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SUPERMASSIVE BLACK HOLES AND HOST BULGES AFFAIRS – II. THE RED AND THE BLUE SEQUENCES IN THE MASS – MASS DIAGRAM.

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ABSTRACT

We present correlations between black hole mass, $M_{\rm BH}$, and both the host galaxy's and spheroid's infrared luminosity, $L_{\rm gal}$ and $L_{\rm sph}$, and the spheroid's stellar mass, $M_{*,\rm sph}$, built upon a high-quality data set. Our sample, the largest ever used, counts 66 local galaxies with a dynamical measurement of $M_{\rm BH}$. Spheroid luminosities come from high signal-to-noise 3.6 μm *Spitzer* satellite imagery, and were derived from our state-of-the-art multicomponent galaxy decompositions that, for the first time, were checked to be consistent with the galaxy kinematics. **limit of 250 words, no room for mentioning the gaalxy components, more appropriate for data paper** Previous studies have used galaxy samples that were overwhelmingly dominated by high-mass, early-type objects. Instead, our sample includes 17 spiral galaxies, half of which have $M_{\rm BH} < 10^7$ M$_\odot$, and allows us to better investigate the poorly studied low-mass end of the $M_{\rm BH} - M_{*,\rm sph}$ correlation. The bulges of early-type (E + S0) galaxies follow $M_{\rm BH} \propto M_{*,\rm sph}^{1.04\pm0.10}$, consistent with a dry-merging formation scenario, and define a tight *red sequence* with intrinsic scatter $\epsilon_{(Y|X)} = 0.43 \pm 0.06$ dex. On the other hand, the bulges of late-type (Sp) galaxies define a much steeper *blue sequence*, with $M_{\rm BH} \propto M_{*,\rm sph}^{2-3}$, indicating that gas-rich processes feed the black hole more efficiently than the host bulge. We conclude that: i) Sérsic galaxies follow $M_{\rm BH} \propto M_{*,\rm sph}^{x\pm x}$, a less steep sequence than previously reported; ii) bulges with Sérsic index $n_{\rm sph} < 2$, argued by some to be pseudo-bulges, are not offset to lower $M_{\rm BH}$ from the correlation defined by bulges with $n_{\rm sph} > 2$; iii) $L_{\rm sph}$ and $L_{\rm gal}$ correlate equally well with $M_{\rm BH}$, in terms of intrinsic scatter, only for early-type galaxies; once reasonable numbers of spiral galaxies are included, the correlation with $L_{\rm sph}$ is better than that with $L_{\rm gal}$.

Subject headings: keywords

1. INTRODUCTION

More than two and a half decades ago, Dressler (1989) foresaw a "rough scaling of black hole mass with the mass of the spheroidal component", as suggested by the sequence of five galaxies (M87, M104, M31, M32 and the Milky Way). His "rough scaling" was a premature version of the nowadays popular correlation between black hole mass, $M_{\rm BH}$, and host spheroid luminosity, $L_{\rm sph}$, and also host spheroid mass, $M_{\rm sph}$ (Yee 1992; Kormendy & Richstone 1995; Magorrian et al. 1998; Marconi & Hunt 2003; Häring & Rix 2004). These early studies were dominated by high-mass, early-type galaxies, for which they reported a quasi-linear $M_{\rm BH} - M_{\rm sph}$ relation, consistent with a dry-merging formation scenario. Subsequent studies of the $M_{\rm BH} - L_{\rm sph}$ and $M_{\rm BH} - M_{\rm sph}$ diagrams (Ferrarese & Ford 2005; Lauer et al. 2007a; Graham 2007, 2008; Gültekin et al. 2009; Sani et al. 2011; Beifiori et al. 2012; Erwin & Gadotti 2012; Vika et al. 2012; van den Bosch et al. 2012; McConnell & Ma 2013; Kormendy & Ho 2013; Rusli et al. 2013a; see Graham 2015b for an extensive review about the early discovery and successive improvements of these correlations) used similar galaxy samples, which remained dominated by high-mass, early-type objects having $M_{\rm BH} \gtrsim 0.5 \times 10^8$ M$_\odot$, and recovered a near-linear relation. However, the consensus about a linear $M_{\rm BH} - M_{\rm sph}$ correlation was not unanimous. Some studies reported a slope steeper than one, or noticed that low-mass spheroids were downwards offset from the relation traced by their high-mass counterparts (Laor 1998; Wandel 1999; Laor 2001; Ryan et al. 2007). Recently, Läsker et al. (2014a,b) derived 2.2 μm bulge luminosities for 35 galaxies (among which only 4 were classified as spiral galaxies), and reported a slope below unity for their $M_{\rm BH} - M_{\rm sph}$ relation. They also claimed that the black hole mass correlates equally well with the total galaxy luminosity as it does with the bulge luminosity.

The $M_{\rm BH} - L_{\rm sph}$ relation can be predicted from other two correlations involving the bulge velocity dispersion, σ. The first of these two is the $M_{\rm BH} - \sigma$ relation (Ferrarese & Merritt 2000; Gebhardt et al. 2000), which can be described by a single power-law ($M_{\rm BH} \propto \sigma^5$) over the range in velocity dispersion $70 - 350$ km s^{-1}

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(e.g. Graham et al. 2011; McConnell et al. 2011; Graham & Scott 2013). The second is the $L_{\rm sph}-\sigma$ relation, which has long been known to be a "double power-law", being $L_{\rm sph}\propto\sigma^5$ at the luminous end (Schechter 1980; Malumuth & Kirshner 1981; von der Linden et al. 2007; Liu et al. 2008), and $L_{\rm sph}\propto\sigma^2$ at intermediate and faint luminosities (Davies et al. 1983; Held et al. 1992; Matković & Guzmán 2005; de Rijcke et al. 2005; Balcells et al. 2007; Chilingarian et al. 2008; Forbes et al. 2008; Cody et al. 2009; Tortora et al. 2009; Kourkchi et al. 2012). The change in slope of the $L_{\rm sph}-\sigma$ relation occurs at $M_B\approx-20.5$ mag, corresponding to $\sigma\approx200$ km s^{-1}. That is, the $M_{\rm BH}-L_{\rm sph}$ relation should be better described by a "broken", rather than a single, power-law, having $M_{\rm BH}\propto L_{\rm sph}^{2.5}$ at the low-luminosity end, and $M_{\rm BH}\propto L_{\rm sph}^{1}$ at the high-luminosity end. Due to the scatter in the $M_{\rm BH}-L_{\rm sph}$ (or $M_{\rm BH}-M_{\rm sph}$) diagram, studies that have not sufficiently probed below $M_{\rm BH}\approx10^7$ M$_\odot$ can easily miss the change in slope occuring at $M_{\rm BH}\approx10^{(8\pm1)}$ M$_\odot$, and erroneously recover a single log-linear relation.

When Graham (2012) pointed out this overlooked inconsistency, he identified two different populations of galaxies, namely the core-Sérsic (Graham et al. 2003; Trujillo et al. 2004) and Sérsic spheroids[1], and attributed the change in slope (from log-quadratic to log-linear) to their different formation mechanisms. In this scenario, core-Sérsic spheroids are built in additive dry merger events, where the black hole and the bulge grow at the same pace, increasing their mass in lock steps ($M_{\rm BH}\propto L_{\rm sph}^{1}$), whereas Sérsic spheroids originate from gas-rich processes, in which the mass of the black hole increases more rapidly than the mass of its host spheroid ($M_{\rm BH}\propto L_{\rm sph}^{2.5}$). Graham & Scott (2013, hereafter GS13) and Scott et al. (2013, hereafter S+13) presented double power-law linear regressions for Sérsic/core-Sérsic spheroids in the $M_{\rm BH}-L_{\rm sph}$ and $M_{\rm BH}-M_{*,\rm sph}$ (spheroid stellar mass) diagrams, respectively, probing down to $M_{\rm BH}\approx10^6$ M$_\odot$. To obtain their dust-corrected *bulge* magnitudes, they did not perform bulge/disc decompositions, but instead they converted $B-$band and K_S-band observed, total *galaxy* magnitudes using a mean statistical correction based on each object's morphological type and disc inclination[2]. However, this mean statistical correction was obtained from the results of non-modern bulge/disk decompositions, which did not include extra components. It should also be noted that ∼80% of their core-Sérsic spheroids were morphologically classified as elliptical galaxies, and ∼80% of their Sérsic spheroids were morphologically classified as bulges of disk galaxies (lenticulars and spirals).

