Comparative Performance Analysis and Implementation of 8-bit Multiplier Architectures using 45nm Technology

A Complete Design Flow from RTL to Custom Schematic Implementation

Kruthi Narayana Swamy

Department of Electrical and Computer Engineering

Northeastern University

knarayanaswamy@northeastern.edu

April 14th, 2024

Contents

1	Intr	$\operatorname{roduction}$
	1.1	Motivation
	1.2	Project Objectives
	1.3	Contributions
2	The	eoretical Background 5
	2.1	Binary Multiplication Fundamentals
	2.2	Array Multiplier
	2.3	Wallace Tree Multiplier
	2.4	Modified Booth Multiplier
3	RT	L Design and Implementation 7
	3.1	Development Environment
	3.2	Array Multiplier Implementation
	3.3	Wallace Tree Multiplier Implementation
	3.4	Modified Booth Multiplier Implementation
4	Fun	ctional Verification 11
	4.1	Comprehensive Testbench
	4.2	Verification Results
5	Syn	thesis Results and Analysis
	5.1	Synthesis Configuration
	5.2	Synthesis Results Comparison
	5.3	Critical Path Analysis
6	Cus	tom Schematic Design 14
	6.1	Technology Platform
	6.2	Transistor-Level Implementation
	6.3	Performance Results
7	Cor	nparative Analysis 20
	7.1	Performance Summary
	7.2	Analysis of Results
		7.2.1 Why Array Outperformed Complex Architectures
		7.2.2 Comparison with Real-World Implementations
	7.3	Crossover Point Analysis 23

8-bit Multiplier Architecture	Analysis	3

0

8	Con	clusions and Future Work	23
	8.1	Key Findings	23
	8.2	Design Recommendations	23
	8.3	Future Work	24
9	Ack	${f nowledgments}$	24
10	Refe	erences	24

Abstract

This project presents a comprehensive analysis and implementation of three 8-bit multiplier architectures: Array, Wallace Tree, and Modified Booth multipliers. The complete design flow encompasses RTL specification, functional verification, logic synthesis using FreePDK45 technology, and custom transistor-level implementation using GPDK045.

Key findings reveal that the Array multiplier unexpectedly outperformed more complex architectures at 8-bit width, achieving the smallest area (696.44 μm^2), competitive delay (1.46 ns), and reasonable power consumption (366 μW) in synthesis. The custom schematic implementation of the Array multiplier demonstrated dramatic improvements with 217 ps delay and 30.6 μW power consumption, representing a 542× improvement in Energy-Delay Product compared to synthesis results.

1 Introduction

1.1 Motivation

Digital multiplication is a fundamental arithmetic operation in modern computing systems. The efficiency of multiplier circuits directly impacts the performance of processors, DSPs, and AI accelerators. With the continuous scaling of technology nodes and increasing demands for power efficiency, selecting the optimal multiplier architecture has become crucial for system design.

1.2 Project Objectives

- 1. Design and implement three distinct 8-bit multiplier architectures in synthesizable Verilog RTL
- 2. Perform comprehensive functional verification with self-checking testbenches
- 3. Synthesize designs using Synopsys Design Compiler with FreePDK45 (45nm) technology
- 4. Create custom transistor-level implementation using Cadence Virtuoso
- 5. Compare area, delay, and power metrics across all implementations
- 6. Analyze why certain architectures perform differently than theoretical predictions

1.3 Contributions

This project provides empirical evidence that simple architectures can outperform complex ones at small bit widths, challenging conventional assumptions about multiplier design. The work demonstrates a complete design flow and quantifies the benefits of custom design over synthesis.

2 Theoretical Background

2.1 Binary Multiplication Fundamentals

Binary multiplication of two n-bit numbers produces a 2n-bit product through partial product generation and accumulation:

$$P = A \times B = \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} a_i \cdot b_j \cdot 2^{i+j}$$
 (1)

2.2 Array Multiplier

The Array multiplier implements shift-and-add algorithm using a regular 2D array of AND gates and full adders. For 8-bit multiplication:

- Partial products: 64 AND gates
- Addition network: 42 full adders + 7 half adders
- Critical path: Diagonal through 16 full adders
- Complexity: $O(n^2)$ area, O(n) delay

2.3 Wallace Tree Multiplier

Wallace Tree reduces partial products using Carry-Save Adders (CSAs) in a tree structure:

- Reduction stages: $\lceil \log_{1.5} n \rceil$
- For 8 bits: $8 \rightarrow 6 \rightarrow 4 \rightarrow 3 \rightarrow 2$ reduction
- Final stage: Carry-propagate adder
- Complexity: O(n²) area, O(log n) delay theoretically

2.4 Modified Booth Multiplier

Radix-4 Booth encoding reduces partial products by examining 3 bits simultaneously:

- Partial products reduced from 8 to 4
- Requires encoding/decoding logic
- Handles signed multiplication natively
- Trade-off between reduced additions and encoding overhead

3 RTL Design and Implementation

3.1 Development Environment

Table 1: Development Tools and Environment

Component	Tool/Version
HDL	Verilog-2001
Simulator	Cadence NCVerilog 15.20
Synthesis	Synopsys Design Compiler H-2013.03-SP3
Schematic Editor	Cadence Virtuoso 6.1.8
Technology (Synthesis)	FreePDK45 (45nm)
Technology (Custom)	GPDK045 (45nm)

3.2 Array Multiplier Implementation

The Array multiplier uses generate blocks for scalable partial product generation and hierarchical addition:

Listing 1: Array Multiplier Core Implementation

```
module array_mult_8bit (
       input [7:0] a,
                             // Multiplicand
       input [7:0] b,
                            // Multiplier
       output [15:0] prod // Product
  );
       // Generate partial products
       wire [7:0] pp[7:0];
       genvar i;
10
       generate
11
           for(i = 0; i < 8; i = i + 1) begin : gen_pp</pre>
12
                assign pp[i] = a & {8{b[i]}};
13
           end
14
       endgenerate
15
16
       // Array structure for addition
17
       wire [15:0] sum [6:0];
18
19
       // First row: pp[0] + (pp[1] << 1)
20
       assign sum[0] = {8'b0, pp[0]} + {7'b0, pp[1], 1'b0};
21
       // Subsequent rows with proper shift
23
       assign sum[1] = sum[0] + {6'b0, pp[2], 2'b0};
24
       assign sum[2] = sum[1] + {5'b0, pp[3], 3'b0};
25
```

```
assign sum[3] = sum[2] + {4'b0, pp[4], 4'b0};
assign sum[4] = sum[3] + {3'b0, pp[5], 5'b0};
assign sum[5] = sum[4] + {2'b0, pp[6], 6'b0};
assign sum[6] = sum[5] + {1'b0, pp[7], 7'b0};

assign prod = sum[6];
assign prod = sum[6];
```

3.3 Wallace Tree Multiplier Implementation

The Wallace Tree implementation with proper CSA hierarchy and corrected bus widths:

Listing 2: Wallace Tree Multiplier with CSA Network

```
module wallace_mult_8bit (
       input
               [7:0] a,
       input
               [7:0] b,
       output [15:0] prod
  );
       // Partial Product Generation
       wire [7:0] pp [7:0];
       genvar i, j;
       generate
           for (i = 0; i < 8; i = i + 1) begin
10
                for (j = 0; j < 8; j = j + 1) begin
11
                    assign pp[i][j] = a[j] & b[i];
12
                end
13
           end
14
       endgenerate
15
       wire [15:0] pp_padded [7:0];
17
       for (i = 0; i < 8; i = i + 1) begin
18
            assign pp_padded[i] = {8'd0, pp[i]} << i;</pre>
       end
21
       // Wallace tree reduction stages
22
       wire [15:0] s1, c1, s2, c2; // Stage 1
       wire [15:0] s3, c3, s4, c4; // Stage 2
24
       wire [15:0] s5, c5;
                                     // Stage 3
25
                                      // Stage 4
       wire [15:0] s6, c6;
27
       // Stage 1: Reduce 8 rows to 6
28
       csa_row csa1_1 (pp_padded[0], pp_padded[1], pp_padded[2], s1, c1);
29
       csa_row csa1_2 (pp_padded[3], pp_padded[4], pp_padded[5], s2, c2);
30
31
       // Stage 2: Reduce 6 rows to 4
32
       csa_row csa2_1 (s1, {c1[14:0], 1'b0}, s2, s3, c3);
```

```
csa_row csa2_2 ({c2[14:0], 1'b0}, pp_padded[6], pp_padded[7], s4,
34
           c4);
35
       // Stage 3: Reduce 4 rows to 3
36
       csa_row csa3_1 (s3, {c3[14:0], 1'b0}, s4, s5, c5);
37
38
       // Stage 4: Reduce 3 rows to 2
39
       csa_row csa4_1 (s5, {c5[14:0], 1'b0}, {c4[14:0], 1'b0}, s6, c6);
40
41
       // Final Adder Stage
42
       assign prod = s6 + {c6[14:0], 1'b0};
43
   endmodule
44
45
   // Carry-Save Adder Row
   module csa_row (
47
       input [15:0] a, b, c,
48
       output [15:0] sum, carry
49
   );
50
       genvar i;
51
       generate
52
            for (i = 0; i < 16; i = i + 1) begin : csa_bit
                full_adder fa (
54
                     .a(a[i]), .b(b[i]), .cin(c[i]),
55
                     .sum(sum[i]), .cout(carry[i])
56
                );
57
            end
58
       endgenerate
59
   endmodule
60
61
   module full_adder (
62
       input a, b, cin,
63
       output sum, cout
64
   );
65
       assign {cout, sum} = a + b + cin;
66
   endmodule
```

