

Traveling Salesman Problem (G)

// assume that the n cities are v_1, v_2, \dots, v_n

$$n = |V|$$

$$\text{minCost} = \infty$$

$$\text{minTour} = \emptyset$$

// without loss of generality, assume that all tours start from v_1

$O((n-1)!)$ for each permutation of vertices $v_2, v_3, v_4, \dots, v_n$

// compute the cost of the tour

$$\text{crtCost} = 0$$

$O(n)$ for $i = 2$ to $n-1$

$$\text{crtCost} = \text{crtCost} + w(v_i, v_{i+1})$$

if $\text{crtCost} < \text{minCost}$

$$\text{minCost} = \text{crtCost}$$

$$\text{minTour} = (v_1, v_2, v_3, \dots, v_n)$$

return minTour

$$\text{Total RT} = O((n-1)! \cdot n) = \underline{O(n!)}$$

$$\boxed{\text{RT} = O(n!)}$$

Knapsack Problem (v, w, W)

if $v.length \neq w.length$
return error

$n = v.length$ // n is the number of items

$maxValue = 0$

$maxValueSubset = \emptyset$

$O(2^n)$ for each subset S of items

totalWeight = 0

totalValue = 0

$O(n)$ for $i = 1$ to n

if item $i \in S$

totalWeight = totalWeight + $w[i]$

totalValue = totalValue + $v[i]$

if totalWeight $\leq W$ and totalValue $> maxValue$

$maxValue = totalValue$

$maxValueSubset = S$

return $maxValueSubset$

$RT = O(n \cdot 2^n)$

Assignment Problem (c)

// c has size $n \times n$

$n = c.size$

$minCost = \infty$

$minCostAssign = \emptyset$

$O(n!)$ for each permutation $j_1, j_2, j_3, \dots, j_n$

cost = 0

$O(n)$ for $i = 1$ to n

cost = cost + $c[i, j_i]$

if cost $< minCost$

$minCost = cost$

$minCostAssign = j_1, j_2, \dots, j_n$

return $minCostAssign$

$RT = O(n \cdot n!)$