$\frac{T(R)}{\text{Dom}(R, A)}$$

$$\frac{T(R)}{\text{Dom}(R, A)} = \frac{100}{20} = 50$$

$$\frac{T(R)}{\sqrt{R+A}}$$

Has wrong?

Each value of domain occurs uniformly in R

$\text{Dom}(R, A) = 20$

$$T(R) = 100$$

one val
 $A = \frac{125}{\omega}$ $T(\omega) = 50$

$$\omega = \frac{125}{A=50} (R)$$

$$= \frac{100}{8} = 125$$

we may get relative
estimates

$$VCR, A) = 8$$

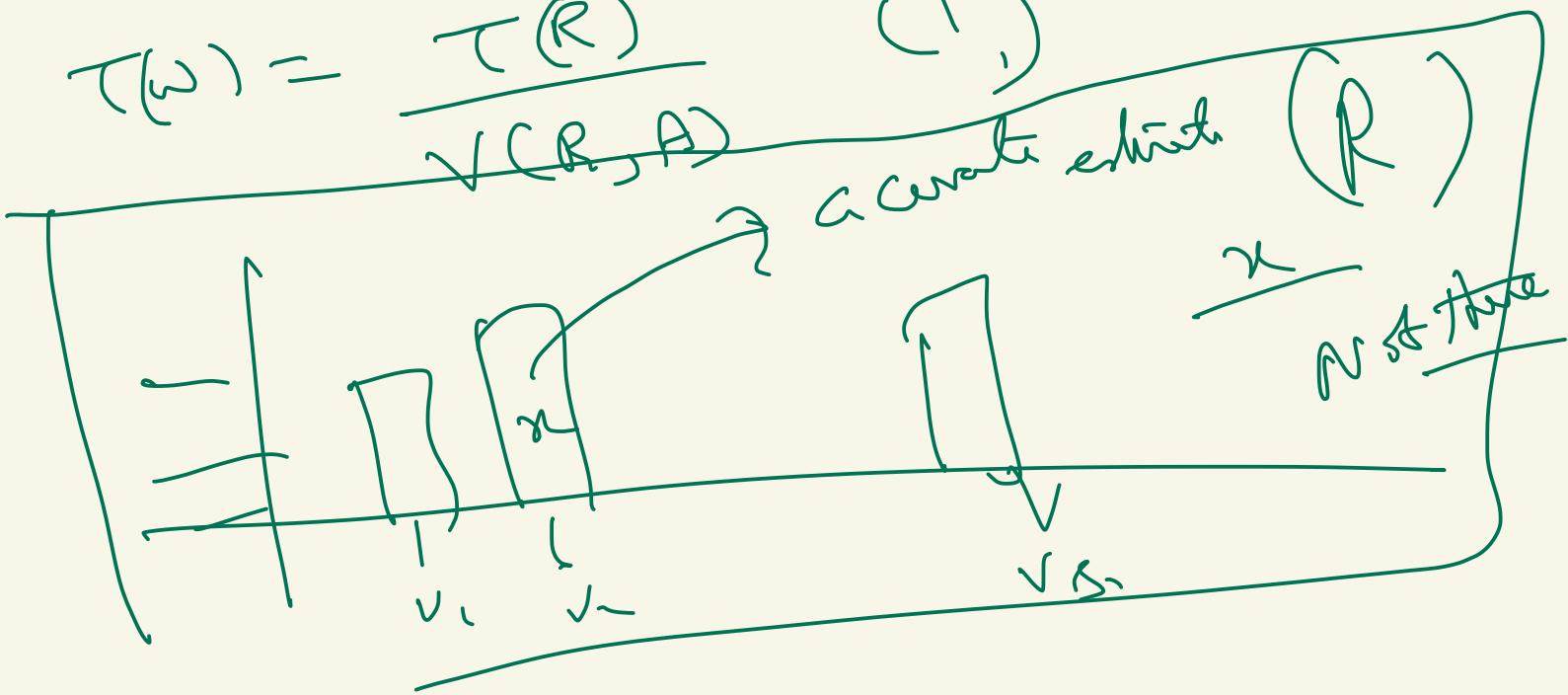
$$T(\omega) = \frac{125}{2 \cdot 5 \times 50}$$

$V(R, A)$
stronger

① $\Omega_m(R, A)$
is weaker
etc

$$\omega = \sigma_{A=\text{val}}(R)$$

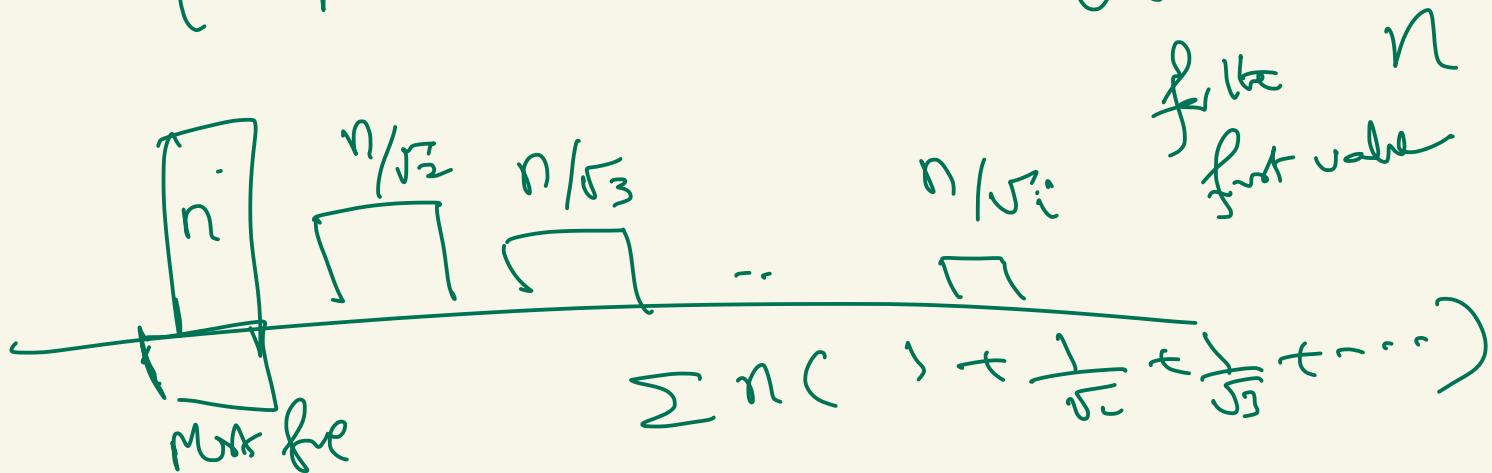
$$T(\omega) = \frac{T(R)}{V(R, A)}$$



In my scenarios (A)
one value \square large $\square \square \square \square \square$

~~Zip for distribution~~
~~the most common value~~

$\frac{1}{\sqrt{i}}$ times.



