M-M PAPER, MORPHOLOGICAL DEPENDENCE, RED SEQUENCE

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ABSTRACT

We present the latest scaling relations between black hole mass, $M_{\rm BH}$, and spheroid luminosity, $L_{\rm sph}$, spheroid stellar mass, $M_{*,sph}$, and galaxy luminosity, L_{gal} , built upon an unprecedented high-quality data set (provided here in a ready-to-use table). Our sample, the largest ever used, counts 66 local galaxies with a dynamical measurement of $M_{
m BH}$. Spheroid luminosities come from high signal-tonoise 3.6 μ m Spitzer satellite imagery, which is minimally affected by dust and star formation. These luminosities were derived from our state-of-the-art multicomponent galaxy decompositions, that take into account bulges, disks, bars, spiral arms, rings, haloes, extended or unresolved nuclear sources and partially depleted cores, and that – for the first time – were checked to be consistent with the galaxy kinematics. Previous studies used galaxy samples that were overwhelmingly dominated by high-mass, early-type objects. Instead, our sample includes 17 spiral galaxies, half of which have $M_{\rm BH} < 10^7 {\rm M}_{\odot}$, and allows us to investigate the poorly studied low-mass end of the correlations. We provide updated linear regressions (symmetrical, to be compared with theoretical expectations, and non-symmetrical, to be used to predict black hole masses) for Sérsic/core-Sérsic galaxies and for different morphological types (E/S0, Sp). The bulges of early-type (E/S0) galaxies follow $M_{\rm BH} \propto M_{\rm *,sph}^{1.0\pm0.1}$, as expected from a dry-merging formation scenario, and define a tight red sequence with intrinsic scatter $\epsilon = 0.43\pm0.06$. On the other hand, the bulges of late-type (Sp) galaxies define a much steeper blue sequence, with $M_{\rm BH} \propto M_{*,\rm sph}^{3.0\pm1.3}$, indicating that gas-rich processes feed the black hole three times more efficiently than the host bulge. Disproving some previous claims, we also conclude that: 1) Sérsic and core-Sérsic galaxies do not define two distinct sequences; 2) bulges with Sérsic index $n_{\rm sph} < 2$, argued by some to be pseudo-bulges, are not offset to lower $M_{\rm BH}$ from the correlation defined by bulges with $n_{\rm sph} > 2$; 3) $L_{\rm sph}$ and $L_{\rm gal}$ correlate equally well with $M_{\rm BH}$ only for early-type galaxies.

$Subject\ headings:$ keywords

1. INTRODUCTION

More than two and a half decades ago, Dressler (1989) foresaw a "rough scaling of black hole mass with the mass of the spheroidal component", as suggested by the sequence of five galaxies (M87, M104, M31, M32 and the Milky Way). His "rough scaling" was a premature version of the nowadays popular correlation between black hole mass, $M_{\rm BH}$, and host spheroid luminosity, $L_{\rm sph}$, and also host spheroid mass, $M_{\rm sph}$ (Yee 1992; Kormendy & Richstone 1995; Magorrian et al. 1998; Marconi & Hunt 2003; Häring & Rix 2004). These early studies were dominated by high-mass, early-type galaxies, for which they reported a quasi-linear $M_{\rm BH}-M_{\rm sph}$ relation, consistent with a dry-merging formation scenario. Subsequent studies of the $M_{\rm BH}-L_{\rm sph}$ and $M_{\rm BH}-M_{\rm sph}$ diagrams (Ferrarese & Ford 2005; Lauer et al. 2007a; Graham 2007,

2008; Gültekin et al. 2009; Sani et al. 2011; Beifiori et al. 2012; Erwin & Gadotti 2012; Vika et al. 2012; van den Bosch et al. 2012; McConnell & Ma 2013; Kormendy & Ho 2013; Rusli et al. 2013a; see Graham 2015 for an extensive review about the early discovery and successive improvements of these correlations) used similar galaxy samples, which remained dominated by high-mass, earlytype objects having $M_{\rm BH} \gtrsim 0.5 \times 10^8 {\rm M}_{\odot}$, and recovered a near-linear relation. However, the consensus about a linear $M_{\rm BH}-M_{\rm sph}$ correlation was not unanimous. Some studies reported a slope steeper than one, or noticed that low-mass spheroids were downwards offset from the relation traced by their high-mass counterparts (Laor 1998; Wandel 1999; Laor 2001; Ryan et al. 2007). Recently, Läsker et al. (2014a,b) derived 2.2 μ m bulge luminosities for 35 galaxies (among which only 4 were classified as spiral galaxies), and reported a slope below unity for their $M_{\rm BH}-M_{\rm sph}$ relation. They also claimed that the black hole mass correlates equally well with the total galaxy luminosity as it does with the bulge luminosity.

The $M_{\rm BH}-L_{\rm sph}$ relation can be predicted from other two correlations involving the bulge velocity dispersion, σ . The first of these two is the $M_{\rm BH}-\sigma$ relation (Ferrarese & Merritt 2000; Gebhardt et al. 2000), which can be described by a single power-law $(M_{\rm BH} \propto \sigma^5)$ over the range in velocity dispersion $70 - 350 \text{ km s}^{-1}$ (e.g. Graham et al. 2011; McConnell et al. 2011; Graham & Scott 2013). The second is the $L_{\rm sph}-\sigma$ relation, which has long been known to be a "double power-law", being $L_{\rm sph} \propto \sigma^5$ at the luminous end (Schechter 1980; Malumuth & Kirshner 1981; von der Linden et al. 2007; Liu et al. 2008), and $L_{\rm sph} \propto \sigma^2$ at intermediate and faint luminosities (Davies et al. 1983; Held et al. 1992; Matković & Guzmán 2005; de Rijcke et al. 2005; Balcells et al. 2007; Chilingarian et al. 2008; Forbes et al. 2008; Cody et al. 2009; Tortora et al. 2009; Kourkchi et al. 2012). The change in slope of the $L_{\rm sph}$ – σ relation occurs at $M_B \approx -20.5$ mag, corresponding to $\sigma \approx 200 \text{ km s}^{-1}$. That is, the $M_{\rm BH} - L_{\rm sph}$ relation should be better described by a "broken", rather than a single, power-law, having $M_{\rm BH} \propto L_{\rm sph}^{2.5}$ at the low-luminosity end, and $M_{\rm BH} \propto L_{\rm sph}^1$ at the high-luminosity end. Due to the scatter in the $M_{\rm BH}-L_{\rm sph}$ (or $M_{\rm BH}-M_{\rm sph}$) diagram, studies that have not sufficiently probed below $M_{\rm BH} \approx 10^7 \ {\rm M_{\odot}}$ can easily miss the change in slope occuring at $M_{\rm BH} \approx 10^{(8\pm1)}~{\rm M}_{\odot}$, and erroneously recover a single log-linear relation.

When Graham (2012) pointed out this overlooked inconsistency, he identified two different populations of galaxies, namely the core-Sérsic (Graham et al. 2003; Trujillo et al. 2004) and Sérsic spheroids¹, and attributed the change in slope (from log-quadratic to log-linear) to their different formation mechanisms. In this scenario, core-Sérsic spheroids are built in additive dry merger events, where the black hole and the bulge grow at the same pace, increasing their mass in lock steps $(M_{\rm BH} \propto L_{\rm sph}^1)$, whereas Sérsic spheroids originate from gas-rich processes, in which the mass of the black hole increases more rapidly than the mass of its host spheroid $(M_{\rm BH} \propto L_{\rm sph}^{2.5})$. Graham & Scott (2013, hereafter GS13) and Scott et al. (2013, hereafter S+13) presented double power-law linear regressions for Sérsic/core-Sérsic spheroids in the $M_{\rm BH}-L_{\rm sph}$ and $M_{\rm BH}-M_{*,\rm sph}$ (spheroid stellar mass) diagrams, respectively, probing down to $M_{\rm BH} \approx 10^6 {\rm M}_{\odot}$. To obtain their dust-corrected bulge magnitudes, they did not perform bulge/disc decompositions, but instead they converted B-band and K_S -band observed, total galaxy magnitudes using a mean statistical correction based on each object's morphological type and disc inclination². However, this mean statistical

correction was obtained from the results of non-modern bulge/disk decompositions, which did not include extra components. It should also be noted that $\sim\!80\%$ of their core-Sérsic spheroids were morphologically classified as elliptical galaxies, and $\sim\!80\%$ of their Sérsic spheroids were morphologically classified as bulges of disk galaxies (lenticulars and spirals).

