

# Bank Telemarketing Dataset

## Content

- A. Introduction
- B. Problem Statement
- C. Our Data
- D. Modeling Process
- E. Final Thoughts

## A. Introduction

Telemarketing is a method of selling products and services over the phone to customers. It has always been a controversial approach. On one hand, it is easy to directly reach out to customers and also cheaper than other marketing methods. On the other hand, it has bad reputations of damaging the company's image and some of the startup costs are very expensive.

In this project, we are looking into how other factors can affect the outcome of telemarketing campaigns for a specific institution, Portuguese retail bank, and make prediction based on our model. The main focus of this project is incredibly interesting since we typically feel annoyed by telemarketing.

## B. Problem Statement

Our main question is what is likely to be the outcome of the telemarketing campaigns based on the characteristics of the clients and the calls. Our goal is to predict if the client will subscribe (yes/no) to a term deposit (variable  $y$ ).

Note: A term deposit is a type of deposit account held at a financial institution where money is locked up for some set period of time

## C. Our Data

### 1. Data Source

- Dataset name: **Bank Tele-Marketing Data Set**
- Original Source of the Dataset: [Moro et al., 2014] S. Moro, P. Cortez and P. Rita. A Data-Driven Approach to Predict the Success of Bank Telemarketing. Decision Support Systems, Elsevier, 62:22-31, June 2014
- We retrieve the data from UCI Machine Learning Repository. The data is accessible [here](#).

### 2. Background

- The data is collected from several telemarketing campaigns in which the Portuguese bank attempted to target customers through phone calls to sell long-term deposits.
- The dataset includes both the phone calls of which the bank executed and the phone calls of which clients contacted the help center.
- Each observation includes the outcome, whether or not the target customers subscribed the term deposit, and the characteristics of the customers and the phone calls themselves.

### 3. Variable Description

This dataset was collected from May 2008 to November 2010 with 41188 observations and 20 variables.

No.	Variable Name	Variable Definiton	Data Type	Units/Categories	Note
1	age	Client's age	Discrete	years	
2	job	Type of client's job	Categorical	admin, blue-collar, entrepreneur, housemaid, management, retired, self-employed, services, student, technician, unemployed	

<b>3</b>	marital	Marital status	Categorical	divorced, married, single	'divorced' means divorced or widowed
<b>4</b>	education	Education level	Categorical	basic.4y, basic.6y, basic.9y, high.school, illiterate, professional.course, university.degree	
<b>5</b>	default	Has credit in default?	Categorical	yes, no	
<b>6</b>	housing	Has housing loan?	Categorical	yes, no	
<b>7</b>	loan	Has personal loan?	Categorical	yes, no	
<b>8</b>	contact	Contact communication type	Categorical	cellular, telephone	
<b>9</b>	month	Last contact month of year	Categorical	jan, feb, mar, ..., nov, dec	
<b>10</b>	day_of_week	Last contact day of the week	Categorical	mon, tue, wed, thu, fri	
<b>11</b>	duration	Last contact duration	Discrete	seconds	This attribute highly affects the output target (e.g., if duration=0 then y='no'). Yet, the duration is not known before a call is performed.
<b>12</b>	campaign	Number of contacts performed during this campaign and for this client	Discrete	contacts	including last contact
<b>13</b>	pdays	Number of days that passed by after the client was last contacted from a previous campaign	Discrete	days	999 means client was not previously contacted
<b>14</b>	previous	Number of contacts performed before this campaign and for this client	Discrete	contacts	
<b>15</b>	outcome	Outcome of the previous marketing campaign	Categorical	failure, success, nonexistent	

<b>16</b>	emp.var.rate	Employment variation rate - quarterly indicator	Continuous	-	Calculate the variation of employment rate ⇒ higher variation means the employment rate changes a lot (unstable economy)
<b>17</b>	cons.price.idx	Consumer price index - monthly indicator	Continuous	-	The average change in prices over time that consumers pay for a basket of goods and services
<b>18</b>	cons.conf.idx	Consumer confidence index - monthly indicator	Continuous	-	Defined as the degree of optimism about the state of the economy that consumers are expressing through their activities of saving and spending
<b>19</b>	euribor3m	Euribor 3 month rate - daily indicator	Continuous	-	Euribor is an overnight interbank rate comprised of the average interest rates from a panel of large European banks that are used for lending to one another in euros
<b>20</b>	nr.employed	Number of employees - quarterly indicator	Numeric	-	
<b>21</b>	y	Has the client subscribed to a term deposit?	Categorical	yes, no	

## 4. Problems with Data

1. There are too many categorical variables that aren't Bernoulli variables, and it would be complicated to interpret with too many of them

⇒ Possible solutions: change some of them (month, day\_of\_week, contact, etc) to other type of variables or group some of the categories together

1. Some of the data are not in its correct form (Bernoulli not broken into 0 and 1)
2. Some variables are terminologies
3. Some variables have many NAs
4. Some variables have special cases such as marital, duration, pdays

### Read and explore the dataset

```
bankDf <- read.csv2("bank-additional-full.csv")
summary(bankDf)
```

```
##      age          job          marital          education
##  Min.   :17.00   Length:41188   Length:41188   Length:41188
##  1st Qu.:32.00   Class :character   Class :character   Class :character
##  Median :38.00   Mode  :character   Mode  :character   Mode  :character
##  Mean    :40.02
##  3rd Qu.:47.00
##  Max.    :98.00
##  default        housing        loan          contact
##  Length:41188   Length:41188   Length:41188   Length:41188
##  Class :character   Class :character   Class :character   Class :character
##  Mode  :character   Mode  :character   Mode  :character   Mode  :character
##
##
##  month          day_of_week        duration        campaign
##  Length:41188   Length:41188   Min.   : 0.0   Min.   : 1.000
##  Class :character   Class :character   1st Qu.:102.0   1st Qu.: 1.000
##  Mode  :character   Mode  :character   Median :180.0   Median : 2.000
##                                     Mean    :258.3   Mean    : 2.568
##                                     3rd Qu.:319.0   3rd Qu.: 3.000
##                                     Max.    :4918.0   Max.    :56.000
##  pdays          previous        poutcome        emp.var.rate
##  Min.   : 0.0   Min.   :0.000   Length:41188   Length:41188
##  1st Qu.:999.0   1st Qu.:0.000   Class :character   Class :character
##  Median :999.0   Median :0.000   Mode  :character   Mode  :character
##  Mean    :962.5   Mean    :0.173
##  3rd Qu.:999.0   3rd Qu.:0.000
##  Max.    :999.0   Max.    :7.000
##  cons.price.idx  cons.conf.idx    euribor3m        nr.employed
##  Length:41188   Length:41188   Length:41188   Length:41188
##  Class :character   Class :character   Class :character   Class :character
```

```

## Mode :character Mode :character Mode :character Mode :character
##
##
##
##      y
## Length:41188
## Class :character
## Mode :character
##
##
##

glimpse(bankDf)

## Rows: 41,188
## Columns: 21
## $ age      <int> 56, 57, 37, 40, 56, 45, 59, 41, 24, 25, 41, 25, 29,
57,...
## $ job      <chr> "housemaid", "services", "services", "admin.", "ser
vice...
## $ marital  <chr> "married", "married", "married", "married", "marrie
d", ...
## $ education <chr> "basic.4y", "high.school", "high.school", "basic.6y
", "...
## $ default  <chr> "no", "unknown", "no", "no", "no", "unknown", "no",
"un...
## $ housing  <chr> "no", "no", "yes", "no", "no", "no", "no", "no", "y
es",...
## $ loan     <chr> "no", "no", "no", "no", "yes", "no", "no", "no", "n
o", ...
## $ contact  <chr> "telephone", "telephone", "telephone", "telephone",
"te...
## $ month    <chr> "may", "may", "may", "may", "may", "may", "may", "m
ay",...
## $ day_of_week <chr> "mon", "mon", "mon", "mon", "mon", "mon", "mon", "m
on",...
## $ duration <int> 261, 149, 226, 151, 307, 198, 139, 217, 380, 50, 55
, 22...
## $ campaign <int> 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
1, 1...
## $ pdays    <int> 999, 999, 999, 999, 999, 999, 999, 999, 999, 999, 999, 9
99, ...
## $ previous <int> 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0...
## $ poutcome <chr> "nonexistent", "nonexistent", "nonexistent", "nonex
iste...
## $ emp.var.rate <chr> "1.1", "1.1", "1.1", "1.1", "1.1", "1.1", "1.1", "1
.1",...
## $ cons.price.idx <chr> "93.994", "93.994", "93.994", "93.994", "93.994", "
93.9...

```

```
## $ cons.conf.idx <chr> "-36.4", "-36.4", "-36.4", "-36.4", "-36.4", "-36.4",  
    ", "...  
## $ euribor3m      <chr> "4.857", "4.857", "4.857", "4.857", "4.857", "4.857"  
    ", "...  
## $ nr.employed   <chr> "5191", "5191", "5191", "5191", "5191", "5191", "51  
91",...  
## $ y             <chr> "no", "no", "no", "no", "no", "no", "no", "no", "no"  
    ", "...
```

## Data Wrangling

## Turn all “unknown” to NA value

```
bankDf <- bankDf %>% replace_with_na_all(condition = ~.x == "unknown")
```

## Turn Bernoulli variables into 0 and 1 categories

```
bankDf <- rename(bankDf, telephone = contact)
bankDf <- rename(bankDf, deposit = y)
```

```
bankDf <- bankDf %>%
  #mutate(employed = ifelse(employed == "unemployed", 0, 1)) %>%
  mutate(default = ifelse(default == "yes", 1, 0)) %>%
  mutate(housing = ifelse(housing == "yes", 1, 0)) %>%
  mutate(loan = ifelse(loan == "yes", 1, 0)) %>%
  mutate(telephone = ifelse(telephone == "telephone", 1, 0)) %>%
  mutate(deposit = ifelse(deposit == "yes", 1, 0))
```

## Turn other variables into its suitable types of variables

```
#bankDf$employed <- as.factor(bankDf$employed)
bankDf$job <- as.factor(bankDf$job)
bankDf$marital <- as.factor(bankDf$marital)
bankDf$education <- as.factor(bankDf$education)
bankDf$default <- as.factor(bankDf$default)
bankDf$housing <- as.factor(bankDf$housing)
bankDf$loan <- as.factor(bankDf$loan)
bankDf$telephone <- as.factor(bankDf$telephone)
bankDf$poutcome <- as.factor(bankDf$poutcome)
bankDf$month <- as.factor(bankDf$month)
bankDf$day_of_week <- as.factor(bankDf$day_of_week)

bankDf$previous <- as.numeric(bankDf$previous)
bankDf$emp.var.rate <- as.numeric(bankDf$emp.var.rate)
bankDf$cons.price.idx <- as.numeric(bankDf$cons.price.idx)
bankDf$cons.conf.idx <- as.numeric(bankDf$cons.conf.idx)
bankDf$euribor3m <- as.numeric(bankDf$euribor3m)
bankDf$nr.employed <- as.numeric(bankDf$nr.employed)

bankDf$pdays <- as.factor(bankDf$pdays)
```