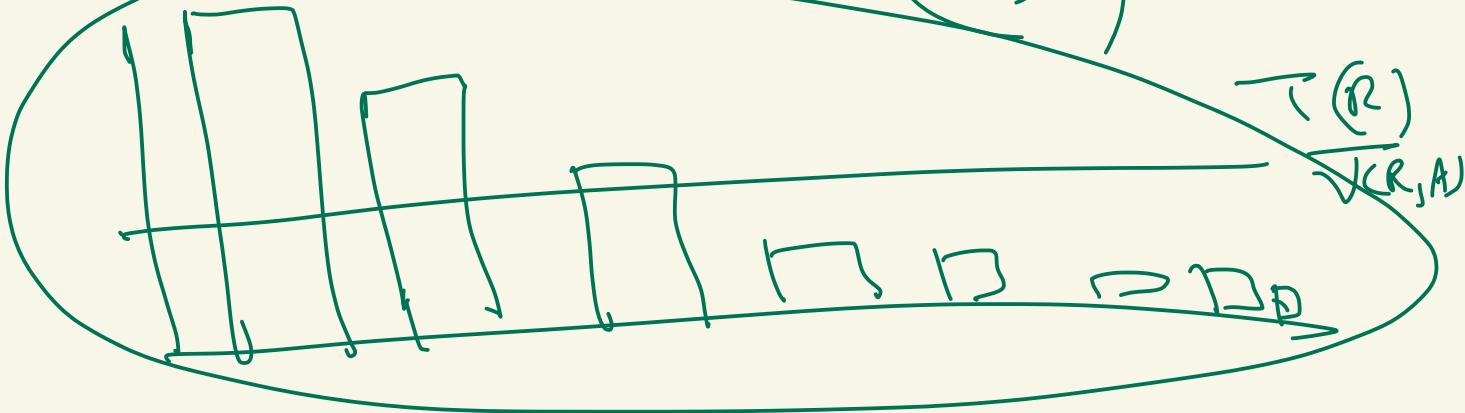
$$\frac{1000}{\sqrt{2}}$$

$$\frac{1000}{\sqrt{2}} = 707$$

$$\frac{1000}{\sqrt{3}} = \underline{\underline{577}}$$

$$T(R)$$

$$\frac{V(R, A)}{T(R)}$$



$$\omega = \overline{\sigma}_{A_{7, \text{val}}} (R)$$

$$T(\omega) = \frac{T(R)}{2}$$

In direct :- hopes to not get more rows

$$T(\omega) = \frac{T(R)}{3}.$$

$$T(R) = 1000$$

$$JCR, A) = 10$$

$$VC(R_1, b) = 5$$

$$\omega = \overline{\sigma}_{\substack{A_{7, \text{val}} \text{ AND} \\ \overline{B=x}}} (R)$$

$$= \frac{T(R)}{(A_{7, \text{val}})} * \frac{1}{(B=x)}$$

$$= \frac{1000}{3 \times 5} = \frac{\cancel{1000}}{\cancel{3} \cancel{5} 3} = 66$$

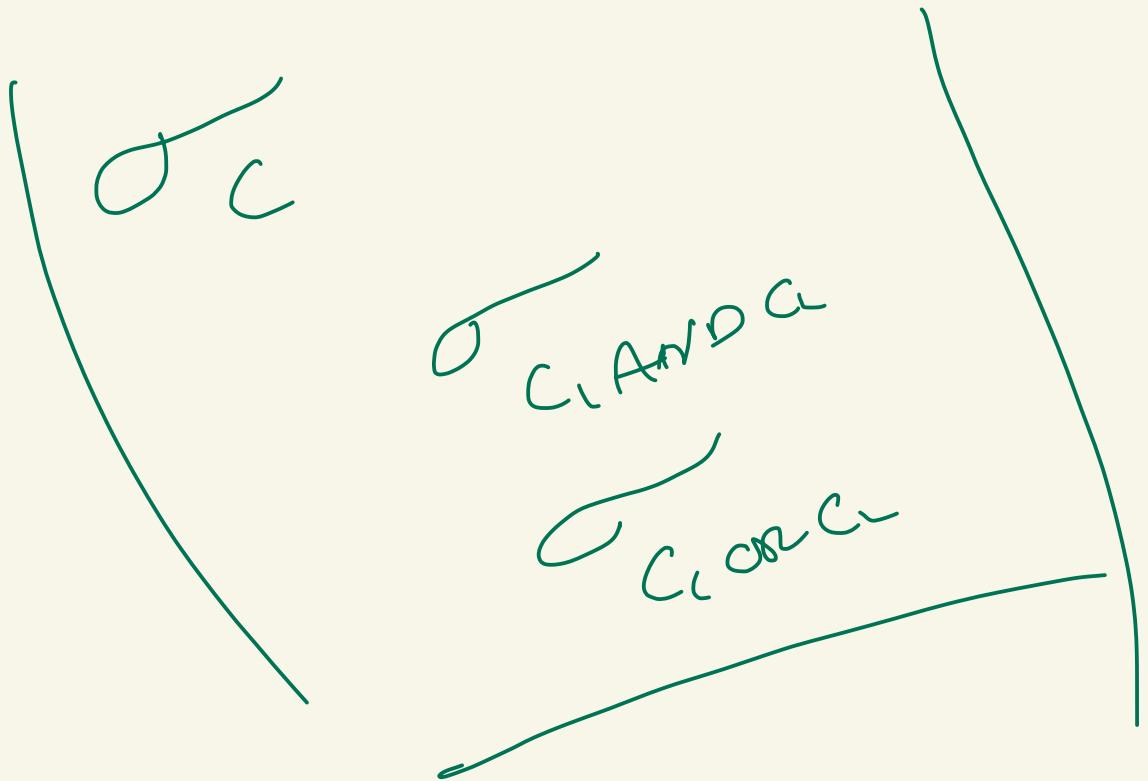
PCA \approx 5)

$$\omega = \sum_i \left(\begin{array}{l} \text{if } A = \text{val} \text{ or } \\ \text{if } B = \text{val} \end{array} \right) \text{ AND } \left(\begin{array}{l} R \\ \text{if } A \neq \text{val} \end{array} \right)$$

$$T(x) = \left(1 - \left(1 - m_1 \right) \left(1 - \frac{m_1}{m_2} \right) \right) T(x) \left(1 - (A \neq \text{val}) \right)$$

See last slide

$$\begin{aligned} &= \left(1 - \left(1 - \frac{900}{1000} \right) \left(1 - \frac{800}{1000} \right) \right) T(x) \\ &= \left(1 - \left(\frac{100}{1000} \times \frac{200}{1000} \right) \right) T(x) \\ &= \frac{100}{1000} - 20 = 980 \end{aligned}$$



Example

R

	A	B	C	D
cat	1	10	a	
cat	1	20	b	
dog	1	30	a	
dog	1	40	c	
bat	1	50	d	

$$V(R,A)=3$$

$$V(R,B)=1$$

$$V(R,C)=5$$

$$V(R,D)=4$$

$$W = \sigma_{z=val}(R) \quad T(W) =$$

Example

R

	A	B	C	D
cat	1	10	a	
cat	1	20	b	
dog	1	30	a	
dog	1	40	c	
bat	1	50	d	

$$V(R,A)=3$$

$$V(R,B)=1$$

$$V(R,C)=5$$

$$V(R,D)=4$$

what is probability this tuple will be in answer?

$$W = \sigma_{z=\text{val}}(R) \quad T(W) =$$

Example

R

	A	B	C	D
cat	1	10	a	
cat	1	20	b	
dog	1	30	a	
dog	1	40	c	
bat	1	50	d	

$$V(R, A) = 3$$

$$V(R, B) = 1$$

$$V(R, C) = 5$$

$$V(R, D) = 4$$

$$W = \sigma_{z=\text{val}}(R)$$

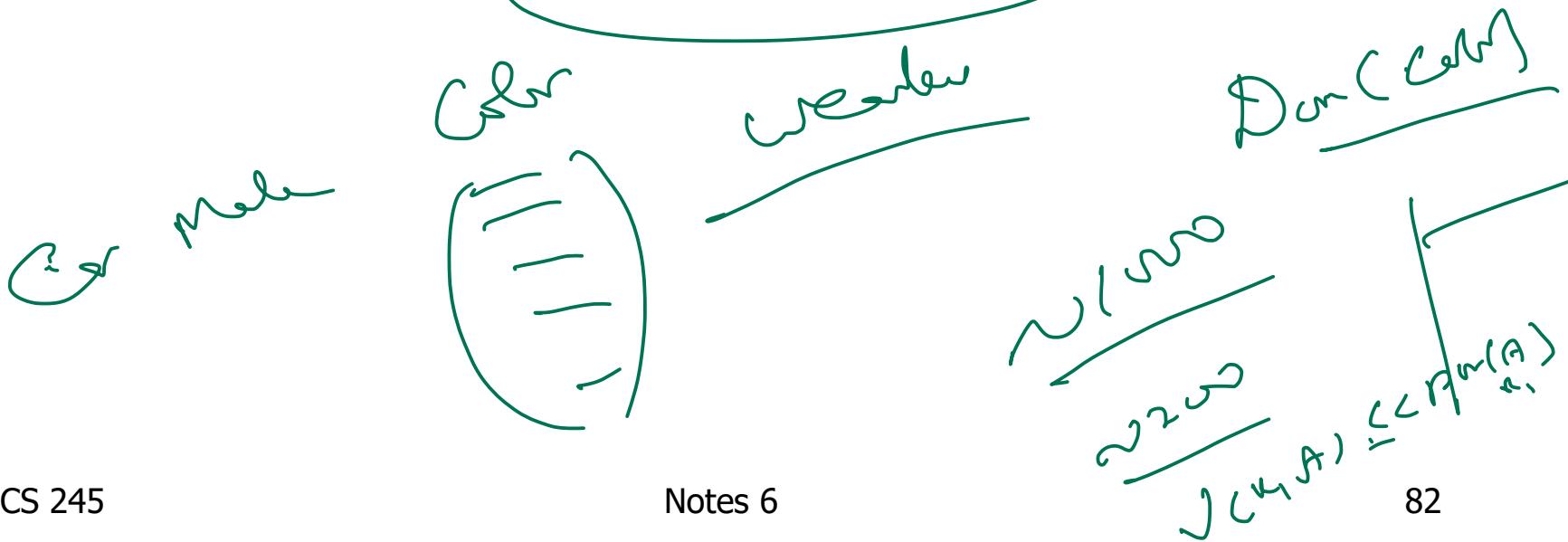
$$T(W) = \frac{T(R)}{V(R, Z)}$$

Assumption:

Values in select expression $Z = \text{val}$
are uniformly distributed
over possible $V(R, Z)$ values.