Several recent papers (Jiang et al. 2011, 2013; Mathur et al. 2012; Reines et al. 2013) claimed an offset at the low-mass end of the $M_{\rm BH}-M_{*,\rm sph}$ diagram, such that the black hole mass is lower than expected from the near-linear correlation traced by the high-mass, early-type spheroids. However, Graham & Scott (2013) showed that the low-mass spheroids ($10^{8.5}\lesssim M_{*,\rm sph}/{\rm M}_\odot\lesssim10^{10.5}$) are not randomly offset from the high-mass, near-linear correlation, but follow the two times steeper relation traced by the Sérsic spheroids. Using data from Jiang et al. (2011), Graham & Scott (2015) showed that this appears to extend to spheroids with even lower black hole masses ($10^5\lesssim M_{*,\rm sph}/{\rm M}_\odot\lesssim2\times10^6$), and a more detailed analysis will be presented in Graham et al. (2015, *in preparation*).

Here we investigate substructure in the $M_{\rm BH}-L_{\rm sph}$ and $M_{\rm BH}-M_{*,\rm sph}$ diagrams using state-of-the-art galaxy decompositions (Savorgnan & Graham 2015, *in preparation*, hereafter *Paper I*) for the largest sample of galaxies with directly measured black hole masses. Our galaxies are large and nearby, which allows us to perform accurate multicomponent decompositions (instead of simple bulge/disk decompositions) without incurring in significant parameter degeneracies. Our decompositions were obtained from 3.6 μm *Spitzer* satellite imagery, which is an excellent proxy for the stellar mass, superior to the $K-$band (Sheth et al. 2010 and references therein). Nine of our galaxies have $M_{\rm BH}\lesssim10^7$ M$_\odot$, which allows us to accurately constrain the slope of the correlation at the low-mass end. In addition to this, our galaxy sample includes 17 spiral galaxies, representing a notable improvement over the past studies dominated by early-type systems. In a forthcoming paper, we will explore the relation between black hole mass and bulge dynamical mass, $M_{\rm dyn,sph}\propto R_{\rm e}\sigma^2$, and address the issue of a black hole fundamental plane. This paper is structured as follows...

2. DATA

Our galaxy sample (see Table 1) consists of 66 objects for which a dynamical measurement of the black hole mass had been reported in the literature (by GS13 or Rusli et al. 2013b) at the time we started this project, and for which we were able to obtain useful bulge parameters from 3.6 μm *Spitzer* satellite imagery. Bulge magnitudes were derived from our state-of-the-art galaxy decompositions, which take into account bulges, disks, spiral arms, bars, rings, haloes, extended or unresolved nuclear sources and partially depleted cores. Kinematical information (Emsellem et al. 2011; Scott et al. 2014; Arnold et al. 2014) was used to confirm the presence of rotationally supported components in most early-type galaxies, and to identify their extent (intermediate-scale disks, that are fully embedded in the bulge, or large-scale disks, that encase the bulge and dominate the light at large radii). *Paper I* will present the dataset used here, give details about the data reduction process and the sophisticated galaxy modelling technique that we developed, discuss how we estimated the uncertainties[3] on the bulge magnitudes, and illustrate the individual 66

[1] Core-Sérsic spheroids have partially depleted cores relative to their outer Sérsic light profile, whereas Sérsic spheroids have no central deficit of stars. While core-Sérsic spheroids are also "core galaxies", as given by the Nuker definition (Lauer et al. 2007b), it should be noted that ∼20% of "core galaxies" are not core-Sérsic spheroids (Dullo & Graham 2014, their Appendix A.2), i.e. do not have depleted cores. The change in slope of the $L_{\rm sph}-\sigma$ relation corresponds to the division between core-Sérsic and Sérsic spheroids (e.g. Graham & Guzmán 2003).

[2] While this resulted in individual bulge magnitudes not being exactly correct, their large sample size allowed them to obtain a reasonably ensemble average correction.

[3] By comparing, for our galaxies, the measurements of the bulge magnitude obtained by different authors with those obtained by us, we estimated the uncertainties on the bulge magnitudes with a method that takes into account systematic errors. Systematic errors include incorrect sky subtraction, inaccurate masking of contaminating sources, imprecise description of the PSF, erroneous

galaxy decompositions.

Bulge luminosities[4] were first converted into stellar masses using a constant 3.6 μm mass-to-light ratio, $\Gamma_{3.6} = 0.6$ (Meidt et al. 2014). We then explored a more sophisticated way to compute mass-to-light ratios, using the color-$\Gamma_{3.6}$ relation published by Meidt et al. (2014, their equation 4), which allows one to estimate $\Gamma_{3.6}$ of a galaxy from its $[3.6]-[4.5]$ color. Individual $[3.6]-[4.5]$ colors[5] were taken from Peletier et al. (2012, column 8 of their Table 1) when available for our galaxies, or were estimated from the bulge stellar velocity dispersion, σ, using the color-σ relation presented by Peletier et al. (2012, their Figure 6). We found that the range in $[3.6]-[4.5]$ color is small (0.06 mag), and thus the range in $\Gamma_{3.6}$ is also small (0.04). After checking that using a single $\Gamma_{3.6} = 0.6$, independent of $[3.6]-[4.5]$ color, does not significantly affect the results of our analysis, we decided to use individual, color-dependent mass-to-light ratios.

The Sérsic/core-Sérsic classification presented in this work comes from the compilation of **?**, who identified partially depleted cores according to the same criteria used by GS13. When no high-resolution image analysis was available from the literature, they inferred the presence of a partially depleted core based on the stellar velocity dispersion: a galaxy is classified as core-Sérsic if $\sigma > 270$ km s^{-1}, or as Sérsic if $\sigma < 166$ km s^{-1}.

For each galaxy, the total luminosity (or galaxy luminosity, $L_{\rm gal}$) is the sum of the luminosities of all its subcomponents. Due to the complexity of their modelling, four galaxies (see Table 1, column 7) had their galaxy luminosities underestimated[6], which are given here as lower limits. Following GS13, we assumed a fixed uncertainty (0.25 mag) for $MAG_{\rm gal}$.

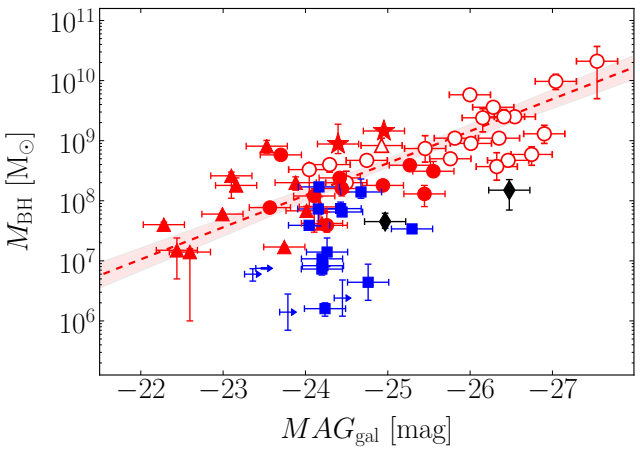

FIG. 1.— Black hole mass against 3.6 μm galaxy absolute magnitude. Symbols are coded according to the galaxy morphological type: red circle = elliptical, red star = elliptical/lenticular, red upward triangle = lenticular, blue downward triangle = lenticular/spiral, blue square = spiral, black diamond = merger. Empty symbols represent core-Sérsic spheroids, whereas filled symbols are used for Sérsic spheroids. The red dashed line indicates the BCES bisector linear regression for early-type galaxies (ellipticals+lenticulars), with the red shaded area denoting its 1σ uncertainty. Four spiral galaxies had their magnitudes overestimated and are shown as upper limits.

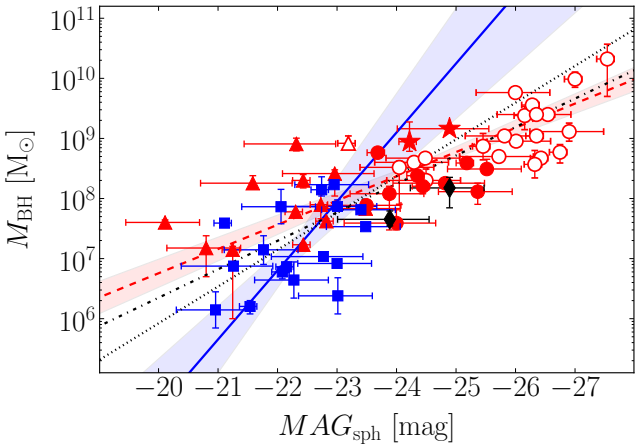

FIG. 2.— Black hole mass against 3.6 μm spheroid absolute magnitude. Symbols are coded according to the galaxy morphological type: red circle = elliptical, red star = elliptical/lenticular, red upward triangle = lenticular, blue downward triangle = lenticular/spiral, blue square = spiral, black diamond = merger. Empty symbols represent core-Sérsic spheroids, whereas filled symbols are used for Sérsic spheroids. The red dashed line indicates the BCES bisector linear regression for early-type galaxies (ellipticals+lenticulars), with the red shaded area denoting its 1σ uncertainty. The blue solid line shows the BCES bisector linear regression for spiral galaxies, with the blue shaded area denoting its 1σ uncertainty. The black dashed-dotted and dotted lines represent the BCES bisector linear regressions for core-Sérsic and Sérsic spheroids, respectively.