## Data Exploration

```
summary(bankDf)
```

```

##          age                job                marital
## Min.      :17.00    admin.      :10422    divorced: 4612
## 1st Qu.:32.00    blue-collar: 9254    married  :24928
## Median :38.00    technician : 6743    single   :11568
## Mean      :40.02    services   : 3969    NA's     :    80
## 3rd Qu.:47.00    management : 2924
## Max.      :98.00    (Other)    : 7546
##                      NA's      :   330
##                      education    default      housing      loan      teleph
one
## university.degree :12168    0      :32588    0      :18622    0      :33950    0:2614
4
## high.school      : 9515    1      :    3    1      :21576    1      : 6248    1:1504
4
## basic.9y          : 6045    NA's: 8597    NA's: 990    NA's: 990
## professional.course: 5243
## basic.4y          : 4176
## (Other)           : 2310
## NA's              : 1731
##      month      day_of_week      duration      campaign      pdays
## may      :13769    fri:7827    Min.      : 0.0    Min.      : 1.000    999      :396
73
## jul      : 7174    mon:8514    1st Qu.: 102.0    1st Qu.: 1.000    3        : 4
39
## aug      : 6178    thu:8623    Median : 180.0    Median : 2.000    6        : 4
12
## jun      : 5318    tue:8090    Mean    : 258.3    Mean     : 2.568    4        : 1
18
## nov      : 4101    wed:8134    3rd Qu.: 319.0    3rd Qu.: 3.000    9        :
64
## apr      : 2632                Max.      :4918.0    Max.      :56.000    2        :
61
## (Other): 2016                                (Other): 4
21
##      previous      poutcome      emp.var.rate      cons.price.idx
## Min.      :0.000    failure      : 4252    Min.      :-3.40000    Min.      :92.20
## 1st Qu.:0.000    nonexistent:35563    1st Qu.: -1.80000    1st Qu.:93.08
## Median :0.000    success      : 1373    Median : 1.10000    Median :93.75
## Mean      :0.173                Mean      : 0.08189    Mean      :93.58
## 3rd Qu.:0.000                3rd Qu.: 1.40000    3rd Qu.:93.99
## Max.      :7.000                Max.      : 1.40000    Max.      :94.77
##
##      cons.conf.idx      euribor3m      nr.employed      deposit
## Min.      :-50.8    Min.      :0.634    Min.      :4964    Min.      :0.0000
## 1st Qu.: -42.7    1st Qu.:1.344    1st Qu.:5099    1st Qu.:0.0000
## Median : -41.8    Median :4.857    Median :5191    Median :0.0000
## Mean      : -40.5    Mean      :3.621    Mean      :5167    Mean      :0.1127
## 3rd Qu.: -36.4    3rd Qu.:4.961    3rd Qu.:5228    3rd Qu.:0.0000
## Max.      : -26.9    Max.      :5.045    Max.      :5228    Max.      :1.0000
##

```



## Make some decisions

We decide to remove those columns below: - default because it has too many NAs - poutcome (previous campaign's outcome) because it has too many "nonexistent" result - pdays (days after the customers were last contacted in the previous campaigns) because most of the customers had never been contacted before

```
bankDf <- bankDf %>%
  select(!default) %>%
  select(!poutcome) %>%
  select(!pdays)

bankDf <- na.omit(bankDf)
summary(bankDf)
```

##	age	job	marital			
##	Min. :17.00	admin. :9937	divorced: 4302			
##	1st Qu.:32.00	blue-collar:8560	married :23183			
##	Median :38.00	technician :6380	single :10760			
##	Mean :39.86	services :3716				
##	3rd Qu.:47.00	management :2728				
##	Max. :98.00	retired :1577				
##		(Other) :5347				
##		education	housing	loan	telephone	month
##	basic.4y	: 4002	0:17667	0:32286	0:24441	may :12794
##	basic.6y	: 2204	1:20578	1: 5959	1:13804	jul : 6630
##	basic.9y	: 5856				aug : 5822
##	high.school	: 9244				jun : 4846
##	illiterate	: 18				nov : 3898
##	professional.course: 5100					apr : 2436
##	university.degree :11821					(Other): 1819
##	day_of_week	duration	campaign	previous		
##	fri:7224	Min. : 0.0	Min. : 1.000	Min. :0.00		
##	mon:7927	1st Qu.: 102.0	1st Qu.: 1.000	1st Qu.:0.00		
##	thu:8011	Median : 180.0	Median : 2.000	Median :0.00		
##	tue:7481	Mean : 258.2	Mean : 2.567	Mean :0.17		
##	wed:7602	3rd Qu.: 319.0	3rd Qu.: 3.000	3rd Qu.:0.00		
##		Max. :4918.0	Max. :43.000	Max. :7.00		
##						
##	emp.var.rate	cons.price.idx	cons.conf.idx	euribor3m		
##	Min. :-3.40000	Min. :92.20	Min. :-50.80	Min. :0.634		
##	1st Qu.: -1.80000	1st Qu.:93.08	1st Qu.: -42.70	1st Qu.:1.344		
##	Median : 1.10000	Median :93.44	Median : -41.80	Median :4.857		
##	Mean : 0.08286	Mean :93.57	Mean : -40.54	Mean :3.623		
##	3rd Qu.: 1.40000	3rd Qu.:93.99	3rd Qu.: -36.40	3rd Qu.:4.961		
##	Max. : 1.40000	Max. :94.77	Max. : -26.90	Max. :5.045		
##						
##	nr.employed	deposit				
##	Min. :4964	Min. :0.0000				
##	1st Qu.:5099	1st Qu.:0.0000				

```
## Median :5191 Median :0.0000
## Mean :5167 Mean :0.1113
## 3rd Qu.:5228 3rd Qu.:0.0000
## Max. :5228 Max. :1.0000
##
```

### Split into training and test dataset

```
set.seed(1)
N <- seq(38245)
S <- sample(N,30596)
bankTrain <- bankDf[S,]
bankTest <- bankDf[-S,]
summary(bankTrain)
```

```
##      age                job                marital                educati
on
## Min.   :17.00   admin.       :7937   divorced: 3427   basic.4y           :3
184
## 1st Qu.:32.00   blue-collar:6856   married :18600   basic.6y           :1
786
## Median :38.00   technician :5117   single  : 8569   basic.9y           :4
696
## Mean   :39.86   services   :3001                high.school         :7
392
## 3rd Qu.:47.00   management :2174                illiterate          :
14
## Max.   :98.00   retired    :1249                professional.course:4
070
##                (Other)    :4262                university.degree :9
454
## housing   loan       telephone   month        day_of_week   duration
## 0:14180   0:25811   0:19517   may         :10233   fri:5792   Min.    : 0.0
## 1:16416   1: 4785   1:11079   jul         : 5316   mon:6357   1st Qu.: 102.0
##                aug         : 4673   thu:6447   Median : 180.0
##                jun         : 3876   tue:5954   Mean    : 257.6
##                nov         : 3113   wed:6046   3rd Qu.: 320.0
##                apr         : 1927                Max.    :4199.0
##                (Other): 1458
##      campaign      previous      emp.var.rate      cons.price.idx
## Min.   : 1.000   Min.   :0.0000   Min.   : -3.40000   Min.   :92.20
## 1st Qu.: 1.000   1st Qu.:0.0000   1st Qu.: -1.80000   1st Qu.:93.08
## Median : 2.000   Median :0.0000   Median : 1.10000   Median :93.44
## Mean   : 2.556   Mean    :0.1704   Mean    : 0.08556   Mean    :93.57
## 3rd Qu.: 3.000   3rd Qu.:0.0000   3rd Qu.: 1.40000   3rd Qu.:93.99
## Max.   :43.000   Max.    :6.0000   Max.    : 1.40000   Max.    :94.77
##
## cons.conf.idx      euribor3m      nr.employed      deposit
## Min.   : -50.80   Min.   :0.634   Min.   :4964   Min.   :0.0000
## 1st Qu.: -42.70   1st Qu.:1.344   1st Qu.:5099   1st Qu.:0.0000
## Median : -41.80   Median :4.857   Median :5191   Median :0.0000
```

```

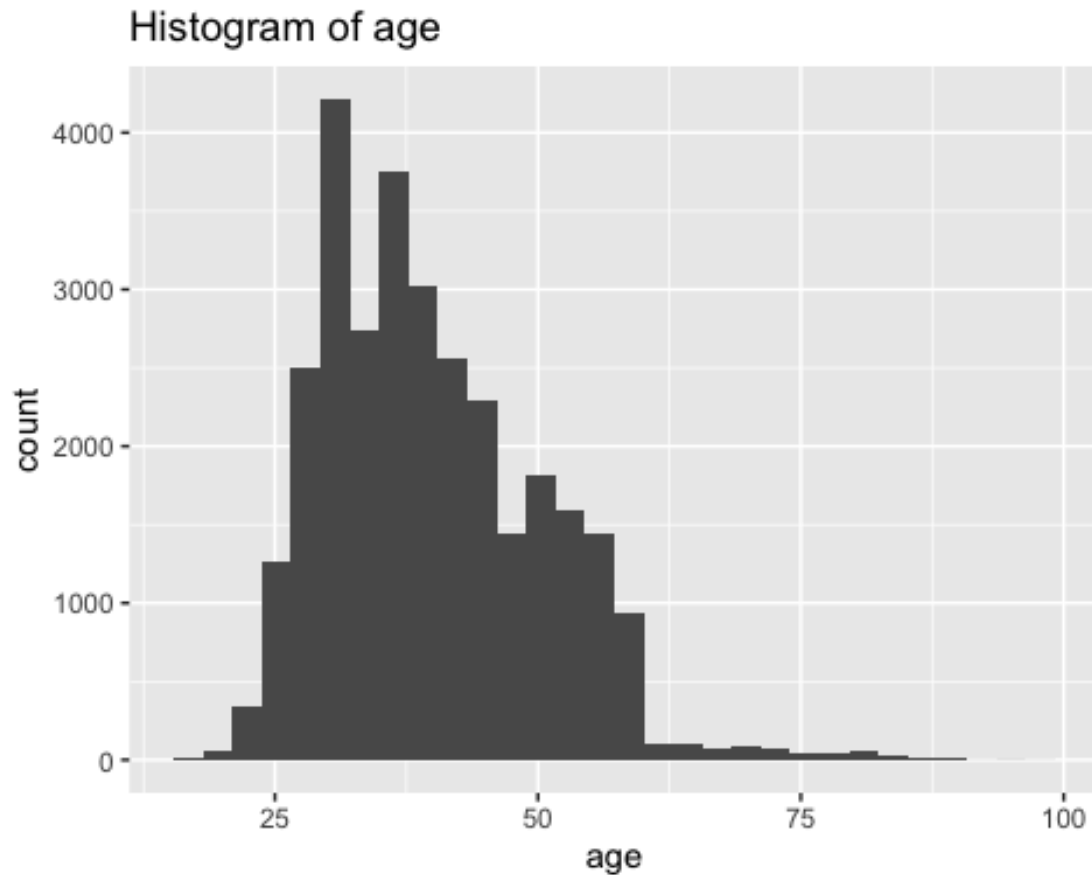
## Mean      :-40.53      Mean      :3.625      Mean      :5167      Mean      :0.1105
## 3rd Qu.   :-36.40      3rd Qu.   :4.961      3rd Qu.   :5228      3rd Qu.   :0.0000
## Max.      :-26.90      Max.       :5.045      Max.       :5228      Max.       :1.0000
##
summary(bankTest)
##          age          job          marital          educatio
n
## Min.      :18.00      admin.      :2000      divorced: 875      basic.4y          : 8
18
## 1st Qu.   :32.00      blue-collar:1704      married  :4583      basic.6y          : 4
18
## Median    :38.00      technician :1263      single   :2191      basic.9y          :11
60
## Mean      :39.87      services   : 715                                high.school       :18
52
## 3rd Qu.   :47.00      management : 554                                illiterate        :
4
## Max.      :98.00      retired    : 328                                professional.course:10
30
##          (Other)      :1085                                university.degree :23
67
## housing loan      telephone      month      day_of_week      duration
## 0:3487  0:6475      0:4924      may      :2561      fri:1432      Min.      : 0.0
## 1:4162  1:1174      1:2725      jul      :1314      mon:1570      1st Qu.   :104.0
##          aug      :1149      thu:1564      Median    :179.0
##          jun      : 970      tue:1527      Mean      :260.8
##          nov      : 785      wed:1556      3rd Qu.   :318.0
##          apr      : 509                                Max.      :4918.0
##          (Other): 361
##          campaign      previous      emp.var.rate      cons.price.idx
## Min.      : 1.000      Min.      :0.0000      Min.      : -3.40000      Min.      :92.20
## 1st Qu.   : 1.000      1st Qu.   :0.0000      1st Qu.   : -1.80000      1st Qu.   :93.08
## Median    : 2.000      Median    :0.0000      Median    : 1.10000      Median    :93.44
## Mean      : 2.611      Mean      :0.1685      Mean      : 0.07205      Mean      :93.57
## 3rd Qu.   : 3.000      3rd Qu.   :0.0000      3rd Qu.   : 1.40000      3rd Qu.   :93.99
## Max.      :42.000      Max.      :7.0000      Max.      : 1.40000      Max.      :94.77
##
## cons.conf.idx      euribor3m      nr.employed      deposit
## Min.      : -50.80      Min.      :0.634      Min.      :4964      Min.      :0.0000
## 1st Qu.   : -42.70      1st Qu.   :1.344      1st Qu.   :5099      1st Qu.   :0.0000
## Median    : -41.80      Median    :4.857      Median    :5191      Median    :0.0000
## Mean      : -40.59      Mean      :3.616      Mean      :5167      Mean      :0.1145
## 3rd Qu.   : -36.40      3rd Qu.   :4.961      3rd Qu.   :5228      3rd Qu.   :0.0000
## Max.      : -26.90      Max.      :5.045      Max.      :5228      Max.      :1.0000
##