Several recent papers (Jiang et al. 2011, 2013; Mathur et al. 2012; Reines et al. 2013) claimed an offset at the low-mass end of the $M_{\rm BH}-M_{\rm *,sph}$ diagram, such that the black hole mass is lower than expected from the nearlinear correlation traced by the high-mass, early-type spheroids. However, Graham & Scott (2015) showed that the low-mass spheroids ($10^{8.5} \lesssim M_{\rm *,sph}/{\rm M}_{\odot} \lesssim 10^{10.5}$) are not somehow randomly offset from the high-mass, near-linear correlation, but lie on the two times steeper relation traced by the Sérsic spheroids. AL: would you like to add a sentence here, mentioning your forthcoming paper with ewan?

Here we investigate substructure in the $M_{\rm BH}-L_{\rm sph}$ and $M_{\rm BH}-M_{*,\rm sph}$ diagrams using state-of-the-art galaxy decompositions (Savorgnan & Graham in preparation, hereafter Paper I) for the largest sample of galaxies with directly measured black hole masses. Our galaxies are large and nearby, which allows us to perform accurate multicomponent decompositions (instead of simple bulge/disk decompositions) without incurring in significant parameter degeneracies. Our decompositions were obtained from 3.6 μ m Spitzer satellite imagery, which is an excellent proxy for the stellar mass, superior to the K-band (Sheth et al. 2010 and references therein). Nine of our galaxies have $M_{\rm BH} \lesssim 10^7~{\rm M}_{\odot}$, which allows us to accurately constrain the slope of the correlation at the low-mass end. In addition to this, our galaxy sample includes 17 spiral galaxies, representing a notable improvement over the past studies dominated by early-type systems. In a forthcoming paper, we will explore the relation between black hole mass and bulge dynamical mass, $M_{\rm dyn,sph} \propto R_{\rm e}\sigma^2$, and address the issue of a black hole fundamental plane. This paper is structured as follows...

2. Data

Our galaxy sample (see Table 1) consists of 66 objects for which a dynamical measurement of the black hole mass had been reported in the literature (GS13, Rusli et al. 2013b) at the time we started this project, and for which we were able to obtain useful bulge parameters from 3.6 μ m Spitzer satellite imagery. Bulge magnitudes were derived from our state-of-the-art galaxy decompositions, which take into account bulges, disks, spiral arms, bars, rings, haloes, extended or unresolved nuclear sources and partially depleted cores. Kinematical information (Emsellem et al. 2011; Scott et al. 2014; Arnold et al. 2014) was used to confirm the presence of rotationally supported components in most early-type galaxies, and to identify their extent (intermediate-scale, embedded disks or large-scale disks). Paper I will present the dataset used here to investigate the $M_{\rm BH}-L_{\rm sph}$ and $M_{\rm BH} - M_{*,\rm sph}$ diagrams, give details about the data reduction process and the sophisticated galaxy modelling technique that we developed, discuss how we estimated the uncertainties on the bulge parameters, and illustrate

reasonably ensemble average correction.

 $^{^1}$ Core-Sérsic spheroids have partially depleted cores relative to their outer Sérsic light profile, whereas Sérsic spheroids have no central deficit of stars. While core-Sérsic spheroids are also "core galaxies", as given by the Nuker definition (Lauer et al. 2007b), it should be noted that $\sim\!20\%$ of "core galaxies" are not core-Sérsic spheroids (Dullo & Graham 2014, their Appendix A.2), i.e. do not have depleted cores. The change in slope of the $L_{\rm sph}-\sigma$ relation corresponds to the division between core-Sérsic and Sérsic spheroids (e.g. Graham & Guzmán 2003).

spheroids (e.g. Graham & Guzmán 2003).

² While this resulted in individual bulge magnitudes not being exactly correct, their large sample size allowed them to obtain a

the individual 66 galaxy decompositions.

Bulge luminosities³ were first converted into stellar masses using a constant 3.6 μ m mass-to-light ratio, $\Gamma_{3.6} = 0.6$ (Meidt et al. 2014). We then explored a more sophisticated way to compute mass-to-light ratios, using the color- $\Gamma_{3.6}$ relation published by Meidt et al. (2014, their equation 4), which allows one to estimate $\Gamma_{3.6}$ of a galaxy from its [3.6] - [4.5] color. Individual [3.6] - [4.5]colors⁴ were taken from Peletier et al. (2012, column 8 of their Table 1) when available for our galaxies, or were estimated from the bulge stellar velocity dispersion, σ , using the color- σ relation presented by Peletier et al. (2012, their Figure 6). We found that the range in [3.6] - [4.5]color is small (0.06 mag), and thus the range in $\Gamma_{3.6}$ is also small (0.04). After checking that using a single $\Gamma_{3.6} = 0.6$, independent of [3.6] - [4.5] color, does not significantly affect the results of our analysis, we decided to use individual, color-dependent mass-to-light ratios. The Sérsic/core-Sérsic classification presented in this work comes from the compilation of Savorgnan & Graham (2014), who identified partially depleted cores according to the same criteria used by GS13. When no high-resolution image analysis was available from the literature, they inferred the presence of a partially depleted core based on the stellar velocity dispersion: a galaxy is classified as core-Sérsic if $\sigma > 270 \text{ km s}^{-1}$, or as Sérsic if $\sigma < 166 \text{ km s}^{-1}$.

For each galaxy, the total luminosity (or galaxy luminosity, $L_{\rm gal}$) is the sum of the luminosities of all its subcomponents. Due to the complexity of their modelling, four galaxies (see Table 1, column 7) had their galaxy luminosities underestimated⁵, which are given here as lower limits.

3. ANALYSIS

We performed a linear regression analysis of the $M_{\rm BH} L_{\rm sph},~M_{\rm BH}-M_{*,\rm sph}$ and $M_{\rm BH}-L_{\rm gal}$ diagrams using the BCES code from Akritas & Bershady (1996) and also the FITEXY routine (Press et al. 1992) modified by Tremaine et al. (2002) to account for the intrinsic vertical scatter, ϵ . Because the BCES routine **AL**: did you wanna write (correctly) this sentence for me please? can give biased results (wrong slope) when the scatter is comparable to the range of the data, we checked that the best-fit parameters obtained with the BCES code were consistent with those output by the modified FITEXY code. In Table 3 we report the BCES and modified FITEXY linear regressions. both symmetrical and non-symmetrical, for Sérsic/core-Sérsic galaxies and for different galaxy morphological types (elliptical/lenticular, spiral). Symmetrical regressions are meant to be compared with theoretical expectations, whereas non-symmetrical Ordinary Least Squares (Y|X) regressions – since they minimize the scatter in the vertical direction – can be used to predict black hole masses.

4. RESULTS AND DISCUSSION

 $\begin{array}{c} 10^{11} \\ 10^{10} \\ \hline \\ 10^{8} \\ 10^{8} \\ 10^{6} \\ \hline \\ -20 \ -21 \ -22 \ -23 \ -24 \ -25 \ -26 \ -27 \\ \hline \\ MAG_{\rm sph} \ [{\rm mag}] \end{array}$

FIG. 1.— Black hole mass against 3.6 μm spheroid absolute magnitude. Symbols are coded according to the galaxy morphological type: red circle = elliptical, red star = elliptical/lenticular, red upward triangle = lenticular, blue downward triangle = lenticular/spiral, blue square = spiral, black diamond = merger. Empty symbols represent core-Sérsic spheroids, whereas filled symbols are used for Sérsic spheroids. The red dashed line indicates the BCES bisector linear regression for early-type galaxies (ellipticals+lenticulars), with the red shaded area denoting its 1σ uncertainty. The blue solid line shows the BCES bisector linear regression for spiral galaxies, with the blue shaded area denoting its 1σ uncertainty. The black dashed-dotted and dotted lines represent the BCES bisector linear regressions for core-Sérsic and Sérsic spheroids, respectively.

