CHAPTER FOUR

LOCIES OF SERVICES

John K. Kruschke Indiana University, Bloomington, IN, USA

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NIRODUCTION

One of the primary factors in the resurgence of connectionist modeling is these models' ability to learn input-output mappings. Simply by presenting the models with examples of inputs and the corresponding outputs, the models can learn to reproduce the examples and to generalize in interesting ways. After the limitations of perceptron learning (Minsky & Papert, 1969; Rosenblatt, 1958) were overcome, most notably by the back-propagation algorithm (Rumelhart, Hinton, & Williams, 1986) but also by other ingenious learning methods (e.g. Ackley, Hinton, & Sejnowski, 1985; Hopfield, 1982), connectionist learning models exploded into popularity. Connectionist models provide a rich language in which to express theories of associative learning. Architectures and learning rules abound, all waiting to be explored and tested for their ability to account for learning by humans or other animals.

incorporate rapidly shifting selective attention and and rational solution to the demands of learning many new associations as quickly as possible. This chapter describes three experiments (one previously to mimic learning by humans and other animals, it is also a highly effective tional redistributions. This kind of attentional shifting is not only necessary published and two new) that demonstrate the action thesis of results this chapter is that connectionist are fitted by connectionist models the learning of attentional learning. ability that shift to learn attenmodels and must learn

shut off. attention, but the results cannot be fitted when the attention mechanisms are

Shifts of attention facilitate learning

is retained, it generates a conflicting response, i.e. eating room? If the animal learns to associate both features of the with nausea, then it will inappropriately destroy part of its ledge about healthy mushrooms, i.e. the previous association texture to edibility will be destroyed. On the other hand, if the nausea. How is the animal to quickly learn about this new room, without destroying still-useful knowledge about the old kind of mushwith a smooth texture but a flat top. This using this knowledge for some time, the animal encounters a new mushroom round top and smooth texture hypothetical situation in which an animal for any creature that confronts a rich and c A basic fact of learning is that people quickly learn new associations without rapidly forgetting old associations. Presumably this ability is highly adaptive are tasty and omplex environment. Consider other hand, if the old association mushroom turns nutritious. After successfully association from smooth that mushrooms with the mushroom. the new mushroom previous knowkind of mushout to induce

attention to the flat top, away from the smooth texture. This will allow animal to properly anticipate nausea, and to avoid the mushroom." model. exactly this kind of attentional shifting during learning. third example in this chapter describes a selectively attend to the distinctive feature, mal encounters a mushroom with smooth texture shifted attentional distribution should itself ate this feature with nausea. By selectively theorist is expressing these intuitions ture, previous knowledge is preserved, and To facilitate learning about the new case, it should attention be shifted in this way about viz. flat top, and learn to new attending to the distinctive feasituation in be learned: Whenever the oto attention in would be advantageous to learning is facilitate and flat top, it should shift The challenge to which people learning, a fully facilitated. specified but the assocıanı-Not use the

earning of attention can be assessed b subsequent

is being strongly attended to, then that feature should have a strong influence synonymously. This treatment is a natural c influence of attention on learning is sometimes referred to an immediate response and the influence of a feature on learning. If a feature associability. The term "attention", as used here, refers to immediate response and on the In this chapter, these two influences imminent learning. both the influence of a feature onsequence of the of attention asconnectionist the feature's This are treated latter

> models described below, but the treatment inappropriate in the face of future data. might ultimately turn out to be

to the now-irrelevant feature. In general, learned attention to features or dimensions can be inferred from the ease with which subsequent associations are learned. This technique is used in all three examples presented below. vant to new responses, then learning about this new correspondence should be relatively slow, because the person will have to unlearn the attention given attend to that feature. If subsequent training makes of an appropriate response, then, presumably, the person has also learned to ing ability. If a person has learned that a particular feature degree of attentional learning can be assayed by examining subsequent learn-Because redistribution of attention is a learned response a different feature is highly indicative to stimuli, the

INTRA- AND EXTRADIMENSIONAL SHIFTS

attentional learning mechanism is "turned off" learning is shown to fit the data, whereas the model cannot fit the data if its ence is summarized, and a connectionist model that shift perseverates into the second phase (e.g. Mackintosh, 1965; Wolff, 1967). In this section of the chapter, a recent experiment demonstrating this differthan extradimensional shift, a fact that can be explained by the hypothesis that subjects learn to attend to the relevant dimension, and this attentional Many studies in many species have shown that intradimensional shift is easier extradimensional shift, and the latter change is called intradimensional shift. dimension remains dimensions learned attention across phases of training. In the learn that one stimulus dimension is relevant to t outcomes changes so that either a different dimension is relevant or the same A traditional learning paradigm in psychology investigates perseveration of are irrelevant. In the second phase, the mapping of stimuli to relevant. The former change the outcome while other incorporates attentional first phase, participants of and this attentional relevance SI. called 1967).

Experiment design and results

car would appear on a computer screen, the learner would make his/her choice of the route of the car by pressing a corresponding key, and then the correct route would be displayed. During the first few trials, the learner could 4.1. They vary on three binary dimensions: height, door position, and wheel color. In an experiment conducted in my lab (Kruschke, 1996b), people only guess, but after many trials, she/he could learn the correct answers. learned to classify these cars into one of two routes. Consider the simple line drawings of freight train box cars shown in Figure On each trial in a series, a

Figure 4.2 indicates the mapping of cars to routes. correspond with the cube shown in Figure 4.1. Each corner is marked with a The cubes in Figure 4.2

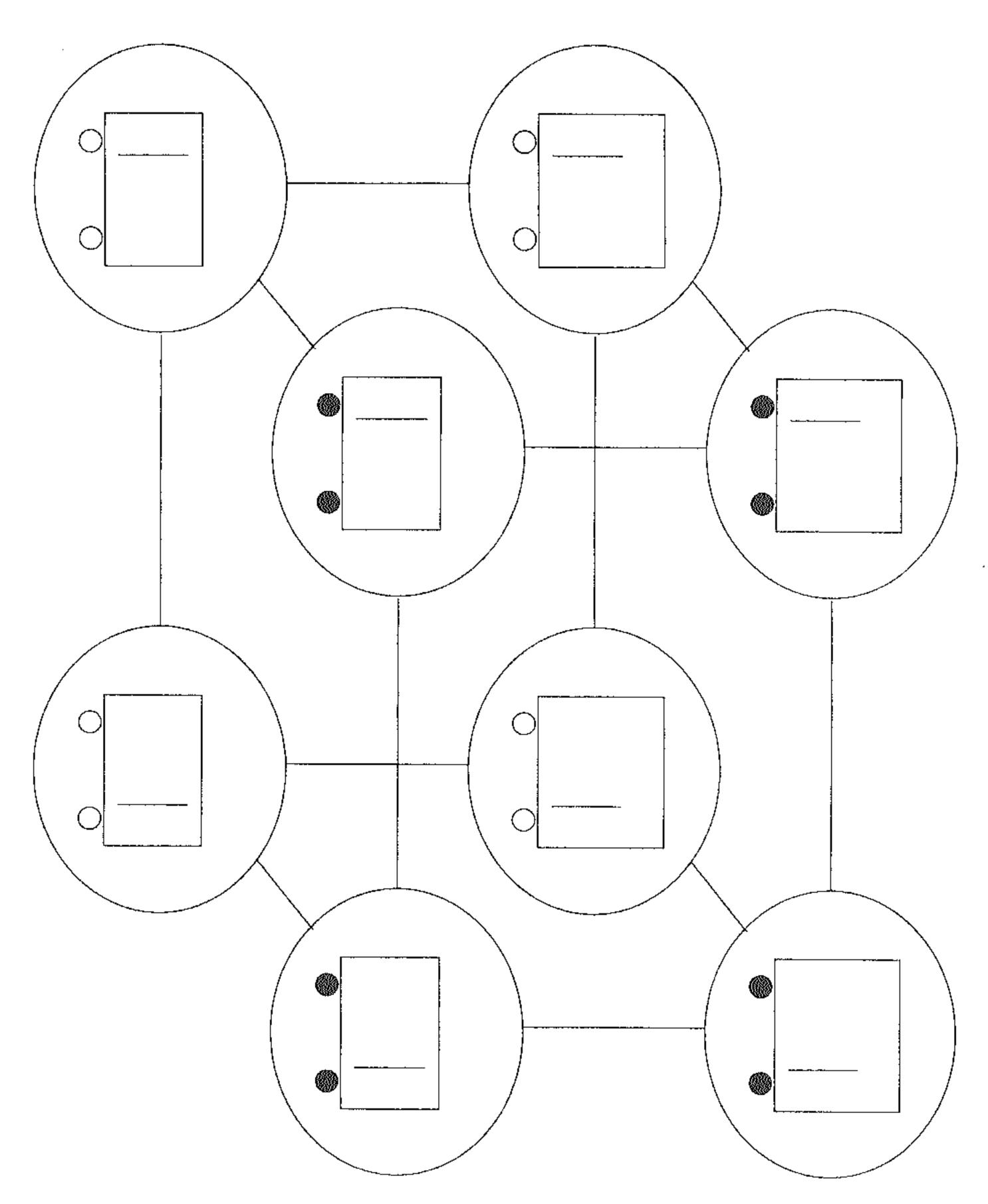


Figure demarcate the indicate Stimuli used for relevance shift the dimensions of different stimuli and are variation between sti not part of the experim muli. ent stimuli ofruschke per se. (1996b). The lines The connecting the ovals merely

disk whose words, color the color of the indicates the disk route indicates take by category the corresponding the stimulus. train; Ξ.

phase irrelevant. sequently. loss in categorization accuracy. The other (XOR) structure variation vant in The left side of Figure 4.2 shows of the training, in categorization: This means In the first phase. on the two relevant dimen first and phase, Some readers that variation on the the right side The can vertical d might be show the se en categorization OW/O imension recognize the vertical dimension that dimensions, categorization the can this vertical be learned $\mathcal{Z}_{\mathcal{S}}$ however, **ignored** the dimension produces learned exclusive-or Ħ the are with no rele dus O

initially irrelevant, the initially dimension is relevant, mensional, bottom-right structure. right structure the subsequent whereas relevant of Figure so the shift of relevance I phase, dimensions, but in the top the In both of these 4 bottom some learners and other lea SO shift shift ti the secondhift his rners S he experienced called newly relevant ofexperienced relevance phase extradimensional. relevant dimension structures change S a change dimension called was only the ıntradi-Notice one was one the