```

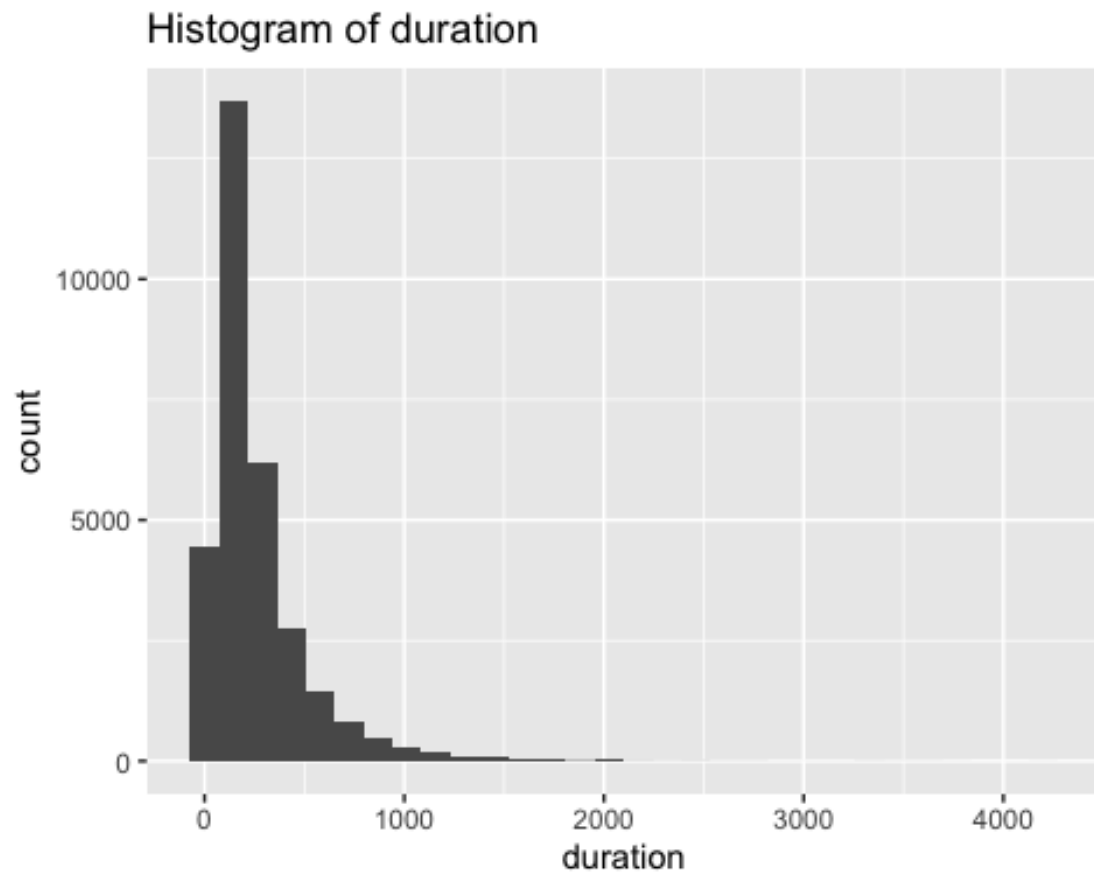
## Histogram showing the distribution

Looking at the summary table, a histogram of age, duration, campaign, previous may be worth looking at since the data seems to be skewed and needs some transformation.

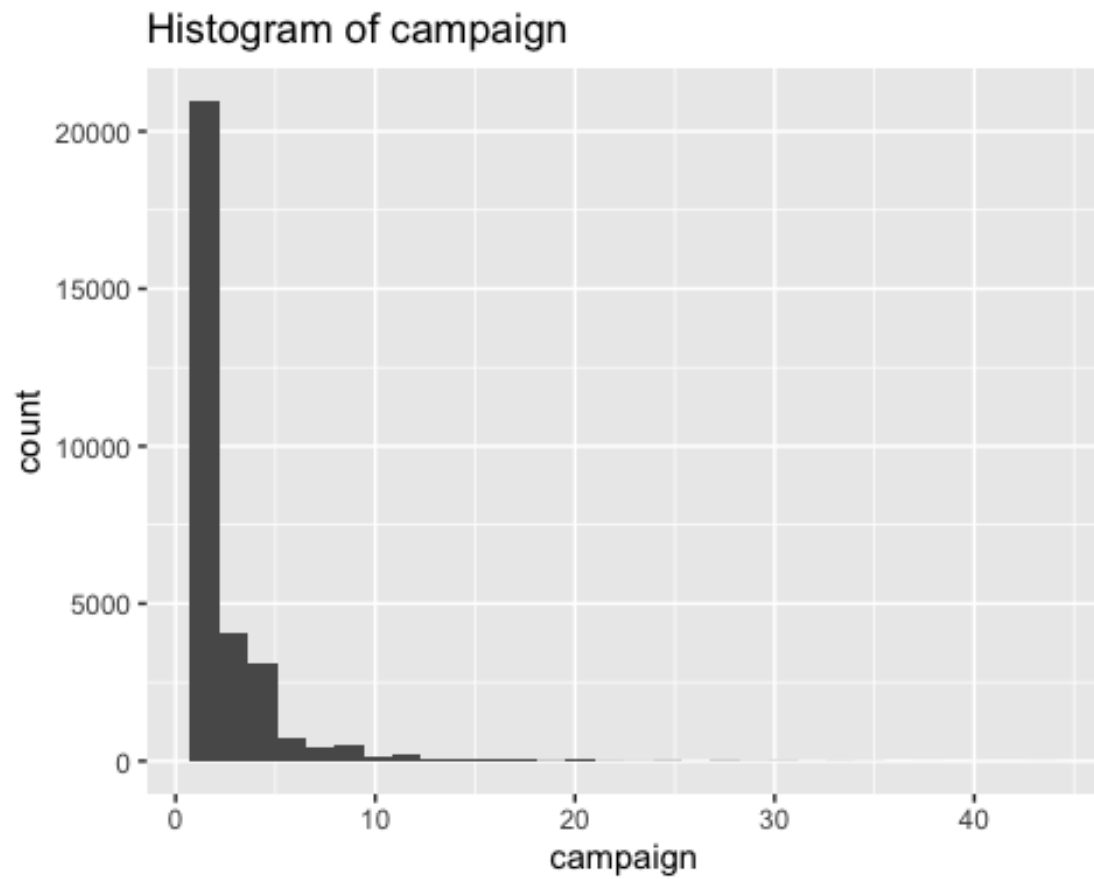
```
bankTrain %>%  
  ggplot(aes(age)) + geom_histogram() +  
  labs(title = "Histogram of age")  
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



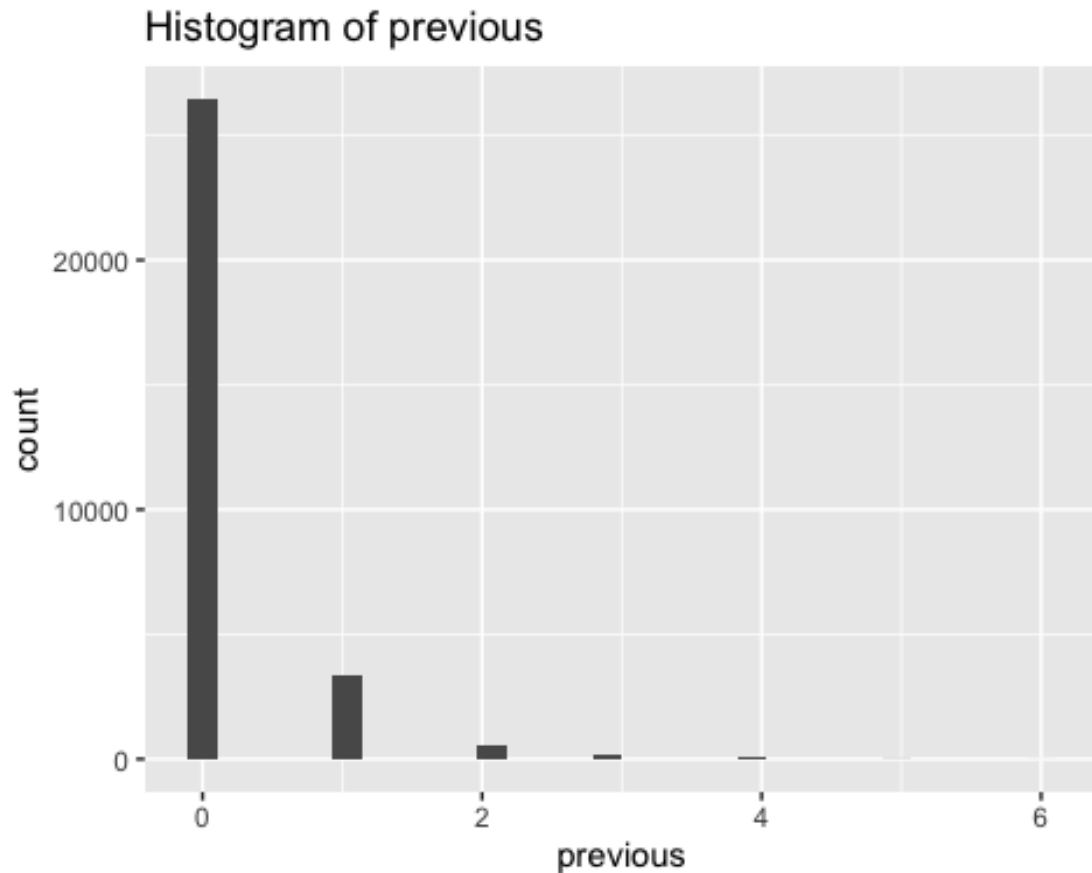
```
bankTrain %>%  
  ggplot(aes(duration)) + geom_histogram() +  
  labs(title = "Histogram of duration")  
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



```
bankTrain %>%  
  ggplot(aes(duration)) + geom_histogram() +  
  labs(title = "Histogram of duration")  
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



```
bankTrain %>%  
  ggplot(aes(previous)) + geom_histogram() +  
  labs(title = "Histogram of previous")  
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



```
table(bankTrain$previous)
```

```
##  
##      0      1      2      3      4      5      6  
## 26451  3386   531   164    50    11     3
```

We will use log transformation on duration and campaign.

```
#log transformation
```