3. ANALYSIS

We performed a linear regression analysis of the $M_{\rm BH} - L_{\rm gal}$ (see Table 2), $M_{\rm BH} - L_{\rm sph}$ (see Table 3) and

choice of model components (for example, when failing to identify a galaxy subcomponent and thus omitting it in the model, or when describing a galaxy sub-component with an inadequate function), the radial extent of the surface brightness profile and its sampling. These factors are not included in popular 2D fitting codes which report only the random errors associated with their fitted parameters. In fact, when performing multi-component decomposition of high signal-to-noise images of nearby – therefore well spatially resolved – galaxies, errors are dominated by systematics rather than Poisson noise.

[4] Absolute luminosities were calculated assuming a 3.6 μm solar absolute magnitude of 3.25 mag (Sani et al. 2011).

[5] These are integrated $[3.6]-[4.5]$ colors, measured in a circular aperture within one galaxy's effective radius.

[6] These four cases will be discussed in *Paper I*.

TABLE 1
Galaxy sample.

Galaxy	**Type**	**Core**	**Distance**	$M_{\mathbf{BH}}$	$MAG_{\mathbf{sph}}$	$MAG_{\mathbf{gal}}$	**[3.6] − [4.5]**	$M_{*,\mathbf{sph}}$
			[Mpc]	[10^8 $M_\odot$]	[mag]	[mag]	[mag]	[10^{10} $M_\odot$]
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
IC 1459	E	yes	28.4	24^{+10}_{-10}	$-26.15^{+0.18}_{-0.11}$	-26.15 ± 0.15	−0.12	27^{+30}_{-23}
IC 2560	Sp (bar)	no?	40.7	$0.044^{+0.044}_{-0.022}$	$-22.27^{+0.66}_{-0.58}$	-24.76 ± 0.08	−0.08	$1.0^{+1.8}_{-0.6}$
IC 4296	E	yes?	40.7	11^{+2}_{-2}	$-26.35^{+0.18}_{-0.11}$	-26.35 ± 0.10	−0.12	31^{+34}_{-26}
M104	S0/Sp	yes	9.5	$6.4^{+0.4}_{-0.4}$	$-23.91^{+0.66}_{-0.58}$	-25.21 ± 0.06	−0.12	$3.4^{+5.8}_{-1.9}$
M105	E	yes	10.3	4^{+1}_{-1}	$-24.29^{+0.66}_{-0.58}$	-24.29 ± 0.27	−0.10	$5.6^{+9.5}_{-3.0}$
M106	Sp (bar)	no	7.2	$0.39^{+0.01}_{-0.01}$	$-21.11^{+0.18}_{-0.11}$	-24.04 ± 0.17	−0.08	$0.37^{+0.41}_{-0.31}$
M31	Sp (bar)	no	0.7	$1.4^{+0.9}_{-0.3}$	$-22.74^{+0.18}_{-0.11}$	-24.67 ± 0.02	−0.09	$1.5^{+1.6}_{-1.3}$
M49	E	yes	17.1	25^{+3}_{-1}	$-26.54^{+0.18}_{-0.11}$	-26.54 ± 0.11	−0.12	39^{+43}_{-33}
M59	E	no	17.8	$3.9^{+0.4}_{-0.4}$	$-25.18^{+0.18}_{-0.11}$	-25.27 ± 0.02	−0.09	14^{+15}_{-11}
M64	Sp	no?	7.3	$0.016^{+0.004}_{-0.004}$	$-21.54^{+0.18}_{-0.11}$	-24.24 ± 0.06	−0.06	$0.64^{+0.71}_{-0.55}$
M81	Sp (bar)	no	3.8	$0.74^{+0.21}_{-0.11}$	$-23.01^{+0.88}_{-0.66}$	-24.43 ± 0.30	−0.09	$1.9^{+3.6}_{-0.9}$
M84	E	yes	17.9	$9.0^{+0.9}_{-0.8}$	$-26.01^{+0.66}_{-0.58}$	-26.01 ± 0.02	−0.10	28^{+47}_{-15}
M87	E	yes	15.6	$58.0^{+3.5}_{-3.5}$	$-26.00^{+0.66}_{-0.58}$	-26.00 ± 0.12	−0.11	26^{+44}_{-14}
M89	E	yes	14.9	$4.7^{+0.5}_{-0.5}$	$-24.48^{+0.66}_{-0.58}$	-24.74 ± 0.10	−0.11	$6.3^{+10.7}_{-3.4}$
M94	Sp (bar)	no?	4.4	$0.060^{+0.014}_{-0.014}$	$-22.08^{+0.18}_{-0.11}$	≤ -23.36	−0.07	$1.00^{+1.11}_{-0.85}$
M96	Sp (bar)	no	10.1	$0.073^{+0.015}_{-0.015}$	$-22.15^{+0.18}_{-0.11}$	-24.20 ± 0.27	−0.08	$0.97^{+1.08}_{-0.83}$
NGC 0524	S0	yes	23.3	$8.3^{+2.7}_{-1.3}$	$-23.19^{+0.18}_{-0.11}$	-24.92 ± 0.05	−0.09	$2.2^{+2.5}_{-1.9}$
NGC 0821	E	no	23.4	$0.39^{+0.26}_{-0.09}$	$-24.00^{+0.88}_{-0.66}$	-24.26 ± 0.01	−0.09	$4.7^{+8.7}_{-2.1}$
NGC 1023	S0 (bar)	no	11.1	$0.42^{+0.04}_{-0.04}$	$-22.82^{+0.18}_{-0.11}$	-24.20 ± 0.02	−0.10	$1.5^{+1.7}_{-1.3}$
NGC 1300	Sp (bar)	no	20.7	$0.73^{+0.69}_{-0.35}$	$-22.06^{+0.66}_{-0.58}$	-24.16 ± 0.00	−0.10	$0.70^{+1.19}_{-0.38}$
NGC 1316	merger	no	18.6	$1.50^{+0.75}_{-0.80}$	$-24.89^{+0.66}_{-0.58}$	-26.48 ± 0.05	−0.10	$9.5^{+16.2}_{-5.2}$
NGC 1332	E/S0	no	22.3	14^{+2}_{-2}	$-24.89^{+0.88}_{-0.66}$	-24.95 ± 0.03	−0.12	$8.2^{+15.0}_{-3.6}$
NGC 1374	E	no?	19.2	$5.8^{+0.5}_{-0.5}$	$-23.68^{+0.18}_{-0.11}$	-23.70 ± 0.08	−0.09	$3.6^{+4.0}_{-3.0}$
NGC 1399	E	yes	19.4	$4.7^{+0.6}_{-0.6}$	$-26.43^{+0.18}_{-0.11}$	-26.46 ± 0.04	−0.12	33^{+37}_{-28}
NGC 2273	Sp (bar)	no	28.5	$0.083^{+0.004}_{-0.004}$	$-23.00^{+0.66}_{-0.58}$	-24.21 ± 0.15	−0.08	$2.0^{+3.4}_{-1.1}$
NGC 2549	S0 (bar)	no	12.3	$0.14^{+0.02}_{-0.13}$	$-21.25^{+0.18}_{-0.11}$	-22.60 ± 0.02	−0.10	$0.35^{+0.39}_{-0.30}$
NGC 2778	S0 (bar)	no	22.3	$0.15^{+0.09}_{-0.10}$	$-20.80^{+0.66}_{-0.58}$	-22.44 ± 0.07	−0.09	$0.25^{+0.43}_{-0.14}$
NGC 2787	S0 (bar)	no	7.3	$0.40^{+0.04}_{-0.05}$	$-20.11^{+0.66}_{-0.58}$	-22.28 ± 0.06	−0.10	$0.12^{+0.20}_{-0.07}$
NGC 2974	Sp (bar)	no	20.9	$1.7^{+0.2}_{-0.2}$	$-22.95^{+0.66}_{-0.58}$	-24.16 ± 0.04	−0.09	$1.8^{+3.1}_{-1.0}$
NGC 3079	Sp (bar)	no?	20.7	$0.024^{+0.024}_{-0.012}$	$-23.01^{+0.66}_{-0.58}$	≤ -24.45	−0.07	$2.4^{+4.0}_{-1.3}$
NGC 3091	E	yes	51.2	36^{+1}_{-2}	$-26.28^{+0.18}_{-0.11}$	-26.28 ± 0.09	−0.12	30^{+34}_{-26}
NGC 3115	E/S0	no	9.4	$8.8^{+10.0}_{-2.7}$	$-24.22^{+0.18}_{-0.11}$	-24.40 ± 0.02	−0.11	$4.9^{+5.4}_{-4.1}$
NGC 3227	Sp (bar)	no	20.3	$0.14^{+0.10}_{-0.06}$	$-21.76^{+0.66}_{-0.58}$	-24.26 ± 0.10	−0.08	$0.67^{+1.15}_{-0.37}$
NGC 3245	S0 (bar)	no	20.3	$2.0^{+0.5}_{-0.5}$	$-22.43^{+0.18}_{-0.11}$	-23.88 ± 0.03	−0.10	$1.0^{+1.1}_{-0.9}$
NGC 3377	E	no	10.9	$0.77^{+0.04}_{-0.06}$	$-23.49^{+0.66}_{-0.58}$	-23.57 ± 0.06	−0.06	$4.0^{+6.8}_{-2.2}$
NGC 3384	S0 (bar)	no	11.3	$0.17^{+0.01}_{-0.02}$	$-22.43^{+0.18}_{-0.11}$	-23.74 ± 0.01	−0.08	$1.2^{+1.3}_{-1.0}$
NGC 3393	Sp (bar)	no	55.2	$0.34^{+0.02}_{-0.02}$	$-23.48^{+0.66}_{-0.58}$	-25.29 ± 0.10	−0.10	$2.8^{+4.7}_{-1.5}$
NGC 3414	E	no	24.5	$2.4^{+0.3}_{-0.3}$	$-24.35^{+0.18}_{-0.11}$	-24.42 ± 0.02	−0.09	$6.5^{+7.2}_{-5.5}$
NGC 3489	S0/Sp (bar)	no	11.7	$0.058^{+0.008}_{-0.008}$	$-21.13^{+0.66}_{-0.58}$	-23.07 ± 0.05	−0.06	$0.42^{+0.72}_{-0.23}$
NGC 3585	E	no	19.5	$3.1^{+1.4}_{-0.6}$	$-25.52^{+0.66}_{-0.58}$	-25.55 ± 0.03	−0.10	18^{+30}_{-10}
NGC 3607	E	no	22.2	$1.3^{+0.5}_{-0.5}$	$-25.36^{+0.66}_{-0.58}$	-25.45 ± 0.11	−0.10	15^{+25}_{-8}
NGC 3608	E	yes	22.3	$2.0^{+1.1}_{-0.6}$	$-24.50^{+0.66}_{-0.58}$	-24.50 ± 0.15	−0.08	$7.8^{+13.4}_{-4.3}$
NGC 3842	E	yes	98.4	97^{+30}_{-26}	$-27.00^{+0.18}_{-0.11}$	-27.04 ± 0.06	−0.11	61^{+68}_{-52}
NGC 3998	S0 (bar)	no	13.7	$8.1^{+2.0}_{-1.9}$	$-22.32^{+0.88}_{-0.66}$	-23.53 ± 0.01	−0.12	$0.78^{+1.43}_{-0.35}$
NGC 4026	S0 (bar)	no	13.2	$1.8^{+0.6}_{-0.3}$	$-21.58^{+0.88}_{-0.66}$	-23.16 ± 0.04	−0.09	$0.50^{+0.92}_{-0.22}$
NGC 4151	Sp (bar)	no	20.0	$0.65^{+0.07}_{-0.07}$	$-23.40^{+0.66}_{-0.58}$	-24.44 ± 0.19	−0.09	$2.8^{+4.8}_{-1.5}$
NGC 4261	E	yes	30.8	5^{+1}_{-1}	$-25.72^{+0.66}_{-0.58}$	-25.76 ± 0.20	−0.12	18^{+30}_{-10}
NGC 4291	E	yes	25.5	$3.3^{+0.9}_{-2.5}$	$-24.05^{+0.66}_{-0.58}$	-24.05 ± 0.14	−0.11	$3.9^{+6.7}_{-2.1}$
NGC 4388	Sp (bar)	no?	17.0	$0.075^{+0.002}_{-0.002}$	$-21.26^{+0.88}_{-0.66}$	≤ -23.50	−0.07	$0.46^{+0.85}_{-0.21}$
NGC 4459	S0	no	15.7	$0.68^{+0.13}_{-0.13}$	$-23.48^{+0.66}_{-0.58}$	-24.01 ± 0.05	−0.09	$2.9^{+5.0}_{-1.6}$
NGC 4473	E	no	15.3	$1.2^{+0.4}_{-0.9}$	$-23.88^{+0.66}_{-0.58}$	-24.11 ± 0.02	−0.10	$3.9^{+6.6}_{-2.1}$
NGC 4564	S0	no	14.6	$0.60^{+0.03}_{-0.09}$	$-22.30^{+0.18}_{-0.11}$	-22.99 ± 0.07	−0.11	$0.82^{+0.91}_{-0.70}$
NGC 4596	S0 (bar)	no	17.0	$0.79^{+0.38}_{-0.33}$	$-22.73^{+0.18}_{-0.11}$	-24.18 ± 0.05	−0.08	$1.6^{+1.7}_{-1.3}$