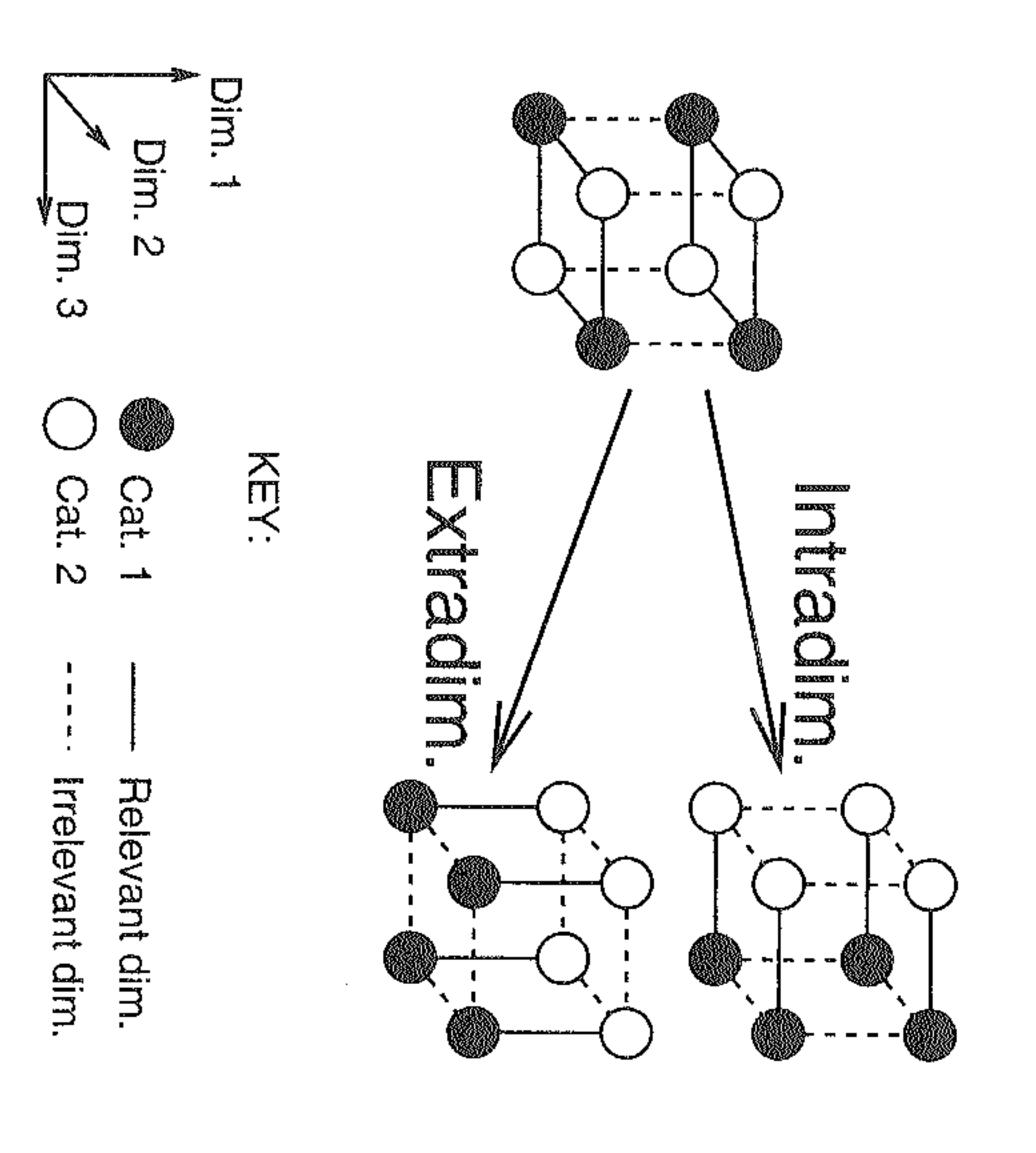


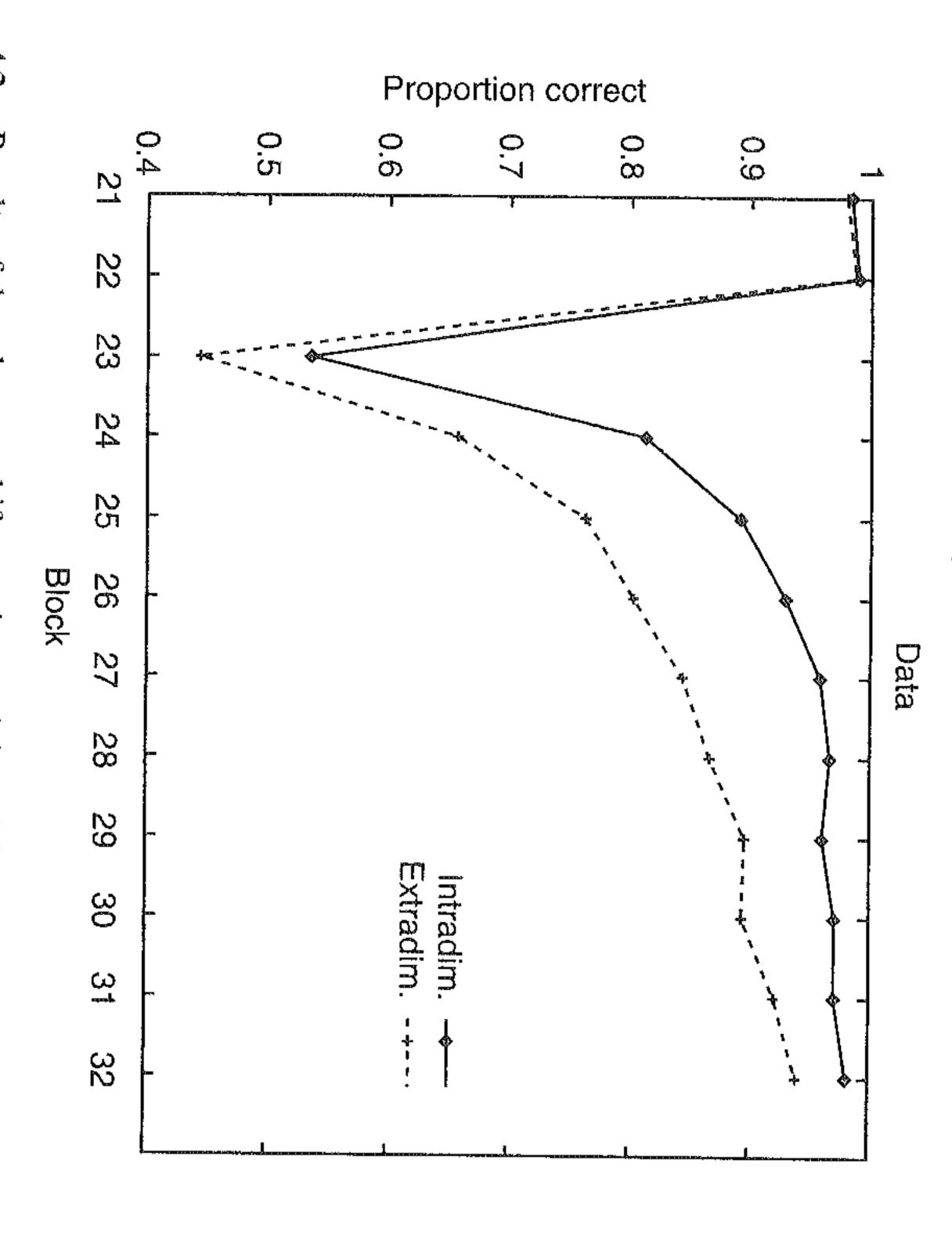
Figure 4.2. The structure of two types of relevance shifts. The cube at left indicates the initially learned categorization; the cubes at right indicate the alternative subsequently learned categorizations. Adapted from Kruschke, 1996b.

that the two second-phase category structures are isomorphic, so any differences in ease of learning the second phase cannot be attributed to differences in structural complexity.

relevant dimensions, and no novel values at all in the shift phase. new design solves these implement an intradimensional shift, relevant dimension, it might be the case that differences in learnability of the dimensions were caused by differences in novelty. If novel features are added and blue indicates Y. Unfortunately, if novel features are ment of categories to colors, is to add novel colors; e.g. yellow dimension. For example, the initial phase might have or green indicating category X and red indicating category the novel values to attributable to differences in degree of novelty, or differences in similarity of sional and extradimensional shifts can be directly founded changes in novelty. In traditional studies of intradimensional shift, because no novel stimulus values are used in either both dimensions, it might be the case that differences in learnability This shift is accompanied by introduction of design is <u>a</u>n the previous values, advance over problems by making the initial problem all without and so forth (Slamecka, 1968). previous novel values on the merely studies shift. compared without conreversing added to the initially color relevant, Y. The only way to Thus, intradimenof shift \sim involve two indicates the learning relevant assignwith are

Human learning performance in this experiment is shown in Figure 4.3. It can be seen that people learned the intradimensional shift much faster than the extradimensional shift $[t(118) = 3.65, SE_{diff} = .026, p < .0001 \text{ two-tailed}].$

Notice that the advantage of the intradimensional shift over the



Results of the relevance experimen Adapted from Kruschke,

extradimensional shift extradimensional their one relevance Jud the learning possibl Shif ance results elevance was types by explanation for which the in the intradimensional shift, even more from there number ---only the another were of difficult extradimensional two the four exemplars that condition difference dimensions exemplars than the Ħ S

learning that purports particularly advantage many compelling previous intradimensional because studies learning by the design over o other species, involved no natural intelligent organisms. extradimensional shift has addressed but the confounded variation уd results any model here been

connectionist model with attentional learning

implement expe advantage of intradimensional shift phase $\ddot{\mathbf{S}}$ learned exp. lanatory attention S principle. dimensi learn over y ons. \mathbf{S} extradimensional shift the model nonlinear XOR model ofcategory H the of learning should the relevance-shift two structure suggests relevant

> dimensions, meaning that no simple additive combination of the two relevant dimensions can accurately compute the correct categories. Instead, conjunctive combinations of dimensional values must be encoded in the model. There has been much research that suggests that people can and do encode configurations of values, also called exemplars, during learning (e.g. this notion of exemplar representation, along with attention to dimensions. Nosofsky, 1992). The model to be fitted to the shift-learning data formalizes the notion of learned

ism can be functionally removed, and the restricted model can be tested for its the corresponding aspect of the model. In particular, the attentional mechanhave specific psychological motivations, and formalize explicit explanatory principles. Because of this correspondence between model parts and explanaability to fit to data. tory principles, because it is a variant of the ALCOVE model (Kruschke, 1992). The architecture of (part of) AMBRY is shown in Figure 4.4. All aspects of the model The model fit to these data was called AMBRY by Kruschke (1996b) the principles can be tested for their importance by excising

Activation propagation

activation of input node i is simply that scale value: denotes the psychological scale value of the stimulus on dimension i, then the AMBRY, each dimension is encoded by a separate input node. }------ Ψ_i

$$a_i^{\rm in} = \psi_i. \tag{1}$$

sions in Figure 4.1 to abstract dimensions in Figure values were simply assumed to be 1.0 and 2.0; e.g. Because the experiment counter-balanced the assignment of physical dimen-1.0, and for the tall car, $\psi_{\text{height}} = 2.0$. for the short car, ψ_{height} 4.2, the dimensional

plar node is significantly activated only by stimuli that are fairly similar to the exemplar represented by the node. In other words, each exemplar node has a limited "receptive field" in stimulus space. Formally, the activation value is chologically separable dimensions (Garner, drops off exponentially with distance in psychological space, as argued by Shepard (1987), and distance is computed using a city-block metric for psyactivation of an exemplar node corresponds to the psychological similarity of the current stimulus There is one exemplar node established for each of the eight cars. to the exemplar represented 1974; Shepard, фy the node. Similarity 1964). An exem-The

$$a_j^{\text{ex}} = \exp\left(-c\sum_i \alpha_i^j |\psi_{ji} - a_i^{\text{in}}|\right) \tag{2}$$