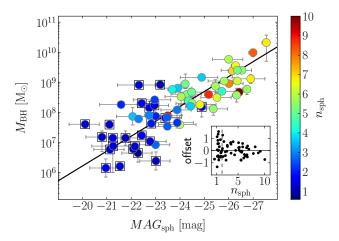


FIG. 2.— Black hole mass against 3.6 $\mu \rm m$ spheroid absolute magnitude. Symbols are color coded according to the spheroid Sérsic index $n_{\rm sph}$. Bulges with $n_{\rm sph} < 2$, claimed by some to be pseudobulges, are marked with an empty square. The black solid line shows the BCES bisector linear regression for spheroids with $n_{\rm sph} \geq 2$. The inset displays, for all spheroids, the vertical offset from the correlation defined by spheroids with $n_{\rm sph} \geq 2$ only versus the spheroid Sérsic index. The vertical dashed line corresponds to $n_{\rm sph} = 2$. Bulges with $n_{\rm sph} < 2$ are not randomly offset to lower black hole masses from the correlation traced by bulges with $n_{\rm sph} \geq 2$.

4.1. Black hole mass - spheroid luminosity

We show the $M_{\rm BH}-L_{\rm sph}$ diagram in Figure 1. Sérsic and core-Sérsic spheroids have slopes consistent with each other (within their 1σ uncertainties), in dis-

 $^{^3}$ Absolute luminosities were calculated assuming a 3.6 μm solar absolute magnitude of 3.25 mag (Sani et al. 2011).

 $^{^4}$ These are integrated [3.6] – [4.5] colors, measured in a circular aperture within one galaxy's effective radius.

⁵ These four cases will be discussed in *Paper I*.

TABLE 1

TABLE 1

Galaxy sample. Column (1): Galaxy name. Column (2): Morphological type (E=elliptical, S0(B)=(barred) lenticular, Sp(B)=(barred) spiral, merger=merger). Column (3): Presence of a partially depleted core. The question mark is used when the classification has come from the velocity dispersion criteria mentioned in Section 2. Column (4): Distance. Column (5): Black hole mass. Column (6): Absolute 3.6 μm bulge magnitude. Column (7): Absolute 3.6 μm galaxy magnitude. The four galaxy magnitudes marked with a * are upper limits. Column (8): [3.6] – [4.5] colour. Column (9): Bulge stellar mass.