Galaxy	**Type**	**Core**	**Distance**	$\boldsymbol{M_{\rm BH}}$	$\boldsymbol{MAG_{\rm sph}}$	$\boldsymbol{MAG_{\rm gal}}$	$\boldsymbol{[3.6]-[4.5]}$	$\boldsymbol{M_{*,\rm sph}}$
			[Mpc]	[10^8 M$_\odot$]	[mag]	[mag]	[mag]	[10^{10} M$_\odot$]
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
NGC 4697	E	no	11.4	$1.8^{+0.2}_{-0.1}$	$-24.82^{+0.88}_{-0.66}$	-24.94 ± 0.00	-0.09	10^{+18}_{-4}
NGC 4889	E	yes	103.2	210^{+160}_{-160}	$-27.54^{+0.18}_{-0.11}$	-27.54 ± 0.00	-0.12	91^{+101}_{-77}
NGC 4945	Sp (bar)	no?	3.8	$0.014^{+0.014}_{-0.007}$	$-20.96^{+0.66}_{-0.58}$	≤ -23.79	-0.06	$0.36^{+0.62}_{-0.20}$
NGC 5077	E	yes	41.2	$7.4^{+4.7}_{-3.0}$	$-25.45^{+0.18}_{-0.11}$	-25.45 ± 0.06	-0.11	15^{+17}_{-13}
NGC 5128	merger	no?	3.8	$0.45^{+0.17}_{-0.10}$	$-23.89^{+0.88}_{-0.66}$	-24.97 ± 0.13	-0.07	$5.0^{+9.1}_{-2.2}$
NGC 5576	E	no	24.8	$1.6^{+0.3}_{-0.4}$	$-24.44^{+0.18}_{-0.11}$	-24.44 ± 0.07	-0.09	$7.1^{+7.9}_{-6.0}$
NGC 5845	S0	no	25.2	$2.6^{+0.4}_{-1.5}$	$-22.96^{+0.88}_{-0.66}$	-23.10 ± 0.13	-0.12	$1.4^{+2.6}_{-0.6}$
NGC 5846	E	yes	24.2	11^{+1}_{-1}	$-25.81^{+0.66}_{-0.58}$	-25.81 ± 0.10	-0.10	22^{+38}_{-12}
NGC 6251	E	yes?	104.6	5^{+2}_{-2}	$-26.75^{+0.18}_{-0.11}$	-26.75 ± 0.11	-0.12	46^{+51}_{-39}
NGC 7052	E	yes	66.4	$3.7^{+2.6}_{-1.5}$	$-26.32^{+0.18}_{-0.11}$	-26.32 ± 0.03	-0.11	33^{+36}_{-28}
NGC 7619	E	yes	51.5	25^{+8}_{-3}	$-26.35^{+0.66}_{-0.58}$	-26.41 ± 0.16	-0.11	33^{+56}_{-18}
NGC 7768	E	yes	112.8	13^{+5}_{-4}	$-26.90^{+0.66}_{-0.58}$	-26.90 ± 0.02	-0.11	57^{+98}_{-31}
UGC 03789	Sp (bar)	no?	48.4	$0.108^{+0.005}_{-0.005}$	$-22.77^{+0.88}_{-0.66}$	-24.20 ± 0.15	-0.07	$1.9^{+3.4}_{-0.8}$

NOTE. — *Column (1)*: Galaxy name. *Column (2)*: Morphological type (E=elliptical, S0=lenticular, Sp=spiral, merger). The morphological classification of four galaxies is uncertain (E/S0 or S0/Sp). The presence of a bar is indicated. *Column (3)*: Presence of a partially depleted core. The question mark is used when the classification has come from the velocity dispersion criteria mentioned in Section 2. *Column (4)*: Distance. *Column (5)*: Black hole mass. *Column (6)*: Absolute 3.6 μm bulge magnitude. *Column (7)*: Absolute 3.6 μm galaxy magnitude. The four galaxy magnitudes marked with a $\leq$ are upper limits. *Column (8)*: [3.6] − [4.5] colour. *Column (9)*: Bulge stellar mass.