Alternate Assumption:

Values in select expression $Z = \text{val}$
are uniformly distributed
over domain with $\text{DOM}(R, Z)$ values.



Example

R

	A	B	C	D
cat	1	10	a	
cat	1	20	b	
dog	1	30	a	
dog	1	40	c	
bat	1	50	d	

Alternate assumption

$V(R,A)=3 \quad DOM(R,A)=10$

$V(R,B)=1 \quad DOM(R,B)=10$

$V(R,C)=5 \quad DOM(R,C)=10$

$V(R,D)=4 \quad DOM(R,D)=10$

$$W = \sigma_{z=val}(R) \quad T(W) = ?$$

Example

R

	A	B	C	D
cat	1	10	a	
cat	1	20	b	
dog	1	30	a	
dog	1	40	c	
bat	1	50	d	

Alternate assumption

$V(R,A)=3 \text{ } DOM(R,A)=10$

$V(R,B)=1 \text{ } DOM(R,B)=10$

$V(R,C)=5 \text{ } DOM(R,C)=10$

$V(R,D)=4 \text{ } DOM(R,D)=10$

what is probability this tuple will be in answer?

$$W = \sigma_{z=val}(R) \quad T(W) = ?$$

Example

R

	A	B	C	D
cat	1	10	a	
cat	1	20	b	
dog	1	30	a	
dog	1	40	c	
bat	1	50	d	

Alternate assumption

$$V(R, A) = 3 \quad DOM(R, A) = 10$$

$$V(R, B) = 1 \quad DOM(R, B) = 10$$

$$V(R, C) = 5 \quad DOM(R, C) = 10$$

$$V(R, D) = 4 \quad DOM(R, D) = 10$$

$$W = \sigma_{z=val}(R) \quad T(W) = \frac{T(R)}{DOM(R, Z)}$$

Selection cardinality

$SC(R,A)$ = average # records that satisfy
equality condition on $R.A$

$$SC(R,A) = \left\{ \begin{array}{l} \frac{T(R)}{V(R,A)} \\ \frac{T(R)}{\text{DOM}(R,A)} \end{array} \right\}$$

The equation is annotated with green arrows and marks:

- A curved arrow points from the text "equality condition on R.A" above to the term $V(R,A)$.
- A straight arrow points from the text "average # records that satisfy" above to the term $T(R)$.
- A vertical curly brace groups the two terms $\frac{T(R)}{V(R,A)}$ and $\frac{T(R)}{\text{DOM}(R,A)}$.
- A large checkmark is drawn next to the term $\frac{T(R)}{V(R,A)}$.
- A large X is drawn next to the term $\frac{T(R)}{\text{DOM}(R,A)}$.

What about $W = \sigma_{z \geq \text{val}}(R)$?

$T(W) = ?$

What about $W = \sigma_{z \geq \text{val}}(R)$?

$T(W) = ?$

- Solution # 1:

$$T(W) = T(R)/2$$

What about $W = \sigma_{z \geq \text{val}}(R)$?

$$T(W) = ?$$

- Solution # 1:

$$T(W) = T(R)/2$$

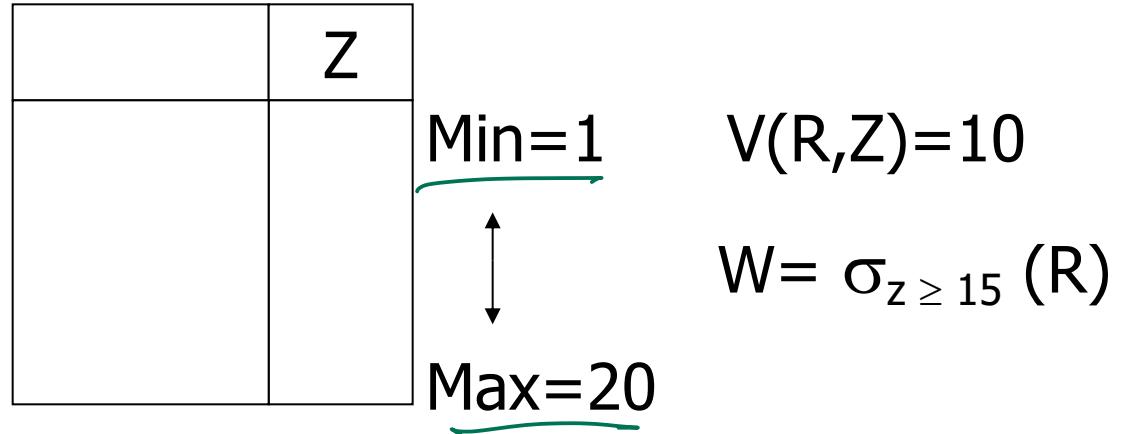
- Solution # 2:

$$T(W) = T(R)/3$$

Human
to reduce
query out

- Solution # 3: Estimate values in range

Example R



- Solution # 3: Estimate values in range

Example R

	Z

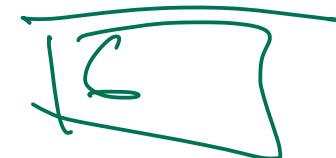
Min=1

Max=20



$$V(R, Z) = 10$$

$$W = \sigma_{z \geq 15}(R)$$



$$f = \frac{20-15+1}{20-1+1} = \frac{6}{20}$$

(fraction of range)

$$T(W) = f \times T(R)$$

Notes 6

A \geq Val
Val - ... map in
new numbers
 $V(R.A)$ 91

Equivalently:

$$f \times V(R, Z) = \text{fraction of distinct values}$$
$$T(W) = \frac{[f \times V(Z, R)] \times T(R)}{V(Z, R)} = f \times T(R)$$

A \approx , Aus
A is
C ...

$\checkmark R \propto S \propto T \propto U$ $\sim 4! =$

$\checkmark R \propto T \propto S \propto U$

$R \propto U$ $\propto T \propto S$



Jan order

left long

$\overline{I_2}$

$R.$

I_2, \overline{R}

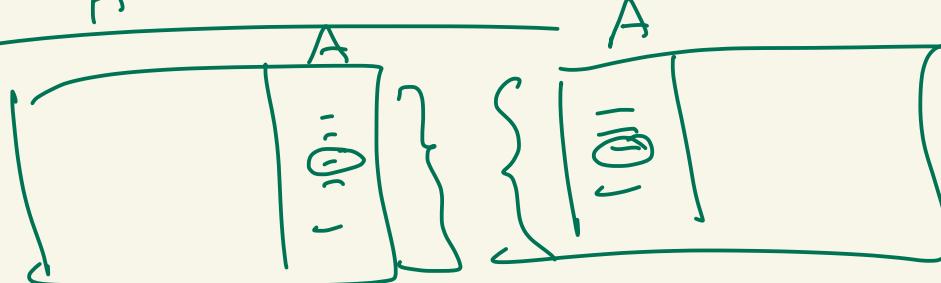
$\overline{I_1}$ is very small

R \otimes T \otimes S \otimes U \otimes R - - -
↓
Smaller

Estimar $w = R \otimes S \quad T(w) ?$

R \otimes_A S

$\sqrt{V(R,A)}_R$
 $\sqrt{V(S,A)}_R$



(A) is
like
S

S
 $k \times l$

Two Assumptions

Constant & Value set.