| Galaxy | Type | Core | Distance [Mpc] | $M_{ m BH} = [10^8 { m M}_{\odot}]$ | MAG_{sph} [mag] | $MAG_{ m gal}$ [mag] | [3.6] - [4.5] [mag] | $M_{*,{ m sph}} = [10^{10} { m M}_{\odot}]$ |
|----------|----------------------------|------|-------------------|--|---|----------------------|---------------------|--|
| (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) |
| IC 1459 | \mathbf{E} | yes | 28.4 | 24^{+10}_{-10} | $-26.15^{+0.18}_{-0.11}$ | -26.15 ± 0.15 | -0.12 | 27^{+30}_{-23} |
| IC 2560 | SpB | no? | 40.7 | $0.044^{+0.044}_{-0.022}$ | $-22.27_{-0.58}^{-0.11}$ | -24.76 ± 0.08 | -0.08 | $1.0_{-0.6}^{-23.8}$ |
| IC 4296 | \mathbf{E} | yes? | 40.7 | 11^{+2}_{-2} | $-26.35^{+0.18}_{-0.11}$ | -26.35 ± 0.10 | -0.12 | 31^{+34}_{-26} |
| M104 | S0/Sp | yes | 9.5 | $6.4_{-0.4}^{+0.4}$ | $-23.91^{+0.66}_{-0.58}$ | -25.21 ± 0.06 | -0.12 | $3.4^{+5.8}_{-1.9}$ |
| M105 | E | yes | 10.3 | 4_{-1}^{+1} | $-24.29^{+0.66}_{-0.58}$ | -24.29 ± 0.27 | -0.10 | $5.6^{+9.5}_{-3.0}$ |
| M106 | SpB | no | 7.2 | $0.39^{+0.01}_{-0.01}$ | $-21.11^{+0.18}_{-0.11}$ | -24.04 ± 0.17 | -0.08 | $0.37^{+0.41}_{-0.31}$ |
| M31 | SpB | no | 0.7 | $1.4^{+0.9}_{-0.3}$ | $-22.74^{+0.18}_{-0.11}$ | -24.67 ± 0.02 | -0.09 | $1.5^{+1.6}_{-1.3}$ |
| M49 | E | yes | 17.1 | 25^{+3}_{-1} | $-26.54^{+0.18}_{-0.11}$ | -26.54 ± 0.11 | -0.12 | 39^{+43}_{-33} |
| M59 | E | no | 17.8 | $3.9_{-0.4}^{+0.4}$ | $-25.18^{+0.18}_{-0.11}$ | -25.27 ± 0.02 | -0.09 | 14^{+15}_{-11} |
| M64 | Sp | no? | 7.3 | $0.016^{+0.004}_{-0.004}$ | $-21.54^{+0.18}_{-0.11}$ | -24.24 ± 0.06 | -0.06 | $0.64_{-0.55}^{+0.71}$ |
| M81 | SpB | no | 3.8 | $0.74^{+0.21}_{-0.11}$ | $-23.01^{+0.88}_{-0.66}$ | -24.43 ± 0.30 | -0.09 | $1.9^{+3.6}_{-0.9}$ |
| M84 | \mathbf{E} | yes | 17.9 | $9.0^{+0.9}_{-0.8}$ | $-26.01^{+0.66}_{-0.58}$ | -26.01 ± 0.02 | -0.10 | 28^{+47}_{-15} |
| M87 | \mathbf{E} | yes | 15.6 | $58.0_{-3.5}^{+3.5}$ | $-26.00^{+0.66}_{-0.58}$ | -26.00 ± 0.12 | -0.11 | 26^{+44}_{-14} |
| M89 | \mathbf{E} | yes | 14.9 | $4.7^{+0.5}_{-0.5}$ | $-24.48^{+0.66}_{-0.58}$ | -24.74 ± 0.10 | -0.11 | $6.3^{+10.7}_{-3.4}$ |
| M94 | SpB | no? | 4.4 | $0.060^{+0.014}_{-0.014}$ | $-22.08^{+0.18}_{-0.11}$ | -23.36 ± 0.08 * | -0.07 | $1.00_{-0.85}^{+1.11}$ |
| M96 | SpB | no | 10.1 | $0.073^{+0.015}_{-0.015}$ | $-22.15^{+0.18}_{-0.11}$ | -24.20 ± 0.27 | -0.08 | $0.97^{+1.08}_{-0.83}$ |
| NGC 0524 | $\hat{S0}$ | yes | 23.3 | $8.3^{+2.7}_{-1.3}$ | $-23.19_{-0.11}^{+0.18}$ | -24.92 ± 0.05 | -0.09 | $2.2^{+2.5}_{-1.9}$ |
| NGC 0821 | \mathbf{E} | no | 23.4 | $0.39^{+0.26}_{-0.09}$ | $-24.00^{+0.88}_{-0.66}$ | -24.26 ± 0.01 | -0.09 | $4.7^{+8.7}_{-2.1}$ |
| NGC 1023 | SOB | no | 11.1 | $0.42^{+0.04}_{-0.04}$ | $-22.82^{+0.18}_{-0.11}$ | -24.20 ± 0.02 | -0.10 | $1.5^{-1.7}_{-1.3}$ |
| NGC 1300 | SpB | no | 20.7 | $0.73^{+0.69}_{-0.25}$ | $-22.06^{+0.66}_{-0.58}$ | -24.16 ± 0.00 | -0.10 | $0.70^{+1.19}_{-0.28}$ |
| NGC 1316 | merger | no | 18.6 | $1.50_{-0.80}^{+0.75}$ | $-24.89^{+0.66}_{-0.58}$ | -26.48 ± 0.05 | -0.10 | $9.5^{+16.2}_{5.2}$ |
| NGC 1332 | E/S0 | no | 22.3 | 14^{+2}_{-2} | $-24.89_{-0.66}^{+0.88}$ | -24.95 ± 0.03 | -0.12 | $8.2^{+15.0}_{-3.6}$ |
| NGC 1374 | E | no? | 19.2 | $5.8_{-0.5}^{-2.5}$ | $-23.68^{+0.18}_{-0.11}$ | -23.70 ± 0.08 | -0.09 | $3.6^{+3.0}_{-3.0}$ |
| NGC 1399 | \mathbf{E} | yes | 19.4 | $4.7^{+0.6}_{-0.6}$ | $-26.43^{+0.11}_{-0.11}$ | -26.46 ± 0.04 | -0.12 | 33^{+37}_{-28} |
| NGC 2273 | SpB | no | 28.5 | $0.083^{+0.004}_{-0.004}$ | 99.00 + 0.66 | -24.21 ± 0.15 | -0.08 | $2.0^{+3.4}$ |
| NGC 2549 | S0B | no | 12.3 | $0.14^{+0.02}_{-0.13}$ | $-23.00_{-0.58} -21.25_{-0.11}^{+0.18}$ | -22.60 ± 0.02 | -0.10 | $0.35^{+0.39}_{-0.30}$ |
| NGC 2778 | S0B | no | 22.3 | $0.15^{+0.09}_{-0.10}$ | $-20.80^{+0.66}_{-0.58}$ | -22.44 ± 0.07 | -0.09 | $0.25^{+0.43}_{-0.14}$ |
| NGC 2787 | S0B | no | 7.3 | $0.40^{+0.04}_{-0.05}$ | $-20.11^{+0.66}_{-0.58}$ | -22.28 ± 0.06 | -0.10 | $0.12^{+0.14}_{-0.07}$ |
| NGC 2974 | SpB | no | 20.9 | $1.7^{+0.2}_{-0.2}$ | $-22.95^{+0.66}_{-0.58}$ | -24.16 ± 0.04 | -0.09 | $1.8^{+3.1}_{-1.0}$ |
| NGC 3079 | SpB | no? | 20.7 | $0.024^{+0.024}_{-0.012}$ | $-23.01_{-0.58}^{+0.66}$ | -24.45 ± 0.04 * | -0.07 | $2.4^{+4.0}$ |
| NGC 3091 | E | yes | 51.2 | 36^{+1}_{-2} | $-26.28^{+0.18}_{-0.11}$ | -26.28 ± 0.09 | -0.12 | 30^{+34}_{-26} |
| NGC 3115 | E/S0 | no | 9.4 | $8.8^{+10.0}_{-2.7}$ | $-24.22^{+0.11}_{-0.11}$ | -24.40 ± 0.02 | -0.11 | $4.9^{+5.4}$ |
| NGC 3227 | $_{\mathrm{SpB}}^{\prime}$ | no | 20.3 | $0.14_{-0.06}^{+0.10}$ | $-21.76_{-0.58}^{+0.11}$ | -24.26 ± 0.10 | -0.08 | $0.67^{+1.15}_{-0.27}$ |
| NGC 3245 | S0B | no | 20.3 | $2.0^{+0.5}_{-0.5}$ | $-22.43^{+0.18}$ | -23.88 ± 0.03 | -0.10 | $1.0^{+1.1}_{-0.0}$ |
| NGC 3377 | E | no | 10.9 | $0.77^{+0.04}_{-0.06}$ | $-23.49^{+0.66}_{-0.58}$ | -23.57 ± 0.06 | -0.06 | $4.0^{+6.8}$ |
| NGC 3384 | SOB | no | 11.3 | $0.17^{+0.01}_{-0.02}$ | $-22.43^{+0.18}_{-0.11}$ | -23.74 ± 0.01 | -0.08 | $1.2^{+1.3}$ |
| NGC 3393 | SpB | no | 55.2 | $0.34_{-0.02}^{+0.02}$ | $-23.48^{+0.66}_{-0.58}$ | -25.29 ± 0.10 | -0.10 | $2.8^{-1.7}$ |
| NGC 3414 | E | no | 24.5 | 10.9 | 0.18 | -24.42 ± 0.02 | -0.09 | $6.5^{+7.2}$ |
| NGC 3489 | S0/SpB | no | 11.7 | $0.058^{+0.008}$ | $-21.13^{+0.66}_{-0.58}$ | -23.07 ± 0.05 | -0.06 | $0.42^{+0.72}$ |
| NGC 3585 | E | no | 19.5 | $3.1^{+1.4}_{-0.6}$ | $-25.52^{+0.66}_{-0.58}$ | -25.55 ± 0.03 | -0.10 | $18^{+30}_{10}^{-0.23}$ |
| NGC 3607 | E | no | 22.2 | $2.4_{-0.3}^{+0.3}$ $0.058_{-0.008}^{+0.008}$ $3.1_{-0.6}^{+1.4}$ $1.3_{-0.5}^{+0.5}$ $2.0_{-0.6}^{+1.1}$ 97_{-26}^{+30} $9.1_{-2.6}^{+2.0}$ | $\begin{array}{c} -24.59_{-0.11} \\ -21.13_{-0.58}^{+0.66} \\ -25.52_{-0.58}^{+0.66} \\ -25.36_{-0.58}^{+0.66} \\ -24.50_{-0.58}^{+0.66} \\ -27.00_{-0.11}^{+0.18} \\ -29.24_{-0.28}^{+0.86} \end{array}$ | -25.45 ± 0.11 | -0.10 | $0.5_{-5.5}^{+5.72}$ $0.42_{-0.23}^{+0.72}$ 18_{-10}^{+30} 15_{-8}^{+25} $7.8_{-4.3}^{+13.4}$ 61_{-52}^{+68} |
| NGC 3608 | E | yes | 22.3 | $2.0^{+1.1}$ | $-24.50^{+0.66}$ | -24.50 ± 0.15 | -0.08 | $7.8^{+13.4}$ |
| NGC 3842 | E | yes | 98.4 | 97^{+30}_{-36} | $-27.00^{+0.18}$ | -27.04 ± 0.06 | -0.11 | 61^{+68}_{-52} |
| NGC 3998 | S0B | no | 13.7 | 8.1 1.6 | $-22.32^{+0.88}_{-0.66}$ | -23.53 ± 0.01 | -0.12 | $0.78^{+1.43}$ |
| NGC 4026 | S0B | no | 13.2 | $1.8^{+0.6}_{-0.3}$ | $\begin{array}{c} 21.66_{-0.11} \\ -22.32_{-0.66}^{+0.88} \\ -21.58_{-0.66}^{+0.88} \\ -23.40_{-0.58}^{+0.66} \end{array}$ | -23.16 ± 0.04 | -0.09 | $0.78^{+1.43}_{-0.35}$ $0.50^{+0.92}_{-0.22}$ |
| NGC 4151 | $_{\mathrm{SpB}}$ | no | 20.0 | $0.65^{+0.07}_{-0.07}$ | $-23.40^{+0.66}$ | -24.44 ± 0.19 | -0.09 | $2.8^{+4.8}$ |
| NGC 4261 | E | yes | 30.8 | 5^{+1}_{-1} | $-25.72^{+0.66}_{-0.58}$ | -25.76 ± 0.20 | -0.12 | $2.8_{-1.5}^{+4.8}$ 18_{-10}^{+30} |
| NGC 4291 | E | yes | 25.5 | $3.3^{+0.9}_{-0.5}$ | $-24.05^{+0.66}$ | -24.05 ± 0.14 | -0.11 | $3.9^{+6.7}_{-2.1}$ |
| NGC 4388 | $_{\mathrm{SpB}}$ | no? | 17.0 | $0.075^{+0.002}_{-0.002}$ | 91.96 ± 0.88 | -23.50 ± 0.03 * | -0.07 | $0.46^{+0.85}_{-0.21}$ |
| NGC 4459 | SO | no | 15.7 | $\begin{array}{c} -2.3 \\ 0.075^{+0.002}_{-0.002} \\ 0.68^{+0.13}_{-0.13} \end{array}$ | $-23.48^{+0.66}_{-0.58}$ | -24.01 ± 0.05 | -0.09 | $2.9^{+5.0}_{-1.6}$ |