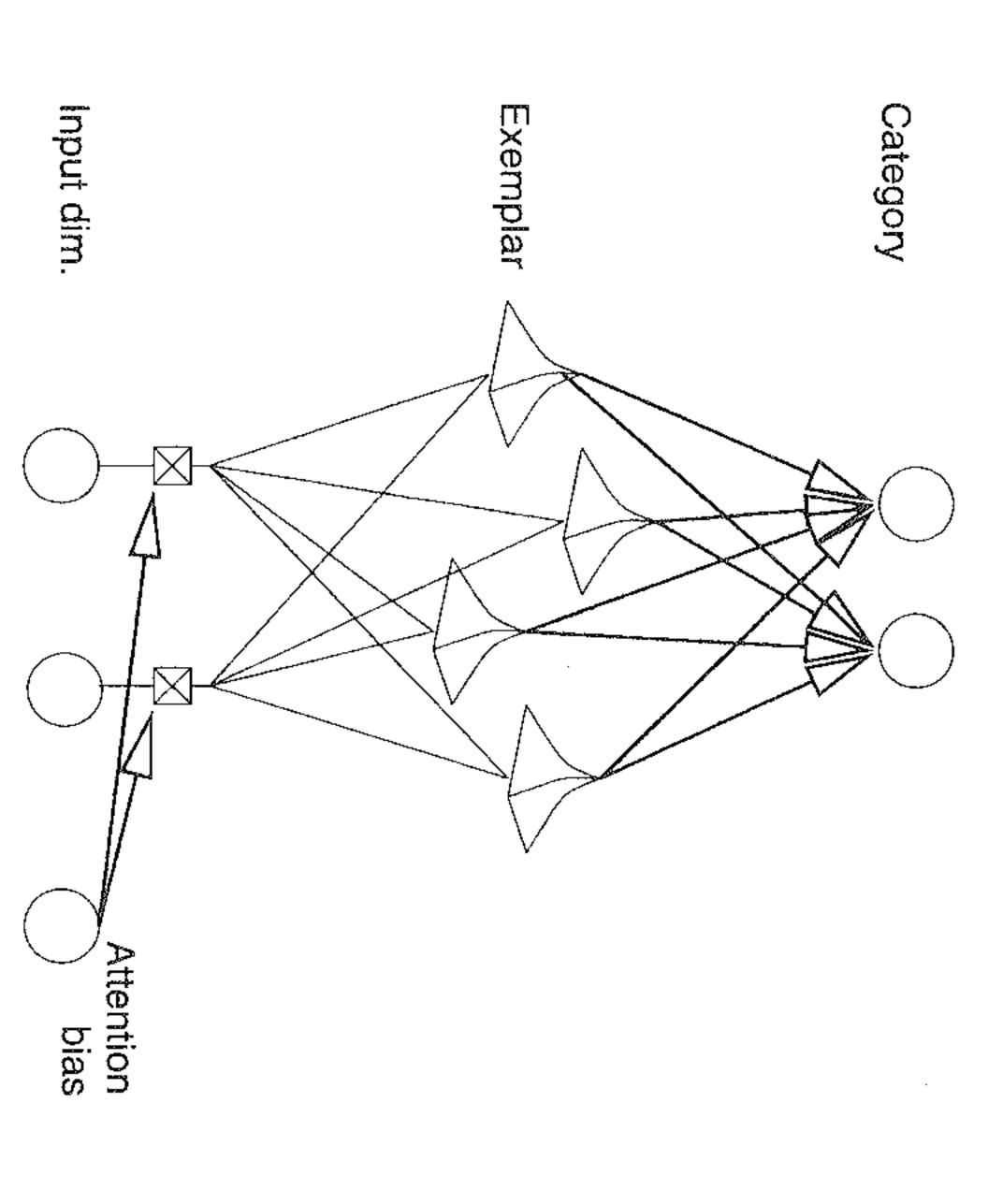


Figure 4.4. Architecture of model used for predictions of relevance shift experiments. Thicker arrows denote learned associative weights. The Xs in boxes above the input dimensions represent the multiplicative weighting of the attention on the dimensions.

stimulus where ψ_{ji} receptive Figure is the values a constant called field, scale are shows where α_i is the value of either the the specificity . activation the jth exemplar 0r attention 2.0, 닭 űď ofile strength hat determines the 9 the exemplar dimension. ith dimension the are narrowness either node Because and

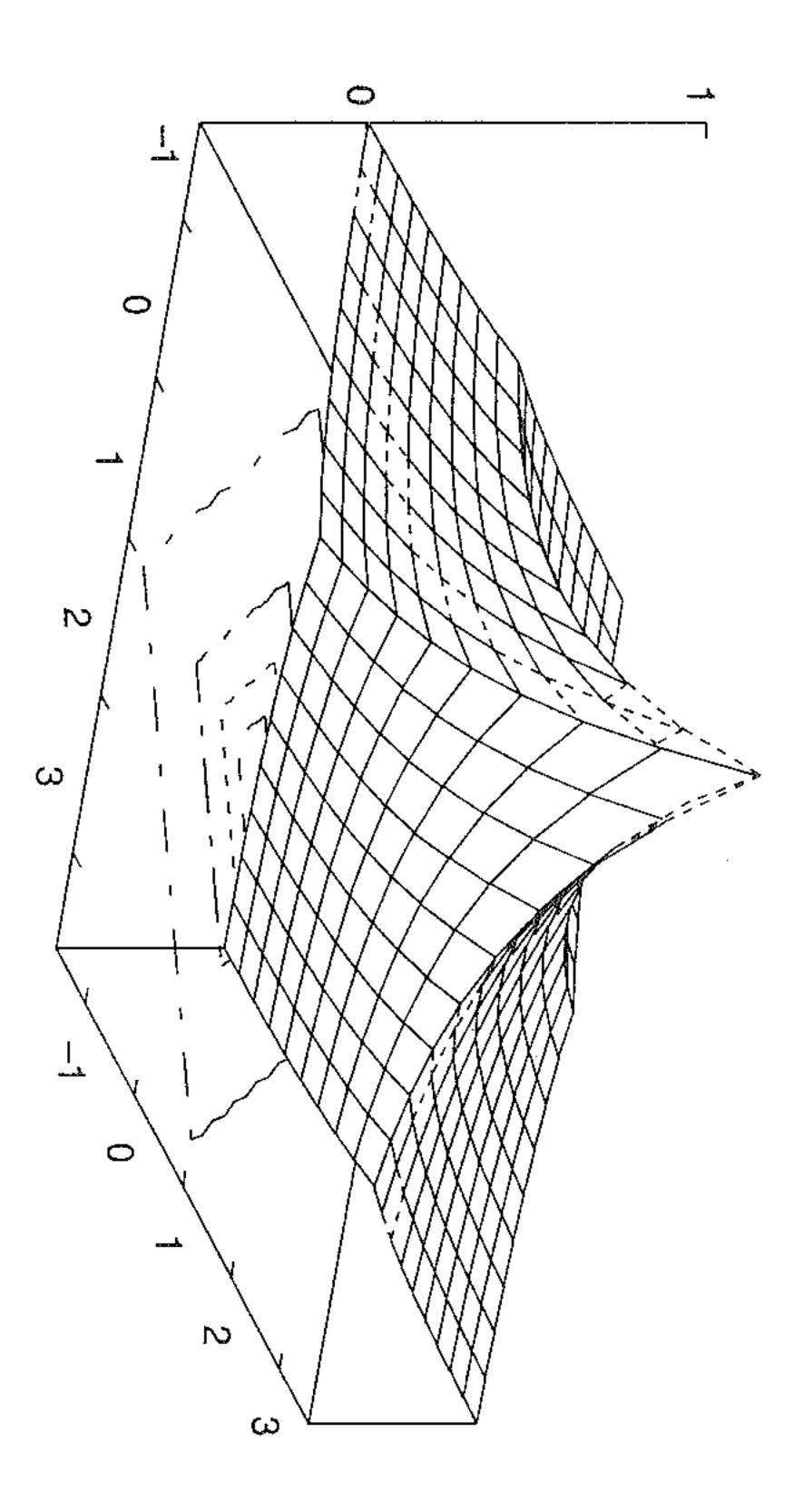


Figure 4.5. Activation function of an exemplar node. The surface shows a_j^{ex} as a function of a_l^{in} and a_2^{in} , from equation (2) applied to a two-dimensional stimulus space, with c = 1, $\alpha_l = 1$, $\alpha_l = 1$ and $\psi_{j1} = 1$ and $\psi_{j2} = 1$. The diamonds on the plane underneath the surface indicate the level contour of the surface.

two-dimensional stimulus space. It is this pyramid-shaped activation profile that is used to represent the exemplar nodes in Figure 4.4.

is always activated) to the boxes marked with Xs above the input modes. The multiplier on the input. the dimensional attention strengths to facilitate categorization. The attention boxes are marked with Xs strengths are indicated in Figure 4.4 by the arrows from a "bias" node (which impede learning. As will be explained below, AMBRY tion decreased, so that differences along that dimension do not needlessly that dimension can be increased to better distinguish the exemplars from the that differences along the dimension have a larger influence on the similarity. two categories. On the other hand, an irrelevant dimension can have its atten-Thus, if a dimension is relevant to a categorization, a dimension has the effect of magnifying differences on that dimension, Importantly, equation (2) implies that increasing to indicate that each attentional the attention strength on the attention strength on learns how to adjust strength is

Activation from the exemplar nodes is propagated to category nodes via weighted connections, illustrated in Figure 4.4 by the arrows from exemplar nodes to category nodes. The activation of each category node is determined by a standard linear combination of weighted exemplar-node activations. Finally, the activations of the category nodes are converted to choice probabilities by a ratio rule, such that the probability of choosing a category corresponds with the activation of the category relative to the total activation of all categories. The mathematical details of these operations are not critical for the present discussion, and can be found in the original article (Kruschke, 1996b).

Learning of attention and associations

(1996b).the associative weights in such a way that the error is reduced as compossible. Not necessarily all the error is eliminated on a single trial. ing the derivative of the error with respect to th associative weights. Formulae for these derivatives are provided by stitutes an error. The model then adjusts the dimensional attention values and Just as human learners are told the correct answer on each trial, the model is told the desired activation of the category nodes on each trial. Any discrepof error reduction is called "gradient descent" ancy between the desired activation and the model-generated activation conare learned by standard back-propagation of error The association weights between the exemplar nodes and the category nodes because it is based on comput-(Rumelhart et al., 1986). attention strengths quickly as Kruschke This type

Of importance here is to note that the learning of the attention strengths is based on error reduction, and the amount or speed of learning is governed by a single parameter called the attentional learning rate. When this attentional

learning rate is fixed at zero, the model has no ability to learn to selectively attend to relevant dimensions (but it can still learn categorizations because of the learnable association weights between exemplars and categories). By testing whether the model can fit the empirical data with its attentional learning rate set to zero, we can discover whether attentional learning is an essential principle in the model.

This model is an algorithmic description of learning. The model makes no claims about physical implementation. Different species might neurally implement the algorithm, or approximations to the algorithm, in different ways. In particular, there is no claim that nodes in the model correspond to neurons in the brain, neither is there any claim that gradient descent on error is implemented as back-propagation of error signals through neural synapses. The model is therefore referred to as a type of *connectionist* model, and is never referred to as a *neural network* model.

Fit of the model

shift is more difficult for the model. learning in the first phase to attend to the ignore the irrelevant dimension. This learned the predictions would be even closer to the here. If AMBRY were fitted only to the i The top graph of Figure 4.6 shows the pretage of intradimensional shifts very robustly. unlearned in the extradimensional shift, a AMBRY is simultaneously fitted to two or shown in Figure 4.3. (In fact, shift accommodates conditions, not discussed extradimensional shifts distribution must dimensions data

Attentional learning is critical to account for the data. When the attentional learning rate is fixed at zero, the best fit of the model exhibits no difference between the types of shift, as can be seen in the bottom graph of Figure 4.6. The best the model can do without attentional learning is settle on the mean of the two types of shift.