γ occurs in $R_i - R_1 \cup \dots \cup R_k$

$R_i = y_1, y_2, \dots, y_j$ $\text{Dom}(R_i)$
 $v(R_i, \gamma)$

$R_i \quad R_j \quad x \in \gamma \cap R_i$
 $v(R_i, \gamma) \leq v(R_j, \gamma) \quad x \in \gamma \cap R_j$

few value
 $\text{Dom}(R_j, \gamma)$

$\text{Dom}(R_j, \gamma)$

$$\begin{array}{c}
 R_1 \quad R_2 \\
 V(R_1 Y) \leq V(R_2 Y) \leq \\
 \overbrace{\quad\quad\quad}^{\subseteq} \quad \overbrace{\quad\quad\quad}^{\subseteq} \\
 S_1 \quad \cong \quad S_2 \\
 \overbrace{\quad\quad\quad}^{\subseteq} \quad \overbrace{\quad\quad\quad}^{\subseteq} \quad \subseteq S_K
 \end{array}$$

$$\begin{array}{c}
 P_K = F_K \\
 \text{circled } S_{F_K} \in (S_{P_K}) \\
 \overbrace{\quad\quad\quad}^{\subseteq}
 \end{array}$$

A is j.m. attribute
R.B is an attribute of R.

$V(R, B)$
 $\underline{V(R, A)}$
of distinct values \Rightarrow Tuples in R.

$\omega = R \bowtie_A S$
 $\underline{V(\omega, A)} = V(R, A)$

R does not have any value of JA
~~at~~ The j.m.

$$\omega = R \times_A S$$

$$(S \vee (R, A)) \wedge (S \vee (\cancel{S}, A)) = \emptyset$$

R ×
 Colours
 S
 Colours
 Top

$\tau(\omega) = \emptyset.$

$$(R \times \overset{\text{PK}}{\cancel{S}}) = \tau(S)$$

Hde = =
 -
 older int
 FK
 Set g(S) ⊂ cfg(R)

$\underbrace{\text{PK} = \text{FK}}$

$S \cdot \text{FK}$ is an value $\emptyset.$

$$S = \overset{\circ}{C_1 \text{ or } C_2} (n)$$

7 $C_7(c_1) \text{ AND } C_7(c_2)$
- C) } In Depth.

$$\tau(r) =$$

$$\text{Value} = \left(1 - \frac{1}{1 + \frac{100}{\text{Rate}}} \right) \left(1 - \frac{200}{\text{Rate}} \right)$$

$$1000 \left(1 - \left(1 - \frac{100}{1000}\right)^{100}\right) = 673$$

$$100 \left(1 - \left(1 - \frac{990}{999}\right)^{999}\right) = 99$$

$$1000 - 673 - 99 = \boxed{228}$$

$$\tau(R \bowtie S) = \tau(R) \times \tau(S)$$

if each row of
R joins with
more rows of S
& vice-versa

$R, \tau(R)$
 $\vee(R, A) -$
 $S, \tau(S)$
 $\vee(S, A)$

$$\boxed{\frac{\tau(R)}{\vee(R, A)}}$$

$$\frac{\vee(R, A)}{\equiv} \leq \vee(S, A) \leq \frac{\tau(S)}{\vee(S, A)}$$

$$\frac{\tau(S)}{\vee(S, A)}$$

one that has
max values dominates

$$\boxed{\equiv}$$

$$\frac{\tau(R)}{\vee(R, A)}$$

$$\frac{\vee}{\tau(S)} \leq \frac{\vee}{\vee(S, A)}$$

$$\frac{\tau(S)}{\sqrt{v(S,A)}} \rightarrow \sum \left[\begin{array}{c} S \\ \vdash \end{array} \right] \in \sum \left[\begin{array}{c} \vdash \\ \vdash \end{array} \right]$$

$$\frac{R}{\sqrt{v(R,A)}} \rightarrow \sum \left[\begin{array}{c} R \\ \vdash \end{array} \right] = \sum \left[\begin{array}{c} \vdash \\ \vdash \end{array} \right]$$

$\frac{\tau(R) \cdot \tau(S)}{\sqrt{v(S,A)}}$

$$\tau(R \times S) = \frac{\tau(R) \cdot \tau(S)}{\max(v(R,A), v(S,A))}$$

$\frac{\tau(R) \cdot \tau(S)}{\sqrt{v(S,A)}, \sqrt{v(R,A)}}$

$$R \bowtie_A S$$

$$\tau(R \bowtie_A S)$$

$$= \overbrace{\tau(R) - \tau(S)}^{\max(V(R, A), V(S, A))}$$

$$R \bowtie_{A, B} S$$

$$\begin{aligned} R \cdot A &= S \cdot A \text{ AND} \\ R \cdot B &= S \cdot B \end{aligned}$$

$$= \frac{\tau(R) \cdot \tau(S)}{\tau(R) + \tau(S)}$$

$$= \overbrace{\max(V(R, A), V(S, A)) \cdot \min(V(R, B), V(S, B))}^{\rightarrow}$$

$$R(a, b)$$

$$\tau(R) = 1000$$

$$\nu(R, b) = 20$$

$$S(b, c)$$

$$\tau(S) = 2000$$

$$\nu(S, b) = 50$$

$$\nu(S, c) = 100$$

$$U(c, d)$$

$$\tau(U) = 5000$$

$$\nu(U, b) = 100$$

$$\nu(U, c) = 5000$$

$$\tau(R \bowtie_b S \bowtie_c U). \quad \nu(R \bowtie_b S, c) = 100 \quad \nu(U, c) = 5000$$

$$\tau(R \bowtie_b S) = \frac{\tau(R) - \tau(S)}{\max(20, 50)} = \frac{1000 - 2000}{\cancel{20} \cancel{50}} = 40,000$$

$$\tau((R \bowtie_b S) \bowtie_c U) = \frac{40,000 \times 5000}{\max(100, 5000)}$$

$$= 40,000$$

$$(S \bowtie_c U) \overline{\bowtie_b R}$$

↓

$$2000 \times 50\text{pp}$$

$$\underline{20,000}$$

5pp

$$1000 \times 25\text{pp}$$

400

89

$$= 400,000$$

Size estimate for $W = R_1 \bowtie R_2$

Let x = attributes of R_1

y = attributes of R_2

$R(a, b), S(b, c), U(b, d)$

$(R \times_b S)$

$$V(R \times_b S, b) = \min(V(R, b), V(S, b))$$



Size estimate for $W = R1 \bowtie R2$

Let x = attributes of $R1$

y = attributes of $R2$

Case 1

$$X \cap Y = \emptyset$$

Same as $R1 \times R2$

Case 2

$$W = R1 \bowtie R2 \quad X \cap Y = A$$

R1	A	B	C

R2	A	D

Case 2

$$W = R1 \bowtie R2 \quad X \cap Y = A$$

R1	A	B	C

R2	A	D

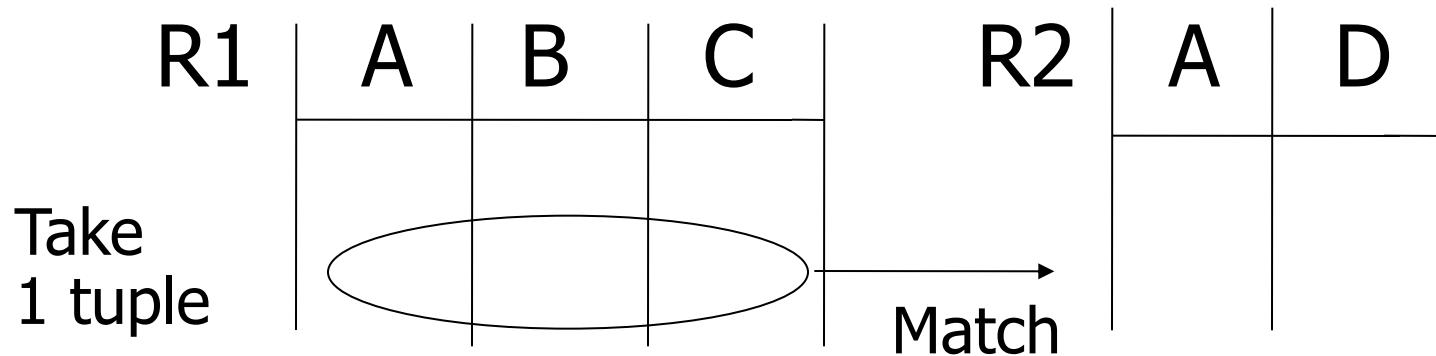
Assumption:

$V(R1, A) \leq V(R2, A) \Rightarrow$ Every A value in R1 is in R2

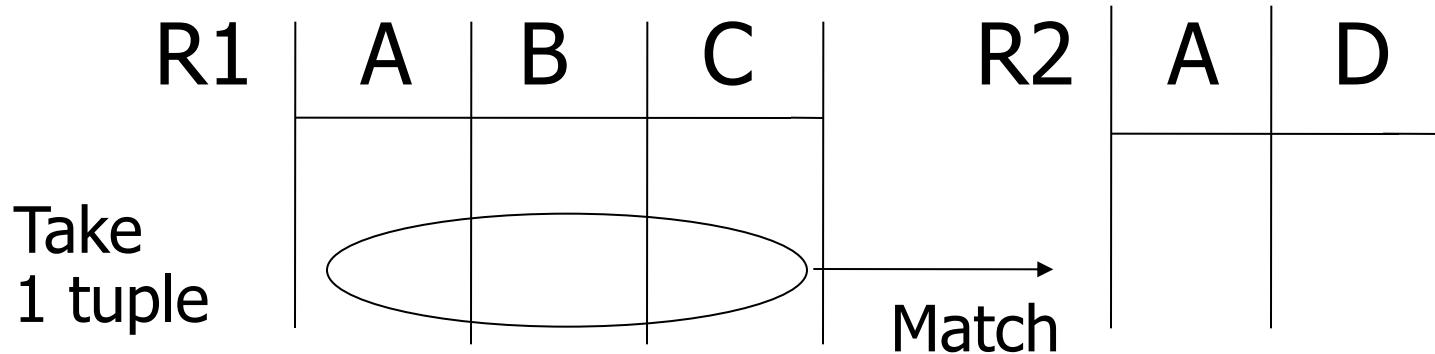
$V(R2, A) \leq V(R1, A) \Rightarrow$ Every A value in R2 is in R1

“containment of value sets” Sec. 7.4.4

Computing $T(W)$ when $V(R_1, A) \leq V(R_2, A)$



Computing $T(W)$ when $V(R_1, A) \leq V(R_2, A)$



1 tuple matches with $\frac{T(R_2)}{V(R_2, A)}$ tuples...

so $T(W) = \frac{T(R_2)}{V(R_2, A)} \times T(R_1)$

- $V(R_1, A) \leq V(R_2, A) \quad T(W) = \frac{T(R_2) T(R_1)}{V(R_2, A)}$
- $V(R_2, A) \leq V(R_1, A) \quad T(W) = \frac{T(R_2) T(R_1)}{V(R_1, A)}$

[A is common attribute]

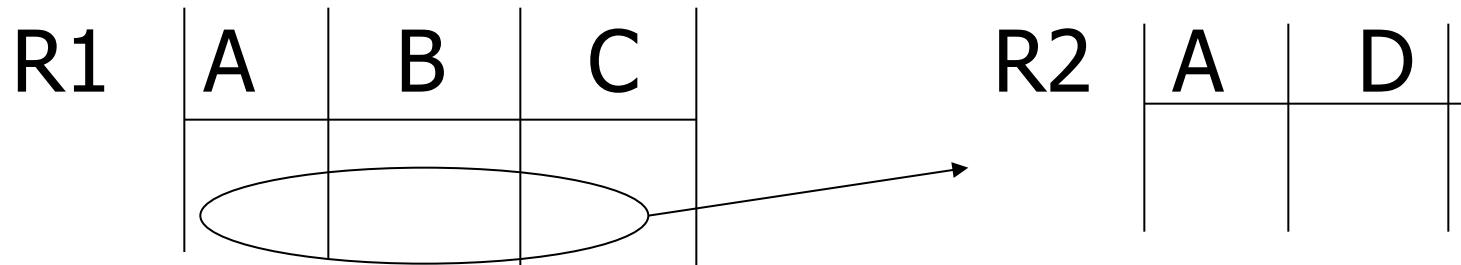
In general $W = R_1 \bowtie R_2$

$$T(W) = \frac{T(R_2) T(R_1)}{\max\{ V(R_1, A), V(R_2, A) \}}$$



Case 2 with alternate assumption

Values uniformly distributed over domain



This tuple matches $T(R2)/\text{DOM}(R2, A)$ so

$$T(W) = \frac{T(R2) T(R1)}{\text{DOM}(R2, A)} = \frac{T(R2) T(R1)}{\text{DOM}(R1, A)}$$

Assume the same

In all cases:

$$S(W) = \underbrace{S(R1)}_{\text{size of relation R1}} + \underbrace{S(R2)}_{\text{size of relation R2}} - \underbrace{S(A)}_{\text{size of attribute A}}$$

Using similar ideas,
we can estimate sizes of:

$\Pi_{AB}(R)$ Sec. 16.4.2 (same for either edition)

$\Sigma_{A=a \wedge B=b}(R)$ Sec. 16.4.3

$R \bowtie S$ with common attrs. A,B,C
Sec. 16.4.5

Union, intersection, diff,
Sec. 16.4.7

Note: for complex expressions, need intermediate T,S,V results.

E.g. $W = [\sigma_{A=a}(R1)] \bowtie R2$

Treat as relation U

$$T(U) = \underline{T(R1)/V(R1,A)} \quad S(U) = \underline{S(R1)}$$

Also need $V(U, *)$!!

To estimate Vs

E.g., $U = \sigma_{A=a}(R1)$

Say $R1$ has attrs A,B,C,D

$V(U, A) =$

$V(U, B) =$

$V(U, C) =$

$V(U, D) =$

Example

R1

	A	B	C	D
cat	1	10	10	
cat	1	20	20	
dog	1	30	10	
dog	1	40	30	
bat	1	50	10	

$$V(R1, A) = 3$$

$$V(R1, B) = 1$$

$$V(R1, C) = 5$$

$$V(R1, D) = 3$$

$$U = \sigma_{A=a}(R1)$$

Example

R1

	A	B	C	D
cat	1	10	10	
cat	1	20	20	
dog	1	30	10	
dog	1	40	30	
bat	1	50	10	

$$V(R1, A) = 3$$

$$V(R1, B) = 1$$

$$V(R1, C) = 5$$

$$V(R1, D) = 3$$

$$U = \sigma_{A=a}(R1)$$

$$V(U, A) = 1 \quad V(U, B) = 1 \quad V(U, C) = \frac{T(R1)}{V(R1, A)}$$

$V(D, U)$... somewhere in between

Possible Guess $U = \sigma_{A=a}(R)$

$$V(U, A) = 1$$

$$V(U, B) = V(R, B)$$

For Joins $U = R1(A,B) \bowtie R2(A,C)$

$$V(U,A) = \min \{ V(R1, A), V(R2, A) \}$$

$$V(U,B) = V(R1, B)$$

$$V(U,C) = V(R2, C)$$

[called “preservation of value sets” in
section 7.4.4]

Example:

$$Z = R1(A,B) \bowtie R2(B,C) \bowtie R3(C,D)$$

R1	$T(R1) = 1000$	$V(R1,A)=50$	$V(R1,B)=100$
R2	$T(R2) = 2000$	$V(R2,B)=200$	$V(R2,C)=300$
R3	$T(R3) = 3000$	$V(R3,C)=90$	$V(R3,D)=500$