| Galaxy | Type | Core | Distance | $M_{ m BH}$ | MAG_{sph} | $MAG_{ m gal}$ | [3.6] - [4.5] | $M_{ m *,sph}$ |
|-----------|----------------------|------|----------|---------------------------|---------------------------|---------------------|---------------|-----------------------------|
| | | | [Mpc] | $[10^8 {\rm M}_{\odot}]$ | [mag] | [mag] | [mag] | $[10^{10} {\rm M}_{\odot}]$ |
| (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) |
| NGC 4473 | E | no | 15.3 | $1.2^{+0.4}_{-0.9}$ | $-23.88^{+0.66}_{-0.58}$ | -24.11 ± 0.02 | -0.10 | $3.9^{+6.6}_{-2.1}$ |
| NGC 4564 | S0 | no | 14.6 | $0.60_{-0.09}^{+0.03}$ | $-22.30^{+0.18}_{-0.11}$ | -22.99 ± 0.07 | -0.11 | $0.82^{+0.91}_{-0.70}$ |
| NGC 4596 | SOB | no | 17.0 | $0.79^{+0.38}_{-0.33}$ | $-22.73^{+0.18}_{-0.11}$ | -24.18 ± 0.05 | -0.08 | $1.6^{+1.7}_{-1.3}$ |
| NGC 4697 | \mathbf{E} | no | 11.4 | $1.8^{+0.2}_{-0.1}$ | $-24.82^{+0.88}_{-0.66}$ | -24.94 ± 0.00 | -0.09 | 10^{+18}_{-4} |
| NGC 4889 | \mathbf{E} | yes | 103.2 | 210^{+160}_{-160} | $-27.54^{+0.18}_{-0.11}$ | -27.54 ± 0.00 | -0.12 | 91^{+101}_{-77} |
| NGC 4945 | SpB | no? | 3.8 | $0.014^{+0.014}_{-0.007}$ | $-20.96^{+0.66}_{-0.58}$ | -23.79 ± 0.22 * | -0.06 | $0.36^{+0.62}_{-0.20}$ |
| NGC 5077 | \mathbf{E} | yes | 41.2 | $7.4^{+4.7}_{-3.0}$ | $-25.45^{+0.18}_{-0.11}$ | -25.45 ± 0.06 | -0.11 | 15^{+17}_{-13} |
| NGC 5128 | merger | no? | 3.8 | $0.45^{+0.17}_{-0.10}$ | $-23.89^{+0.88}_{-0.66}$ | -24.97 ± 0.13 | -0.07 | $5.0^{+9.1}_{-2.2}$ |
| NGC 5576 | \mathbf{E} | no | 24.8 | $1.6^{+0.3}_{-0.4}$ | $-24.44^{+0.18}_{-0.11}$ | -24.44 ± 0.07 | -0.09 | $7.1_{-6.0}^{+7.9}$ |
| NGC 5845 | S0 | no | 25.2 | $2.6_{-1.5}^{+0.4}$ | $-22.96^{+0.88}_{-0.66}$ | -23.10 ± 0.13 | -0.12 | $1.4^{+2.6}_{-0.6}$ |
| NGC 5846 | \mathbf{E} | yes | 24.2 | 11^{+1}_{-1} | $-25.81^{+0.66}_{-0.58}$ | -25.81 ± 0.10 | -0.10 | 22^{+38}_{-12} |
| NGC 6251 | \mathbf{E} | yes? | 104.6 | 5^{+2}_{-2} | $-26.75^{+0.18}_{-0.11}$ | -26.75 ± 0.11 | -0.12 | 46^{+51}_{-39} |
| NGC 7052 | \mathbf{E} | yes | 66.4 | $3.7^{+2.6}_{-1.5}$ | $-26.32_{-0.11}^{+0.118}$ | -26.32 ± 0.03 | -0.11 | 33^{+36}_{-28} |
| NGC 7619 | \mathbf{E} | yes | 51.5 | 25^{+8}_{-3} | $-26.35^{+0.66}_{-0.58}$ | -26.41 ± 0.16 | -0.11 | 33^{+56}_{-18} |
| NGC 7768 | \mathbf{E} | yes | 112.8 | 13^{+5} | $-26.90^{+0.66}_{-0.58}$ | -26.90 ± 0.02 | -0.11 | 57^{+98}_{-31} |
| UGC 03789 | SpB | no? | 48.4 | $0.108^{+0.005}_{-0.005}$ | $-22.77^{+0.88}_{-0.66}$ | -24.20 ± 0.15 | -0.07 | $1.9_{-0.8}^{+3.4}$ |

 $\begin{array}{c} {\rm TABLE} \ 2 \\ {\rm Linear} \ {\rm regression} \ {\rm analysis}. \ {\bf X0} \ {\bf is} \ {\bf the} \ {\bf average} \ {\bf X} \ {\bf of} \ {\bf the} \ {\bf subsample...} \end{array}$