TABLE 2
LINEAR REGRESSION ANALYSIS OF THE $M_{\rm BH} - MAG_{\rm gal}$ DIAGRAM.

Subsample (size)	**Regression**	$\boldsymbol{\alpha}$	$\boldsymbol{\beta}$	$\langle MAG_{\rm gal}\rangle$	$\boldsymbol{\epsilon}$	$\boldsymbol{\Delta}$
	$\log[M_{\rm BH}/{\rm M}_\odot] = \alpha + \beta[(MAG_{\rm gal} - \langle MAG_{\rm gal}\rangle)/{\rm mag}]$					
All (62)	BCES $(Y\|X)$	8.26 ± 0.08	-0.49 ± 0.06	-24.78	–	0.64
	BCES $(X\|Y)$	8.26 ± 0.12	-1.01 ± 0.15	-24.78	–	0.92
	BCES Bisector	8.26 ± 0.09	-0.72 ± 0.07	-24.78	–	0.71
	mFITEXY $(Y\|X)$	$8.26^{+0.08}_{-0.08}$	$-0.49^{+0.06}_{-0.07}$	-24.78	$0.61^{+0.07}_{-0.06}$	0.64
	mFITEXY $(X\|Y)$	$8.26^{+0.11}_{-0.12}$	$-1.03^{+0.13}_{-0.16}$	-24.78	$0.88^{+0.10}_{-0.08}$	0.93
	mFITEXY Bisector	$8.26^{+0.10}_{-0.10}$	$-0.73^{+0.09}_{-0.10}$	-24.78	–	0.71
	`linmix_err` $(Y\|X)$	8.26 ± 0.09	-0.49 ± 0.07	-24.78	0.63 ± 0.07	0.64
	`linmix_err` $(X\|Y)$	8.26 ± 0.12	-1.02 ± 0.15	-24.78	0.91 ± 0.17	0.93
	`linmix_err` Bisector	8.26 ± 0.10	-0.72 ± 0.15	-24.78	–	0.71
Early-type (E+S0) (45)	BCES $(Y\|X)$	8.56 ± 0.07	-0.44 ± 0.05	-24.88	–	0.45
	BCES $(X\|Y)$	8.56 ± 0.08	-0.64 ± 0.05	-24.88	–	0.53
	BCES Bisector	8.56 ± 0.07	-0.53 ± 0.04	-24.88	–	0.47
	mFITEXY $(Y\|X)$	$8.56^{+0.06}_{-0.06}$	$-0.42^{+0.05}_{-0.05}$	-24.88	$0.41^{+0.06}_{-0.05}$	0.45
	mFITEXY $(X\|Y)$	$8.56^{+0.08}_{-0.08}$	$-0.66^{+0.07}_{-0.08}$	-24.88	$0.51^{+0.07}_{-0.06}$	0.55
	mFITEXY Bisector	$8.56^{+0.07}_{-0.07}$	$-0.54^{+0.06}_{-0.06}$	-24.88	–	0.47
	`linmix_err` $(Y\|X)$	8.56 ± 0.07	-0.42 ± 0.06	-24.88	0.43 ± 0.06	0.45
	`linmix_err` $(X\|Y)$	8.56 ± 0.09	-0.65 ± 0.08	-24.88	0.53 ± 0.10	0.54
	`linmix_err` Bisector	8.56 ± 0.08	-0.53 ± 0.10	-24.88	–	0.47
Late-type (Sp) (17)	BCES $(Y\|X)$	7.37 ± 0.17	-0.33 ± 0.87	-24.39	–	0.65
	BCES $(X\|Y)$	7.37 ± 1.97	-21.66 ± 53.74	-24.39	–	7.73
	BCES Bisector	7.37 ± 0.20	-1.32 ± 0.94	-24.39	–	0.77
	FITEXY $(Y\|X)$	$7.38^{+0.17}_{-0.18}$	$-0.34^{+0.74}_{-0.80}$	-24.39	$0.63^{+0.19}_{-0.11}$	0.65
	FITEXY $(X\|Y)$			-24.39		
	FITEXY Bisector			-24.39	–	
	`linmix_err` $(Y\|X)$			-24.39		
	`linmix_err` $(X\|Y)$			-24.39		
	`linmix_err` Bisector			-24.39	–	

TABLE 3
LINEAR REGRESSION ANALYSIS OF THE $M_{\rm BH} - MAG_{\rm sph}$ DIAGRAM.