Partial Result: $U = R1 \bowtie R2$

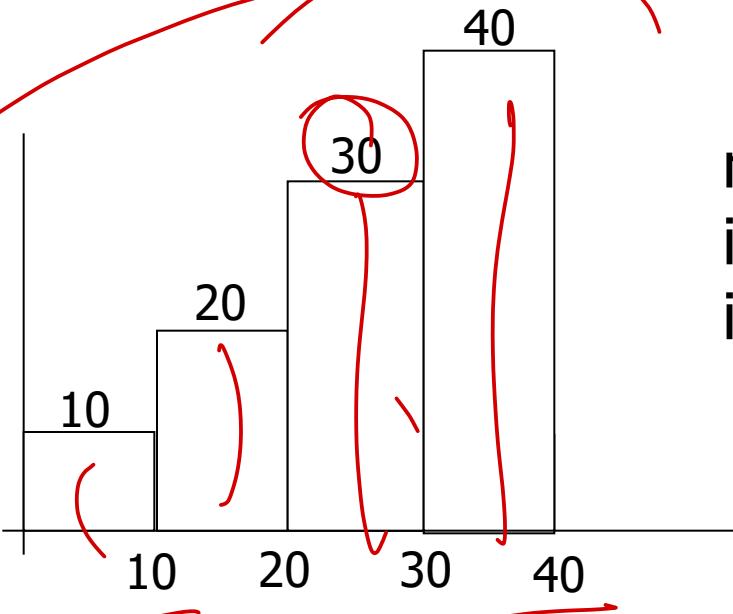
$$T(U) = \frac{1000 \times 2000}{200}$$

$$\begin{aligned}V(U,A) &= 50 \\V(U,B) &= 100 \\V(U,C) &= 300\end{aligned}$$

$$Z = U \times R^3$$

$$\begin{aligned} T(Z) &= \frac{1000 \times 2000 \times 3000}{200 \times 300} & V(Z, A) &= 50 \\ && V(Z, B) &= 100 \\ && V(Z, C) &= 90 \\ && V(Z, D) &= 500 \end{aligned}$$

A Note on Histograms



number of tuples
in R with A value
in given range

$$\sigma_{A=val}(R) = ?$$

$$\begin{aligned} A &\geq 30 \\ A &\geq 10 \Rightarrow 10 \end{aligned}$$

Summary

$\nabla C(R, A)$
 $A \leftarrow R$

- Estimating size of results is an “art”

- Don’t forget:

Statistics must be kept up to date...
(cost?)

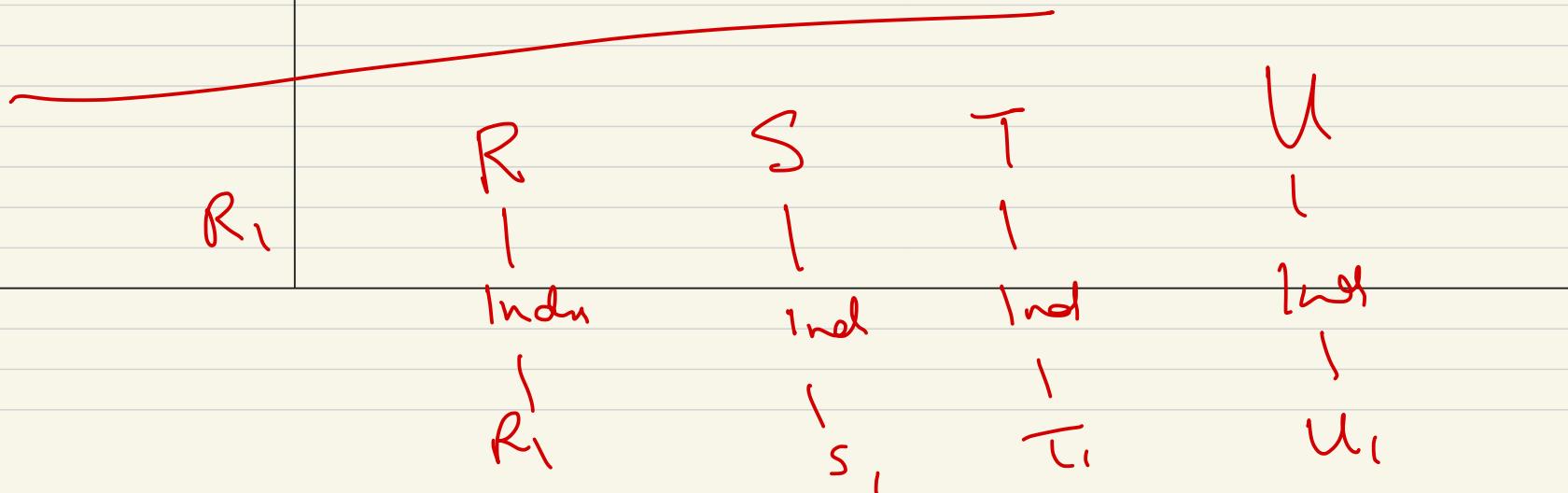
Outline

- Estimating cost of query plan
 - Estimating size of results ← done!
 - Estimating # of IOs ← next...
- Generate and compare plans

$$R \times_{\substack{(A=\text{val})}} R \times_{\substack{(B=\text{val})}} S \times_{\substack{(C=\text{val})}} T \times_{\substack{(D=\text{val})}} U \cong V(R_1, K_1) = V(R_1, K_1).$$