| Subsample (size) | Regression | α | β | X_0 | ϵ | Δ |
|------------------------|--|---|---|---|--|---|
| | Black hole mass – sphe $\log[M_{\rm BH}/{\rm M_{\odot}}] = \alpha + \beta$ | | | | | |
| All (66) | BCES OLS($Y X$) BCES OLS($X Y$) BCES Bisector mFITEXY OLS($Y X$) mFITEXY OLS($X Y$) mFITEXY Bisector Kelly OLS($Y X$) | $\begin{array}{c} 8.16 \pm 0.07 \\ 8.16 \pm 0.08 \\ 8.16 \pm 0.07 \\ 8.17 ^{+0.07} \\ 8.15 ^{+0.07} \\ 8.16 ^{+0.07} \\ 8.16 ^{+0.07} \\ 8.16 ^{+0.07} \end{array}$ | $\begin{array}{c} -0.44 \pm 0.04 \\ -0.61 \pm 0.05 \\ -0.52 \pm 0.04 \\ -0.43 ^{+0.03} \\ -0.61 ^{+0.05} \\ -0.51 ^{+0.05} \\ -0.51 ^{+0.04} \\ -0.42 \pm 0.04 \\ -0.05 \\ -0.01 ^{+0.05} \\$ | -23.86 -23.86 -23.86 -23.86 -23.86 -23.86 | $\begin{array}{c} -\\ -\\ -\\ 0.49^{+0.06}_{-0.05} \\ 0.58^{+0.07}_{-0.06} \\ -\\ 0.50 \pm 0.06 \end{array}$ | 0.56 0.68 0.60 0.56 0.67 0.60 0.56 |
| $n > 2 \ (43)$ | Kelly $OLS(X Y)$ Kelly Bisector BCES $OLS(Y X)$ BCES $OLS(X Y)$ BCES Bisector mFITEXY $OLS(Y X)$ mFITEXY $OLS(X Y)$ | 8.16 ± 0.09 8.16 ± 0.08 8.58 ± 0.07 8.58 ± 0.07 8.58 ± 0.07 $8.57^{+0.07}_{-0.06}$ $8.56^{+0.08}_{-0.08}$ | $-0.60 \pm 0.06 -0.5 \pm 0.1$ $-0.42 \pm 0.06 -0.58 \pm 0.06 -0.50 \pm 0.05 -0.41 + 0.04 -0.57 + 0.06 -0.57 + 0.06$ | $ \begin{array}{r} -23.86 \\ -23.86 \\ -24.77 \\ -24.77 \\ -24.77 \\ -24.77 \\ -24.77 \end{array} $ | 0.60 ± 0.10 $ 0.38^{+0.06}_{-0.06}$ $0.44^{+0.08}_{-0.11}$ | 0.67 0.59 0.46 0.56 0.49 0.46 0.55 |
| | mFITEXY Bisector Kelly $OLS(Y X)$ Kelly $OLS(X Y)$ Kelly Bisector | $8.56^{+0.08}_{-0.08}$ $8.57^{+0.07}_{-0.07}$ 8.56 ± 0.07 8.55 ± 0.09 8.56 ± 0.08 | $-0.57_{-0.07}^{+0.06}$ $-0.49_{-0.05}^{+0.05}$ -0.39 ± 0.05 -0.57 ± 0.08 -0.5 ± 0.1 | -24.77 -24.77 -24.77 -24.77 | 0.40 ± 0.06 0.48 ± 0.11 | 0.49 0.46 0.55 0.49 |
| Core-Sérsic (22) | BCES OLS $(Y X)$ BCES OLS $(X Y)$ BCES Bisector mFITEXY OLS $(Y X)$ mFITEXY Bisector Kelly OLS $(Y X)$ Kelly OLS $(X Y)$ Kelly Bisector | $\begin{array}{c} 9.06 \pm 0.09 \\ 9.1 \pm 0.1 \\ 9.1 \pm 0.1 \\ 9.06^{+0.09}_{-0.08} \\ 9.0^{+0.1}_{-0.1} \\ 9.0^{+0.1}_{-0.1} \\ 9.0 \pm 0.1 \\ 9.0 \pm 1.4 \\ 9.0 \pm 1.0 \end{array}$ | $\begin{array}{c} -0.3 \pm 0.1 \\ -0.6 \pm 0.1 \\ -0.47 \pm 0.08 \\ -0.26^{+0.07}_{-0.08} \\ -0.7^{+0.2}_{-0.3} \\ -0.5^{+0.1}_{-0.2} \\ -0.24 \pm 0.09 \\ -0.7 \pm 16.1 \\ -0.4 \pm 1.1 \end{array}$ | $\begin{array}{c} -25.73 \\ -25.73 \\ -25.73 \\ -25.73 \\ -25.73 \\ -25.73 \\ -25.73 \\ -25.73 \\ -25.73 \\ -25.73 \\ -25.73 \end{array}$ | $\begin{array}{c} -\\ -\\ -\\ 0.37^{+0.08}_{-0.06} \\ 0.61^{+0.14}_{-0.09} \\ -\\ 0.40\pm0.09 \\ 0.7\pm19.0 \\ -\\ \end{array}$ | 0.42 0.61 0.48 0.42 0.67 0.48 0.42 0.64 0.46 |
| Sérsic (44) | BCES OLS $(Y X)$ BCES OLS $(X Y)$ BCES Bisector mFITEXY OLS $(Y X)$ mFITEXY Bisector Kelly OLS $(Y X)$ Kelly OLS $(X Y)$ Kelly Bisector | $\begin{array}{c} 7.71 \pm 0.09 \\ 7.7 \pm 0.1 \\ 7.7 \pm 0.1 \\ 7.72 ^{+0.08} \\ 7.7 ^{+0.1} \\ 7.7 ^{+0.1} \\ 7.7 ^{+0.1} \\ 7.7 ^{+0.1} \\ 7.7 ^{+0.1} \\ 7.7 \pm 0.0 \\ 7.7 \pm 0.2 \\ 7.7 \pm 0.1 \end{array}$ | $\begin{array}{c} -0.41 \pm 0.08 \\ -0.9 \pm 0.2 \\ -0.61 \pm 0.08 \\ -0.41 ^{+0.07} \\ -0.9 ^{+0.1} \\ -0.2 \\ -0.61 ^{+0.09} \\ -0.41 \pm 0.09 \\ -0.9 \pm 0.3 \\ -0.6 \pm 0.2 \end{array}$ | $\begin{array}{c} -22.92 \\ -22.92 \\ -22.92 \\ -22.92 \\ -22.92 \\ -22.92 \\ -22.92 \\ -22.92 \\ -22.92 \\ -22.92 \\ -22.92 \\ -22.92 \end{array}$ | $\begin{array}{c} -\\ -\\ -\\ 0.54^{+0.09}_{-0.07}\\ 0.77^{+0.13}_{-0.10}\\ -\\ 0.55\pm0.08\\ 0.79\pm0.27\\ -\\ \end{array}$ | 0.61 0.93 0.71 0.61 0.93 0.71 0.61 0.93 0.71 |
| Early-type (E+S0) (45) | BCES OLS $(Y X)$ BCES OLS $(X Y)$ BCES Bisector mFITEXY OLS $(Y X)$ mFITEXY Bisector Kelly OLS $(Y X)$ Kelly OLS $(X Y)$ Kelly Bisector | $\begin{array}{c} 8.56 \pm 0.07 \\ 8.56 \pm 0.08 \\ \textbf{8.56} \pm \textbf{0.07} \\ 8.56 \pm \textbf{0.07} \\ 8.54 \stackrel{+0.08}{-0.08} \\ 8.54 \stackrel{+0.08}{-0.07} \\ 8.55 \stackrel{+0.07}{-0.07} \\ 8.55 \pm 0.07 \\ 8.55 \pm 0.09 \\ 8.55 \pm 0.08 \end{array}$ | $\begin{array}{c} -0.33 \pm 0.04 \\ -0.48 \pm 0.05 \\ -\textbf{0.40} \pm \textbf{0.04} \\ -0.32^{+0.03}_{-0.04} \\ -0.49^{+0.05}_{-0.06} \\ -0.41^{+0.04}_{-0.05} \\ -0.32 \pm 0.04 \\ -0.49 \pm 0.07 \\ -0.40 \pm 0.09 \end{array}$ | $\begin{array}{c} -24.47 \\ -24.47 \\ -24.47 \\ -24.47 \\ -24.47 \\ -24.47 \\ -24.47 \\ -24.47 \\ -24.47 \\ -24.47 \end{array}$ | $\begin{array}{c} -\\ -\\ -\\ 0.40^{+0.06}_{-0.05}\\ 0.49^{+0.08}_{-0.06}\\ 0.41\pm0.06\\ 0.51\pm0.11\\ -\\ \end{array}$ | 0.46 0.55 0.49 0.46 0.57 0.49 0.46 0.56 0.49 |
| Late-type (Sp) (17) | BCES OLS $(Y X)$ BCES OLS $(X Y)$ BCES Bisector mFITEXY OLS $(Y X)$ mFITEXY Bisector Kelly OLS $(Y X)$ Kelly OLS $(X Y)$ Kelly Bisector | 7.2 ± 0.2 7.2 ± 0.3 7.2 ± 0.2 $7.2_{-0.1}^{+0.1}$ $7.4_{-0.3}^{+0.5}$ $7.3_{-0.3}^{+0.4}$ 7.2 ± 0.2 7.3 ± 8919.5 7.3 ± 6307.0 | $\begin{array}{c} -0.8 \pm 0.4 \\ -1.7 \pm 0.7 \\ -1.1 \pm 0.3 \\ -0.5 ^{+0.2}_{-0.2} \\ -2.0 ^{+0.7}_{-2.4} \\ -1.0 ^{+0.3}_{-0.5} \\ -0.5 \pm 0.3 \\ -1.7 \pm 43265.5 \\ -0.9 \pm 2.9 \end{array}$ | -22.33 -22.33 -22.33 -22.33 -22.33 -22.33 -22.33 -22.33 -22.33 | $\begin{array}{c} -\\ -\\ -\\ 0.55^{+0.15}_{-0.10}\\ 1.08^{+0.40}_{-0.24}\\ -\\ 0.63\pm0.16\\ 1.3\pm31992.6\\ -\\ -\\ \end{array}$ | 0.70 1.26 0.88 0.62 1.50 0.82 0.62 1.3 0.76 |