Subsample (size)	**Regression**	$\boldsymbol{\alpha}$	$\boldsymbol{\beta}$	$\langle MAG_{\rm sph}\rangle$	$\boldsymbol{\epsilon}$	$\boldsymbol{\Delta}$
	$\log[M_{\rm BH}/{\rm M}_\odot] = \alpha + \beta[(MAG_{\rm sph} - \langle MAG_{\rm sph}\rangle)/{\rm mag}]$					
All (66)	BCES $(Y\|X)$	8.16 ± 0.07	-0.44 ± 0.04	-23.86	–	0.56
	BCES $(X\|Y)$	8.16 ± 0.08	-0.61 ± 0.05	-23.86	–	0.68
	BCES Bisector	8.16 ± 0.07	-0.52 ± 0.04	-23.86	–	0.60
	mFITEXY $(Y\|X)$	$8.17^{+0.06}_{-0.07}$	$-0.43^{+0.03}_{-0.04}$	-23.86	$0.49^{+0.06}_{-0.05}$	0.56
	mFITEXY $(X\|Y)$	$8.15^{+0.07}_{-0.08}$	$-0.61^{+0.05}_{-0.05}$	-23.86	$0.58^{+0.07}_{-0.06}$	0.68
	mFITEXY Bisector	$8.16^{+0.07}_{-0.07}$	$-0.51^{+0.04}_{-0.04}$	-23.86	–	0.60
	`linmix_err` $(Y\|X)$	8.16 ± 0.07	-0.42 ± 0.04	-23.86	0.51 ± 0.06	0.56
	`linmix_err` $(X\|Y)$	8.16 ± 0.09	-0.60 ± 0.06	-23.86	0.60 ± 0.09	0.67
	`linmix_err` Bisector	8.16 ± 0.08	-0.51 ± 0.09	-23.86	–	0.59
$n > 2$ (43)	BCES $(Y\|X)$	8.58 ± 0.07	-0.42 ± 0.06	-24.77	–	0.46
	BCES $(X\|Y)$	8.58 ± 0.08	-0.58 ± 0.06	-24.77	–	0.56
	BCES Bisector	8.58 ± 0.07	-0.50 ± 0.05	-24.77	–	0.49
	mFITEXY $(Y\|X)$	$8.57^{+0.07}_{-0.06}$	$-0.41^{+0.04}_{-0.04}$	-24.77	$0.38^{+0.06}_{-0.06}$	0.46
	mFITEXY $(X\|Y)$	$8.56^{+0.08}_{-0.08}$	$-0.57^{+0.06}_{-0.07}$	-24.77	$0.44^{+0.08}_{-0.11}$	0.55
	mFITEXY Bisector	$8.57^{+0.07}_{-0.07}$	$-0.49^{+0.05}_{-0.05}$	-24.77	–	0.49
	`linmix_err` $(Y\|X)$	8.56 ± 0.07	-0.39 ± 0.05	-24.77	0.40 ± 0.06	0.46
	`linmix_err` $(X\|Y)$	8.55 ± 0.09	-0.57 ± 0.08	-24.77	0.49 ± 0.10	0.55
	`linmix_err` Bisector	8.56 ± 0.08	-0.48 ± 0.10	-24.77	–	0.49
Core-Sérsic (22)	BCES $(Y\|X)$	9.06 ± 0.09	-0.32 ± 0.11	-25.73	–	0.42
	BCES $(X\|Y)$	9.06 ± 0.12	-0.65 ± 0.12	-25.73	–	0.61
	BCES Bisector	9.06 ± 0.10	-0.47 ± 0.08	-25.73	–	0.48
	mFITEXY $(Y\|X)$	$9.06^{+0.08}_{-0.09}$	$-0.26^{+0.08}_{-0.07}$	-25.73	$0.36^{+0.09}_{-0.06}$	0.42
	mFITEXY $(X\|Y)$	$9.03^{+0.15}_{-0.16}$	$-0.72^{+0.17}_{-0.31}$	-25.73	$0.61^{+0.14}_{-0.09}$	0.68
	mFITEXY Bisector	$9.05^{+0.12}_{-0.13}$	$-0.47^{+0.12}_{-0.17}$	-25.73	–	0.48
	`linmix_err` $(Y\|X)$	9.04 ± 0.10	-0.24 ± 0.09	-25.73	0.40 ± 0.08	0.42
	`linmix_err` $(X\|Y)$	9.03 ± 0.17	-0.69 ± 0.27	-25.73	0.68 ± 0.30	0.64
	`linmix_err` Bisector	9.04 ± 0.14	-0.44 ± 0.16	-25.73	–	0.46
Sérsic (44)	BCES $(Y\|X)$	7.71 ± 0.09	-0.41 ± 0.08	-22.92	–	0.61
	BCES $(X\|Y)$	7.71 ± 0.14	-0.86 ± 0.16	-22.92	–	0.93
	BCES Bisector	7.71 ± 0.10	-0.61 ± 0.08	-22.92	–	0.71
	mFITEXY $(Y\|X)$	$7.72^{+0.08}_{-0.09}$	$-0.41^{+0.07}_{-0.08}$	-22.92	$0.54^{+0.08}_{-0.07}$	0.61
	mFITEXY $(X\|Y)$	$7.72^{+0.14}_{-0.13}$	$-0.86^{+0.13}_{-0.19}$	-22.92	$0.77^{+0.13}_{-0.10}$	0.93
	mFITEXY Bisector	$7.72^{+0.11}_{-0.11}$	$-0.61^{+0.10}_{-0.12}$	-22.92	–	0.71
	`linmix_err` $(Y\|X)$	7.73 ± 0.09	-0.41 ± 0.08	-22.92	0.55 ± 0.08	0.61
	`linmix_err` $(X\|Y)$	7.73 ± 0.14	-0.86 ± 0.17	-22.92	0.79 ± 0.20	0.93
	`linmix_err` Bisector	7.73 ± 0.12	-0.62 ± 0.15	-22.92	–	0.71
Early-type (E+S0) (45)	BCES $(Y\|X)$	8.56 ± 0.07	-0.33 ± 0.04	-24.47	–	0.46
	BCES $(X\|Y)$	8.56 ± 0.08	-0.48 ± 0.05	-24.47	–	0.55
	BCES Bisector	$\mathbf{8.56 \pm 0.07}$	$\mathbf{-0.40 \pm 0.04}$	$\mathbf{-24.47}$	–	**0.49**
	mFITEXY $(Y\|X)$	$8.56^{+0.06}_{-0.06}$	$-0.32^{+0.03}_{-0.04}$	-24.47	$0.40^{+0.06}_{-0.05}$	0.46
	mFITEXY $(X\|Y)$	$8.54^{+0.08}_{-0.08}$	$-0.49^{+0.05}_{-0.06}$	-24.47	$0.49^{+0.08}_{-0.06}$	0.57
	mFITEXY Bisector	$8.55^{+0.07}_{-0.07}$	$-0.41^{+0.04}_{-0.05}$	-24.47	–	0.49
	`linmix_err` $(Y\|X)$	8.55 ± 0.07	-0.32 ± 0.04	-24.47	0.41 ± 0.06	0.46
	`linmix_err` $(X\|Y)$	8.55 ± 0.09	-0.48 ± 0.06	-24.47	0.51 ± 0.10	0.56
	`linmix_err` Bisector	8.55 ± 0.08	-0.40 ± 0.09	-24.47	–	0.49
Late-type (Sp) (17)	BCES $(Y\|X)$	7.18 ± 0.16	-0.79 ± 0.43	-22.33	–	0.70
	BCES $(X\|Y)$	7.18 ± 0.29	-1.71 ± 0.71	-22.33	–	1.26
	BCES Bisector	$\mathbf{7.18 \pm 0.20}$	$\mathbf{-1.15 \pm 0.27}$	$\mathbf{-22.33}$	–	**0.88**
	mFITEXY $(Y\|X)$	$7.20^{+0.15}_{-0.15}$	$-0.53^{+0.22}_{-0.24}$	-22.33	$0.55^{+0.15}_{-0.10}$	0.63
	mFITEXY $(X\|Y)$	$7.38^{+0.54}_{-0.36}$	$-2.02^{+0.71}_{-2.13}$	-22.33	$1.09^{+0.41}_{-0.24}$	1.50
	mFITEXY Bisector	$7.26^{+0.40}_{-0.28}$	$-1.03^{+0.33}_{-0.52}$	-22.33	–	0.82
	`linmix_err` $(Y\|X)$	7.24 ± 0.19	-0.46 ± 0.32	-22.33	0.63 ± 0.16	0.62
	`linmix_err` $(X\|Y)$	7.34 ± 0.43	-1.93 ± 1.30	-22.33	1.31 ± 0.97	1.43
	`linmix_err` Bisector	7.27 ± 0.33	-0.96 ± 0.50	-22.33	–	0.78

TABLE 4
LINEAR REGRESSION ANALYSIS OF THE $M_{\rm BH} - M_{*,\rm sph}$ DIAGRAM.

Subsample (size)	**Regression**	$\boldsymbol{\alpha}$	$\boldsymbol{\beta}$	$\langle M_{*,\rm sph}\rangle$	$\boldsymbol{\epsilon}$	$\boldsymbol{\Delta}$
	$\log[M_{\rm BH}/{\rm M}_\odot] = \alpha + \beta\log[(M_{*,\rm sph} - \langle M_{*,\rm sph}\rangle)/{\rm M}_\odot]$					
Early-type (E+S0) (45)	BCES $(Y\|X)$	8.56 ± 0.07	0.85 ± 0.12	10.81	–	0.48
	BCES $(X\|Y)$	8.56 ± 0.09	1.27 ± 0.13	10.81	–	0.59
	BCES Bisector	$\mathbf{8.56 \pm 0.07}$	$\mathbf{1.04 \pm 0.10}$	**10.81**	–	**0.51**
	mFITEXY $(Y\|X)$	$8.56^{+0.06}_{-0.07}$	$0.83^{+0.11}_{-0.11}$	10.81	$0.42^{+0.07}_{-0.05}$	0.48
	mFITEXY $(X\|Y)$	$8.54^{+0.08}_{-0.09}$	$1.32^{+0.18}_{-0.15}$	10.81	$0.53^{+0.08}_{-0.07}$	0.61
	mFITEXY Bisector	$8.55^{+0.07}_{-0.08}$	$1.05^{+0.14}_{-0.12}$	10.81	–	0.51
	`linmix_err` $(Y\|X)$	8.55 ± 0.07	0.82 ± 0.12	10.81	0.43 ± 0.06	0.48
	`linmix_err` $(X\|Y)$	8.55 ± 0.09	1.29 ± 0.17	10.81	0.54 ± 0.11	0.59
	`linmix_err` Bisector	8.55 ± 0.08	1.03 ± 0.19	10.81	–	0.51
Late-type (Sp) (17)	BCES $(Y\|X)$	7.18 ± 0.17	1.95 ± 1.52	10.05	–	0.74
	BCES $(X\|Y)$	7.18 ± 0.39	5.89 ± 3.40	10.05	–	1.70
	BCES Bisector	$\mathbf{7.18 \pm 0.21}$	$\mathbf{3.00 \pm 1.30}$	**10.05**	–	**0.94**
	mFITEXY $(Y\|X)$	$7.20^{+0.15}_{-0.16}$	$1.22^{+0.70}_{-0.62}$	10.05	$0.59^{+0.16}_{-0.11}$	0.66
	mFITEXY $(X\|Y)$	$7.44^{+1.45}_{-0.52}$	$7.14^{+26.31}_{-3.01}$	10.05	$1.49^{+0.56}_{-0.36}$	2.08
	mFITEXY Bisector	$7.24^{+1.04}_{-0.39}$	$2.28^{+1.67}_{-1.01}$	10.05	–	0.79
	`linmix_err` $(Y\|X)$	7.23 ± 0.19	0.96 ± 0.96	10.05	0.67 ± 0.16	0.65
	`linmix_err` $(X\|Y)$	7.42 ± 0.64	6.96 ± 6.73	10.05	1.83 ± 1.86	2.03
	`linmix_err` Bisector	7.26 ± 0.47	1.94 ± 216.38	10.05	–	0.74