BLOCKING OF ASSOCIATIVE LEARNING

learn that A by itself predicts the outcome, B seems to be very weak. It appears th come. Typically both cues will acquire mod Suppose two predictive of the outcome as A. The pheno blocked, i.e. prevented, learning about B, d paradigms and in many different species. Kamin (1968), is ubiquitous, occurri On the other hand, if the subject cues, A and B, are presented of lockin training that previous first trength now reported

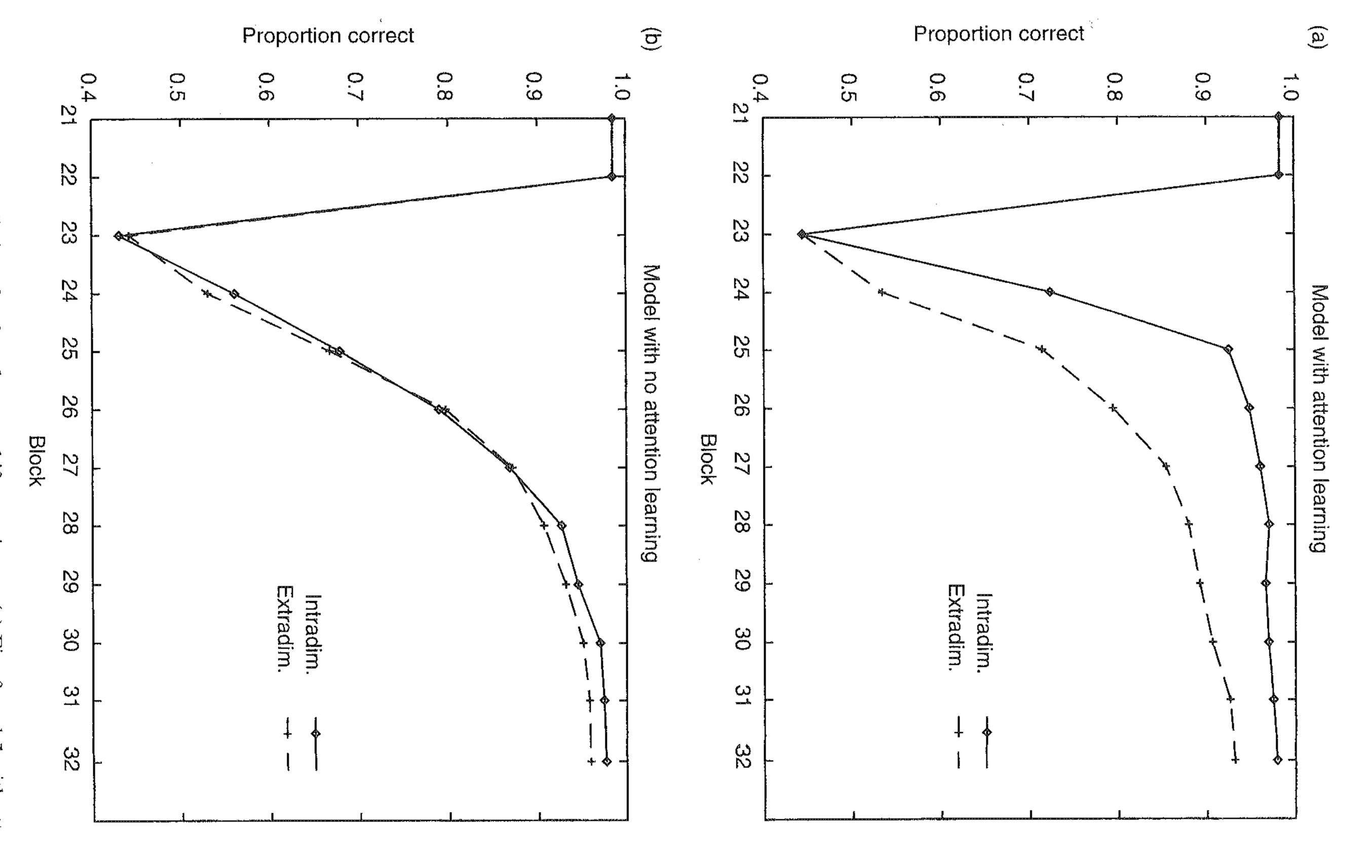


Figure 4.6. Model predictions for the relevance shift experiment. (a) Fit of model with attentional learning. (b) Fit of restricted model with no attentional learning. Adapted from Kruschke, 1996b.

strength whenever a cue and outcome coing is not based on merely the co-occuri p. 618). Blocking is important because it contradicts a whole raft of learning theoretical importance than the phenom "No empirical finding in the study of models ence. shows clearly that associative learnanimal learning that increment associative cue and outcome. blocking" (Williams, of This fact 1999

is error-driven. Because the subject has the outcome, when cue B occurs there is and equivalent to the delta rule of connec (Miller, Barnet, & Grahame, 1995; Siegel & Allan, A competing theory, first suggested by Sutherl learning. The Rescorla-Wagner model was motivated to a large degree by phenomenon of blocking, and the mode For more than 30 years there have been a second the dominant theory, formalized in l has O already learned that cue A predicts the Rescorlaerror in prediction and hence been monumentally prominent theories models, 1996). -Wagner argues that learning model (1972) influential

expanded their experimental design sequent learning. Mackintosh & Turner shifts, learned attention can be assessed emphasized in the previous section reg and extended by Mackintosh (1975), claims learned about the redundant relevant c non-blocked control cue. cue. Learning about a blocked cue was other words, subjects learn to suppress attention to the redundant cue. As robust evidence that people favor of the learned attention theory. Kr viously blocked cue could be learned about by rats, and found evidence in learn Ħ much arding intra- and interdimensional ue; namely, that it is irrelevant. (1971) measured how quickly by measuring the difficulty suppress that there weaker land & with humans, Blair (2000) extended and attention than learning <u>s</u>. Mackintosh (1971) Ξ. fact something to and ω about blocked ofa presub-

results demonstrating the effects of bloc tion. Models of natural learning should connectionist model that uses learned att model cannot exhibit the critical effects. attention. The will be shown that when attentional learn This ubiquitous learning phenomeno remainder of this section incorporate blocking, reports in the on subsequent learning, s in the model previously mechanisms of involves learned attenprevious "turned off" unpublished section, learned and a

Experiment design and results

indicated certain fictitious diseases. A learning trial might consist lowing sequence of events. First, a list of symptoms is presented corresponding key. puter screen, e.g. In an experiment conducted in my lab, p indicate which disease he/she thought wa "back pain" Then the correct resp and "blurred vision". correct diagnosis, had to learn which displayed The is presented on subject would the by of pressing screen. the tol-

> the initial trials the person would just be guessing, l could learn the correct diagnoses. but after several trials she/

symptoms B and D (denoted B.D \rightarrow 3). The two diseases share symptom B, structure is present for diseases 5 and 6: H.F letters, and diseases are indicated by learn to discriminate diseases that share a symptom. Thus, disease phase of training. The central aspect of the third phase is that people must cated by symptoms B and C (denoted B.C \rightarrow Table 4.1 shows the design of this experiment. Symptoms are indicated by ters, and diseases are indicated by numerals. I will first describe the third therefore learning the diseases might be somewhat difficult. \rightarrow 5 and H.G -2), and disease 3 is indicated \downarrow 6 The 2 is indithird

symptoms were suppressed, then discrimination learning should symptom B should by paired with symptom A as a redundant relevant cue, cates disease 1, which is contrast, the first two phases are designed to block pression of attention. Notice that in the first phase, learning should be easier. On the other hand, if attention to the symptom B should by blocked, and should suf Hence, subsequent learning of B.C \rightarrow 2 and B.D \rightarrow The first two phases of training were designed to bring about just such supand G, so that learning of H.F attention to the shared symptom were suppressed, denoted $A \rightarrow 1$. In the second phase, ψ 5 and H.G. suffer 6 should be worsened. 3 should be enhanced. By the distinctive symptoms symptom A always indisuppressed i.e. A.B then discrimination symptom B \downarrow be distinctive attention. **}----**-\ harder. Hence

and G. strengths can be directly assessed. In these cases, of association established for the diseases that had a diseases associated with vs. the diseases that had blocked distinctive symptoms. The final testing phase is an additional assessment of the relative strengths and D.G present conflicting symptoms, and D more than the diseases people blocked shared symptom SO The test that associated with should select the their cases relative

Design of experiment assessing discrimination learning after blocking TABLE 4.1

		Testing			Training III (discrimination learning)		Training II (blocking of B, F, and G)	Training I
C.F, C.G, D.F,	A	B.C, B.D	$A \rightarrow 1$	$B.D \rightarrow 3$	$B.C \rightarrow 2$	$A.B \rightarrow 1$	$A.B \rightarrow 1$	$A \rightarrow 1$
D.F, D.G	ĮJ.	H.F, H.G		$H.G \rightarrow 6$	$H.F \rightarrow 5$	$E.G \rightarrow 4$	$E.F \longrightarrow 4$	$\mathbb{E} \to 4$

Letters denote symptoms, numerals denote diseases

selected for each subject from the followin safely assume that blocking occurred. phase II because numerous experiments in blocking in this type of procedure (e.g. K pain, dizziness, nausea, insomnia, bad breat Response keys (disease labels) were D, F, G to diseases for each subject. Phase There were 40 trials of training phase I, III, followed by 20 test trials. The The ruschke eight my and ymptoms no have vision, phase K, randomly ache, Blair, test shown skin and were 2000). blocking and very nose rash, randomly assigned 6 We robust bleed trials back can

accuracy on the diseases with a blocked shared attentional learning. In the first third of tra introductory psychology course. difference in percentage correct was 2.9%). than on the diseases with the blocked distinctive A total of 89 students volunteered to participate = 2.97, p = .004 (collapsed across a The resu. Burur confirmed the phase symptoms symptom third joi partial the people phase, 40. predictions 2% credit 3% had correct), correct mean Ï her

symptom (F used in the test phase. Of most interest ar shows the choice proportions for the five from the diseases with a blocked shared syn C.F, C.G, D.F and D.G. In each of these cas The final testing phase showed more robust or G) from the diseases Wit] motqu the pes bloc a distinctive s effects conflicting Of ked <u>S</u>. paired ymptom of distinctive blocking. ymptom with symptom combinations symptoms distinctive Table paurs, 70°

Choice percentages from the test phase of dis TABLE 4.2 natio J ē rning blocking

Symptoms			:					Resp	Response	choice	ce			:			:	
		Δ			E			C/D			F/G	:		C/Do		Ĭ.	F/Go	
	H	M	R	Н	M	R	Н	M	R	Н	M	R	H	M	R	H	M	R
A	94	95	94	ယ)-med		2)a) 	} 4	}	⊢	 		—	} ⁴	⊷	
Ţ	သ		ightharpoonup	95	95	94	فسنا						0					}
BC/BD	 	Ş	4		S	4	74	76	75	5	S	4	10	6	9	9	Ο ₁	4
HF/HG	<u> </u>	4	4	}	4	4	~]	4	4	71	74	75	7	4	4	13	9	9
CFICGIDFIDG	2	5	5	2	5	5	49	46	a Garant	33	34		7	5	γ	6	5	2
									İ									

disease corresponding to symptom A, i.e. disease 1. The residisease corresponding to symptom C if a test case including denote the symptom corresponding to the disease selected, the disease corresponding to symptom D if a test ca Under each choice, the column headed "H" indicates headed "M" indicates the full model percentage, an Letters in the left column denote symptom combination restricted model percentage with no attention learning e.g. response column symptom ymptom headed choice percentage, choice tops was \Box wwas presented, presented columns and the

> for Table 4. Attentional theory suggests that learning about symptoms C and D should be This difference is highly significant by a binomial test the C/D diseases cases hence stronger, and D over the 2 shows that this result did indeed occur, with 49% of the choices being of conflict and only 33% of the choices than diseases corresponding with F the choices learning about should favor symptoms the being for the F/G diseases. diseases corresponding (z = 4.62, p < .001).and G. The last row of 1 and G. Therefore,

should address these attentional effects. Because These S learned results, blocking is attention in blocking along so pervasive with those of in natural learning, Kruschke at least & Blair (2000), show this type of models of procedure). learning that

connectionist model with attentional learn

extended ation does have exemplars between the inputs and the attention nodes. The motivexemplar parameters, and is not a theoretical commitment. Figure 4.7 depicts very similar in spirit to the Al exemplar-specific. This for 4.4). by Si. nodes between the this merely Kruschke One S. the the difference a pragmatic simplification to For example, (2001),idea ADIT model introduced that inputs and the categories, IBRY model described between referred to learned when the here a mushroom is smooth and flat, attentional models as the by reduce the number of free S Kruschke in the previous section EXIT model. EXIT is the other hand, EXIT distributions that whereas EXIT AMBRY (1996a)should used does and