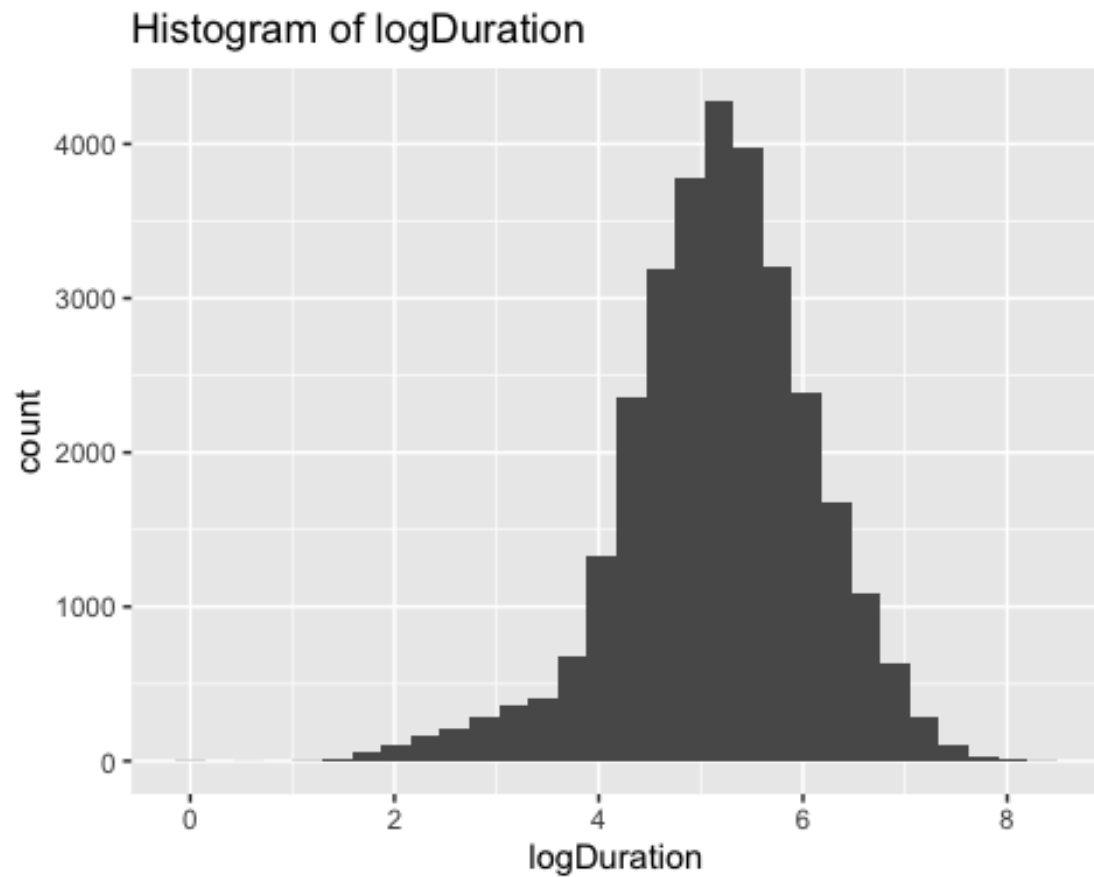
```
bankTrain <- bankTrain %>%  
  mutate(logDuration = log(duration))
```

```
bankTrain <- bankTrain %>%  
  mutate(logCampaign = log(campaign))
```

```
bankTrain %>%  
  ggplot(aes(logDuration)) + geom_histogram() +  
  labs(title = "Histogram of logDuration")
```

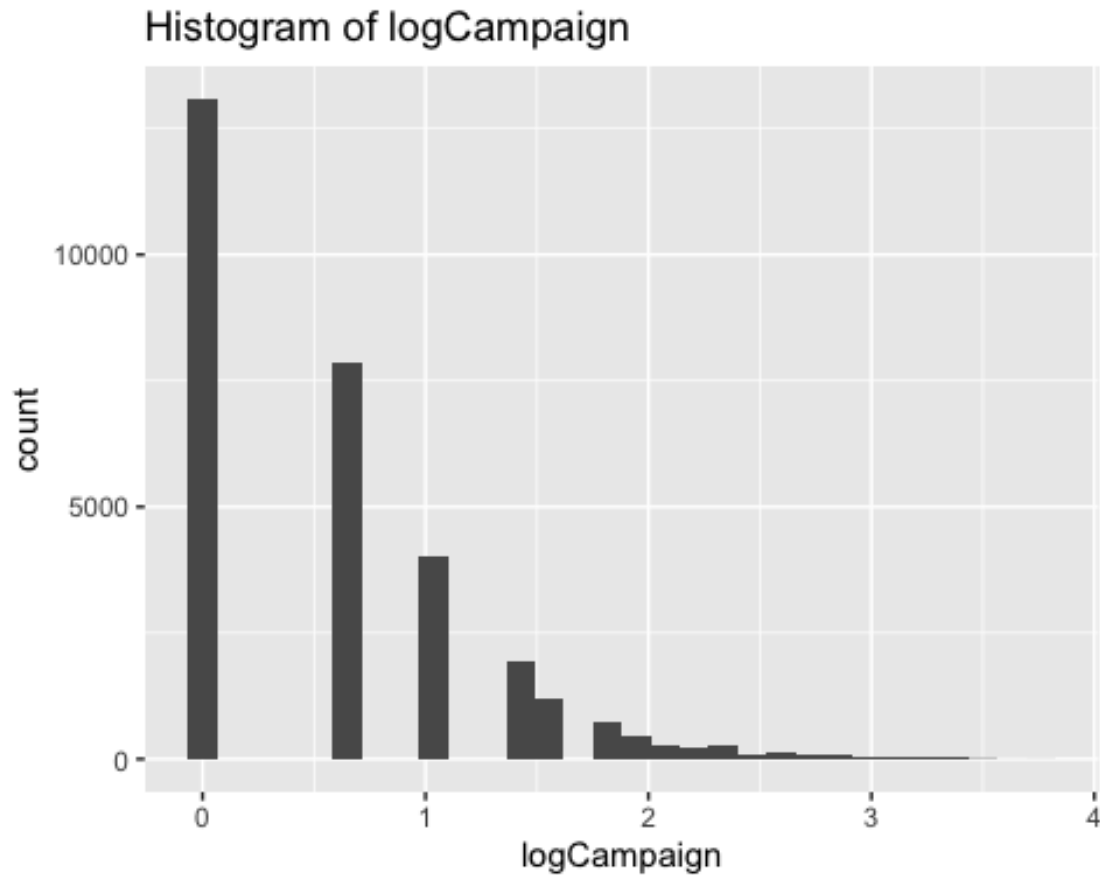
```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

```
## Warning: Removed 2 rows containing non-finite values (stat_bin).
```



```
bankTrain %>%  
  ggplot(aes(logCampaign)) + geom_histogram() +  
  labs(title = "Histogram of logCampaign")  
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```





campaign seems to be worsened off so we may leave it alone instead of taking the log transformation.

```
bankTrain <- bankTrain %>%  
  select(!logCampaign) %>%  
  select(!duration)
```

### Modeling process

```
bankTrain <- bankTrain %>%  
  filter(logDuration != -Inf)
```

```
reg <- glm(deposit ~ ., bankTrain, family = binomial)  
summary(reg)
```

```
##  
## Call:  
## glm(formula = deposit ~ ., family = binomial, data = bankTrain)  
##  
## Deviance Residuals:  
##      Min       1Q   Median       3Q      Max   
## -3.5561  -0.3189  -0.1485  -0.0632   3.7500   
##  
## Coefficients:
```

```

##               Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -2.530e+02  4.478e+01  -5.651 1.59e-08 ***
## age           -2.421e-03  2.850e-03  -0.850 0.395576
## jobblue-collar -2.300e-01  9.211e-02  -2.497 0.012529 *
## jobentrepreneur -1.958e-01  1.453e-01  -1.348 0.177596
## jobhousemaid   -1.132e-01  1.708e-01  -0.663 0.507475
## jobmanagement  -8.614e-03  9.853e-02  -0.087 0.930332
## jobretired      4.055e-01  1.268e-01   3.198 0.001383 **
## jobself-employed -1.192e-01  1.356e-01  -0.879 0.379300
## jobservices    -2.502e-01  1.006e-01  -2.486 0.012911 *
## jobstudent      2.193e-01  1.428e-01   1.536 0.124587
## jobtechnician   2.858e-02  8.226e-02   0.347 0.728259
## jobunemployed   1.060e-01  1.473e-01   0.719 0.471833
## maritalmarried  -8.433e-04  7.851e-02  -0.011 0.991430
## maritalsingle   4.821e-03  9.012e-02   0.053 0.957341
## educationbasic.6y 1.770e-01  1.346e-01   1.315 0.188473
## educationbasic.9y 8.958e-02  1.067e-01   0.840 0.400958
## educationhigh.school 1.414e-01  1.051e-01   1.345 0.178665
## educationilliterate 1.181e+00  8.270e-01   1.428 0.153161
## educationprofessional.course 2.212e-01  1.150e-01   1.923 0.054458 .
## educationuniversity.degree 2.847e-01  1.060e-01   2.686 0.007236 **
## housing1        1.754e-04  4.763e-02   0.004 0.997062
## loan1           -5.632e-02  6.627e-02  -0.850 0.395396
## telephone1      -6.686e-01  9.534e-02  -7.012 2.35e-12 ***
## monthaug         1.193e+00  1.482e-01   8.045 8.60e-16 ***
## monthdec         4.219e-01  2.532e-01   1.666 0.095679 .
## monthjul         3.602e-01  1.144e-01   3.148 0.001643 **
## monthjun        -3.054e-01  1.510e-01  -2.022 0.043135 *
## monthmar         2.478e+00  1.800e-01  13.765 < 2e-16 ***
## monthmay        -3.496e-01  9.853e-02  -3.548 0.000388 ***
## monthnov        -3.442e-01  1.403e-01  -2.454 0.014145 *
## monthoct         4.315e-01  1.804e-01   2.391 0.016794 *
## monthsep         8.618e-01  2.126e-01   4.054 5.04e-05 ***
## day_of_weekmon  -9.379e-02  7.695e-02  -1.219 0.222946
## day_of_weekthu   6.718e-02  7.457e-02   0.901 0.367675
## day_of_weektue    2.946e-02  7.739e-02   0.381 0.703414
## day_of_weekwed    1.707e-01  7.610e-02   2.243 0.024916 *
## campaign        -2.040e-02  1.329e-02  -1.535 0.124803
## previous         1.590e-01  3.948e-02   4.027 5.64e-05 ***
## emp.var.rate    -2.003e+00  1.709e-01 -11.721 < 2e-16 ***
## cons.price.idx   2.342e+00  2.974e-01   7.878 3.34e-15 ***
## cons.conf.idx    2.603e-02  9.512e-03   2.737 0.006208 **
## euribor3m       5.835e-01  1.523e-01   3.830 0.000128 ***
## nr.employed      3.442e-03  3.605e-03   0.955 0.339654
## logDuration      2.235e+00  4.037e-02  55.354 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##

```

```
##      Null deviance: 21272  on 30593  degrees of freedom
## Residual deviance: 12182  on 30550  degrees of freedom
## AIC: 12270
##
## Number of Fisher Scoring iterations: 7
```