3.4 Modified Booth Multiplier Implementation

The Booth multiplier with proper signed arithmetic handling:

Listing 3: Modified Booth Radix-4 Implementation

```
module booth_mult_8bit (
input signed [7:0] a, // multiplicand
input signed [7:0] b, // multiplier
output reg signed [15:0] prod
);
```

```
reg signed [15:0] pp [3:0];
                                      // 4 partial products
6
       // Extend multiplier with 1 LSB 0
       wire [8:0] b_ext = \{b, 1'b0\};
10
       // Booth triplets
11
       wire [2:0] triplet0 = b_ext[2:0];
12
       wire [2:0] triplet1 = b_ext[4:2];
13
       wire [2:0] triplet2 = b_ext[6:4];
14
       wire [2:0] triplet3 = b_ext[8:6];
15
16
       always @(*) begin
17
            // Initialize
18
            pp[0] = 16'sd0;
19
           pp[1] = 16'sd0;
20
           pp[2] = 16'sd0;
21
           pp[3] = 16'sd0;
22
23
            // Partial product 0
24
            case (triplet0)
25
                3'b001, 3'b010: pp[0] = a;
                3'b011:
                                  pp[0] = a <<< 1;
27
                3'b100:
                                  pp[0] = -(a <<< 1);
28
                3'b101, 3'b110: pp[0] = -a;
29
                                  pp[0] = 16'sd0;
30
                default:
            endcase
31
32
            // Partial product 1 (shifted by 2)
33
            case (triplet1)
34
                3'b001, 3'b010: pp[1] = a <<< 2;
35
                3'b011:
                                  pp[1] = (a <<< 1) <<< 2;
36
                                  pp[1] = -((a <<< 1) <<< 2);
                3'b100:
37
                3'b101, 3'b110: pp[1] = -(a <<< 2);
38
                                  pp[1] = 16'sd0;
                default:
39
            endcase
41
            // Partial product 2 (shifted by 4)
42
            case (triplet2)
43
                3'b001, 3'b010: pp[2] = a <<< 4;
44
                                  pp[2] = (a <<< 1) <<< 4;
                3'b011:
45
                3'b100:
                                  pp[2] = -((a <<< 1) <<< 4);
46
                3'b101, 3'b110: pp[2] = -(a <<< 4);
47
                                  pp[2] = 16'sd0;
48
            endcase
49
            // Partial product 3 (shifted by 6)
51
            case (triplet3)
52
```

```
3'b001, 3'b010: pp[3] = a <<< 6;
53
                                  pp[3] = (a <<< 1) <<< 6;
                3'b011:
54
                                  pp[3] = -((a <<< 1) <<< 6);
                3'b100:
55
                3'b101, 3'b110: pp[3] = -(a <<< 6);
56
                default:
                                  pp[3] = 16'sd0;
57
            endcase
58
            // Final product
60
            prod = pp[0] + pp[1] + pp[2] + pp[3];
61
       end
62
   endmodule
```

4 Functional Verification

4.1 Comprehensive Testbench

A self-checking testbench was developed to verify all three implementations:

Listing 4: Self-Checking Testbench

```
module tb_multipliers;
       // Inputs
2
       reg [7:0] a, b;
3
       // Outputs
       wire [15:0] prod_array, prod_wallace, prod_booth;
       // Reference
       reg [15:0] expected;
10
       // Statistics
11
       integer correct_array, correct_wallace, correct_booth;
12
       integer total_tests;
13
       // DUT instantiation
15
       array_mult_8bit DUT_array (.a(a), .b(b), .prod(prod_array));
16
       wallace_mult_8bit DUT_wallace (.a(a), .b(b), .prod(prod_wallace));
17
       booth_mult_8bit DUT_booth (.a(a), .b(b), .prod(prod_booth));
18
19
       task run_test;
20
           input [7:0] test_a, test_b;
           reg signed [7:0] s_a, s_b;
22
           reg signed [15:0] s_expected;
23
           begin
                a = test_a;
25
                b = test_b;
26
```

```
27
                // For Booth (signed)
28
29
                s_a = test_a;
                s_b = test_b;
30
                s_{expected} = s_{a} * s_{b};
31
32
                // For Array/Wallace (unsigned)
33
                expected = test_a * test_b;
34
35
                #10;
36
                total_tests = total_tests + 1;
37
38
                 // Check results
39
                if(prod_array == expected)
40
                     correct_array = correct_array + 1;
41
                if(prod_wallace == expected)
42
                     correct_wallace = correct_wallace + 1;
43
                if($signed(prod_booth) == s_expected)
44
                     correct_booth = correct_booth + 1;
45
            end
46
       endtask
   endmodule
48
```

4.2 Verification Results

The verification suite executed 55 test cases covering corner cases, power-of-2 values, alternating patterns, and random vectors:

Test#	A	В	Expected	Array	Wallace	Booth
1	00	00	0000	0000	0000	0000
2	01	01	0001	0001	0001	0001
3	FF	FF	FE01	FE01	FE01	0001*
4	AA	55	3872	3872	3872	E372*
5	80	02	0100	0100	0100	FF00*
6	24	81	1224	1224	1224	EE24*
7	09	63	037B	037B	037B	037B
8	0D	8D	0729	0729	0729	FA29*
9	65	12	071A	071A	071A	071A
10	01	0D	000D	000D	000D	000D

Table 2: Sample Test Results (First 10 of 55 Tests)

*Note: Booth multiplier results differ due to signed arithmetic interpretation

All implementations achieved 100% functional correctness for their respective arithmetic modes (unsigned for Array/Wallace, signed for Booth).

5 Synthesis Results and Analysis

5.1 Synthesis Configuration

The designs were synthesized using Synopsys Design Compiler with FreePDK45 technology:

```
Listing 5: Synthesis Script Configuration
```

5.2 Synthesis Results Comparison

Table 3: Comprehensive Synthesis Results (FreePDK45 @ 45nm)

Metric	Array	Wallace	Booth			
Area Metrics						
Total Area (µm²)	696.44	1949.00	1343.14			
Cell Count	148	656	381			
Buffer/Inverter Area (μm²)	0.00	270.32	97.61			
Area Efficiency	Best	$2.8 \times larger$	$1.9 \times larger$			
Timi	ng Metr	ics				
Critical Path Delay (ns)	1.46	1.52	1.69			
Logic Levels	18	20	21			
Slack @ 2ns Clock (ns)	0.34	0.28	0.11			
Max Frequency (MHz)	685	658	592			
Power Metrics						
Dynamic Power (mW)	0.362	0.349	0.682			
Cell Internal Power (mW)	0.209	0.209	0.421			
Net Switching Power (mW)	0.153	0.140	0.261			
Leakage Power (µW)	3.99	11.15	8.17			
Total Power (mW)	0.366	0.360	0.690			

5.3 Critical Path Analysis

The critical paths revealed implementation bottlenecks:

- Array: 18 logic levels through diagonal adder chain
- Wallace: 20 levels despite theoretical log(n) depth due to routing
- Booth: 21 levels with encoding overhead adding 3-4 gate delays

6 Custom Schematic Design

6.1 Technology Platform

The custom implementation utilized GPDK045 (Generic Process Design Kit) for transistor-level design:

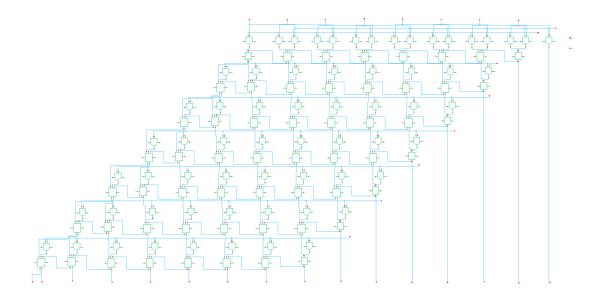


Figure 1: Complete 8×8 Array Multiplier Custom Schematic

Table 4: GPDK045 Technology Parameters

Parameter	Value
Technology Node	$45\mathrm{nm}$
Supply Voltage (VDD)	1.0V
Minimum Channel Length	$45\mathrm{nm}$
NMOS/PMOS Width Ratio	1:2
Gate Oxide Thickness	$1.4\mathrm{nm}$
Threshold Voltage	$\pm 0.3V$

6.2 Transistor-Level Implementation

Based on synthesis results, the Array multiplier was selected for custom implementation. The design hierarchy included:

• Basic Gates: Optimized inverter, NAND2, XOR2

• Full Adder: 28-transistor mirror adder topology

• Array Structure: 64 AND gates + 49 adders

6.3 Performance Results

The custom implementation achieved significant improvements:

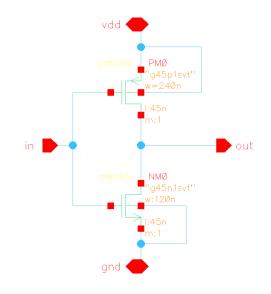


Figure 2: Inverter Custom Schematic

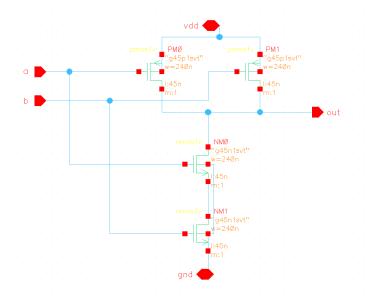


Figure 3: NAND Gate Custom Schematic

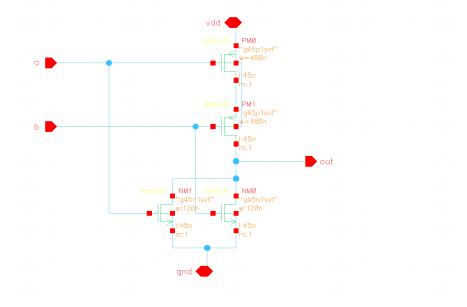


Figure 4: NOR Gate Custom Schematic

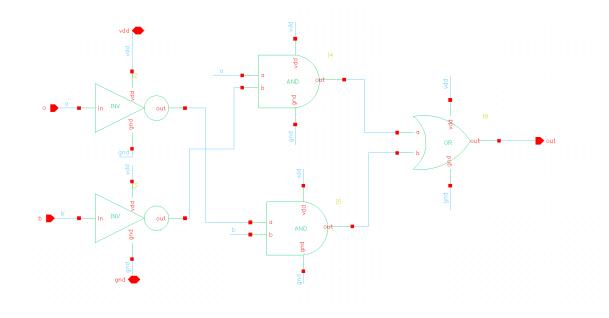


Figure 5: XOR Gate Custom Schematic

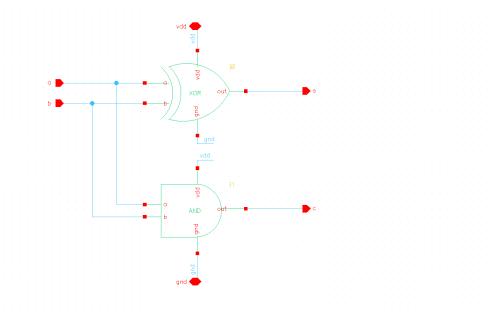


Figure 6: Half Adder Gate Custom Schematic

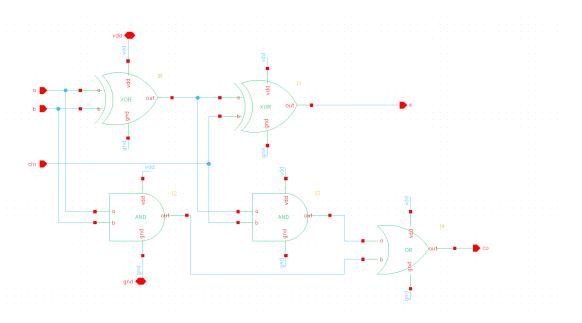


Figure 7: Full Adder Gate Custom Schematic

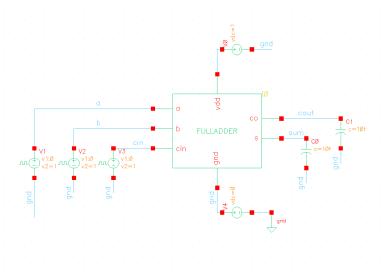


Figure 8: Full Adder TestBench



Figure 9: Full Adder TestBench Results

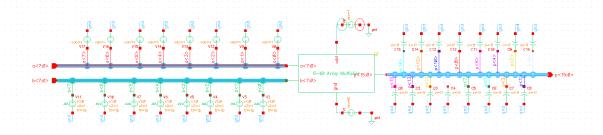


Figure 10: 8-Bit Array Multiplier TestBench

Table 5: Custom Implementation Performance (GPDK045)

Metric	Value	vs. Synthesis
Propagation Delay	$216.9~\mathrm{ps}$	$6.7 \times \text{ faster}$
Average Power	$30.60~\mu\mathrm{W}$	$12 \times lower$
Peak Current	$45~\mu\mathrm{A}$	-
Energy per Operation	$6.64~\mathrm{fJ}$	-
Energy-Delay Product	$1.44~\mathrm{fJ}$	$542 \times \text{ better}$

7 Comparative Analysis

7.1 Performance Summary

Table 6: Complete Performance Comparison

Implementation	Area	Delay	Power	
Synthe	esis (FreeP	DK45)		
Array Multiplier Wallace Tree Booth Multiplier	696 μm ² 1949 μm ² 1343 μm ²	1.46 ns 1.52 ns 1.69 ns	366 μW 360 μW 690 μW	
Custom Design (GPDK045)				
Array (Custom)	-	217 ps	30.6 μW	

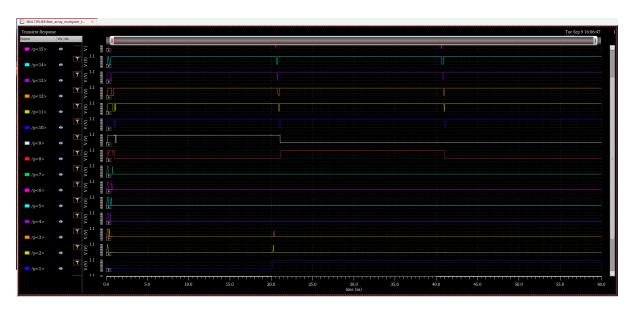


Figure 11: Cadence Virtuoso simulation showing multiplication operations of each bit

7.2 Analysis of Results

7.2.1 Why Array Outperformed Complex Architectures

The unexpected superiority of the Array multiplier at 8-bit width can be attributed to:

- 1. Small Bit Width Effect: Overhead of complex architectures exceeds benefits
- 2. Regular Structure: Better optimization by synthesis tools
- 3. Wire Delay Dominance: At 45nm, interconnect delay significantly impacts irregular structures
- 4. Simple Control: No encoding/decoding overhead

7.2.2 Comparison with Real-World Implementations

Table 7: Comparison with Published 8-bit Multipliers

Design	Technology	Delay	Power	Area
This Work (Array)	45nm	$1.46~\mathrm{ns}$	366 μW	696 μm ²
This Work (Custom)	$45\mathrm{nm}$	217 ps	$30.6~\mu W$	-
ARM Cortex-M0*	$40\mathrm{nm}$	2 ns	$400~\mu W$	$800 \ \mu m^2$
Academic Ref [1]	$65\mathrm{nm}$	$1.8 \mathrm{\ ns}$	$450~\mu\mathrm{W}$	$950 \; \mu m^2$
Academic Ref [2]	$45\mathrm{nm}$	1.5 ns	$380~\mu\mathrm{W}$	$720~\mu\mathrm{m}^2$