 $\begin{array}{c} {\rm TABLE~3} \\ {\rm Linear~regression~analysis.}~{\bf X0}~{\bf is~the~average~X~of~the~subsample...} \end{array}$

| Subsample (size) | Regression | α | β | X_0 | ϵ | Δ | | |
|-------------------------------------|---|--|--|----------------------------------|---|--------------------------|--|--|
| | | Black hole mass – galaxy luminosity $\log[M_{\rm BH}/{\rm M}_{\odot}] = \alpha + \beta[(MAG_{\rm gal} - X_0)/{\rm mag}]$ | | | | | | |
| All (62) | BCES $OLS(Y X)$ BCES $OLS(X Y)$ BCES Bisector | 8.26 ± 0.08 8.3 ± 0.1 8.26 ± 0.09 | -0.48 ± 0.06 -1.0 ± 0.1 -0.71 ± 0.06 | -24.78 -24.78 -24.78 | - - - - 0.02+0.07 | 0.64 0.92 0.70 | | |
| | mFITEXY $OLS(Y X)$ mFITEXY $OLS(X Y)$ mFITEXY Bisector | $8.26_{-0.07}^{+0.08} \\ 8.3_{-0.1}^{+0.1} \\ 8.3_{-0.1}^{+0.1}$ | $\begin{array}{c} -0.47^{+0.06}_{-0.06} \\ -1.0^{+0.1}_{-0.2} \\ -0.71^{+0.08}_{-0.10} \end{array}$ | -24.78 -24.78 -24.78 | $0.62_{-0.05}^{+0.07} \\ 0.91_{-0.08}^{+0.10} \\ -$ | 0.64 0.93 0.70 | | |
| | Kelly $OLS(Y X)$ Kelly $OLS(X Y)$ Kelly Bisector | 8.27 ± 0.08 8.3 ± 0.1 8.3 ± 0.1 | $-0.47 \pm 0.07 -1.0 \pm 0.2 -0.7 \pm 0.1$ | -24.78 -24.78 -24.78 | 0.63 ± 0.06 0.94 ± 0.2 | $0.64 \\ 0.93 \\ 0.70$ | | |
| Early-type (E+S0) (45) | BCES $OLS(Y X)$ BCES $OLS(X Y)$ BCES Bisector | 8.56 ± 0.06 8.56 ± 0.08 8.56 ± 0.07 | -0.43 ± 0.05 -0.63 ± 0.05 -0.53 ± 0.04 | -24.88 -24.88 -24.88 | _ _ _ _ _ | $0.45 \\ 0.53 \\ 0.47$ | | |
| | mFITEXY $OLS(Y X)$ mFITEXY $OLS(X Y)$ mFITEXY Bisector | $\begin{array}{c} 8.56^{+0.06}_{-0.06} \\ 8.55^{+0.09}_{-0.07} \\ 8.55^{+0.08}_{-0.06} \end{array}$ | $\begin{array}{c} -0.41^{+0.05}_{-0.04} \\ -0.66^{+0.06}_{-0.08} \\ -0.53^{+0.05}_{-0.06} \end{array}$ | -24.88 -24.88 -24.88 | $0.42_{-0.05}^{+0.05} \\ 0.53_{-0.05}^{+0.07} \\ -$ | 0.45 0.55 0.47 | | |
| | Kelly $OLS(Y X)$ Kelly $OLS(X Y)$ Kelly Bisector | 8.56 ± 0.07 8.56 ± 0.09 8.56 ± 0.08 | $-0.41 \pm 0.05 -0.65 \pm 0.09 -0.5 \pm 0.1$ | -24.88 -24.88 -24.88 | 0.44 ± 0.06 0.55 ± 0.11 | $0.45 \\ 0.54 \\ 0.47$ | | |
| | Black hole mass – spheroid stellar mass $\log[M_{\rm BH}/{ m M_{\odot}}] = \alpha + \beta \log[(M_{*,\rm sph} - X_0)/{ m M_{\odot}}]$ | | | | | | | |
| Early-type (E+S0) (45) | BCES $OLS(Y X)$ BCES $OLS(X Y)$ BCES Bisector | 8.56 ± 0.07 8.56 ± 0.08 8.56 ± 0.07 | 0.8 ± 0.1 1.3 ± 0.1 1.0 ± 0.1 | $10.81 \\ 10.81 \\ 10.81$ | - - - | 0.48 0.59 0.51 | | |
| | mFITEXY $OLS(Y X)$ mFITEXY $OLS(X Y)$ mFITEXY Bisector | $\begin{array}{c} 8.56^{+0.06}_{-0.07} \\ 8.54^{+0.09}_{-0.08} \\ 8.55^{+0.07}_{-0.08} \end{array}$ | $0.8_{-0.1}^{+0.1} \\ 1.3_{-0.1}^{+0.2} \\ 1.0_{-0.1}^{+0.1}$ | 10.81 10.81 10.81 | $0.42_{-0.05}^{+0.06} \\ 0.53_{-0.07}^{+0.08}$ | 0.48 0.61 0.51 | | |
| | Kelly $OLS(Y X)$ Kelly $OLS(X Y)$ Kelly Bisector | 8.56 ± 0.07 8.55 ± 0.09 8.55 ± 0.08 | 0.8 ± 0.1 1.3 ± 0.2 1.0 ± 0.2 | 10.81 10.81 10.81 | 0.43 ± 0.06 0.54 ± 0.12 | 0.48 0.59 0.51 | | |
| Late-type (Sp) (17) | BCES $OLS(Y X)$ BCES $OLS(X Y)$ BCES Bisector | 7.2 ± 0.2 7.2 ± 0.4 7.2 ± 0.2 | 1.9 ± 1.5 5.9 ± 3.4 $\mathbf{3.0 \pm 1.3}$ | $10.05 \\ 10.05 \\ 10.05$ | _ _ _ | 0.74 1.70 0.94 | | |
| | mFITEXY $OLS(Y X)$ mFITEXY $OLS(X Y)$ | $7.2_{-0.2}^{+0.1} \\ 7.4_{-0.5}^{+1.5} \\ 7.2_{-0.4}^{+1.0}$ | $1.2_{-0.6}^{+0.7} 7.1_{-3.0}^{+26.3} 2.3_{-1.0}^{+1.7}$ | 10.05 10.05 | $0.59_{-0.11}^{+0.16} \\ 1.49_{-0.35}^{+0.57}$ | 0.66 2.08 | | |
| | mFITEXY Bisector Kelly $OLS(Y X)$ Kelly $OLS(X Y)$ Kelly Bisector | $7.2_{-0.4}$ 7.2 ± 0.2 7.3 ± 25.2 7.2 ± 17.8 | $2.3_{-1.0}$ 1.0 ± 1.0 5.2 ± 740.5 1.8 ± 1.8 | 10.05 10.05 10.05 10.05 | 0.67 ± 0.17 1.7 ± 190.7 | 0.79 0.65 1.5 0.72 | | |

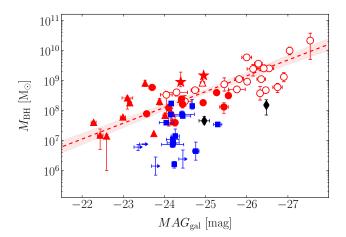


Fig. 3.— Black hole mass against 3.6 μm galaxy absolute magnitude. Symbols are coded as in Figure 1. Four spiral galaxies had their magnitudes overestimated and are shown as upper limits.