We would remove age, job, marital, education, housing, loan, day\_of\_week, campaign, nr.employed

```
reg2 <- glm(deposit ~ telephone + month + previous + emp.var.rate + cons.pric
e.idx + cons.conf.idx + euribor3m + logDuration, bankTrain, family = binomial
)
summary(reg2)

##
## Call:
## glm(formula = deposit ~ telephone + month + previous + emp.var.rate +
##      cons.price.idx + cons.conf.idx + euribor3m + logDuration,
##      family = binomial, data = bankTrain)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -3.5786  -0.3211  -0.1504  -0.0651   3.5965
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -2.180e+02  1.247e+01 -17.482  < 2e-16 ***
## telephone1   -6.623e-01  9.034e-02  -7.332  2.27e-13 ***
## monthaug      1.248e+00  1.325e-01   9.419  < 2e-16 ***
## monthdec      3.976e-01  2.377e-01   1.673  0.094366 .
## monthjul      3.916e-01  1.125e-01   3.482  0.000498 ***
## monthjun     -2.219e-01  1.222e-01  -1.816  0.069418 .
## monthmar      2.465e+00  1.514e-01  16.282  < 2e-16 ***
## monthmay     -4.003e-01  8.953e-02  -4.471  7.77e-06 ***
## monthnov     -3.411e-01  1.252e-01  -2.724  0.006446 **
## monthoct      3.845e-01  1.492e-01   2.577  0.009969 **
## monthsep      8.062e-01  1.612e-01   5.002  5.68e-07 ***
## previous      1.597e-01  3.938e-02   4.055  5.02e-05 ***
## emp.var.rate  -1.957e+00  1.369e-01 -14.303  < 2e-16 ***
## cons.price.idx 2.153e+00  1.291e-01  16.676  < 2e-16 ***
## cons.conf.idx  2.292e-02  6.733e-03   3.405  0.000662 ***
## euribor3m     7.030e-01  1.035e-01   6.794  1.09e-11 ***
## logDuration   2.223e+00  4.009e-02  55.456  < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 21272  on 30593  degrees of freedom
## Residual deviance: 12267  on 30577  degrees of freedom
```

```
## AIC: 12301
##
## Number of Fisher Scoring iterations: 7

lrm(deposit ~ telephone + month + previous + emp.var.rate + cons.price.idx +
cons.conf.idx + euribor3m + logDuration, bankTrain)

## Logistic Regression Model
##
## lrm(formula = deposit ~ telephone + month + previous + emp.var.rate +
##      cons.price.idx + cons.conf.idx + euribor3m + logDuration,
##      data = bankTrain)
##
##
##              Model Likelihood      Discrimination      Rank Discrim
##
##              Ratio Test              Indexes              Indexe
s
## Obs          30594      LR chi2    9005.42      R2          0.509      C          0.93
3
## 0            27212      d.f.         16      g            2.764      Dxy         0.86
6
## 1            3382      Pr(> chi2) <0.0001      gr          15.870      gamma      0.86
6
## max |deriv| 1e-09              gp            0.165      tau-a      0.17
0
##
##              Brier      0.063
##
##              Coef      S.E.      Wald Z Pr(>|Z|)
## Intercept      -218.0026 12.4701 -17.48 <0.0001
## telephone=1     -0.6623  0.0903  -7.33 <0.0001
## month=aug        1.2484  0.1325   9.42 <0.0001
## month=dec        0.3976  0.2377   1.67 0.0944
## month=jul        0.3916  0.1125   3.48 0.0005
## month=jun       -0.2219  0.1222  -1.82 0.0694
## month=mar        2.4646  0.1514  16.28 <0.0001
## month=may       -0.4003  0.0895  -4.47 <0.0001
## month=nov       -0.3411  0.1252  -2.72 0.0064
## month=oct        0.3845  0.1492   2.58 0.0100
## month=sep        0.8062  0.1612   5.00 <0.0001
## previous         0.1597  0.0394   4.05 <0.0001
## emp.var.rate    -1.9575  0.1369 -14.30 <0.0001
## cons.price.idx   2.1529  0.1291  16.68 <0.0001
## cons.conf.idx    0.0229  0.0067   3.40 0.0007
## euribor3m        0.7030  0.1035   6.79 <0.0001
## logDuration      2.2232  0.0401  55.46 <0.0001
##
```

We will remove month because some of the p-values of its categories aren't statistically significant.

```

reg3 <- glm(deposit ~ telephone + previous + emp.var.rate + cons.price.idx +
euribor3m + cons.conf.idx + logDuration, bankTrain, family = binomial)
summary(reg3)

##
## Call:
## glm(formula = deposit ~ telephone + previous + emp.var.rate +
##      cons.price.idx + euribor3m + cons.conf.idx + logDuration,
##      family = binomial, data = bankTrain)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -3.1289  -0.3441  -0.1633  -0.0712   3.7512
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -1.646e+02  7.453e+00 -22.080  < 2e-16 ***
## telephone1   -1.146e+00  7.148e-02 -16.026  < 2e-16 ***
## previous      1.411e-01  3.773e-02   3.739 0.000185 ***
## emp.var.rate  -1.045e+00  7.954e-02 -13.133  < 2e-16 ***
## cons.price.idx 1.647e+00  7.786e-02  21.149  < 2e-16 ***
## euribor3m     3.723e-02  6.222e-02   0.598 0.549589
## cons.conf.idx  9.261e-02  4.803e-03  19.284  < 2e-16 ***
## logDuration    2.124e+00  3.839e-02  55.336  < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 21272  on 30593  degrees of freedom
## Residual deviance: 12803  on 30586  degrees of freedom
## AIC: 12819
##
## Number of Fisher Scoring iterations: 7

lrm(deposit ~ telephone + previous + emp.var.rate + cons.price.idx + euribor3
m + cons.conf.idx + logDuration, bankTrain)

## Logistic Regression Model
##
## lrm(formula = deposit ~ telephone + previous + emp.var.rate +
##      cons.price.idx + euribor3m + cons.conf.idx + logDuration,
##      data = bankTrain)
##
##
##              Model Likelihood      Discrimination      Rank Discrim
##              Ratio Test              Indexes              Indexe
## s
## Obs          30594      LR chi2      8469.29      R2          0.483      C          0.92
## 2

```

```
##      0      27212      d.f.      7      g      2.655      Dxy      0.84
3
##      1      3382      Pr(> chi2) <0.0001      gr      14.231      gamma      0.84
3
## max |deriv| 1e-09      gp      0.161      tau-a      0.16
6
##
##      Brier      0.064
##
##      Coef      S.E.      Wald Z      Pr(>|Z|)
## Intercept      -164.5669      7.4532      -22.08      <0.0001
## telephone=1      -1.1456      0.0715      -16.03      <0.0001
## previous      0.1411      0.0377      3.74      0.0002
## emp.var.rate      -1.0447      0.0795      -13.13      <0.0001
## cons.price.idx      1.6467      0.0779      21.15      <0.0001
## euribor3m      0.0372      0.0622      0.60      0.5496
## cons.conf.idx      0.0926      0.0048      19.28      <0.0001
## logDuration      2.1243      0.0384      55.34      <0.0001
##
```

Also, remove euribor3m.

```
reg4 <- glm(deposit ~ telephone + previous + emp.var.rate + cons.price.idx +
cons.conf.idx + logDuration, bankTrain, family = binomial)
summary(reg4)

##
## Call:
## glm(formula = deposit ~ telephone + previous + emp.var.rate +
##      cons.price.idx + cons.conf.idx + logDuration, family = binomial,
##      data = bankTrain)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -3.1344  -0.3443  -0.1632  -0.0712   3.7661
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -1.618e+02  5.781e+00 -27.982  < 2e-16 ***
## telephone1   -1.134e+00  6.899e-02 -16.444  < 2e-16 ***
## previous      1.376e-01  3.729e-02   3.691 0.000223 ***
## emp.var.rate  -9.994e-01  2.418e-02 -41.330  < 2e-16 ***
## cons.price.idx 1.619e+00  6.193e-02  26.134  < 2e-16 ***
## cons.conf.idx  9.366e-02  4.468e-03  20.963  < 2e-16 ***
## logDuration    2.124e+00  3.838e-02  55.336  < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 21272  on 30593  degrees of freedom
```

```
## Residual deviance: 12803  on 30587  degrees of freedom
## AIC: 12817
##
## Number of Fisher Scoring iterations: 7

lrm(deposit ~ telephone + previous + emp.var.rate + cons.price.idx + cons.conf.idx + logDuration, bankTrain)

## Logistic Regression Model
##
## lrm(formula = deposit ~ telephone + previous + emp.var.rate +
##      cons.price.idx + cons.conf.idx + logDuration, data = bankTrain)
##
##
##              Model Likelihood      Discrimination      Rank Discrim
.
##              Ratio Test              Indexes              Indexe
s
## Obs          30594      LR chi2      8468.93      R2          0.483      C          0.92
2
## 0            27212      d.f.          6      g            2.655      Dxy          0.84
3
## 1            3382      Pr(> chi2) <0.0001      gr          14.221      gamma          0.84
3
## max |deriv| 2e-09              gp            0.161      tau-a          0.16
6
##              Brier            0.064
##
##              Coef      S.E.      Wald Z Pr(>|Z|)
## Intercept      -161.7572  5.7807  -27.98 <0.0001
## telephone=1     -1.1345  0.0690  -16.44 <0.0001
## previous         0.1376  0.0373   3.69 0.0002
## emp.var.rate     -0.9994  0.0242  -41.33 <0.0001
## cons.price.idx    1.6185  0.0619  26.13 <0.0001
## cons.conf.idx     0.0937  0.0045  20.96 <0.0001
## logDuration       2.1239  0.0384  55.34 <0.0001
##

# Drop-in deviance tests

pchisq(21272-12182,43,lower.tail = FALSE)

## [1] 0

pchisq(21272-12267,16,lower.tail = FALSE)

## [1] 0

pchisq(21272-12803,7,lower.tail = FALSE)

## [1] 0

pchisq(21272-12803,6,lower.tail = FALSE)
```

```
## [1] 0
```

We will have to now consider moving forward with one of the models. We should definitely eliminate model 1 as it has too many variables with statistically insignificant p-values. We should also eliminate model 3 because euribor3m has a statistically insignificant p-values. We are left with model 2 and 4. The drop-in deviance tests yield 0 for all models, indicating that the probability of getting a larger or equal drop-in deviance is also statistically significant (lower than 0.05). This indicates that it's hard to have a larger or equal drop-in deviance. Thus, our models are adequate. They are significantly better than the null model, explaining a larger amount of variation of deposit.

Since the drop-in deviance test doesn't point out which model is better, we will take a look at the residual deviance, and the Dxy.

```
lrm(deposit ~ telephone + month + previous + emp.var.rate + cons.price.idx +
cons.conf.idx + euribor3m + logDuration, bankTrain)

## Logistic Regression Model
##
## lrm(formula = deposit ~ telephone + month + previous + emp.var.rate +
##      cons.price.idx + cons.conf.idx + euribor3m + logDuration,
##      data = bankTrain)
##
##              Model Likelihood      Discrimination      Rank Discrim
##              Ratio Test              Indexes              Indexe
s
## Obs          30594      LR chi2      9005.42      R2          0.509      C          0.93
3
## 0            27212      d.f.          16          g          2.764      Dxy        0.86
6
## 1            3382      Pr(> chi2) <0.0001      gr          15.870      gamma     0.86
6
## max |deriv| 1e-09              gp          0.165      tau-a     0.17
0
##              Brier      0.063
##
##              Coef      S.E.      Wald Z Pr(>|Z|)
## Intercept      -218.0026 12.4701 -17.48 <0.0001
## telephone=1     -0.6623  0.0903  -7.33 <0.0001
## month=aug        1.2484  0.1325   9.42 <0.0001
## month=dec        0.3976  0.2377   1.67 0.0944
## month=jul        0.3916  0.1125   3.48 0.0005
## month=jun       -0.2219  0.1222  -1.82 0.0694
## month=mar        2.4646  0.1514 16.28 <0.0001
## month=may       -0.4003  0.0895  -4.47 <0.0001
## month=nov       -0.3411  0.1252  -2.72 0.0064
## month=oct        0.3845  0.1492   2.58 0.0100
## month=sep        0.8062  0.1612   5.00 <0.0001
## previous        0.1597  0.0394   4.05 <0.0001
```



```
## emp.var.rate      -1.9575  0.1369 -14.30 <0.0001
## cons.price.idx    2.1529  0.1291  16.68 <0.0001
## cons.conf.idx     0.0229  0.0067   3.40 0.0007
## euribor3m         0.7030  0.1035   6.79 <0.0001
## logDuration       2.2232  0.0401  55.46 <0.0001
##

lrm(deposit ~ telephone + previous + emp.var.rate + cons.price.idx + cons.conf.idx + logDuration, bankTrain)

## Logistic Regression Model
##
## lrm(formula = deposit ~ telephone + previous + emp.var.rate +
##      cons.price.idx + cons.conf.idx + logDuration, data = bankTrain)
##
##              Model Likelihood    Discrimination    Rank Discrim
.
##              Ratio Test              Indexes              Indexe
s
## Obs          30594    LR chi2    8468.93    R2        0.483    C        0.92
2
## 0            27212    d.f.          6    g          2.655    Dxy      0.84
3
## 1             3382    Pr(> chi2) <0.0001    gr        14.221    gamma    0.84
3
## max |deriv| 2e-09              gp          0.161    tau-a    0.16
6
##              Brier    0.064
##
##      Coef      S.E.    Wald Z Pr(>|Z|)
## Intercept    -161.7572  5.7807 -27.98 <0.0001
## telephone=1   -1.1345  0.0690 -16.44 <0.0001
## previous       0.1376  0.0373   3.69 0.0002
## emp.var.rate   -0.9994  0.0242 -41.33 <0.0001
## cons.price.idx  1.6185  0.0619  26.13 <0.0001
## cons.conf.idx   0.0937  0.0045  20.96 <0.0001
## logDuration    2.1239  0.0384  55.34 <0.0001
##
```