NOTE. — cia

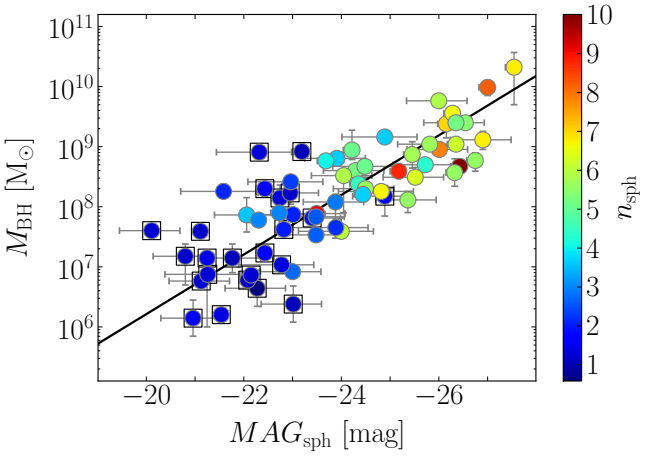

FIG. 3.— Black hole mass versus 3.6 μm spheroid absolute magnitude. Symbols are color coded according to the spheroid Sérsic index $n_{\rm sph}$. Bulges with $n_{\rm sph} < 2$, claimed by some to be pseudobulges, are marked with an empty square. The black solid line shows the BCES bisector linear regression for spheroids with $n_{\rm sph} \geq 2$.

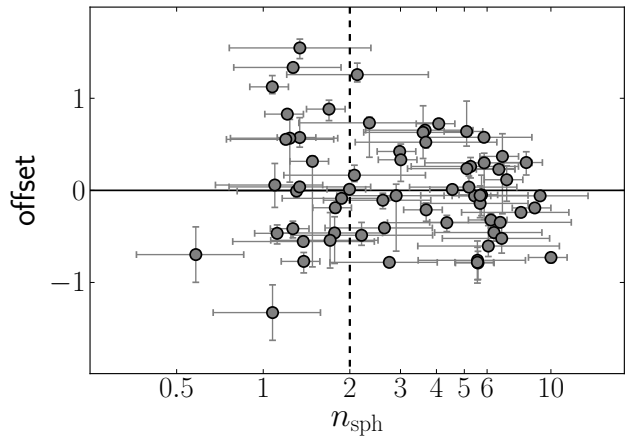

FIG. 4.— Vertical offset from the $M_{\rm BH} - L_{\rm sph}$ correlation defined by spheroids with $n_{\rm sph} \geq 2$. The vertical dashed line corresponds to $n_{\rm sph} = 2$. The horizontal solid line is equivalent to a zero vertical offset. Bulges with $n_{\rm sph} < 2$ are not randomly offset to lower black hole masses from the correlation traced by bulges with $n_{\rm sph} \geq 2$.

$M_{\rm BH} - M_{*,\rm sph}$ (see Table 4), using the BCES code from Akritas & Bershady (1996). We also repeated the analysis with the FITEXY routine (Press et al. 1992), as modified by Tremaine et al. (2002), and the Bayesian estimator `linmix_err` (Kelly 2007). All these three linear regression routines account for the intrinsic scatter, but only the last two allow to quantify it. We report linear regressions, both symmetrical and non-symmetrical, for Sérsic/core-Sérsic galaxies and for different galaxy morphological types (elliptical/lenticular, spiral). Symmetrical regressions are meant to be compared with theoretical expectations, whereas non-symmetrical $(Y|X)$ regressions – since they minimize the scatter in the vertical direction – can be used to predict black hole masses.

4. RESULTS AND DISCUSSION

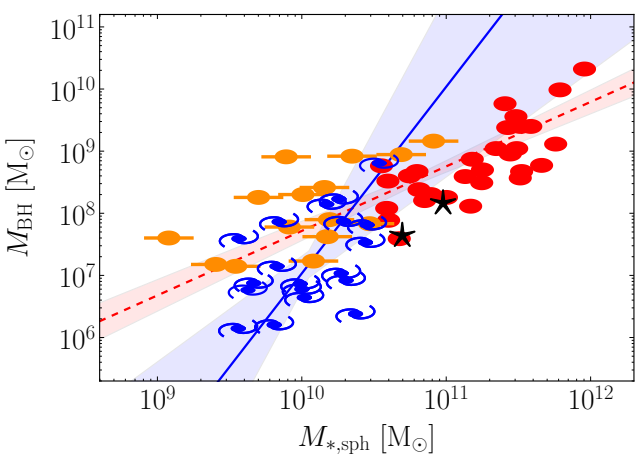

FIG. 5.— Black hole mass against spheroid stellar mass. Symbols are coded according to the galaxy morphological type (red = E, orange = E/S0 and S0, blue = S0/Sp and Sp, black = merger). The red dashed line indicates the BCES bisector linear regression for early-type galaxies (ellipticals+lenticulars), with the red shaded area denoting its 1σ uncertainty. The blue solid line shows the BCES bisector linear regression for spiral galaxies, with the blue shaded area denoting its 1σ uncertainty.

4.1. *Black hole mass – galaxy luminosity*

Figure 1 illustrates the $M_{\rm BH} - L_{\rm gal}$ diagram. Four spiral galaxies had their total luminosities underestimated (see Section 2) and thus are not included in the linear regression analysis.

Upon analyzing a sample of 35 galaxies, among which only four were classified as spiral galaxies, Läsker et al. (2014b) claimed that the $M_{\rm BH} - L_{\rm sph}$ and $M_{\rm BH} - L_{\rm gal}$ relations, which they fit with a single power-law, have consistent intrinsic scatter. Here, instead, thanks to our double-sized galaxy sample that includes 17 spiral galaxies, we show that the claim made by Läsker et al. (2014b) is valid only for early-type galaxies. The $M_{\rm BH} - L_{\rm sph}$ correlation for all galaxies, irrespective of their morphological type, has intrinsic scatter $\epsilon_{(Y|X)} = 0.51 \pm 0.06$ dex (direct linear regression) and $\epsilon_{(X|Y)} = 0.60 \pm 0.09$ dex (inverse linear regression), whereas the $M_{\rm BH} - L_{\rm gal}$ correlation for all galaxies has $\epsilon_{(Y|X)} = 0.63 \pm 0.07$ dex and $\epsilon_{(X|Y)} = 0.91 \pm 0.17$ dex. However, when considering only early-type galaxies, we find that the $M_{\rm BH} - L_{\rm sph}$ and $M_{\rm BH} - L_{\rm gal}$ relations have the same level of intrinsic scatter. Because the value of the intrinsic scatter depends on the uncertainties associated to the luminosities[7], we tested the robustness of our last conclusion by increasing/decreasing the errors associated to $L_{\rm gal}$ (that we originally assumed to be 0.25 mag) and repeating the linear regression analysis. On the other hand, the uncertainties associated to $L_{\rm sph}$ have been estimated with an advanced method that takes into account the systematic errors related to the galaxy decomposition process. We consider these uncertainties trustworthy and, therefore, we decided to vary only the errors associated to $L_{\rm gal}$. We found that the $M_{\rm BH} - L_{\rm sph}$ and $M_{\rm BH} - L_{\rm gal}$ relations for early-type galaxies have inconsistent intrinsic scatter when assuming an error ≥ 0.7 mag on $L_{\rm gal}$. Because such

[7] The smaller (larger) the uncertainties, the larger (smaller) the intrinsic scatter.

error is larger than the typical error on $L_{\rm sph}$ used here – and, in general, is significantly larger than the uncertainties on $L_{\rm gal}$ that are typically used in the literature –, we come to the conclusion that our determination of the intrinsic scatter is reliable, and that, for early-type galaxies, $M_{\rm BH}$ correlates equally well with $L_{\rm sph}$ and $L_{\rm gal}$. As Läsker et al. (2014b) pointed out, from the observer's perspective, measuring galaxy luminosities is obviously easier and faster than performing accurate This, combined with our last conclusion, suggests that one should prefer the galaxy luminosity over the bulge luminosity to predict black hole masses when dealing with samples of elliptical and lenticular galaxies only.