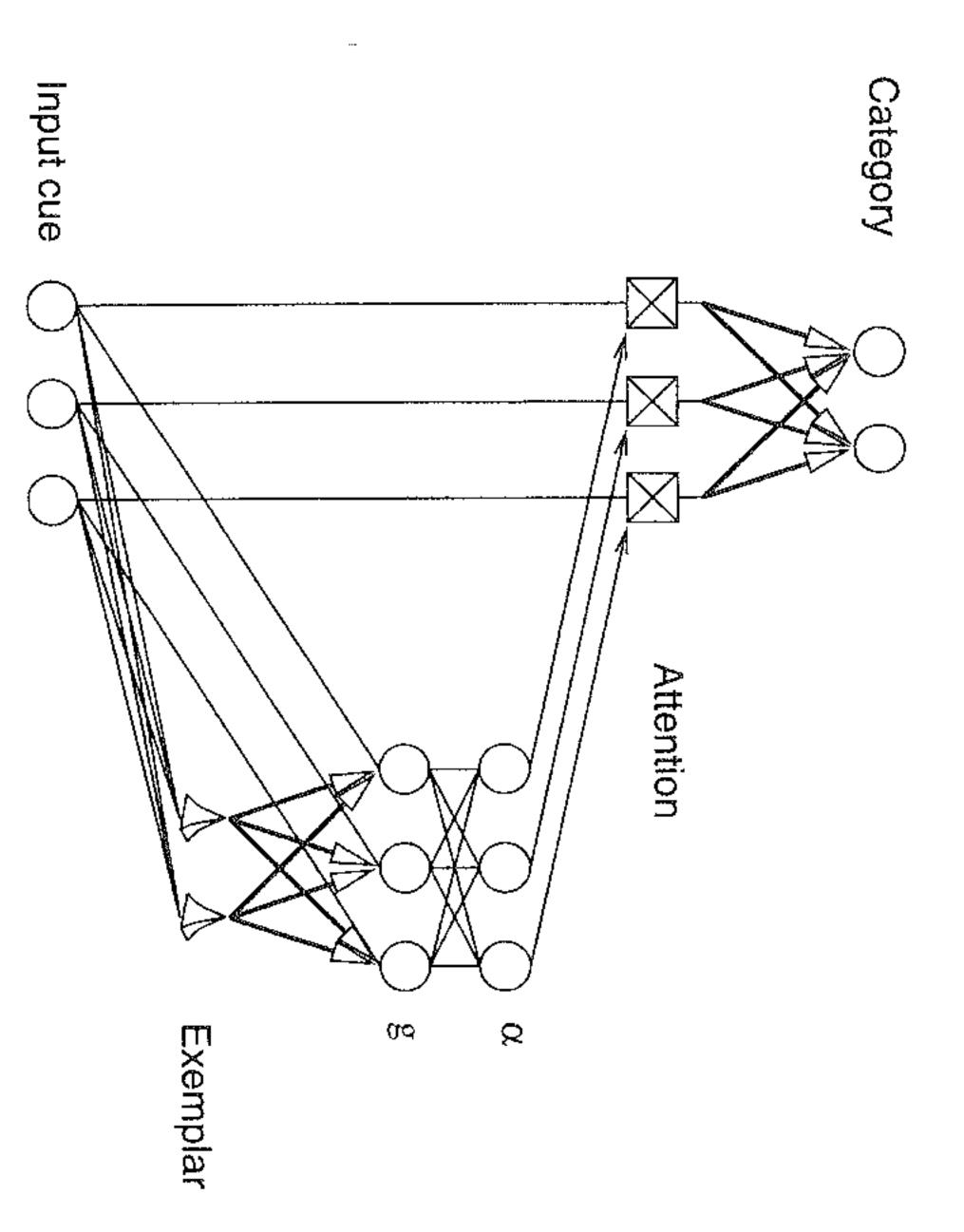


Figure 4.7. attention on the cues The Architecture of the X_{S} boxes above EXIT model. The thicker the input cues represent the arrows multiplicative weighting denote learnable associative of the

attention should be shifted to the flat shabe shifted away from texture to shape. Ď, Jud attention should not always

capacity constraint on the attention strengths. This capacity capacity condel is supposed to reflect attentional capacity constraints are then normalized to produce the overall attention criss-crossing lines between the gain nodes feature is present, the gain node is activated by default, but can also be influenced by learned associations from exemplars. The gains on each feature decreased on another feature. This constraint is other animals: If attention to a feature Another difference between AMBRY and and the attention nodes. increased, indicated in Figure 4.7 by the is that each feature must necessarily EXI constraint in the in humans and imposes When a

rate, across trials. Thus, when corrective feedback is drives a relatively large shift in attention I changes are made. This shifted distribution values to be learned by the associative weights gain nodes. This gives EXIT one more free p executed rapidly within a trial, although t One last but important enhancement of EXIT distinct from the attentional learning hey parameter: is provided on a trial, the error before may of attention between the exemplars and the is that attention be learned any An attentional shift associative acts only as the shifts gradually weight target

the kth category node is determined as: the summed weighted activation of the input cues. activation of the category nodes, and these generation and for learning. Responses are attention in the formulae for categorizati (Kruschke, 2001), but it might be useful These two formulae show clearly the separate roles of attention for response omplete mathematical details of the g here nodes model generated and to associative weight change. Formally, the are activated according describe the influence are proportionally provided activation of elsewhere Ç the Q

$$a_k^{\text{cat}} = \sum_i w_{ki} \alpha_i a_i^{\text{in}} \tag{3}$$

where w_{ki} is the associative weight from the that the cue is attention allocated to the *i*th cue, and a_i^{in} output (denoted Δw_{ki}) is given by: attention. The change Notice that a cue has attended to. Associative w an influence in the associative weight on the eight category ith cue to the kth category, <u>~</u> the changes from activation of choice only to the are ith cue also the affected to the extent Q_i 1S ith cue the the bу

$$\Delta w_{ki} = (t_k - a_k^{\text{cat}}) \alpha_i a_i^{\text{in}}$$
(4)

where t_k is the *teacher* value (correct response) to, and the model attends to whatever reduces being attended to. Thus, the model only learns Notice that a weight from a cue is changed only error best. about what to the for the extent kth S being category that the attended cue node. S

> ized (capacity-constrained) attention then multiplicatively gates the cue activations propagated to the category nodes. Category node activations are mapped to response probabilities as in AMBRY. When the correct classification is provided, the error first drives a relatively large attention shift. After this shift is completed, the associative weights to the attentional gain nodes are adjusted to try to learn this new distribution of attention, and the presented and activate the corresponding input nodes. ponding attention gain nodes are then activated, modulated by any learned redistribution of attention for exemplars similar to the stimulus. remaining predictive error. associative weights to the category nodes are adjusted to try to diminish any In summary, processing in the EXIT model occurs as follows. By default, the corres-The normal-Cues are

Fit of the model

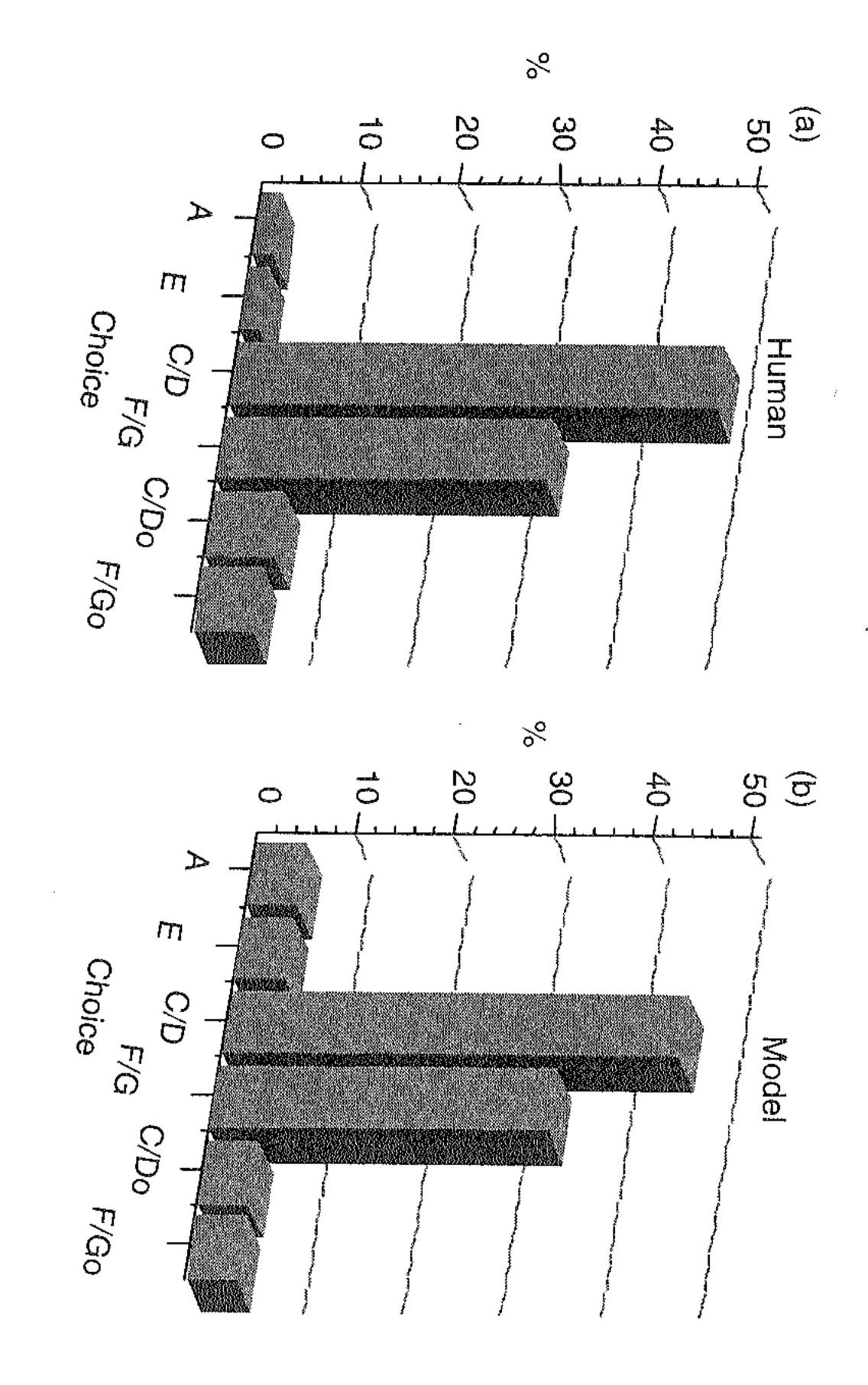
The model was fitted to the testing phase data of Table 4.2 (and not to the third phase learning data) with each test type weighted by the number of distinct cases contributing to the type. The best fitting predictions of the ence for C/D diseases over F/G diseases in the conflicting symptom cases (see the last row of Table 4.2). Although not fitted to the third learning phase, model mirror the data quite well. In particular, EXIT shows a strong prefertheir shared symptom blocked. EXIT, like humans, shows a small (2.2%) advantage for the diseases that had