Clearly, model 2 has a smaller residual deviance (12267) compared to model 4 (12803). Model 2 also has a larger Dxy than model 4, 0.866 compared to 0.843. This means that model 2 fits the data more than model 4, and the variables in model 2 are more significant. The only concern we have is that some of the month is not significant. We may convert month into different Bernoulli variables and eliminate those that are not significant or we may run a drop-in deviance test for month to see if it offers a greater model than the null model.

```
# Drop-in deviance test for month
pchisq(12803-12267,16-7,lower.tail = FALSE)
```

```
## [1] 1.115819e-109
```

It appears that month is quite significant since the drop-in test yields  $1.11 \cdot 10^{-109}$  as the p-value. After some experiment, we realize that using august as the baseline would make all the p-values significant. This can happen due to the fact that the monthaug may affect deposit different from other months a lot.

```
bankTrain$month <- relevel(bankTrain$month, ref = "aug")
reg5 <- glm(deposit ~ telephone + month + previous + emp.var.rate + cons.pric
e.idx + cons.conf.idx + euribor3m + logDuration, bankTrain, family = binomial
)
summary(reg5)
```

```
##
## Call:
## glm(formula = deposit ~ telephone + month + previous + emp.var.rate +
##      cons.price.idx + cons.conf.idx + euribor3m + logDuration,
##      family = binomial, data = bankTrain)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -3.5786  -0.3211  -0.1504  -0.0651   3.5965
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -2.168e+02  1.242e+01 -17.447  < 2e-16 ***
## telephone1    -6.623e-01  9.034e-02  -7.332  2.27e-13 ***
## monthapr      -1.248e+00  1.325e-01  -9.419  < 2e-16 ***
## monthdec      -8.508e-01  2.381e-01  -3.574  0.000352 ***
## monthjul      -8.568e-01  1.180e-01  -7.258  3.92e-13 ***
## monthjun      -1.470e+00  1.599e-01  -9.196  < 2e-16 ***
## monthmar       1.216e+00  1.551e-01   7.841  4.48e-15 ***
## monthmay      -1.649e+00  1.089e-01 -15.145  < 2e-16 ***
## monthnov      -1.590e+00  1.446e-01 -10.996  < 2e-16 ***
## monthoct      -8.639e-01  1.584e-01  -5.453  4.96e-08 ***
## monthsep      -4.422e-01  1.532e-01  -2.886  0.003900 **
## previous       1.597e-01  3.938e-02   4.055  5.02e-05 ***
## emp.var.rate  -1.957e+00  1.369e-01 -14.303  < 2e-16 ***
## cons.price.idx  2.153e+00  1.291e-01  16.676  < 2e-16 ***
## cons.conf.idx  2.292e-02  6.733e-03   3.405  0.000662 ***
## euribor3m      7.030e-01  1.035e-01   6.794  1.09e-11 ***
## logDuration    2.223e+00  4.009e-02  55.456  < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 21272  on 30593  degrees of freedom
## Residual deviance: 12267  on 30577  degrees of freedom
## AIC: 12301
```

```
##
## Number of Fisher Scoring iterations: 7

lrm(deposit ~ telephone + month + previous + emp.var.rate + cons.price.idx +
cons.conf.idx + euribor3m + logDuration, bankTrain)

## Logistic Regression Model
##
## lrm(formula = deposit ~ telephone + month + previous + emp.var.rate +
##      cons.price.idx + cons.conf.idx + euribor3m + logDuration,
##      data = bankTrain)
##
##
##              Model Likelihood      Discrimination      Rank Discrim
.
##              Ratio Test              Indexes              Indexe
s
## Obs          30594      LR chi2      9005.42      R2          0.509      C          0.93
3
## 0            27212      d.f.          16      g            2.764      Dxy          0.86
6
## 1            3382      Pr(> chi2) <0.0001      gr          15.870      gamma        0.86
6
## max |deriv| 1e-09              gp            0.165      tau-a        0.17
0
##
##              Brier      0.063
##
##              Coef      S.E.      Wald Z Pr(>|Z|)
## Intercept      -216.7542 12.4238 -17.45 <0.0001
## telephone=1     -0.6623  0.0903  -7.33 <0.0001
## month=apr        -1.2484  0.1325  -9.42 <0.0001
## month=dec        -0.8508  0.2381  -3.57 0.0004
## month=jul        -0.8568  0.1180  -7.26 <0.0001
## month=jun        -1.4703  0.1599  -9.20 <0.0001
## month=mar         1.2161  0.1551   7.84 <0.0001
## month=may        -1.6488  0.1089 -15.15 <0.0001
## month=nov        -1.5895  0.1445 -11.00 <0.0001
## month=oct        -0.8639  0.1584  -5.45 <0.0001
## month=sep        -0.4422  0.1532  -2.89 0.0039
## previous         0.1597  0.0394   4.05 <0.0001
## emp.var.rate     -1.9575  0.1369 -14.30 <0.0001
## cons.price.idx    2.1529  0.1291  16.68 <0.0001
## cons.conf.idx     0.0229  0.0067   3.40 0.0007
## euribor3m         0.7030  0.1035   6.79 <0.0001
## logDuration       2.2232  0.0401  55.46 <0.0001
##
```

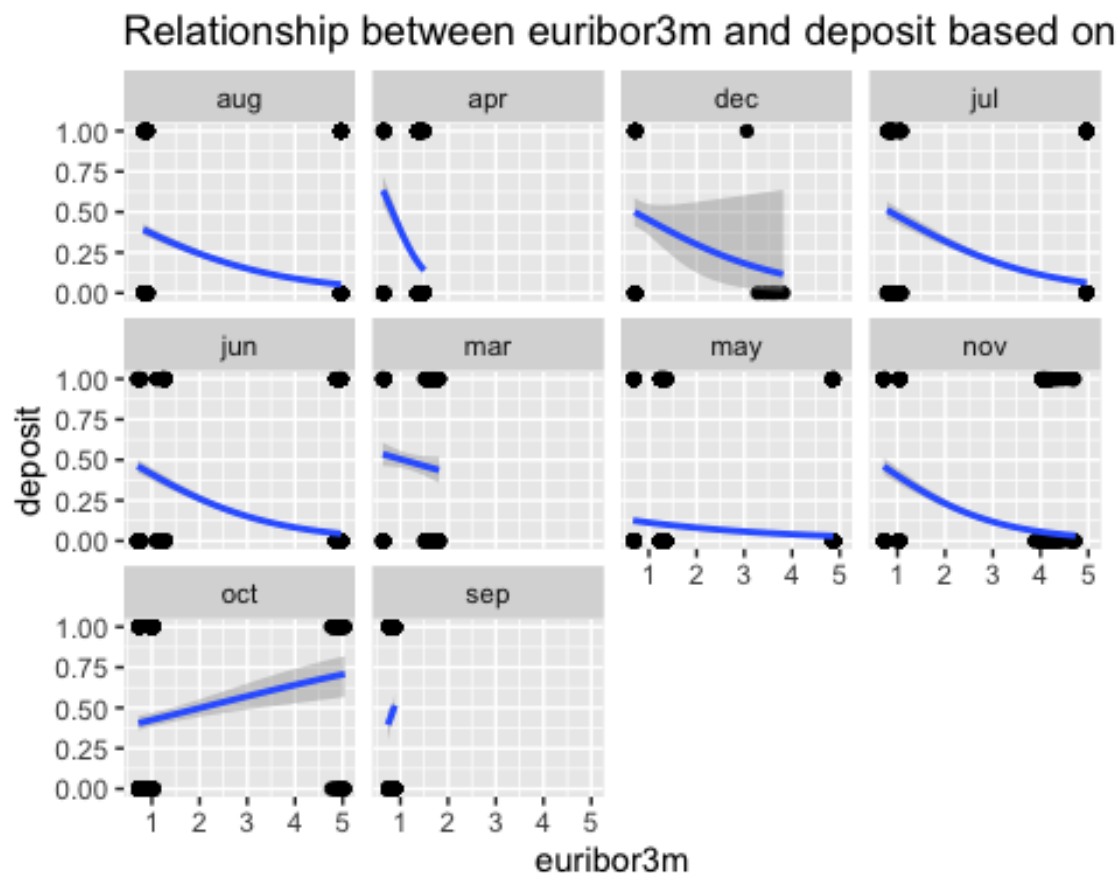
We will move forward with model 2 and try to improve the model by adding interaction terms.

## Interaction Terms

Since when we remove month, euribor3m is also affected a lot, we will try an interaction term between month and euribor3m.

```
bankTrain %>%
  ggplot(aes(euribor3m, deposit)) + geom_point() +
  stat_smooth(method = "glm", method.args = list(family = "binomial")) +
  facet_wrap(~month) +
  labs(title = "Relationship between euribor3m and deposit based on month")

## `geom_smooth()` using formula 'y ~ x'
```



```
reg6 <- glm(deposit ~ telephone + month + previous + emp.var.rate + cons.pric
e.idx + cons.conf.idx + euribor3m + logDuration + month*euribor3m, bankTrain,
family = binomial)
summary(reg6)

##
## Call:
## glm(formula = deposit ~ telephone + month + previous + emp.var.rate +
##     cons.price.idx + cons.conf.idx + euribor3m + logDuration +
##     month * euribor3m, family = binomial, data = bankTrain)
##
```

```

## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -4.0986  -0.3117  -0.1434  -0.0614   3.5207
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -194.43155    19.41146  -10.016 < 2e-16 ***
## telephone1     -0.49594     0.10055   -4.932 8.12e-07 ***
## monthapr        0.96046     0.49553    1.938 0.052594 .
## monthdec       -1.93622     0.47475   -4.078 4.53e-05 ***
## monthjul       -0.46212     0.23329   -1.981 0.047611 *
## monthjun       -0.27596     0.25487   -1.083 0.278927
## monthmar       -0.71979     0.40586   -1.774 0.076145 .
## monthmay       -0.53290     0.22848   -2.332 0.019684 *
## monthnov       -0.86790     0.24884   -3.488 0.000487 ***
## monthoct       -1.71380     0.20999   -8.161 3.31e-16 ***
## monthsep       -5.56421     2.51206   -2.215 0.026760 *
## previous        0.16019     0.03967    4.038 5.39e-05 ***
## emp.var.rate   -1.52489     0.23337   -6.534 6.39e-11 ***
## cons.price.idx  1.94062     0.20144    9.634 < 2e-16 ***
## cons.conf.idx   0.07708     0.01183    6.515 7.28e-11 ***
## euribor3m       0.43797     0.19249    2.275 0.022885 *
## logDuration     2.27451     0.04097   55.511 < 2e-16 ***
## monthapr:euribor3m -1.08968     0.40155   -2.714 0.006654 **
## monthdec:euribor3m  1.91503     0.50571    3.787 0.000153 ***
## monthjul:euribor3m -0.01630     0.05112   -0.319 0.749770
## monthjun:euribor3m -0.22983     0.05471   -4.201 2.66e-05 ***
## monthmar:euribor3m  2.17512     0.35015    6.212 5.23e-10 ***
## monthmay:euribor3m -0.28014     0.07477   -3.747 0.000179 ***
## monthnov:euribor3m -0.06484     0.06480   -1.001 0.317035
## monthoct:euribor3m  1.10094     0.14615    7.533 4.96e-14 ***
## monthsep:euribor3m  6.33062     2.99808    2.112 0.034724 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 21272  on 30593  degrees of freedom
## Residual deviance: 12031  on 30568  degrees of freedom
## AIC: 12083
##
## Number of Fisher Scoring iterations: 7

lrm(deposit ~ telephone + month + previous + emp.var.rate + cons.price.idx +
cons.conf.idx + euribor3m + logDuration + month*euribor3m + campaign, bankTra
in, maxit=1000)

## Logistic Regression Model
##
## lrm(formula = deposit ~ telephone + month + previous + emp.var.rate +

