Rapid Scheduling: A Constraint Satisfaction Approach to River Usage

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1 Preliminaries

1.1 Introduction

Floating down a river is easy enough, but imagine scheduling an entire season of rafting trips for hundreds of people. A *scheduling problem* occurs when there are start and end times and start and end locations for a group of people or objects. The schedules of the group must be arranged such that all participants start and stop as desired. Between the start and stop, they must follow any rules stated in the problem.

We consider a scheduling problem for the Big Long River with visitors who desire to raft down it. The goal is to schedule as many visitors as possible in a six month season. Visitors depart from First Launch and finish at Final Exit, 225 miles downstream. They are seeking a relaxing and authentic experience and will become dissatisfied if they do not receive one. While scheduling dissatisfied visitors is allowed, we seek to schedule them so as many visitors are as satisfied as possible.

1.2 Definitions and Terminology

- Carrying Capacity: The amount of visitors a river can see in a single year, while maintaining the likelihood that all visitors will be scheduled and remain satisfied.
- Constraint Satisfaction Problem (CSP): A type of problem solved by assigning values to variables. Our working definition for such a problem follows: given variables (X), values (D), and constraints (C), find an assignment of value(s) in D for each X such that all constraints in C are satisfied. Generally speaking, a CSP may be defined as a set (X, D, C). A good example of a CSP is any map coloring problem[1].
- Group: See "visitor."
- Itinerary: The ordered list of campsites a visitor will stay at each night.
- Non-deterministic Polynomial-Time Hard Problem (NP-hard): A class of problems whose solutions, if they exist, behave unpredictably, and are provable in polynomial time see "Big O." Constraint Satisfaction Problems are a type of NP-hard problem.
- Visitor: Also "group." A person or a group of people seeking to travel the Big Long River by raft. Their raft could be powered by oar, or it could be motorized.

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Visitors are very irritable and will become unhappy if they see other visitors, don't get their desired water time each day, or don't get scheduled.

- Satisfaction: (of a visitor) Visitors seeking to raft the Big Long River start with a satisfaction of 100. This number will drop each time the visitor passes or is passed by another visitor, or doesn't get their desired water time (too much or too little of it) each day. It is possible for a visitor's satisfaction to drop to zero by these two factors alone. Visitors who are not able to be scheduled have a satisfaction of zero.
- Season: A six month season is assumed to have 180 days; that is, six months times an average of 30 days per month.
- Success Rate: The likelihood a season will have a valid schedule given certain parameters.
- Tolerance: The amount of campsites a visitor's travel plan can be altered by. For instance, a tolerance of 1 would allow a visitor desiring to move four campsites each day to move between three and five campsites each day. This is done in order to accommodate for other visitors who may be in the desired spot.
- Water Time: Visitors specify how much time they want to spend on the water each day. This value is the same for each day of the trip. A visitor's satisfaction rating will drop if they are forced to spend more or less than this amount of time on the water.
- X: The current number of trips taken by visitors down the Big Long River each year.
- Y: The number of campsites on the Big Long River. Unless otherwise stated, this was assumed to be 128, as provided by literature[2].

1.3 Assumptions and Simplifications

- Season Length: A six month season is assumed to have 180 days; that is, six months times an average of 30 days per month. Seasons are consistent, i.e. there exist no peak visitation months or months of higher river flow.
- Trips ranging from "6 to 18 nights of camping on the river, start to finish" are assumed to allow between 7 and 19 days of travel on the river, start to finish.

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• Visitors or groups of visitors travel at a constant speed throughout the trip. We define this speed by the type of boat they use. Oar-powered rubber rafts travel at 4 mph, and motorized boats travel at 8 mph.

- No visitor separates into more than one group or combines with other groups during the trip.
- "Contact with other groups of boats on the river" is only counted if one group passes another group or is passed by another group.
- Groups are capable of passing one another at any point (i.e. passing is not restricted by the width of the river or anything else at any time).
- Visitors specify only their starting date, boat type, and water time, and only valid values for these parameters. Therefore: They may not start before the start of the season or so close to the end of the season it would be impossible for them to finish; they may not have a water time such that their trip takes less than 7 or longer than 19 days; they may only choose an oar-powered rubber raft or a motorized boat.
- Visitors follow the schedule given to them exactly: no backtracking, skipping.