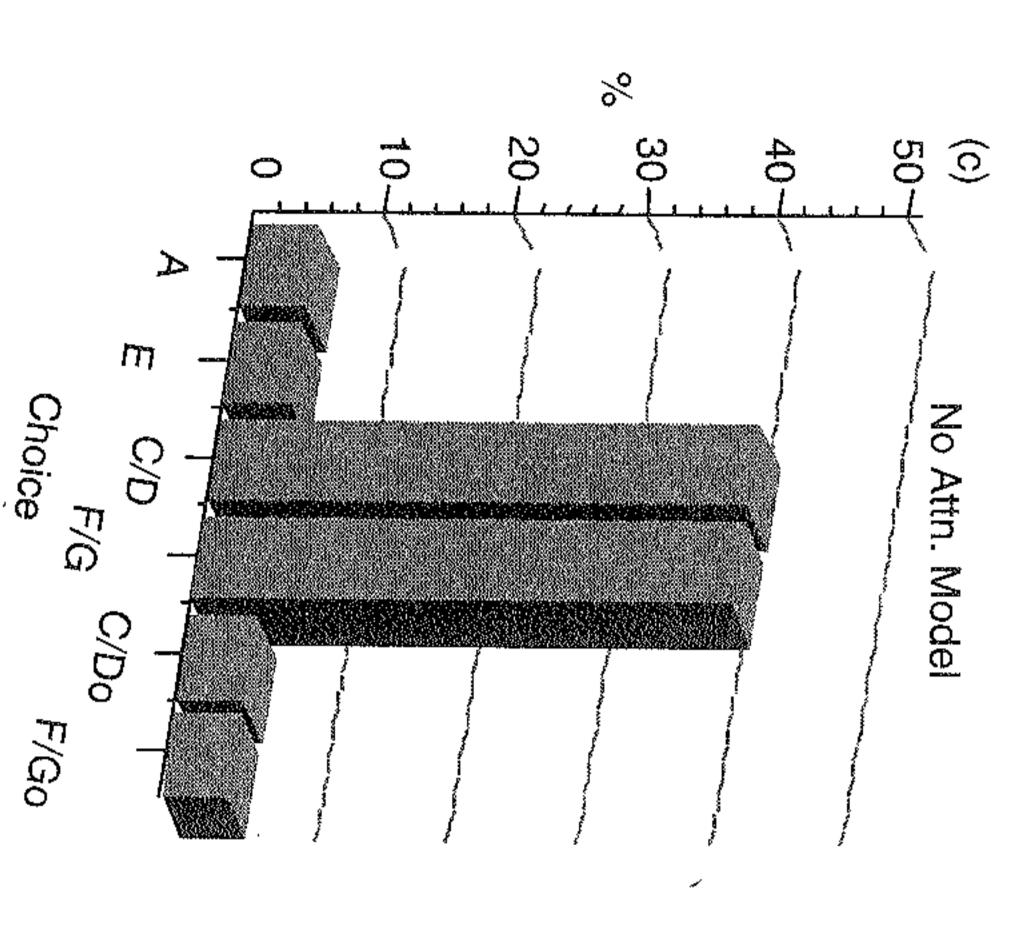
Figure 4.8 displays data from the conflicting symptom tests (CF/CG/DF/DG) of Table 4.2 in the form of a bar graph; (a) displays the human choice percentages; (b) displays the predictions of EXIT. In the human data, the two percentages; (b) displays the predictions of EXIT. In the human data, the two bars for the C/D and F/G choices are at distinctly different heights, as they are in the predictions of EXIT.

restricted version of the model are also shown in Table 4.2 and in Figure 4.8c. (but attentional shifting is still allowed), the critical duced by the model. The best fitting predictions groups in the third learning phase when attention le Thus, attention learning is crucial for the model for conflict tests (last row of table). Moreover, there is zero difference between Notice that there is no difference between C/D and F/G response proportions observed in people. Importantly, when the attentional learning rate critical effects learning was disallowed. of EXIT is fixed at zero of this "no attention" to exhibit cannot be the effects pro-

THE INVERSE BASE RATE EFFECT

The learning behavior reviewed above can be thought of suboptimal. sional shift. The two structures in the second phase Consider the advantage of intradimensional over extradimenof learning (see Figure as irrational and





row of Table 4.2. Results of the conflicting symptom tests of the blocking experiment.

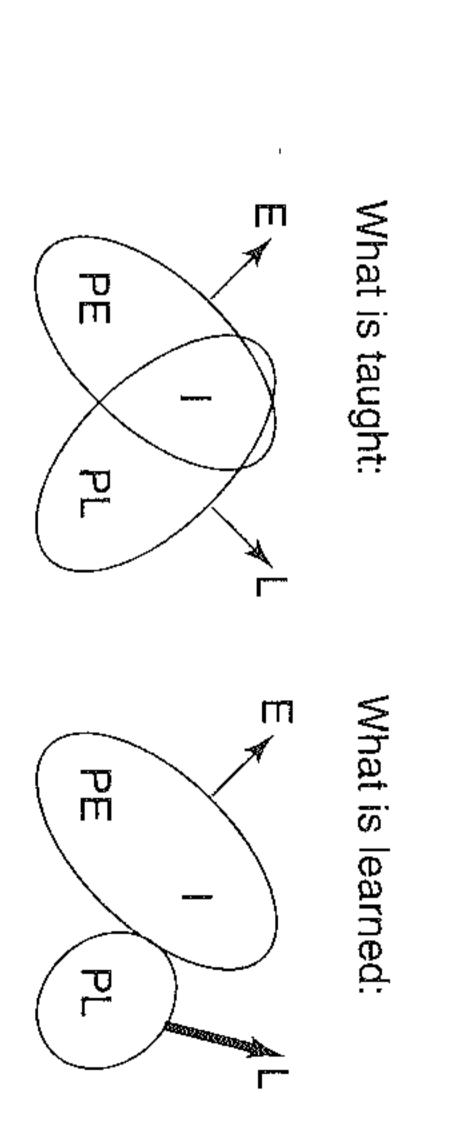
about phase should learn them equally efficiently. (predictive of the outcome, are redundant the Ç are isomorphic, isomorphic, cue. Moreover, relevant cue and so and so they should the and so a one might ij two phase pairs rationa Jonsider the think learned equally optimal learner 211 phenomenon that optimal learning should learn symptom blocking perfectly device

Another prominent example apparently irrational learning

> symptom I is shared by both diseases, and therefore structural symmetry. when the diseases. Symptom PE is a perfect predictor of disease E, and symptom a perfect predictor of disease L. of Figure 4.9. On some together and always indicate do, rate they effect. always Suppose rare occasions, indicate that disease The left panel of Figure 4.9 shows this disease Ţ THE symptoms I and PL occur, e L (I.PL \rightarrow L). Notice ntly symptoms I and \rightarrow E), is an imperfect predictor as shown in the left and

diagnoses for novel combinations of phenomenon. because disease E has a larger base rate, procedure procedure For symptoms PE.PL, Medin & Edelson (1988). This effect is found in disease diagnosis procedures For symptom I by itself, people tend to choose disease E, which is appropriate After learning these his pattern (Fagot, (Dennis 1996a; It has not yet been reported in other Kruschke, Depy, & Medin & Edelson, & Kruschke, 1998), of results however, people strongly diseases, was dubbed experiment symptoms, Vauclair, and in a i.e. a higher frequency of occurrence. participants are such as PE.PL and I by itself. "inverse geometric figure ω tend to choose the rare 9)98), species, however. random so it is a very base rate effect" by word asked to make association association robust

of learning about mushrooms, people shift attention away from the symptom about the the rare disease. empirical and modeling results added supportive learned Figure 4.9. Consequently, already that people tend to learn about the frequent disease before they learn about rapidly shifting Kruschke (1996a) explained the association from symptom PL associations about the diseases of rapidly shifting attention Ç associative strength with associated with the distinctive symptom of rare disease, I.PL dominates the moderate Thus, people attention. One when learn early common disease tested strong consequence the disease E. inverse base As argued in rare disease, there to with PE.PL, the association <u>s</u> illustrated symptoms I and PE each have Then people learn later about rate effect as a consequence the evidence to this explanation and learn predominantly se, thereby building up a from introductory of different base rates I the right panel strong association PE to asymmetry discussion Further



ofcategories in the inverse base

about I in the context of PL should be diffing symptom pair I.PE, attention is not strongly impacted by learned attention shifts. In particular, be shown that the results can be fitted by E when attentional shifting is "turned off", the subsequent learning about I in the context attention should be shifted away from I to single trials of learning, rather than on learned redistributions of attention. that additional learning subsequent to Results of an experiment that tests this prediction are Nevertheless, the notion that attentional redistributions are The emphasis of Kruschke (1996a) was the , the restricted model fails. difficult. inverse base rate rapidly of shifted away with attentional shifting, should be that On the shifting attention for presented here. It will symptom pair I.PL, subsequent other learned suggests from I, effect should relatively easy. hand, learning during that ğ

Experiment design and results

effect. a phased-training version of the inverse base force people to learn I.PE → E before learning Kruschke, 1996a, experiment 2). phase, there is a test phase to measure phase consists of II.PE1 on base rates to accomplish indirectly this Table 4.3 shows the design of an experiment that assesses learned attention in This much of the design is a replication two copies of the same \rightarrow E1 and I2.PE2 E before learning I.PL -> indirectly this ordering of basic structure, the magnitude of the rate E2. After the second training effect. of so, for example, previous learning. The design L, instead of relying The first two phases inverse base rate studies the first œ. (e. g

new disease N1 and N2, in the context of PE1 be relatively easy because there should be some in this phase to learn that symptoms II The third phase of training breaks new ground. Half the subjects went on and 7 and PE2 attention to were relevant to diagnosing This was predicted to |---d and 3

Design of experiment assessing I phased inverse base TABLE 4.3 earned attention in the effect

Training I	II.PEl → El	I2.PE2 → E2
Training II	II.PE1 \rightarrow E1 II.PL1 \rightarrow L1	I2.PE2 \rightarrow E2 I2.PL2 \rightarrow L2
Testing	I, PE.PL, etc.	, etc.
Training III (easy, I in PE)	II.PE1 \rightarrow N1 II.PE2 \rightarrow N1	I2.PE1 \rightarrow N2 I2.PE2 \rightarrow N2
Training III (hard, I in PL)	II.PL1 \rightarrow NI II.PL2 \rightarrow NI	$\begin{array}{c} \text{I2.PL1} \rightarrow \text{N2} \\ \text{I2.PL2} \rightarrow \text{N2} \end{array}$

and N denote disease. I, PE, PL denote symptoms.

I2 were relevant in the context of PL1 and PL2. This was predicted to be relatively difficult because attention to I1 and I2 should be suppressed in the company of PE1 and PE2. The other half of the subjects learned that I1 of PL1 and PL2 and

were selected as in the blocking experiment. There were 40 trials of training phase I, 80 trials of phase II, 28 trials of testing phase, and 80 trials of Phase III. Symptoms and response keys

in the "hard" condition. There were no differences between groups in the first two phases of learning. Table 4.4 shows the choice percentages in the test introductory psychology course. Six subjects' data were excluded from the last half of the analysis because they failed to reach 80% correct in the last half of phase, collapsed across the two groups. For test case I, choices for E were far greater than choice for L (75% vs. 17%), $\chi^2(1,245)/4 = 25.15$, p < .001. For test second phase of training. the inverse base rate effect is strongly in evidence. $\chi^{2}(1,262)/4 = 11.13$, p < .001. For test case PE.PLo, choices for Lo were far greater than choices for E (59% vs. 32%), $\chi^{2}(1,225)/4 = 5.60$, p < .025. Thus, case PE.PL, choices for L A total of 83 students volunteered to participate for partial credit in This left 38 subjects in the were far greater Six subjects' than choices for E (67% vs. 28%), data were "easy" condition and 39 excluded from furthe

phase. The Collapsed across all blocks of the third phase, the mean percentages main novel result regards the relative ease of learning in the third

Results from test phase of experiment assessing discrimination learning after blocking, with prediction of model in TABLE 4.4 parentheses

Symptoms					Re	sponse (choice					
		Æ			L			Eo			Lo	i
	H	M	R	H	M	R	H	M	R	Н	M	R
PE	93	94	93	3	2	ယ	2	2	2	<u> </u>	2	2
IPL	12	9	ယ	85	85	93	0	ယ	2	ယ	ယ	2
	75	00 4	4 .	17	Ŋ	£	S	S	6	w	S	6
	28	24	39	67	88	39		4	1	4	4	,
	32	24	50	6	4	,	သ	4	⊷	59	8	4 2 ∞
I.PE.PL	52	48	43	43	46	43	─	ယ	7	4	်ယ	7
I.PE.PLo	63	61	67	نح	ယ	5	ယ	3	2	29	33	26

Results are collapsed across pairs 1 and 2. For example, symptom I refers to cases of II and I2. If II was presented, then choices E, L, Eo and Lo refer to diseases E1, L1; E2 and L2, respectively. If I2 was presented, then choices E, L, Eo and Lo refer to diseases E2, L2, E1 and L1, respectively. PE.PLo indicates cases of PE1.PL2 and PE2.PL1 combined. Under each choice, the column headed "H" indicates the human choice percentage, the column headed "M" indicates the full model percentage, and the column headed "R" indicates the restricted model percentage with no attention learning.