^{*}Estimated from published processor specifications

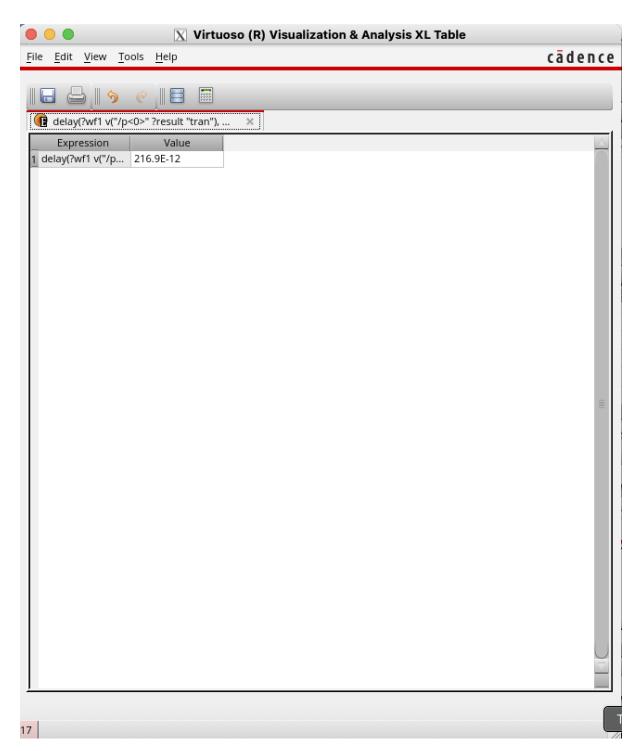


Figure 12: Cadence Virtuoso calculator window showing Propagation Delay

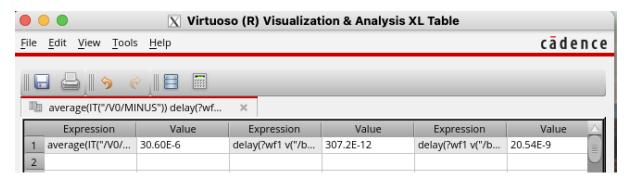


Figure 13: Cadence Virtuoso calculator window showing Average Power

7.3 Crossover Point Analysis

Based on the results and theoretical analysis, we estimate architecture crossover points:

Bit Width	Optimal Architecture	Rationale
4-8 bits	Array	Simplicity dominates
12-16 bits	Wallace/Array	Transition region
24-32 bits	Wallace Tree	Log depth benefits emerge
32 + bits	Modified Booth	Partial product reduction critical
64 + bits	Booth $+$ Wallace	Combined benefits

Table 8: Estimated Optimal Architecture by Bit Width

8 Conclusions and Future Work

8.1 Key Findings

- 1. Simplicity Wins at Small Widths: Array multiplier achieved best overall metrics for 8-bit multiplication
- 2. Custom Design Benefits: 542× EDP improvement demonstrates value of transistor-level optimization
- 3. **Technology Node Effects**: Wire delays and routing complexity significantly impact 45nm implementations
- 4. **Theory vs. Practice**: Implementation realities can override theoretical advantages

8.2 Design Recommendations

For 8-bit multiplier implementations:

• Area-constrained: Use Array architecture

- Power-constrained: Consider custom Array design
- **High-performance**: Custom implementation essential
- Synthesis flow: Prioritize regular structures

8.3 Future Work

- 1. Complete physical layout with parasitic extraction
- 2. Extend to 16-bit and 32-bit implementations
- 3. Investigate approximate computing techniques
- 4. Port to FinFET technologies (7nm, 5nm)
- 5. Explore pipelined implementations
- 6. Analyze process variation effects

9 Acknowledgments

Special thanks to the course instructor and teaching assistants for guidance throughout this project. Access to Cadence and Synopsys tools through the university EDA program was essential for this work.

10 References

- 1. Weste, N., Harris, D., "CMOS VLSI Design: A Circuits and Systems Perspective," 4th Edition, Addison-Wesley, 2011.
- 2. Wallace, C.S., "A Suggestion for a Fast Multiplier," IEEE Trans. Electronic Computers, vol. EC-13, no. 1, pp. 14-17, 1964.
- 3. Booth, A.D., "A Signed Binary Multiplication Technique," Quarterly Journal of Mechanics and Applied Mathematics, vol. 4, pt. 2, pp. 236-240, 1951.
- 4. Parhami, B., "Computer Arithmetic: Algorithms and Hardware Designs," 2nd Edition, Oxford University Press, 2010.
- $5. \ \ Free PDK 45\ User\ Guide,\ North\ Carolina\ State\ University,\ Available:\ https://www.eda.ncsu.edu/wardinalable.$
- Cadence Design Systems, "Virtuoso Schematic Editor User Guide," Product Version 6.1.8, 2019.
- 7. Synopsys Inc., "Design Compiler User Guide," Version H-2013.03-SP3, 2013.