2 The Solution

We view the problem of scheduling rafting trips as a progressive and dynamic CSP. Each day is a constraint satisfaction problem dependent upon the solution to the previous day's problem. By limiting the values any variable may take on and applying efficient algorithms, the CSP becomes reasonably simple algorithmically speaking.

2.1 Constraint Satisfaction

Consider that there are exponentially many combinations of visitors to campsites during a season. Many of these combinations, however, are invalid since no two visitors may stay at the same campsite on the same day. This is an n-ary constraint: a constraint relating n variables. This sort of complexity often causes problems to become computationally intractable. We, however, simply pair all campers and detect collisions at any campsite at the current scheduled day $(O(n^2))$ with n as number of visitors). This small simplification reduces the problem to relatively few constraints.

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Each visitor is considered to be a variable in the CSP and campsites are considered the values. The domain of each visitor's values varies day to day as the visitor travels through the campsites. Travel distance is derived from a visitor's average speed of 4 or 8 mph, v, multiplied with a uniformly distributed random variable for water time, t. This variable must allow the visitor to complete the trip within 7-19 days. The following equations explicitly describe these relationships:

$$v * t = OptimalDayDistance$$

$$v*t*7 \ge L$$

We ensure generated visitors are reasonably parameterized to finish a trip on time. Each visitor is assigned a random uniformly distributed day for departure, dDay, such that

$$v * t * 7 + dDay \le S$$

A visitor's maximum travel speed will allow them to finish before the close of the season.

Visitors are generated en masse using uniformly distributed variables. It is possible to load a file containing visitor information so the program will work on problems of natural rather than simulated origin. Once visitors are generated and basic parameters are set (discussed in **Section 2.2**) the program begins attempting a solution through our solver.

2.1.1 Backtracking Search

In order to solve a CSP, one must navigate many combinations for variables and values. Backtracking search algorithms are often used to assign values to variables [4]. We use such an algorithm to assign campsites to our visitors on a daily basis. On any given day d, the solver looks to see which visitors are set to depart that day and adds them to a list, toDepart. Then, all visitors left on the river from the previous day are added to toDepart. This creates a list of all visitors requiring movement for day d. In order to determine appropriate movements, visitors are assigned campsites one-by-one. Travel between campsites is analogous to distance traveled for the day. Following a visitor-campsite pairing, the day's assignments are checked to see if this pairing is consistent. If the pairing doesn't conflict with existing pairings, it is permanently added to the day's assignments. We then proceed to the next visitor.

When pairings fail, the algorithm attempts new pairings until success is achieved or no more pairings exist. The entire process is structured as a depth-first-search. When Team # 16677 Page 6 of 13

a day's assignment is complete, the algorithm creates a new CSP for the next day and executes again. **Figure 1** highlights the major steps involved in this process with a simple example. The algorithm begins by assigning site 1 to visitor A, denoted by the diamond below and to the left of the tree-top. Assigning site 1 to B is tried but found to fail. Instead the algorithm assigns site 2 to B (rightmost circle). At this point, the day would "end" and the algorithm would begin scheduling the next day. In the event the next day fails, the algorithm returns to a previous level, as seen in the example. In this case, the previous level is the previous day.

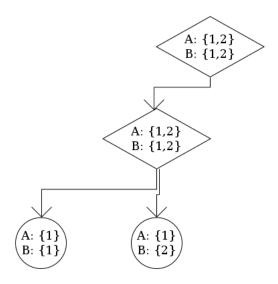


Figure 1: An example of the backtracking algorithm's attempt to schedule visitors A and B with campsites 1 and 2.

Our solver seeks maximal satisfaction of the travelers. That is, the possible campsites a visitor may travel to are presented to the solver in order of ideal travel distance. While not every visitor is guaranteed to travel their desired distance, the algorithm attempts to satisfy it.