These are reliably differences between groups in the first two correct were 82.7% for the "easy" group and These are reliably different (t(75) = 2.10, SE_{dif} unequal-variance corrected df of 62.10). This correct were 82.7% for the "easy" group differences in the initial phases, and phases because difference cannot be 76.2% for the 0.031, p =there .040 two-tailed for were "hard" no attributed hints group.

Fit of the model

fitted the learning in the third phase well, predicting 80.9% correct in the easy condition and 72.5% correct in the hard condition, compared with 82.6% and and a strong preference for Lo when presented with PE.PLo. The model also alone, a strong preference for L when presented with with the model exhibiting a robust preference for E when given symptom ing data. Table 4.4 shows that the model predictions 76.2% by humans. The model, EXIT, was fitted to the testing and to fit the testing data well, symptom pair PE.PL, the third phase train-

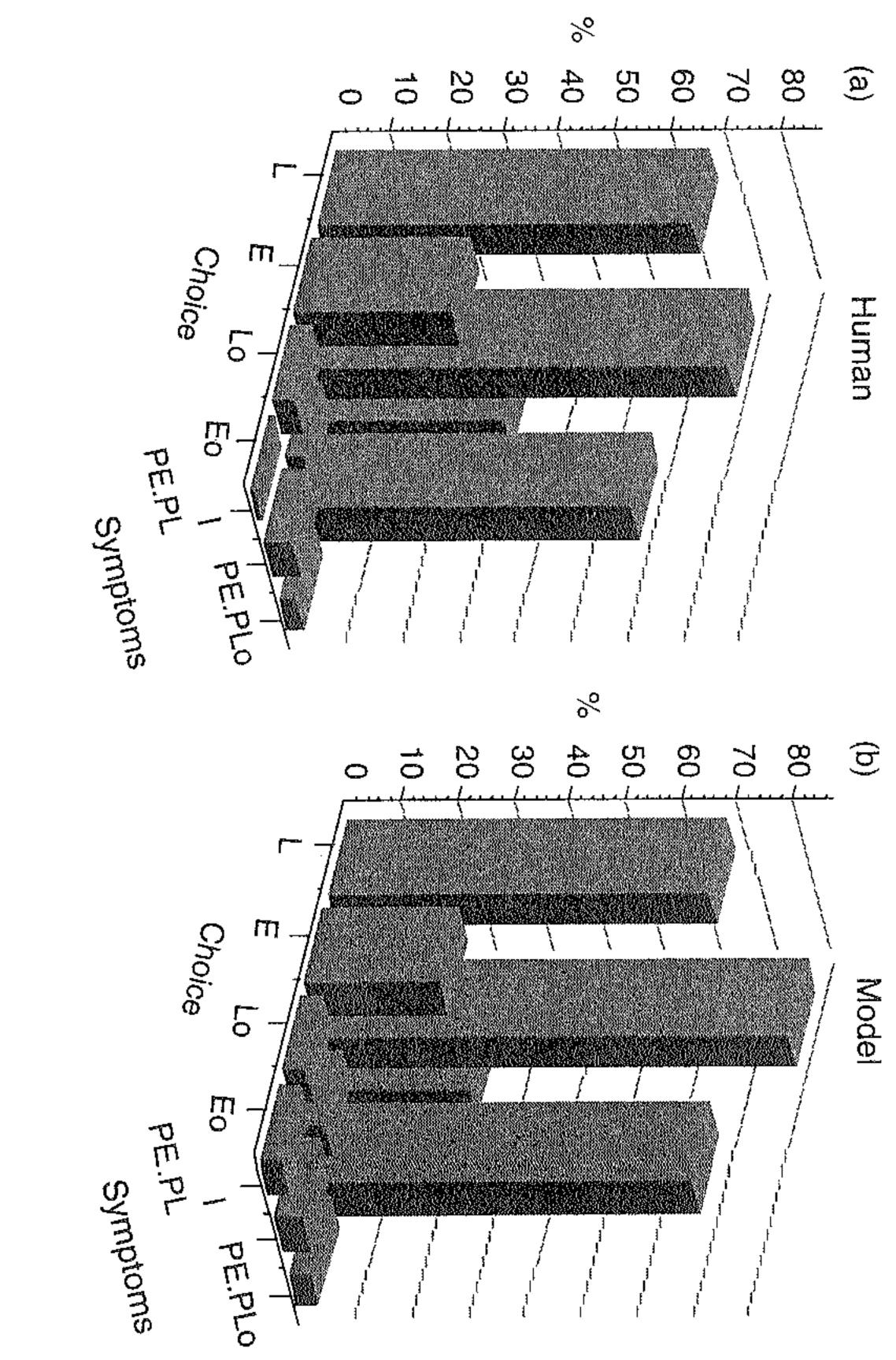
the pattern of results seen in the human day ure 4.10. It Selected (bold font) data from Table 4.4 can be seen from Figure 4.10a ta quite well. and are presented graphically in Figb that the model reproduces

given symptom I alone, no preference for L when prese pair PE.PL, and no preference for Lo when presented PE.PLo. The model also shows no difference between phase of learning, predicting 78.2% correct in the easy c shows that the model without attention exhibits no preference restricted model was entirely unable to show the trends of interest. Table 4.4 fixed value of zero (and hence there was no are critical for the model to fit the data. correct in the hard condition. Yet again we When the attention shifting was turned in the easy condition and 78.3% see that attentional mechanisms off, so that the attentional learning, when presented with symptom between groups in the with symptom pair shift rate for E either), the when third

the model can learn the training patterns but generalizes nothing do, either in the test phase or in the subsequent training phase. Figure 4.10c shows clearly the failure of preferences shown by humans. Without the attention shifting and learning, restricted model like to capture people

SUMMARY AND CONCLUSION

attentional shifts and attentional learning in ignored feature. attend to one feature or ignore another f about the attended-to feature should be attend to one feature or ining the ease of learning in a subsequent all three experiments, attentional learning in one phase was assessed by exam-The preceding sections provided three ill In the first illustration, eature, ustrations phase. If easier advantage models then subsequent than people of natural learning. of of learning the intradimensional have learned to importance about learning



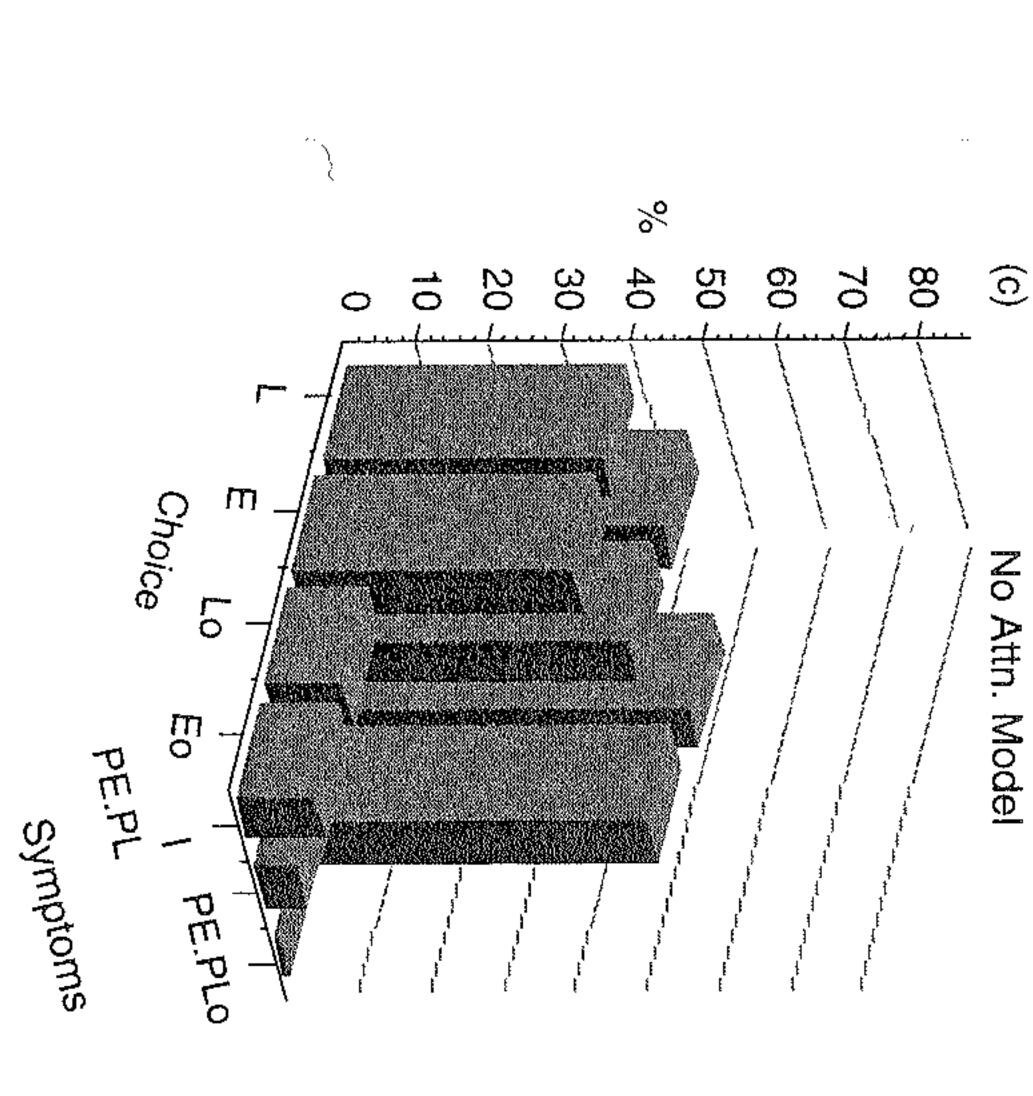


Figure or without attentional Selected data shifting and inverse base rate experiment, with predictions of EXIT model

5 Kruschke, confounded blocked phenomenon extradimensional 1996b) changes cue. that avoided shift problem was Sec. demonstrated common iously ated. d suppression ustration showed that ð with all previous that blocked an discrimination of attention experiment than when designs, the

imperfect predictor was more difficult in (attended to) distinctive cue than in the content of t the distinctive cues were previously blocked. that the rapid attention shifting evident in strongly attended to) distinctive cue. involves learned attention shifts, because ontext subsequent context inverse of the third illustration suggested Of. base rate earlier learned (less learning the later effect about learned

All three phenomena—intradimensional the inverse base rate effect—have been found sought in other species (and the third is relatively recent and has digms and settings. The first two have been found sought in other species). Therefore, atten phenomenon and should not be ignored by -have been found in a variety of attentional those shift not yet been who wish learning advantage, ੂ = ಭ variety to model natural procedural para-S. blocking, systematically ω widespread of animal

signature effects observed in the human data. shifting and learning was "turned off" evidence to the veracity of the attentional t attentional shifting and learning fitted the In all three illustrations, connectionist models (m he data nicely. The modeling adds models that could not When the directly implemented exhibit attentional supportive

Relation to other learning models

none of which address the type of attentional phenomena described here. proposed in recent years, some of which incorporate notions of attention, yet There have been a variety of connectionist models of associative learning

account for results from a modest parametric variation of their experimental researchers, demonstrating the robustness of model's ability to address it. Yet it turned Gluck & Bower (1988) proposed a simple the delta rule, as a model of apparent bases. attention is sufficient (Kruschke, 1996a). design, and instead an enhanced model's ability to Their seminal article initiated address it. a series of model that incorporates of the further linear associator, that learned by rate neglect in human learning. out empirical effect that investigations their rapidly model by and of the shifting cannot several

might the ACM is quite different from the notion expounded in this chapter. The is inversely related to the cue's base rate. Thus, attention in ACM does not shift rapidly in tional connectionist model (ACM), in which the Kruschke (1996a) showed that the ACM does not fit data from an experiment corresponds to the cue's surprisingness or novelty. addition to rapidly shifting error-driven attention examining Shanks (1992) proposed a variation of a demand apparent base rate the inclusion of neglect. ACM-style Nevertheless, response linear associator, the attention allocated to a cue novelty-based attention allocated This notion of attention Ö future empirical data categorization errors. called the attenattention to