```

```

##      cons.price.idx + cons.conf.idx + euribor3m + logDuration +
##      month * euribor3m + campaign, data = bankTrain, maxit = 1000)
##
##              Model Likelihood      Discrimination      Rank Discrim
.
##              Ratio Test              Indexes              Indexe
s
##  Obs          30594      LR chi2      9244.03      R2          0.520      C          0.93
6
##    0          27212      d.f.          26      g          2.845      Dxy          0.87
2
##    1          3382      Pr(> chi2) <0.0001      gr          17.202      gamma          0.87
2
##  max |deriv| 3e-09              gp          0.166      tau-a          0.17
1
##
##              Brier          0.061
##
##              Coef          S.E.      Wald Z Pr(>|Z|)
##  Intercept          -194.0849  19.4093 -10.00 <0.0001
##  telephone=1          -0.4820   0.1009  -4.77 <0.0001
##  month=apr           0.9683   0.4961   1.95 0.0509
##  month=dec          -1.9110   0.4752  -4.02 <0.0001
##  month=jul          -0.4505   0.2335  -1.93 0.0537
##  month=jun          -0.2720   0.2549  -1.07 0.2858
##  month=mar          -0.7321   0.4061  -1.80 0.0714
##  month=may          -0.5236   0.2285  -2.29 0.0219
##  month=nov          -0.8586   0.2490  -3.45 0.0006
##  month=oct          -1.7078   0.2101  -8.13 <0.0001
##  month=sep          -5.5972   2.5127  -2.23 0.0259
##  previous           0.1596   0.0397   4.02 <0.0001
##  emp.var.rate       -1.5179   0.2334  -6.50 <0.0001
##  cons.price.idx       1.9374   0.2014   9.62 <0.0001
##  cons.conf.idx       0.0772   0.0118   6.52 <0.0001
##  euribor3m          0.4369   0.1925   2.27 0.0232
##  logDuration         2.2770   0.0410  55.49 <0.0001
##  campaign           -0.0238   0.0135  -1.76 0.0777
##  month=apr * euribor3m -1.0970   0.4019  -2.73 0.0063
##  month=dec * euribor3m  1.8950   0.5061   3.74 0.0002
##  month=jul * euribor3m -0.0179   0.0511  -0.35 0.7265
##  month=jun * euribor3m -0.2319   0.0547  -4.24 <0.0001
##  month=mar * euribor3m  2.1917   0.3504   6.25 <0.0001
##  month=may * euribor3m -0.2856   0.0748  -3.82 0.0001
##  month=nov * euribor3m -0.0699   0.0649  -1.08 0.2816
##  month=oct * euribor3m  1.0920   0.1463   7.46 <0.0001
##  month=sep * euribor3m  6.3707   2.9988   2.12 0.0336
##

```

Most p-values are statistically significant ( $< 0.05$ ), and Dxy increases from 0.866 to 0.872 so we would move forward with this model.

## Adding one more variable

Looking back at the first model, we realize that higher education (professional.course and university.degree) is actually quite significant. We would try to create a dummy variable for higher education

```
table(bankTrain$education)

##
##           basic.4y           basic.6y           basic.9y           high.s
chool
##           3184           1786           4695
7392
##           illiterate professional.course   university.degree
##           14           4070           9453

bankTrain <- bankTrain %>%
  mutate(higherEd = ifelse(education == "professional.course" | education ==
"university.degree", 1 ,0))

reg6 <- glm(deposit ~ telephone + previous + emp.var.rate + cons.price.idx +
cons.conf.idx + logDuration + month*euribor3m + higherEd, bankTrain, family =
binomial)
summary(reg6)

##
## Call:
## glm(formula = deposit ~ telephone + previous + emp.var.rate +
##       cons.price.idx + cons.conf.idx + logDuration + month * euribor3m +
##       higherEd, family = binomial, data = bankTrain)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -4.1241  -0.3106  -0.1434  -0.0606   3.4987
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -1.926e+02  1.942e+01  -9.914  < 2e-16 ***
## telephone1    -4.998e-01  1.006e-01  -4.968  6.78e-07 ***
## previous       1.606e-01  3.971e-02   4.045  5.24e-05 ***
## emp.var.rate   -1.506e+00  2.334e-01  -6.451  1.11e-10 ***
## cons.price.idx  1.920e+00  2.016e-01   9.522  < 2e-16 ***
## cons.conf.idx   7.659e-02  1.184e-02   6.471  9.74e-11 ***
## logDuration    2.278e+00  4.103e-02  55.523  < 2e-16 ***
## monthapr       9.520e-01  4.959e-01   1.920  0.054884 .
## monthdec      -1.909e+00  4.776e-01  -3.997  6.42e-05 ***
## monthjul       -4.581e-01  2.331e-01  -1.966  0.049351 *
## monthjun       -2.874e-01  2.547e-01  -1.128  0.259281
## monthmar       -7.295e-01  4.060e-01  -1.797  0.072347 .
## monthmay      -5.148e-01  2.286e-01  -2.252  0.024325 *
```

```
## monthnov          -8.559e-01  2.489e-01  -3.439 0.000585 ***
## monthoct          -1.697e+00  2.101e-01  -8.076 6.70e-16 ***
## monthsep          -5.287e+00  2.519e+00  -2.099 0.035806 *
## euribor3m          4.183e-01  1.925e-01   2.173 0.029756 *
## higherEd           1.903e-01  4.867e-02   3.911 9.20e-05 ***
## monthapr:euribor3m -1.067e+00  4.019e-01  -2.655 0.007932 **
## monthdec:euribor3m  1.899e+00  5.104e-01   3.721 0.000199 ***
## monthjul:euribor3m -4.836e-03  5.116e-02  -0.095 0.924686
## monthjun:euribor3m -2.111e-01  5.493e-02  -3.843 0.000122 ***
## monthmar:euribor3m  2.174e+00  3.502e-01   6.208 5.35e-10 ***
## monthmay:euribor3m -2.673e-01  7.488e-02  -3.570 0.000357 ***
## monthnov:euribor3m -6.019e-02  6.483e-02  -0.928 0.353176
## monthoct:euribor3m  1.112e+00  1.461e-01   7.610 2.75e-14 ***
## monthsep:euribor3m  6.002e+00  3.005e+00   1.997 0.045817 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 21272  on 30593  degrees of freedom
## Residual deviance: 12016  on 30567  degrees of freedom
## AIC: 12070
##
## Number of Fisher Scoring iterations: 7

lrm <- lrm(deposit ~ telephone + previous + emp.var.rate + cons.price.idx +
cons.conf.idx + logDuration + month*euribor3m + higherEd, bankTrain, maxit =
1000)
```

Most p-values are statistically significant (lower than 0.05), and Dxy increases from 0.872 to 0.873 so we will decide on using this model

```
summary(reg6)

##
## Call:
## glm(formula = deposit ~ telephone + previous + emp.var.rate +
##      cons.price.idx + cons.conf.idx + logDuration + month * euribor3m +
##      higherEd, family = binomial, data = bankTrain)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -4.1241  -0.3106  -0.1434  -0.0606   3.4987
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -1.926e+02  1.942e+01  -9.914  < 2e-16 ***
## telephone1   -4.998e-01  1.006e-01  -4.968 6.78e-07 ***
## previous      1.606e-01  3.971e-02   4.045 5.24e-05 ***
## emp.var.rate  -1.506e+00  2.334e-01  -6.451 1.11e-10 ***
## cons.price.idx  1.920e+00  2.016e-01   9.522  < 2e-16 ***
```



```

## cons.conf.idx      7.659e-02  1.184e-02   6.471 9.74e-11 ***
## logDuration        2.278e+00  4.103e-02  55.523 < 2e-16 ***
## monthapr           9.520e-01  4.959e-01   1.920 0.054884 .
## monthdec          -1.909e+00  4.776e-01  -3.997 6.42e-05 ***
## monthjul          -4.581e-01  2.331e-01  -1.966 0.049351 *
## monthjun          -2.874e-01  2.547e-01  -1.128 0.259281
## monthmar          -7.295e-01  4.060e-01  -1.797 0.072347 .
## monthmay          -5.148e-01  2.286e-01  -2.252 0.024325 *
## monthnov          -8.559e-01  2.489e-01  -3.439 0.000585 ***
## monthoct          -1.697e+00  2.101e-01  -8.076 6.70e-16 ***
## monthsep          -5.287e+00  2.519e+00  -2.099 0.035806 *
## euribor3m          4.183e-01  1.925e-01   2.173 0.029756 *
## higherEd           1.903e-01  4.867e-02   3.911 9.20e-05 ***
## monthapr:euribor3m -1.067e+00  4.019e-01  -2.655 0.007932 **
## monthdec:euribor3m  1.899e+00  5.104e-01   3.721 0.000199 ***
## monthjul:euribor3m -4.836e-03  5.116e-02  -0.095 0.924686
## monthjun:euribor3m -2.111e-01  5.493e-02  -3.843 0.000122 ***
## monthmar:euribor3m  2.174e+00  3.502e-01   6.208 5.35e-10 ***
## monthmay:euribor3m -2.673e-01  7.488e-02  -3.570 0.000357 ***
## monthnov:euribor3m -6.019e-02  6.483e-02  -0.928 0.353176
## monthoct:euribor3m  1.112e+00  1.461e-01   7.610 2.75e-14 ***
## monthsep:euribor3m  6.002e+00  3.005e+00   1.997 0.045817 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##    Null deviance: 21272  on 30593  degrees of freedom
## Residual deviance: 12016  on 30567  degrees of freedom
## AIC: 12070
##
## Number of Fisher Scoring iterations: 7

lrn

## Logistic Regression Model
##
## lrm(formula = deposit ~ telephone + previous + emp.var.rate +
##      cons.price.idx + cons.conf.idx + logDuration + month * euribor3m +
##      higherEd, data = bankTrain, maxit = 1000)
##
##
##              Model Likelihood      Discrimination      Rank Discrim
.
##              Ratio Test              Indexes              Indexe
s
## Obs          30594      LR chi2      9256.08      R2          0.521      C          0.93
6
## 0            27212      d.f.          26          g          2.838      Dxy          0.87
3
## 1            3382      Pr(> chi2) <0.0001      gr          17.079      gamma          0.87

```

```

3
## max |deriv| 8e-10          gp          0.166      tau-a    0.17
2
##          Brier    0.061
##
##          Coef      S.E.    Wald Z Pr(>|Z|)
## Intercept      -192.5782 19.4250 -9.91 <0.0001
## telephone=1     -0.4998  0.1006 -4.97 <0.0001
## previous         0.1606  0.0397  4.04 <0.0001
## emp.var.rate    -1.5057  0.2334 -6.45 <0.0001
## cons.price.idx   1.9197  0.2016  9.52 <0.0001
## cons.conf.idx    0.0766  0.0118  6.47 <0.0001
## logDuration      2.2783  0.0410 55.52 <0.0001
## month=apr        0.9520  0.4959  1.92 0.0549
## month=dec       -1.9087  0.4776 -4.00 <0.0001
## month=jul       -0.4581  0.2331 -1.97 0.0494
## month=jun       -0.2874  0.2547 -1.13 0.2593
## month=mar       -0.7295  0.4060 -1.80 0.0723
## month=may       -0.5148  0.2286 -2.25 0.0243
## month=nov       -0.8559  0.2489 -3.44 0.0006
## month=oct       -1.6968  0.2101 -8.08 <0.0001
## month=sep       -5.2871  2.5187 -2.10 0.0358
## euribor3m       0.4183  0.1925  2.17 0.0298
## higherEd        0.1904  0.0487  3.91 <0.0001
## month=apr * euribor3m -1.0669  0.4019 -2.65 0.0079
## month=dec * euribor3m  1.8990  0.5104  3.72 0.0002
## month=jul * euribor3m -0.0048  0.0512 -0.09 0.9247
## month=jun * euribor3m -0.2111  0.0549 -3.84 0.0001
## month=mar * euribor3m  2.1740  0.3502  6.21 <0.0001
## month=may * euribor3m -0.2673  0.0749 -3.57 0.0004
## month=nov * euribor3m -0.0602  0.0648 -0.93 0.3532
## month=oct * euribor3m  1.1122  0.1461  7.61 <0.0001
## month=sep * euribor3m  6.0021  3.0055  2.00 0.0458
##

```

## Interpretation:

According to the logistic regression model, we have:

- When all variables equal 0 and it's August, the log odds of deposit is -192.5782, and the probability of the customer subscribing to the term deposit is  $3.54 \cdot 10^{-84}$ , indicating that the customer will not deposit.
- telephone: A shift from using cell phone to telephone is associated with a decrease in the log odds of deposit by 0.4998 units, indicating that if the call method is telephone instead of cell phone, the odds of getting the customers to deposit go down by 1.65 times (or 165%). This makes sense as the dataset also include calls of which customers contact the help center. There will be people who need help and will be frustrated if they don't get what they need immediately but some introduction to a term deposit that they don't care

about instead. Using cellphone will also create a sense of personal relationship between the caller and the customer instead of a sense of being a part of just a telemarketing campaign.