We also calculate the number of encounters between visitors. After the itineraries are created, each visitor's campsite listing is checked to determine how many visitors passed and were passed by this specific visitor. By combining the amount of variation from ideal travel distance and encounters with other visitors, we obtain the total effect on satisfaction. The solver relies heavily on several parameters to relax the problem, making solutions more attainable.

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2.2 Usage of High-Level Parameters

Many values tend to be static. These include river length, number of days in the season, and number of campsites. While each of these values is capable of drastically affecting the outcome of a given attempt, this effect is limited by a well-defined range (see **Section 1.3**). There are likely optimal values, but finding these would likely place our problem into the realm of intractable problems. In an attempt to capture the complexity of this system, we have introduced a unique variable, tolerance.

Tolerance is designed to create a range for the distance a visitor may travel in a given day. This variable is straightforward at the outset but provides several neat nuances for additional complexity in the solution. The introduction of a value range allows for a larger domain of solutions and variability. We desire such flexibility to account for the real-world uncertainty of directing human beings. Tolerance extends as an aggregate for many of the instances where we might expect variability —such as inclement weather, cancellations, or slow visitors— without having to introduce additional parameters. Tolerance is a satisfying opportunistic variable for allowing more visitors to be scheduled. It allows for the rafting season to be enjoyed by more individuals.

It is important to note a lack of tolerance often creates problems with no solutions. With visitors locked between one of two travel distances, scheduling becomes virtually impossible for all but the smallest number of visitors.

3 Predictions and Analysis

3.1 General Expectations

Before creating the model we developed a few "common sense" expectations of the results.

- Increasing the visitor size would make it harder to schedule each visitor at the desired time. The more visitors one is trying to schedule, the faster the schedule fills up.
- As the number of visitors on the river during a season increases, it becomes increasingly likely visitors will pass each other. Passing is a necessity if the visitors are traveling at different daily speeds. Consider a visitor with a daily speed of 8 mph leaving a few days after a visitor traveling at 4 mph.
- As tolerance increases, so will the ease of scheduling each visitor. The greater the

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tolerance, the greater the likelihood of finding a site to stay at if other visitors are also in the area.

- An increase in tolerance will cause a decrease in overall happiness. An increase in tolerance will allow visitors to travel less than or more than their desired time each day. Thus decreasing their overall satisfaction.
- Assigning more visitors to motor boats (those that travel at 8mph) will increase the success rate. Visitors that travel faster will spend fewer days on the river, leaving more space for other visitors.
- Seasons with less variability in visitor speeds (e.g. seasons where all visitors travel at 4mph, or where all visitors travel at 8mph) will result in greater satisfaction. Visitors traveling at the same speed are less likely to pass each other or to want to stay at the same campsite on the same night. Greater variation in group speeds will increase the frequency of these conflicts.

3.2 Results

The following discusses various results from repeated simulations of our model. Each major variable is addressed, but major conclusions are saved for later (beginning in **Section 3.3**)

The results of the model tended to be in line with our expectations (**Section 3.1**), especially with our baseline values for parameters as discussed in **Section 1.3**. For seasons with a 2-site tolerance, the success rate was seen to decrease as the number of visitors increased (**Figure 2 Spark 1**).

The success rate was 100% for seasons with 5, 50, and 100 visitors (see **Figure 3**). Once the number of visitors per season increased past 100, the success rate began decreasing at an increasing rate. Further increases in the number of visitors produced the following points of interest:

• The success rate dropped from 100% to 91% between 100 and 300 visitors.



Figure 2: 1: Success Rate vs. Visitors, 2: Satisfaction vs. Visitors, 3: Satisfaction vs. Visitors, 4: Success Rate and Satisfaction vs. Tolerance, 5: Tolerance vs. Success Rate and Satisfaction

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- By 500 visitors, the success rate had fallen to below 25%.
- At 600 visitors the success rate appears to level off, asymptotically, between zero and 5%.