$$R_1 \times_{K_1} S_1 \times_{K_2} T_1 \times_{K_3} U_1$$

In der A, B, C, D



R

$\sigma_{A=val}$

R

S

$\sigma_{B=rd}$

S

T

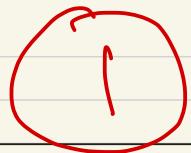
$\sigma_{C=sd}$

T

U

$\sigma_{D=sd}$

U



R

betw aces
medr

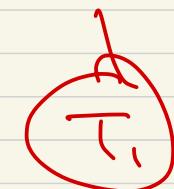


S

Lungs etc

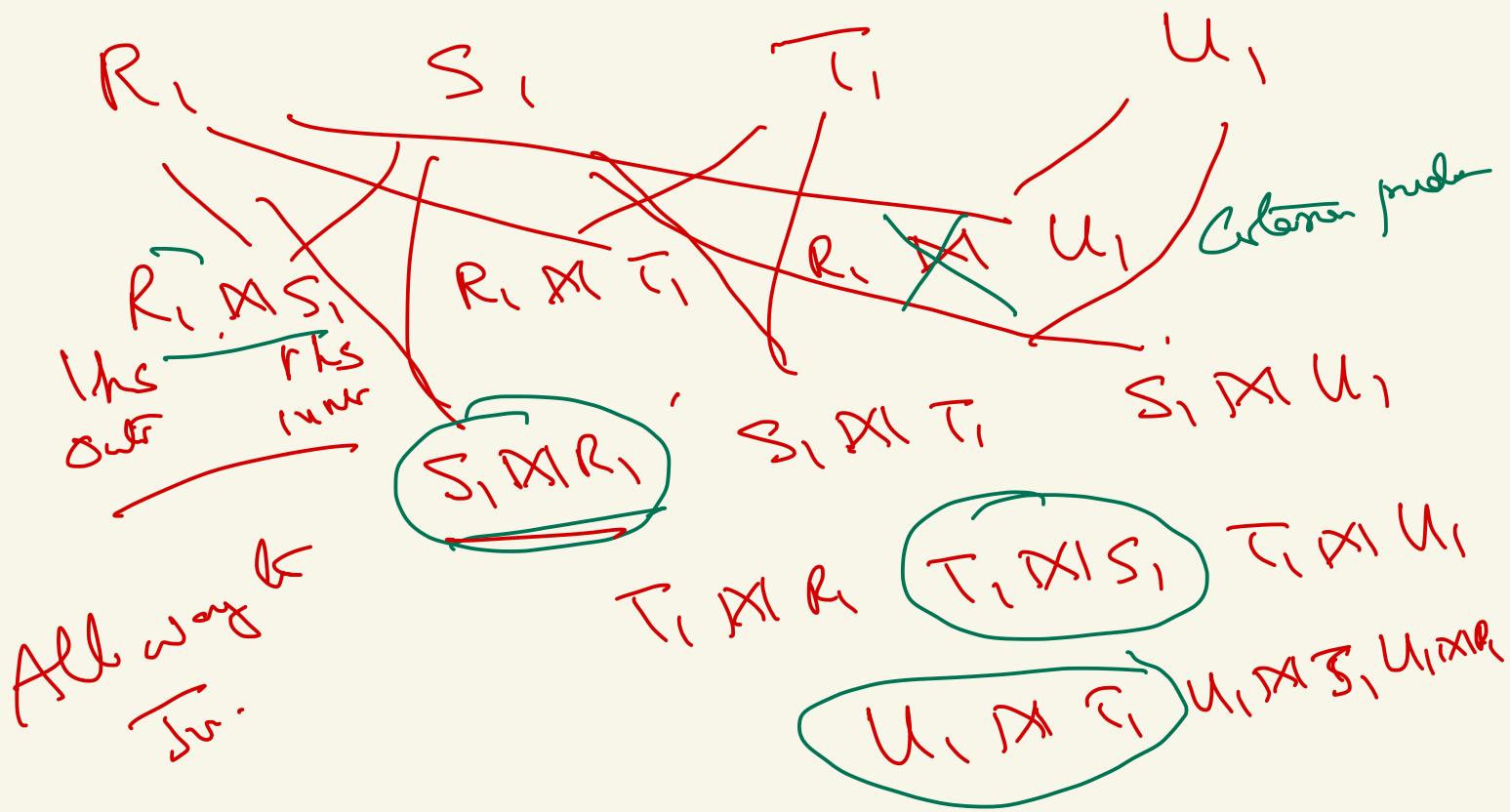


T

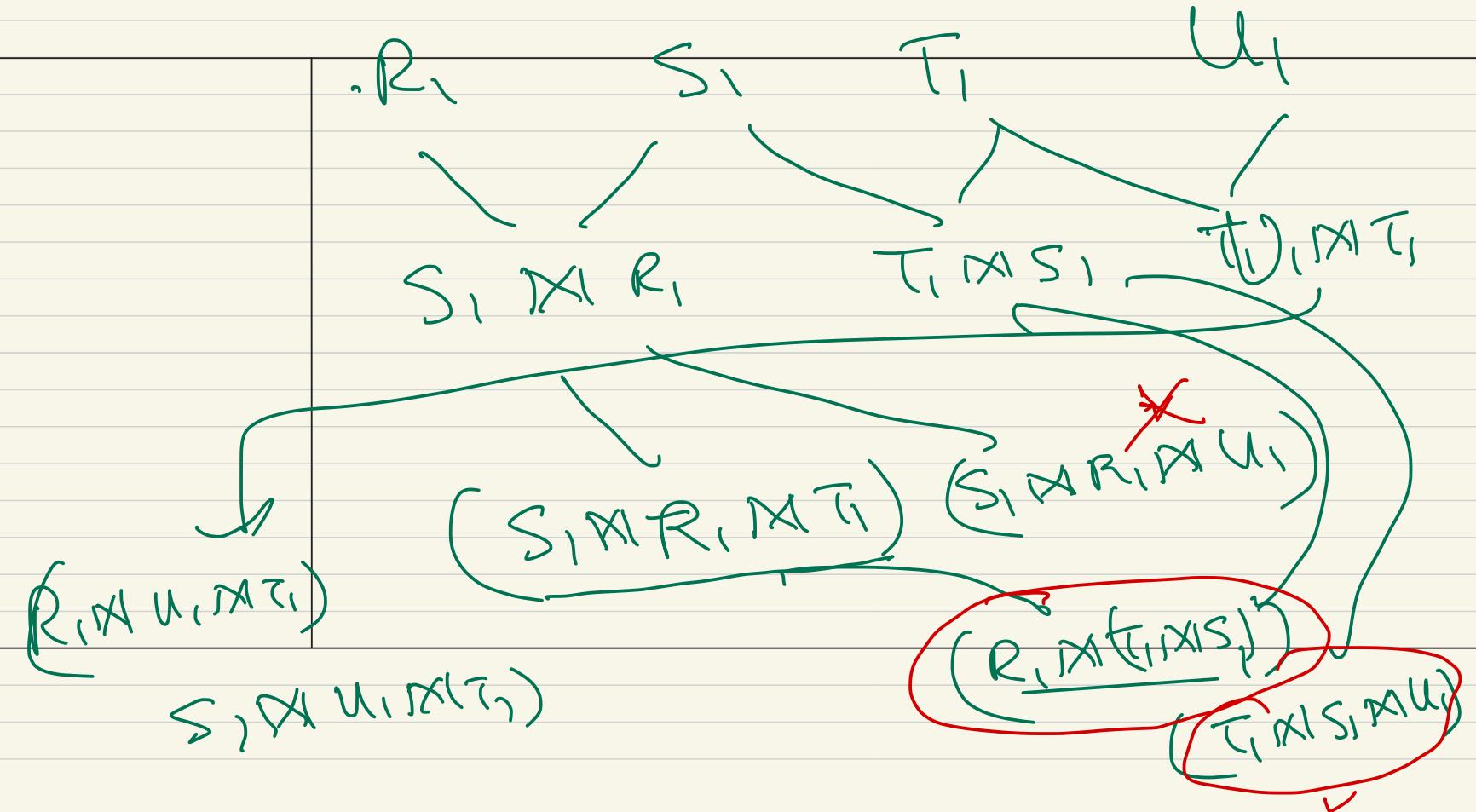


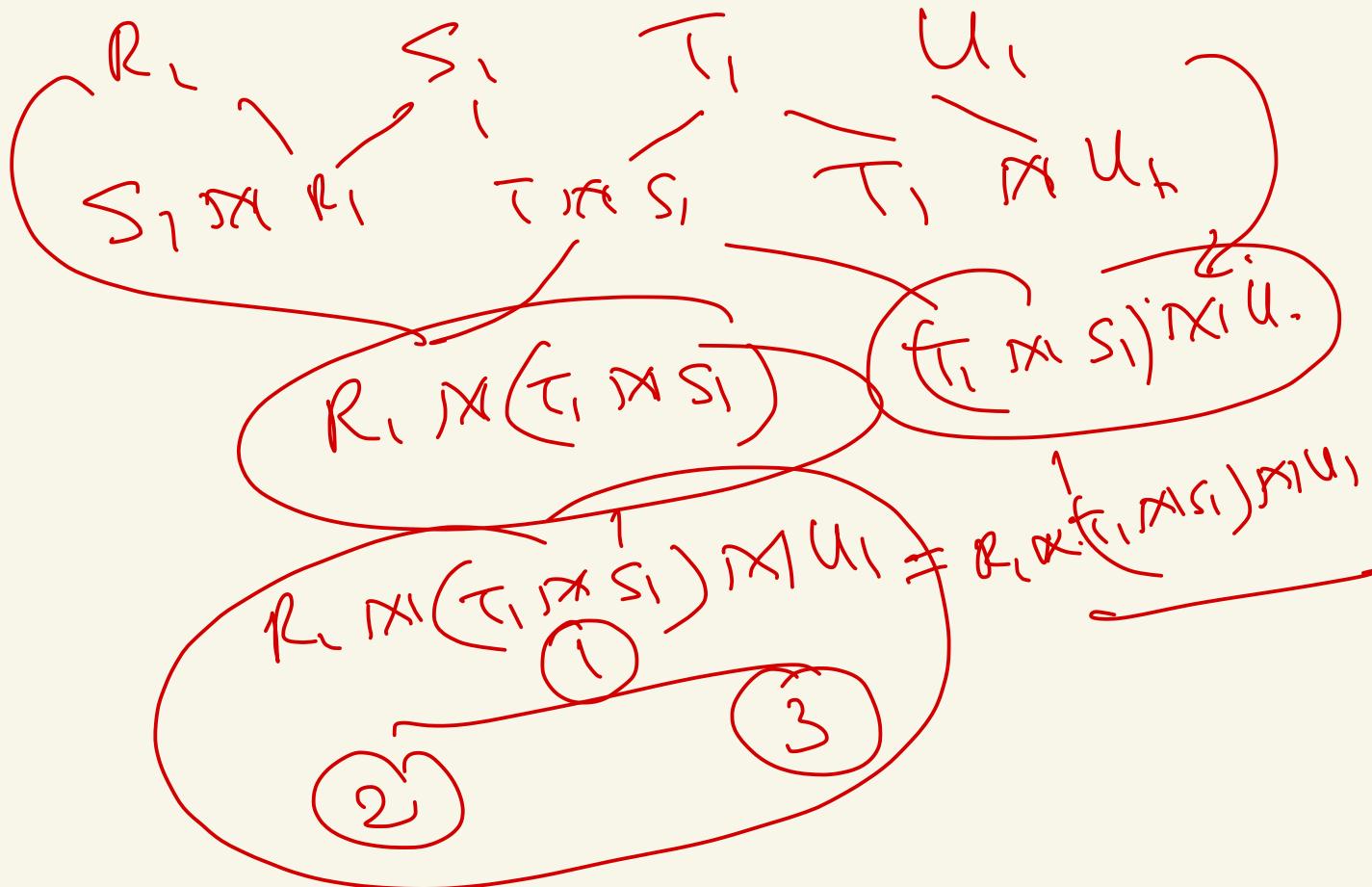
U





$$R_1 \cdot S_1 \equiv S_1 \cdot R_1$$





R_1 T_1 S_1 U_1



$R_1 \Delta (T_1 \cap S_1)$

$R_1 \Delta (T_1 \cap S_1) \Delta (U_1)$

$R_1 \times R_2 \times \dots \times R_n$

order on $R \setminus R$ is ordered on A

$$\frac{\sigma_{A=\text{val}}(R)}{\sigma_{A=\text{val}}(R)} \left| \begin{array}{l} \text{ind on } R \\ (c=2) \end{array} \right. \times \frac{\sigma_{B=\text{val}}(R)}{\sigma_{B=\text{val}}(R)} \stackrel{\text{ind on } R}{=} \sum_{i=1}^n \sigma_{\text{val}}(R_i)$$