- previous: When previous increases by 1, the log odds of deposit increases by 0.16 units, indicating that the odds of successfully having customers deposit go up by 1.17 times (or 117%). As mentioned above in the variable description, previous means number of contacts performed before this campaign and for this client so the more contacts are performed before, the more experience and familiarity the telemarketing team will possess and hence will persuade the customers better.

- emp.var.rate: When emp.var.rate increases by 1, the log odds of deposit decreases by -1.5057 units, indicating that the odds of successfully having customers deposit go down by 4.51 times (or 451%). emp.var.rate measures the variation of employment rate. High emp.var.rate indicates an unstable economy.

- cons.price.idx: When cons.price.idx increases by 1, the log odds of deposit increases by 1.92 units, indicating that the odds of successfully having customers deposit go up by 6.82 times (or 682%). Higher cons.price.idx means higher inflation rate -> higher nominal interest rate so it makes sense that the higher the cons.price.idx, the higher chance the customers want to subscribe to a term deposit.

- cons.conf.idx: When cons.conf.idx increases by 1, the log odds of deposit increases by 0.0766 units, indicating that the odds of successfully having customers deposit go up by 1.08 times (or 108%). It makes sense that the higher the consumer confidence level is, the higher chance they want to subscribe to a term deposit.

- euribor3m: When euribor3m increases by 1, the log odds of deposit increases by 0.4183 units, indicating that the odds of successfully having customers deposit go up by 1.52 times (or 152%). euribor3m is the average interest rates from a panel of large European banks that are used for lending to one another.

- logDuration: When logDuration increases by 1, the log odds of deposit increases by 2.2783 units, indicating that the odds of successfully having customers deposit go up by 9.76 times (or 976%). This makes sense since normally, if customers receive a call that they don't care about, they will try to end the call as soon as possible. Longer duration also indicates that the company has more time to persuade the customer to subscribe to the term deposit.

- higherEd: A shift from having high education level to not having high education level is associated with an increase in the log odds of deposit by 0.1904 units, indicating that if the customer has university degree or professional courses, the odds of getting the customers to deposit go up by 1.21 times (or 121%).

- month: Of all the months, December, September and October are associated with a decrease in the log odds of deposit. This might indicate that customers tend to keep money by themselves or use it at the end of the year.

- C is 0.936. This indicates that 93.6% of pairs of 0 and 1 fit the model (0.5->1 - random guessing).

- Dxy is 0.873. This is a rescale of C to make it range from 0 to 1 instead of 0.5 to 1. 0.873 is still a good number. This model explains about 87.3% of our data.

## Validate the model

### Drop-in deviance test

```
pchisq(21272 - 12016, 27, lower.tail = FALSE)

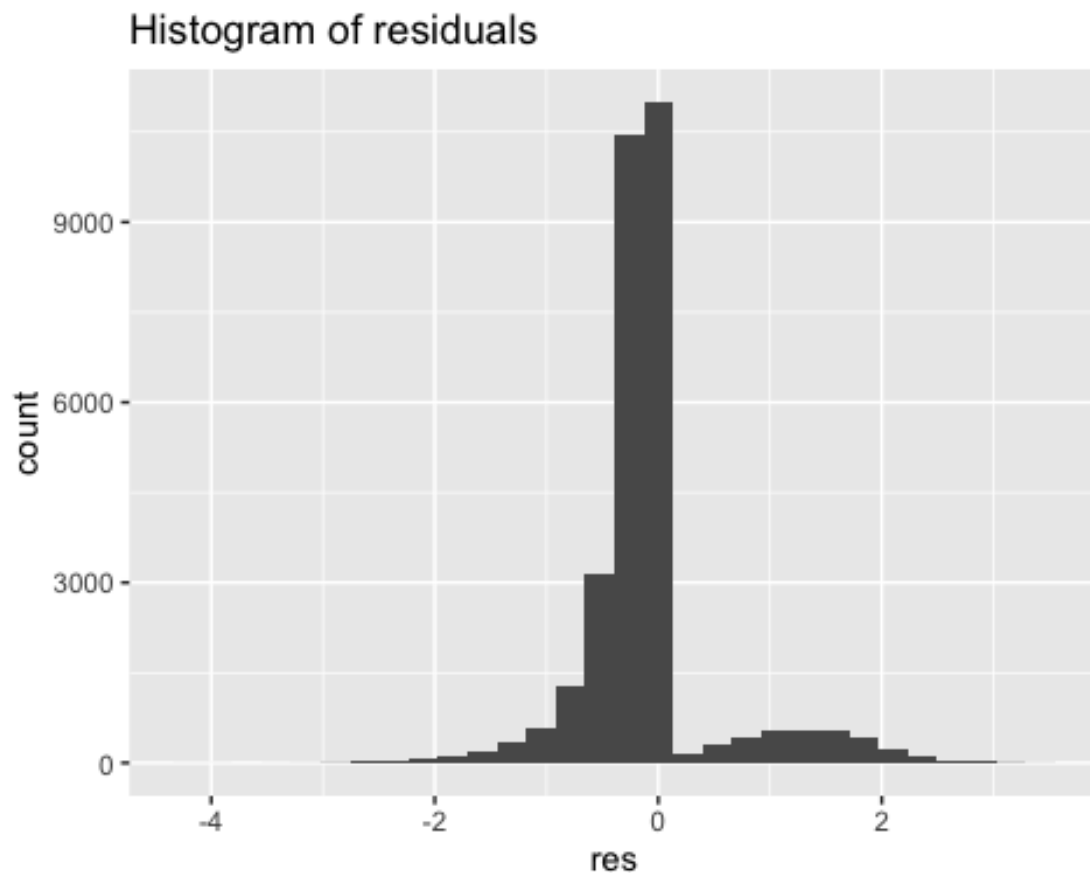
## [1] 0
```

The drop-in deviance tests yield 0, indicating that the probability of getting a larger or equal drop-in deviance is also statistically significant (lower than 0.05). This indicates that it's hard to have a larger or equal drop-in deviance. Thus, our model is adequate. This is significantly better than the null model, explaining a larger amount of variation of deposit.

### Check for binormality and normal distribution

```
bankTrain2 <- bankTrain %>%
  mutate(res = resid(reg6), fit = fitted(reg6))
bankTrain2 %>% ggplot(aes(res)) + geom_histogram() + labs(title = "Histogram
of residuals")

## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



The histogram of residual is unbalanced. This may be due to the unbalanced dataset that we have (more 'no' than 'yes' for deposit). However, the distribution still centers at 0 so this is still acceptable. We will also run the Hosmer-Lem test to check for binormality.

```
hoslem.test(bankTrain2$deposit, bankTrain2$fit, g=3000)
```

```
##  
## Hosmer and Lemeshow goodness of fit (GOF) test  
##  
## data: bankTrain2$deposit, bankTrain2$fit  
## X-squared = 2891.9, df = 2998, p-value = 0.9159
```

We change the number of bins to 3000 to fit the size of the dataset. The p-value is 0.9159. It is not statistically significant (higher than 0.05) so we fail to reject the null hypothesis that if we break our residuals into bins, each bin has a binormal distribution.

## Prediction

### Random Prediction

We will start with predicting 3 random observations from the test set

```
bankTest2 <- bankTest %>%  
  mutate(logDuration = log(duration)) %>%  
  mutate(higherEd = ifelse(education == "professional.course" | education ==  
"university.degree", 1, 0)) %>%  
  filter(logDuration != -Inf)  
  
set.seed(4)  
N <- seq(7649)  
random <- sample(N, 3)  
bankTestPt <- bankTest2[random, ]  
  
bankTestPt <- bankTestPt %>%  
  mutate(result = 0)  
bankTestPt[1, 'result'] <- predict(reg6, bankTestPt[1,], type = "response")  
bankTestPt[2, 'result'] <- predict(reg6, bankTestPt[2,], type = "response")  
bankTestPt[3, 'result'] <- predict(reg6, bankTestPt[3,], type = "response")  
bankTestPt %>%  
  dplyr::select(deposit, result)  
  
## # A tibble: 3 × 2  
##   deposit result  
##   <dbl> <dbl>  
## 1      1 0.271  
## 2      0 0.0109  
## 3      0 0.0621
```

The result when the actual deposit is 1 is quite higher than the results when the actual deposits are 0 but still not high enough. We will make some calculations to better assess the result.

### Recall, Precision, Accuracy

```
bankTest3 <- bankTest2 %>%
  mutate(predict = predict(reg6, bankTest2, type = "response")) %>%
  mutate(predictDeposit = ifelse(predict < 0.5, 0, 1))

N <- seq(nrow(bankTest3))

for (i in N) {
  if ((bankTest3[i, 'predictDeposit'] == 0) && (bankTest3[i, 'deposit'] == 1)) {
    bankTest3[i, 'result'] = "FN"
  }
  else if ((bankTest3[i, 'predictDeposit'] == 1) && (bankTest3[i, 'deposit'] == 1)) {
    bankTest3[i, 'result'] = "TP"
  }
  else if ((bankTest3[i, 'predictDeposit'] == 1) && (bankTest3[i, 'deposit'] == 0)) {
    bankTest3[i, 'result'] = "FP"
  }
  else {
    bankTest3[i, 'result'] = "TN"
  }
}

FN <- sum(bankTest3$result == "FN")
FP <- sum(bankTest3$result == "FP")
TN <- sum(bankTest3$result == "TN")
TP <- sum(bankTest3$result == "TP")
recall <- TP/(TP + FN)
precision <- TP/(TP + FP)
accuracy <- (TP + TN)/(FP + FN + TP + TN)

recall
## [1] 0.4383562

precision
## [1] 0.6748682

accuracy
## [1] 0.9114685
```

- Recall: From all the customers subscribe to the term deposit, we predict 43.8% of them.

- Precision: From all the customers we predict that they subscribe, 67.4% of them actually do.
- Accuracy: From all predictions, 91.14% is correct.

## **F. Final Thoughts**

### **1. Some suggestions to the bank in Portugal**

- Bank should look at the economy of the country before launching a telemarketing campaign
- They should also train their telemarketing team to handle different type of calls appropriately
- Avoid the end of the year for telemarketing campaigns
- They might also aim their campaign at customers who have higher education levels

### **2. Future work**

- We have an unbalanced dataset => oversampling undersampling methods to get more reliable results
- Analyze whether or not we can apply this model to other similar-size banks in Portugal