4.2. *Black hole mass – spheroid luminosity*

We show the $M_{\rm BH} - L_{\rm sph}$ diagram in Figure 2.
Sérsic and core-Sérsic spheroids have slopes consistent with each other (within their 1σ uncertainties), in disagreement with the findings of GS13. The slope that we obtained for core-Sérsic spheroids ($M_{\rm BH} \propto L_{\rm sph}^{1.2\pm0.2}$) is consistent with the slope reported by GS13 in the K_s-band ($M_{\rm BH} \propto L_{\rm sph}^{1.1\pm0.2}$). Instead, the slope that we determined for Sérsic spheroids ($M_{\rm BH} \propto L_{\rm sph}^{1.5\pm0.2}$) is significantly shallower than that found by GS13 ($M_{\rm BH} \propto L_{\rm sph}^{2.7\pm0.5}$). Although the Sérsic/core-Sérsic classification used by GS13 slightly differs[8] from the classification used here, the main cause of such inconsistency is that the bulge-to-total ratios obtained from our galaxy decompositions are different from those assumed by GS13 to convert galaxy luminosities into bulge luminosities. Our bulge-to-total ratios for low-luminosity Sérsic spheroids ($MAG_{\rm sph} \gtrsim -22$ mag) are smaller than those used by GS13. The host galaxies of such bulges are late-type, spiral galaxies, which typically present a complex morphology (bars, double bars, embedded disks, nuclear components, etc). Our sophisticated galaxy models account for the extra components, while the bulge-to-total ratios of GS13 were derived from simple bulge/disk decompositions which overestimated the bulge luminosity. This results in our bulge magnitudes being on average $\sim$1 mag fainter. On the other side, our bulge-to-total ratios for high-luminosity Sérsic spheroids ($MAG_{\rm sph} \lesssim -24$ mag) are on average larger than those adopted by GS13. In this case, the host systems are early-type elliptical/lenticular galaxies that feature intermediate-scale disks[9]. Past bulge/disk decompositions failed to correctly identify the extent of such disks and treated them as large-scale disks, thus underestimating the bulge luminosity. The magnitudes that we obtained for such spheroids are on average $\sim$1 mag brighter.
We have seen that the change in slope of the $M_{\rm BH} - L_{\rm sph}$ correlation – which is expected for consistency with other scaling relations (a single power-law $M_{\rm BH} - \sigma$ correlation and a double power-law $L_{\rm sph} - \sigma$ correlation) – cannot be attributed to the division between the two populations of Sérsic and core-Sérsic spheroids. We now test a new hypothesis, that is to say the change in slope is to be ascribed to the different formation mechanisms of early- and late-type galaxies. If this hypothesis is correct, the spheroids of early-type (elliptical and lenticular) galaxies will follow $M_{\rm BH} \propto L_{\rm sph}^{\sim1}$, whereas the spheroids of late-type (spiral) galaxies will have $M_{\rm BH} \propto L_{\rm sph}^{\sim2.5}$. First, we checked that elliptical and lenticular galaxies, taken separately, have slopes consistent with each other, and thus, taken together, they define a single *red sequence* in the $M_{\rm BH} - L_{\rm sph}$ diagram. We then fit the bulges of early- and late-type galaxies with two separate log-linear regressions, and obtained $M_{\rm BH} \propto L_{\rm sph}^{1\pm0.1}$ and $M_{\rm BH} \propto L_{\rm sph}^{2.75\pm0.75}$ respectively, in excellent agreement with the theoretical expectations of our hypothesis. **AL, can you pls write this: Remember also Ewan's remark about the unsuitability of the Pearson and Spearman correlation coefficients because they do not take into account the error bars on our data - so don't include those simple coefficients. Actually, it would be worth pointing out to readers that a visual inspection of the plotted data requires the viewer to take into account the error bars when judging-by-eye the strength of a correlation. Maybe then mention in the following sentence that this is why the correlation coefficients are not applicable here.**

4.3. *Pseudo- versus classical bulges*

Current views distinguish between classical bulges, which are considered to be spheroidal, pressure-supported systems, formed through violent processes, such as hierarchical clustering via minor mergers, and pseudo-bulges, thought to be disk-like, rotation-supported systems, built from secular evolution processes, such as instabilities of their surrounding disk or bar. Pseudo-bulges are notoriously hard to identify (Graham 2013, 2014, 2015a,c). For example, mergers can create bulges that rotate (e.g. Bekki 2010; Keselman & Nusser 2012), and bars can spin-up classical bulges (e.g. Saha et al. 2012), thus rotation is not a definitive signature of a pseudobulge. Furthermore, many galaxies host both a pseudo- and a classical bulge (e.g. Erwin et al. 2003, 2015; Athanassoula 2005; Gadotti 2009; MacArthur et al. 2009; dos Anjos & da Silva 2013; Seidel et al. 2015). In the recent literature, pseudo- and classical bulges have been frequently told apart by means of a divide at a Sérsic index of $n_{\rm sph} = 2$ (e.g. Fisher & Drory 2010), although, from a selection of hundreds of disc galaxies imaged in the K-band, Graham & Worley (2008) observed no such bimodality in the bulge Sérsic indices. While pseudo-bulges are expected to have exponential-like surface brightness profiles ($n_{\rm sph} \simeq 1$), being disky components that formed from their surrounding exponential disks (e.g. Bardeen 1975; Hohl 1975; Combes & Sanders 1981; Combes et al. 1990; Pfenniger & Friedli 1991), it has been shown that mergers can create bulges with $n_{\rm sph} < 2$ (e.g. Eliche-Moral et al. 2011; Scannapieco et al. 2011; Querejeta et al. 2015), just as low-luminosity elliptical galaxies (not built from the secular evolution of a disk) are well known to have $n_{\rm sph} < 2$ and even $n_{\rm sph} < 1$ (e.g. Davies et al. 1988; Young & Currie 1994). Sani et al. (2011) reported that pseudo-bulges – which they labelled as such according to the $n_{\rm sph} < 2$ criterion – with low black hole masses ($M_{\rm BH} < 10^7$ M$_\odot$) are significantly displaced from the correlation traced by classical

[8] which galaxies?
[9] explain

bulges. In Figure 4, we show the distribution of spheroid Sérsic indices[10] in the $M_{\rm BH}-L_{\rm sph}$ diagram. Our aim is to check whether $n_{\rm sph} < 2$ bulges are offset to lower black hole masses from the correlation defined by $n_{\rm sph} > 2$ bulges. To do this, we fit a symmetrical linear regression to the bulges that have $n_{\rm sph} > 2$ and we compute the vertical offset of all bulges from the regression. In the inset of Figure 4, we plot the vertical offset against $n_{\rm sph}$. From a visual inspection, bulges with $n_{\rm sph} < 2$ do not appear to be offset from the correlation traced by bulges with $n_{\rm sph} > 2$.

4.4. *Black hole mass – spheroid stellar mass*

Finally, we present the $M_{\rm BH} - M_{*,\rm sph}$ diagram in Figure 5. The bulges of early-type galaxies follow $M_{\rm BH} \propto M_{*,\rm sph}^{1.0\pm0.1}$, as expected from a dry-merging formation scenario, and define a tight *red sequence* with intrinsic scatter $\epsilon_{(Y|X)} = 0.43 \pm 0.06$ dex. On the other hand, the bulges of spiral galaxies trace a steeper *blue sequence*, whose slope is not well constrained due to the small size of the subsample and, more importantly, to the small range in $M_{*,\rm sph}$ that the subsample spans. For the bulges of spiral galaxies, the BCES code returns a bisector linear regression $M_{\rm BH} \propto M_{*,\rm sph}^{3.0\pm1.3}$, while the modified FITEXY routine finds a shallower (but still consistent within the 1σ uncertainty) slope of $2.3^{+1.7}_{-1.0}$. The Bayesian estimator of Kelly (2007) fails in performing an inverse $(X|Y)$ linear regression for the subsample of spiral galaxies. **which code do we trust more in this case? BCES or FITEXY? is it a quadratic or a cubic growth?**

Graham & Scott (2015) collected a sample of ∼170 low-redshift ($z \lesssim 0.1$) bulges hosting Active Galactic Nuclei (AGNs) with black hole masses $10^5 \lesssim M_{\rm BH}/{\rm M}_\odot \lesssim 0.5 \times 10^8$, and showed that they roughly follow the quadratic $M_{\rm BH} - M_{*,\rm sph}$ relation defined by predominantly inactive Sérsic bulges. Although we demonstrated that, using our dataset, the Sérsic bulges do not define a quadratic relation, we anticipate here that the correlation traced by our bulges of spiral galaxies tracks the location of the AGNs in the $M_{\rm BH} - M_{*,\rm sph}$ diagram, i.e. the AGNs appears to be the low-mass continuation of the *blue sequence* shown in Figure 5. We also note that the majority of our spiral galaxies hosts an AGN[11].
cite Anne's paper
AL: however we analyze the agns in another paper, blah blah

5. CONCLUSIONS

to be written

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[10] The spheroid Sérsic indices are taken from our one-dimensional fits of the galaxy major-axis surface brightness profiles (*Paper I*).

[11] According to the nuclear classification reported on NED (Nasa Extragalactic Database), among our 17 spiral galaxies, at least 12 host a Seyfert AGN and one hosts a LINER AGN.

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