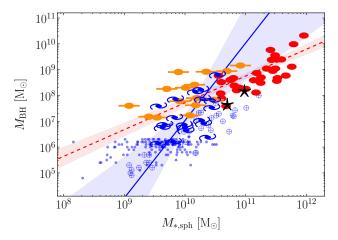


FIG. 4.— Black hole mass against spheroid stellar mass. The galaxies from our sample are shown with large symbols (red = E, orange = E/S0 and S0, blue = S0/Sp and Sp, black = merger). The 139 small blue dots represent the low-mass AGN sample from Jiang et al. (2011). The blue crossed circles denote 35 additional galaxies (see Graham & Scott 2015, their Table 2), some of which might have had their bulge stellar masses overestimated. The red dashed line indicates the BCES bisector linear regression for early-type galaxies (ellipticals+lenticulars), with the red shaded area denoting its 1σ uncertainty. The blue solid line shows the BCES bisector linear regression for spiral galaxies, with the blue shaded area denoting its 1σ uncertainty.

agreement with the findings of GS13. The slope that we obtained for core-Sérsic spheroids $(M_{\rm BH} \propto L_{\rm sph}^{1.2\pm0.2})$ is consistent with the slope reported by GS13 in the K_s -band $(M_{\rm BH} \propto L_{\rm sph}^{1.1\pm0.2})$. Instead, the slope that we determined for Sérsic spheroids $(M_{\rm BH} \propto L_{\rm sph}^{1.5\pm0.2})$ is significantly shallower than that found by GS13 $(M_{\rm BH} \propto L_{\rm sph}^{2.7\pm0.5})$. Although the Sérsic/core-Sérsic classification used by GS13 slightly differs⁶ from the classification used here, the main cause of such inconsistency is that the

bulge-to-total ratios obtained from our galaxy decompositions are different from those assumed by GS13 to convert galaxy luminosities into bulge luminosities. Our bulge-to-total ratios for low-luminosity Sérsic spheroids $(MAG_{\rm sph} \gtrsim -22 \text{ mag})$ are smaller than those used by GS13. The host galaxies of such bulges are late-type, spiral galaxies, which typically present a complex morphology (bars, double bars, embedded disks, nuclear components, etc). Our sophisticated galaxy models account for the extra components, while the bulge-to-total ratios of GS13 were derived from simple bulge/disk decompositions which overestimated the bulge luminosity. This results in our bulge magnitudes being on average ~ 1 mag fainter. On the other side, our bulge-to-total ratios for high-luminosity Sérsic spheroids ($MAG_{\rm sph} \lesssim$ -24 mag) are on average larger than those adopted by GS13. In this case, the host systems are early-type elliptical/lenticular galaxies that feature intermediate-scale disks⁷. Past bulge/disk decompositions failed to correctly identify the extent of such disks and treated them as large-scale disks, thus underestimating the bulge luminosity. The magnitudes that we obtained for such spheroids are on average ~ 1 mag brighter.

We have seen that the change in slope of the $M_{\rm BH}-L_{\rm sph}$ correlation - which is expected for consistency with other scaling relations (a single power-law $M_{\rm BH}-\sigma$ correlation and a double power-law $L_{\rm sph}-\sigma$ correlation) – cannot be attributed to the division between the two populations of Sérsic and core-Sérsic spheroids. We now test a new hypothesis, that is to say the change in slope is to be ascribed to the different formation mechanisms of earlyand late-type galaxies. If this hypothesis is correct, the spheroids of early-type (elliptical and lenticular) galaxies will follow $M_{\rm BH} \propto L_{\rm sph}^{\sim 1}$, whereas the spheroids of late-type (spiral) galaxies will have $M_{\rm BH} \propto L_{\rm sph}^{\sim 2.5}$. First, we checked that the slopes of the bulges of elliptical and lenticular galaxies, separately, are consistent with each other, and thus, together, they define a single red sequence in the $M_{\rm BH}-L_{\rm sph}$ diagram. We then fit the bulges of early- and late-type galaxies with two separate log-linear regressions, and obtained $M_{\rm BH} \propto L_{\rm sph}^{1\pm0.1}$ and $M_{\rm BH} \propto L_{\rm sph}^{2.75\pm0.75}$ respectively, in excellent agreement with the theoretical generativities of the spheroidal consecutivities of the sphero ment with the theoretical expectations of our hypothesis. vertical scatter along the early type sequence is constant? if 2 overmassive bhs removed, what happens?

coming now to figure 1: if I look at the blue points it is difficult to believe that they define a linear relation, their magnitude range is too small and it could just be that at low galaxy luminosities the scatter of the MBH-L relation increases. This is what most models predict. Do the galaxies below the correlation have some special property? Could it just be that spiral bulges simple do not follow a tight relation with BH mass?

Giulia, I think you already plan to do this, but can you include the error bars in all places where a relation is presented, so that readers know if there is a relation or not. Remember also Ewan's remark about the unsuitability

⁶ which galaxies?

⁷ explain

of the Pearson and Spearman correlation coefficients because they do not take into account the error bars on our data - so don't include those simple coefficients. Actually, it would be worth pointing out to readers that a visual inspection of the plotted data requires the viewer to take into account the error bars when judging-by-eye the strength of a correlation. Maybe then mention in the following sentence that this is why the correlation coefficients are not applicable here.

In Figure 2, we show the distribution of spheroid Sérsic indices⁸, $n_{\rm sph}$, in the $M_{\rm BH}-L_{\rm sph}$ diagram. Our aim is to check whether bulges with $n_{\rm sph}<2$, claimed by some to be pseudobulges (e.g. cite), are offset to lower black hole masses from the correlation defined by (classical) bulges with $n_{\rm sph}>2$, as reported by Sani et al. (2011) who else?. To do this, we fit a symmetrical linear regression to the bulges that have $n_{\rm sph}>2$ and we compute the vertical offset of all bulges from the regression. In the inset of Figure 2, we plot the vertical offset against $n_{\rm sph}$. From a visual inspection, bulges with $n_{\rm sph}<2$ do not appear to be offset from the correlation traced by bulges with $n_{\rm sph}>2$.

you $\mathbf{A}\mathbf{s}$ probably know, and explained inof many my papers (e.g.http://arxiv.org/abs/1501.02937http://arxiv.org/abs/1108.0997 http://arxiv.org/abs/1311.7207 pseudobulges are notoriously hard to identify. would be a mistake to have a column labelled "pseudobulge". However a galaxy classification column, indicating the presence of a bar, is good to include. While we do not wish to publish the Sersic indices here (that will be kept for a different paper), we could have a column indicating if n is above or below 2 - given that some people mistakingly think that they can use this as a dividing point. Giulia, can you also include a nearby reference to Graham (2013, http://arxiv.org/abs/1108.0997) so that people can read and understand why n < 2 does not necessarily equate to a pseudobulge.

4.2. Black hole mass – galaxy luminosity

Figure 3 illustrates the $M_{\rm BH}-L_{\rm gal}$ diagram. Four spiral galaxies had their total luminosities underestimated (see Section 2) and thus are not included in the linear regression analysis. Läsker et al. (2014b)

Contrary to a previous claim, the bulge luminosity appears to be a better indicator of the BH mass than the galaxy luminosity.

compare scatter mbh-msph and mbh-mgal for early types intrinsic scatter of early type gals in m-mbul is slightly more than in m-mgal, but this might just depend on the ability of measuring the bulge luminosity, which is model dependent, the gal lum is not. only for early type galaxies one can use the tot luminosity as bh mass indicator

errors on gal mag??????????? 0.2 constant

4.3. Black hole mass – spheroid stellar mass

Finally, we present the $M_{\rm BH}-M_{*,\rm sph}$ diagram in Figure 4, where we include our sample of 66 galaxies, plus the 35 + 139 low-mass AGNs taken from the compilation of Graham & Scott (2015).

addition of agns relations agns consistent w spirals, but analysis deferred to other paper cubic growth

5. CONCLUSIONS

ngc0524 outlier, n1332 non outlier

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 $^{^8}$ The spheroid Sérsic indices are taken from our one-dimensional fits of the galaxy major-axis surface brightness profiles (*Paper I*).

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