These values seem to follow an inverse of the problem's solution space.

Similarly, the average satisfaction of the visitors decreased with an increase in the number of visitors (**Figure 2 Spark 2**). Once the number of visitors per season increased past 100, the satisfaction score began decreasing at an increasing rate. Satisfaction dropped from 97.9% to 89.4% between 100 and 300 campers, then from 89.4% to 24.5% between 300 and 500 campers. For seasons with more than 500 groups, satisfaction leveled off, appearing to have an asymptote just above zero percent. The satisfaction for a season with 600 visitors was 4.9%.

For seasons with a 1-site tolerance, the effect of visitor size increased (**Figure 2 Spark 3**). Both the success rate and satisfaction of visitors decreased with just a visitor size of only 50 people. The success rate dropped from 100% to 96% when visitor sized increased from 5 to 50 visitors per season. By just 250 visitors, both the success rate and the satisfaction were zero percent.

The tolerance for which campsite visitors stayed at each night had a positive effect on success rate of the scheduler and satisfaction of the visitors (**Figure 2 Spark 4**). We noted the following points of interest:

- For seasons with 200 visitors, a tolerance of zero campsites had a success rate of 0% and satisfaction of zero percent.
- Increasing the tolerance to one campsite resulted in a success rate of 52% and a satisfaction of 4.9%.
- Increasing the tolerance to two campsites had the greatest effect, raising success rate to 97.8% and satisfaction to 95.9%.

With any greater tolerances, the success rate was 100%, and the satisfaction leveled off at 97.8%. These results for tolerance agree with the notion that the additional variability allows for more successful schedules.

For seasons with 500 visitors, a greater tolerance was needed to achieve similar results (**Figure 2 Spark 5**). A tolerance of 0 campsites had a success rate of 0; a tolerance of 1 campsite had a success rate of only 2.6%; 2 campsites, 28%; 3 campsites, 90%. The success rate was only 100% with a tolerance of greater than 4 campsites, and the satisfaction was 98%.

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Assigning more visitors to motorboats (those that travel at 8 mph) was seen to increase the success rate. For a homogeneous season of 8 mph visitors, the success rate was 98.2% and the satisfaction 74%. As the number of 4 mph boats increased, both success rate and satisfaction steadily decreased. With half rowboats and half motorboats, the success rate was 92% and the satisfaction 72%. With a 9:1 ratio of rowboats to motorboats, the success rate of the season was only 89.9%. However, there is a jump in success rate to 99% once all visitors are traveling at 4 mph. This jump in successes is not accompanied by a jump in satisfaction; with all rowboats, the satisfaction is only 70%. This sort of relationship between the mix of craft type and success rate is somewhat surprising, given that an even mix might make more sense. At this time, we have no clear explanation for such behavior.

3.3 Analysis

As defined in our definitions section, carrying capacity is the amount of visitors a river can see in a single year while maintaining the likelihood that all visitors will be scheduled and remain satisfied. With a tolerance of 2 campsites (**Figure 3**), we found the river could manage 100 visitors per season with a 100% success rate and a satisfaction of at least 97%. It is worth noting that doubling the capacity to 200 visitors per seasons yields a success rate of 99.5% and a satisfaction still greater than 97%. Once the number of visitors per season increases past 200, both success rate and tolerance begin to drop rapidly. With a tolerance of 1 campsite, we found the river could only manage about five visitors per season with a success rating of 100%. The average satisfaction of these visitors is 97.7%. After the number of visitors per season increases above 50, both satisfaction and success rate begin dropping rapidly as seen in **Figure 4**.

Is our value of 300 visitors, which was reasonably successful and maximal, realistic? Assuming that it is possible to have 60 individuals in a visitor group, we find that our model allows for 18,000 people in a season to travel down the Big Long River. Our sources suggest this is realistic for comparable rivers (i.e. the Colorado River)[3].