Nosofsky, Gluck, Palmeri, McKinley, Glauthier (1994)described ω

> model that maintains separate are adjusted in response to error. This interesting approach was first proposed combination of features. as ALCOVE. This approach is intriguing and deserves 1988). The model was able to capture aspects of a classic learning study that the authors replicated, but the model did not fit the data quantitatively as well produced by rapid attention shifts or by exemplar-specific learned attention. It might be particularly challenged, however, by learning phenomena that are Sutton and colleagues (e.g. Gluck, Glauthier, These individual learning rates, learning rates for & Sutton, 1992; Jacobs, each further investigation. feature or associabilities, and

modulation in learning. In these models, however, the attentional modulation affects all cues simultaneously, and does not rapidly select component cues within an array. It may well turn out that both types mechanism are needed in a comprehensive model of learning. Some neurally-inspired models of learning, such (1992) and Gluck & Myers (1997), implement types of attentional well turn out that both types of attentional as those of Schmajuk &

therefore is unable to address the effects highlighted in this chapter. The configural model of Pearce (1994) incorporates exemplar nodes simito AMBRY, and it incorporates attentional normalization similar to but it does not incorporate any kind of shifting selective attention. Ö (----------(

normative calculation of conditional probabilities, occurrences, and then classifying items according to their Bayesian probabilities. The rational model can be implemented in a network framecan account for many findings in learning, but one work not unlike a connectionist model (Anderson, base rate effect for test symptoms PE.PLo, whereas humans address is the inverse for shifting or learning attention. effect (see Table 4.4 and Figure 4.10). The rational The rational model of categorization (Anderson, to be accumulating statistics about feature base rate effect. In particular, model has no mechanism it fails to show an inverse 1990, p. 137). The model phenomenon it does not such that the 1990) is and show a motivated category learner Bayesian strong by

direct formal expression of intuitions about how attention works, based on empirical findings. The formalism was not couched in any larger-scale learning mechanism. Connectionist modeling adds such a larger-scale perspective. The EXIT model described in this chapter has an architecture motivated by psychological principles similar to Mackintosh's. But the mechanisms for attention shifting, attention learning, and associative weight tationally, or how the attentional mechanism related to the associative weight learning mechanism. Connectionist modeling adds such a larger-scale perframework to explain what the special case of EXIT is very nearly identification Mackintosh (1975) (see Kruschke, 2001). learning are all derived by a common goal: error reduction. It turns out that a Mackintosh's (1975) classic model for attention learning was invented as a model mechanism identical the formulae proposed accomplished compu-

Attentional shifting and learning are

nectionist modelers to ignore attentional le information. Thus, a model that is driven purely by rapid error reduction can situations model called RASHNL generate a number of seemingly irrational behaviors, just Learning). The rash shifts of attention facilitate the rational goal of rapid relevant information, yet for natural learn ence of irrelevant information should not cue decreases when other, irrelevant, outcome. The extent to which people (and irrationality of intradimensional shift advantage, associations without damaging Wagner, Logan, Haberlandt, & Price, 1968 base rate effect has been described above. accelerates learning, it can also lead to apparently learning, and addressed a panoply of irrational behavior with a connectionist Consider (1999) reviewed Attention shifts and learned attention are other animals. The pervasiveness of but also lead to over- or under-commitments a situation wherein a cue is on and across a number of related phenomena in probabilistic category species, suggests that it (which previously stands cues for these learning phenomena, ers it does. arning. other animals) learn to utilize There affect the are learned imperfectly Rapid Attention SHifting would added (e.g. are many other examples. blocking, and the optimal learner, irrational behaviors. The the rapid learning of associations. While ultimate utilization of o C Kruschke to correlated irrational for various like Castellan, 1973; people & Johansen sources , the preswith inverse across connew the

- and elemental learning, see Chapter 2 by fundamental goal of learning in the first smoothness. A problem with this approach is that knowledge does not generalrooms, despite the fact that both pieces of round mushrooms would not interfere wit features in each type of mushroom, and basis of partially matched configurations. An alternative possible solution would be from learned cases to novel cases, Shanks in this volume. place. Ç In this way, knowledge about smooth knowledge about smooth flat mushgeneralization disallow any generalization on the encode the entire configuration of knowledge For a discussion of configural S include the feature perhaps the
- irrelevant dimension relevant. The original design used by Kruschke (1996b) testing other hypotheses about shift learning structure with the previously irrelevant dimensions relevant and one A complete reversal of all categories, These additional types and also included two other types a change of shift t O were another previously useful for XOR
- attentional learning remain the same. these two departure from a strict blocking design, t Strictly speaking, the design does not constitute blocking of F and (symptom B, however, does conform stric symptoms are not perfectly correlated tly to a blocking design). Despite this theoretical implications regarding with the disease Ģ iii phase because

REFERENCES

- Ackley, D. H., Hinton, G. E., & Sejnowski, T. J. (1985). A learning algorithm for Boltzmann machines. Cognitive Science, 9, 147–169.

 Anderson, J. R. (1990). The adaptive character of thought. Hillsdale, NJ: Lawrence Erlbaum
- Castellan, N. J. (1973). Multiple-cue probability learning with irrelevant cues. Organizational Behavior and Human Performance, 9, 16–29. Associates Inc.
- Dennis, S., & Kruschke, J. K. (1998). Shifting attention in cued recall. Australian Journal of Psychology, 50, 131–138.
- papio) and humans (Homo sapiens): Species differences in learned attention to visual features. Kruschke, J. K., Depy, D., & Vauclair, J. (1998). Associative learning in baboons (Papio
- Animal Cognition, I, 123-133.

 Garner, W. R. (1974). The processing of information and structure. Hillsdale, NJ: Lawrence Erlbaum Associates, Inc.
- network model. Journal of Experimental Psychology: General, 117, 227-247.
 Gluck, M. A., Glauthier, P. T., & Sutton, R. S. (1992). Adaptation of cue-specific learning rates & Bower, G. H. (1988). From conditioning to category learning: An adaptive
- in network models of human category learning. In Proceedings of the 14th Annual Conference of
- the Cognitive Science Society (pp. 540–545). Hillsdale, NJ: Lawrence Erlbaum Associates, Inc. ick, M. A., & Myers, C. E. (1997). Psychobiological models of hippocampal function in learning and memory. *Annual Review of Psychology*, 48, 481–514.
- Jacobs, R. A. (1988). Increased rates of convergence through learning rate Hopfield, J. (1982). Neural networks and physical systems with emergent collective computational abilities. *Proceedings of the National Academy of Sciences USA*, 79. adaptation. Neural
- Networks, 1, 295-307.
- Kamin, L. J. (1968). 'Attention-like' processes in classical conditioning. In Miami symposium on the prediction of behavior: Aversive stimulation (pp. 9-33). Coral Gables, FL: University of Miami Press. M. W W Jones (Ed.),
- Kruschke, J. K. (1992). ALCOVE: An exemplar-based connectionist model of category learning.
- Psychological Review, 99, 22-44. Kruschke, J. K. (1996a). Base rate nschke, J. K. (1996a). Base rates in category learning. Journal of Experimental Psychology: Learning, Memory, & Cognition, 22, 3–26.

 Inschke, J. K. (1996b). Dimensional relevance shifts in category learning. Connection Science,
- Kruschke, J. -223.
- Kruschke, J. K. (2001). Toward a unified model of attention in Mathematical Psychology, 45, 812--863. associative learning. Journal of
- Kruschke, J. K., & Blair, N. J. (2000). Blocking and backward blocking involve learned inatten--645
- Kruschke, J. K., & Johansen, M. K. (1999). A model of probabilistic category learning. Journal of Experimental Psychology: Learning, Memory, & Cognition, tion. Psychonomic Bulletin & Review, 7, 636 1083 -1119.
- Mackintosh, N. J. (1965). Selective attention in animal discrimination learning. Psychological
- the associability of stimuli with
- Mackintosh, N. J., ability of UCS. Bulletin, 64, 124–150.
 Mackintosh, N. J. (1975). A theory of attention: Variations in reinforcement. Psychological Review, 82, 276–298.
 Mackintosh, N. J., & Turner, C. (1971). Blocking as a function. a function of novelty of CS and predict-
- Medin, D. L., & Edelson, S. M. (1988). Problem structure and the use of from experience. Journal of Experimental Psychology: General, 117, 68 Miller, R. R., Barnet, R. C., & Grahame, N. J. (1995). Assessment of Quarterly Journal of Experimental Psychology, 23, 359the use of base-rate information -366. <u>85</u>.
- ler, R. R., Barnet, R. C., & Grahame, model. Psychological Bulletin, 117, 363-7. Assessment of the Rescorla-Wagner

KRUSCHKE

- Minsky, M. L., & Papert, S. A. (1969). Perceptrons. Cambridge, edition). MIT (1988 expanded
- Nosofsky, R. Inc. sofsky, R. M. (1992). Exemplars, prototypes, and simi Kosslyn, & R. M. Shiffrin (Eds.), Essays in honor of Will processes to cognitive processes (pp. 149–167). Hillsdale, similarity rules. awrence Estes: In Erlbaum Associates Healy,
- Nosofsky, R. M., Gluck, M. A., Palmeri, T. J., McKining models of rule-based classification learning: Jenkins (1961). *Memory & Cognition*, 22, 352-369 replication Glauthier, Shepard Hovland, Compar-
- Pearce, J. M. (1994). Similarity and discrimination: A selective review and a connectionist model.
- Psychological Review, 101, 587-607.

 Rescorla, R. A., & Wagner, A. R. (1972). A theory of effectiveness of reinforcement and non-reinforce (Eds.), Classical conditioning: Ii. Current roccert.

 Appleton-Century of Paylo Appleton-Century-Crofts. <u>L</u> theory onditioning: (pp. Black, .99). Variations [T] Prokasy I York:

.

- model for information 408 storage and organ
- Rosenblatt, F. (1958). The perceptron: A probabilistic maization in the brain. *Psychological Review*, 65, 386–40 Rumelhart, D. E., Hinton, G. E., & Williams, R. J. (1986) error propagation. In J. L. McClelland & D. E. Rumeling (Vol. 1, pp. 318–362). Cambridge, MA: MIT Pres. Schmajuk, N. A., & DiCarlo, J. J. (1992). Stimulus corhippocampal function. *Psychological Review*, 99, 268-Shanks, D. R. (1992). Connectionist accounts of the in melhart 986). earning (Eds. internal **Parallel** distributed representations proc by
 - configuration, -305classical conditioning, and
- Connection Science, 4, 3-18. inverse base-rate effect ul . categorization.
- Shepard, R. N. (1964). Attention and the metric Mathematical Psychology, 1, 54-87. St the stimulus space.
- generalization psychological science.
- Shepard, R. N. (1987). Toward a universal law of Science, 237, 1317–1323.

 Siegel, S., & Allan, L. G. (1996). The widespread in Psychonomic Bulletin & Review, 3, 314–321. nfluence ofthe Rescorla Wagner model
- learning. Psychological Bulletin, 69, 423-438.
 Sutherland, N. S., & Mackintosh, N. J. (1971). Mec. Slamecka, N. J. (1968). A methodological analysis of paradigms human discrimination
- New York: Academic Press. gner, A. R., Logan, F. A., I hanisms animal discrimination learning
- discrimination learning. Journal of Experimental Psychology, ., Haberlandt, K., & Price, (1968)Stimulus 180 selection in animal
- Williams, B. A. (1999). Associative competition in opereinforcer association. *Psychonomic Bulletin & Rev* conditioning: Blocking the response
- Wolff, J. L. (1967). Concept-shift and discrimination-Bulletin, 68, 369-