$\sigma_{\text{val}}(R_i)$

Selbst Avg (Sal) from E.

$$\left(\overbrace{A = v_{d_1}^T R}^{C=0} \times \overbrace{S = v_{d_2}^T S}^{B=v_{d_2}} \right) \times \overbrace{T}^{E=F, C=v_{d_3}^T} \times \overbrace{\sigma(T)}^{C=v_{d_3}} \quad \text{Salary}$$

✓ $(R' \times I^S) \times T'$

✓ Cost $(R' \times I^S) \times T'$

$R \times (S \times T)$ ✓

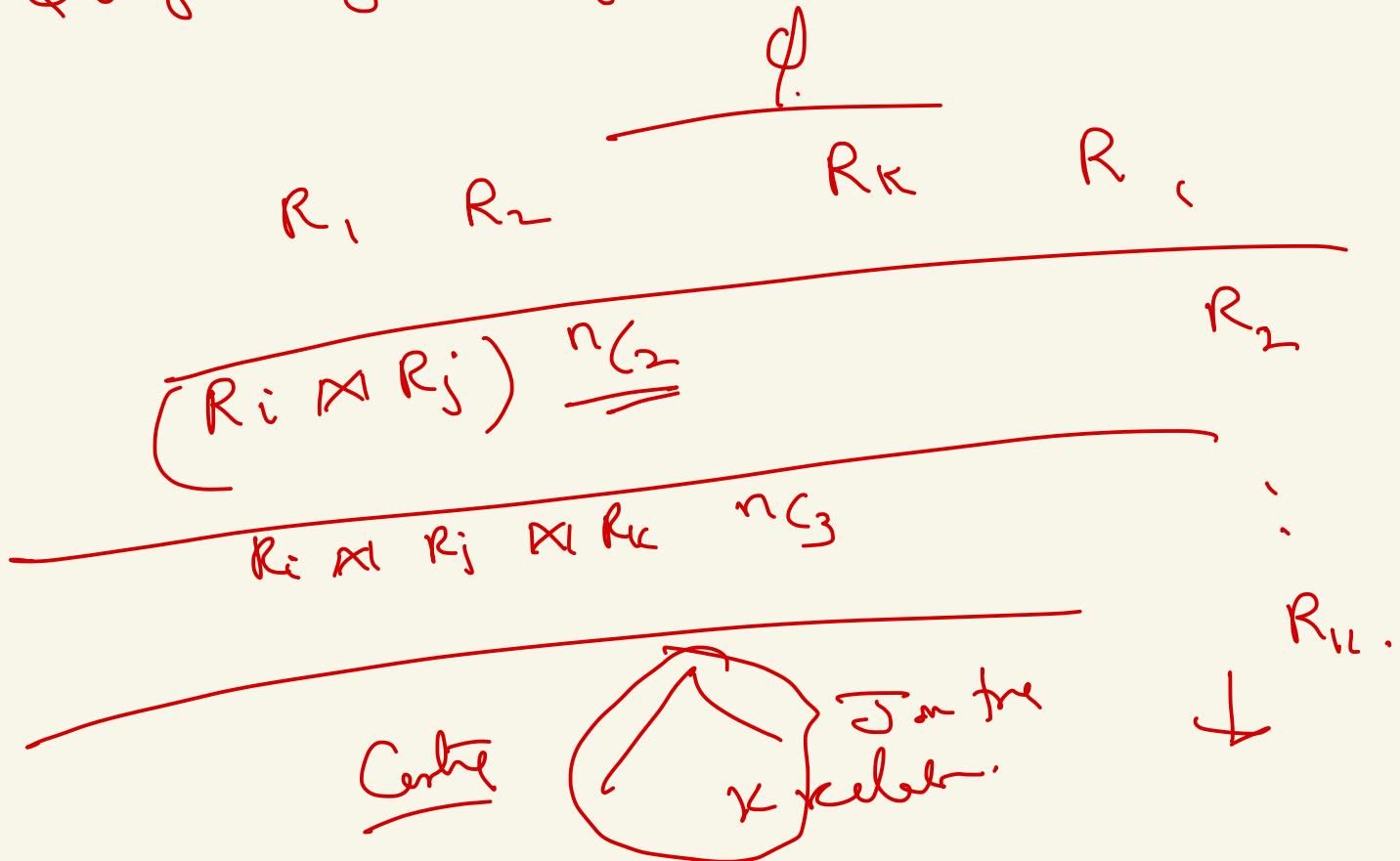
Cost $(R' \times I^S) \times T'$

Same

Equivalent Relational Algebra expression.

$R \times R_1 \times \dots \times R_k$. Now do you systematically get better solutions

Query Optimize Algorithm



$\text{Ind}(R_i) \leq \text{Scan}(R_i)$

R_i
 (Ind, A)

P

R_{iC}
 (Ind, C)

select the
last occur
method
✓ cut

$R_1 \bowtie R_n$ logical expres-
 $\text{NLJ}(C \text{ A scan } \& R_1) \bowtie \text{Scan}(R_i)$

$\cancel{R_i} \bowtie \cancel{R_j}$
 R_{i2}
Cut

Cut $(R_1 \bowtie R_2)$ Cut $(R_2 \bowtie R_3)$.

Cut $(R_1 \bowtie R_2) \bowtie R_3$ g.
Cut
 Σ

$(R_1 \bowtie C \text{ cut } (R_2 \bowtie R_3))$
Cut

Equivalent express.

$R_3 | R_1$ ③
 $R_1 \bowtie R_2 \bowtie R_3$.
 $(R_1 \bowtie R_2 \bowtie R_3) \vee$

$$T(R_1 \times R_2 \times R_3) \quad A \mid B \quad \text{when } S \text{ relevant}$$

$$\begin{aligned}
 & \left(R_1 \parallel R_2 \parallel R_3 \right) \parallel \left(R_4 \parallel R_5 \parallel R_6 \right) \\
 & \text{but events for } f = \left(R_1 \parallel R_2 \parallel \left(R_3 \parallel \left(R_4 \parallel R_5 \parallel R_6 \right) \right) \right) \\
 & \text{and } \left(R_1 \parallel \left(R_2 \parallel \left(R_3 \parallel \left(R_4 \parallel R_5 \parallel R_6 \right) \right) \right) \right) \\
 & \text{but events for } f = \left(R_1 \parallel R_2 \parallel R_3 \parallel R_4 \right)
 \end{aligned}$$

~~$T(R) \times T(C(R))$~~
~~more $(R_i, A), V(C(R))$~~ if relate
 but for $(R_1 \times R_2 \times R_3 \times R_4)$
 join if there is relation

$R_1 \propto R \propto \dots \propto R_n$



\rightarrow
 \rightarrow
 \downarrow

for $i = 1, \dots, K$
 (if $i=1$)
 [take R_i
 get its best plan.
 TempResult(R_i) $\leftarrow S$

if $i > 1$
 a) Take last TempResult $\leftarrow S$
 add a relab $R_i \notin \text{Temp Result}$
 determine cost $(R_i + \text{Temp Res relab})$
 $\leftarrow S$
 b) If there are equiv. result Tier the smallest
 Cost one in S .

$$((R \times S) \times T) \times U.$$