4 Conclusion

Throughout, we have seen that a constraint satisfaction approach to scheduling visitors to a river is a natural fit. This approach allows for a logical approach to the scheduling process, and for fairly quick solutions. In most cases, solutions were found on personal hardware in less than ten minutes. We also found that the structure of our solution

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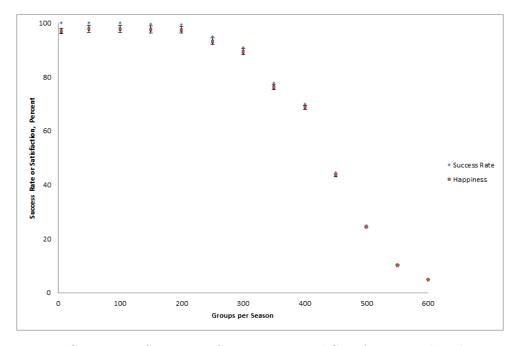


Figure 3: Groups per Season vs. Success Rate and Satisfaction with Tolerance 2

in both code and at a higher level lent itself well to the adjustment of any number of parameters. Moreover, there exists a great deal of flexibility once one begins to define "fuzzy values" that we can assign to the variables. Given more time, extending the model with these fuzzy values would likely lead to better assignments and even more interesting results. We would also consider additional algorithmic improvements for performance or allowing for campsites to rest, providing an ecological component.

In our assumptions (**Section 1.3**) we note that the visitors are basically perfect. This, of course, is not true. Due either to inclement weather, rudeness, or physical constraints we can not expect this behavior. It is not immediately apparent how to deal with this shortcoming other than simply accepting all variables can not be accounted for. Padding the schedules with "free days" on which any amount of travel lag may be recuperated.

The use of a consistent river in our model is less detrimental to the overall performance and accuracy. A realistic river would include areas where passing other groups is impossible, visitors travel faster or slower, and the potential for divisions of the river. These could all be built in as constraints on the campsites and their assignment to visitors. Should we have more time, this would likely be incorporated into the model.

Designating an exact number of visitors to raft down a river each year is a complex problem that may not have only one solution. Managers will need to be assertive in desTeam # 16677 Page 12 of 13

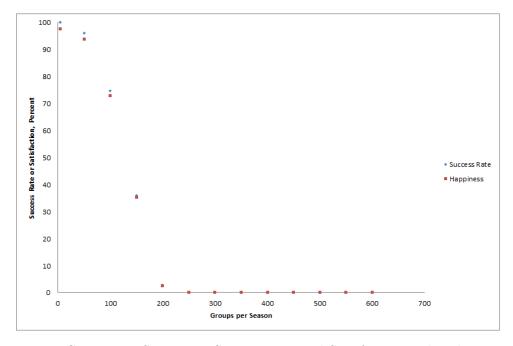


Figure 4: Groups per Season vs. Success Rate and Satisfaction with Tolerance 1

ignating a tolerance, allotting departure days and boat types to visitors, and instructing visitors to follow their schedules carefully. Given certain parameters, however, we recommend a tolerance of 2 campsites, and about 300 visitors per season. Depending upon the current number of visitors each season, X, this would mean increasing the number of visitors by 300-X. Note that those 300 visitors may be groups, not necessarily individuals. A tolerance of 2 campsites permits a large number of visitors per season while maintaining acceptable visitor satisfaction. Any greater tolerance would create a sharp decrease in satisfaction as visitors are forced to travel unfortunate distances; any smaller tolerance greatly decreases the chance of a successful schedule for any large number of visitors. Any more than 300 visitors is likely to drop both the chance of a successful season and the satisfaction of visitors.

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References

[1] R. Dechter and A. Dechter, Belief maintenance in dynamic constraint networks in proc. of aaai-88, 1988.

- [2] Will Hansen, Whitewater Campsites colorado-grand canyon, 2009.
- [3] Catherine A. Roberts Randy Gimblett, Integrating gis and agent based modeling techniques for understanding social and ecological processes, Oxford Press, 2000.
- [4] Stuart J. Russell and Peter Norvig, Artificial intelligence: A modern approach, Prentice Hall, 2010.