

Honey and wine

2D correlation spectroscopy

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Singapore Synchrotron Light Source

24.02.2021

① Introduction

② Classic Visualization

③ Multivariate Statistics

④ Correlation Matrix

⑤ 2D Correlation Spectroscopy

⑥ Summary



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PCA and HCA
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Correlation Matrix
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1 Experiment

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- ▶ FTIR spectrometer
- ▶ mid-IR range
- ▶ ATR accessory
- ▶ liquid samples

- ▶ macro-driven experiment
- ▶ sets of spectra with time-stamp in filename



1 Sample: Propolis

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- ▶ derived from Greek to mean defense for *pro* and city or community for *polis*
- ▶ *bee glue* for sealing holes and cracks and for the reconstruction of the beehive and smoothing the inner surface of the beehive, preventing invasion by predators
- ▶ composed mainly of resin (50%), wax (30%), essential oils (10%), pollen (5%), and other organic compounds (5%) (phenolic compounds, esters, flavonoids, terpenes, beta-steroids, aromatic aldehydes, and alcohols)
- ▶ contains also important vitamins (B1, B2, B6, C and E) and useful minerals (Mg, Ca, K, Na, Cu, Zn, Mn and Fe)
- ▶ numerous applications in treating various diseases due to its antiseptic, anti-inflammatory, antioxidant, antibacterial, antimycotic, antifungal, antiulcer and anticancer



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② Classic Visualization

All Spectra

Wavenumbers time dependence

③ Multivariate Statistics

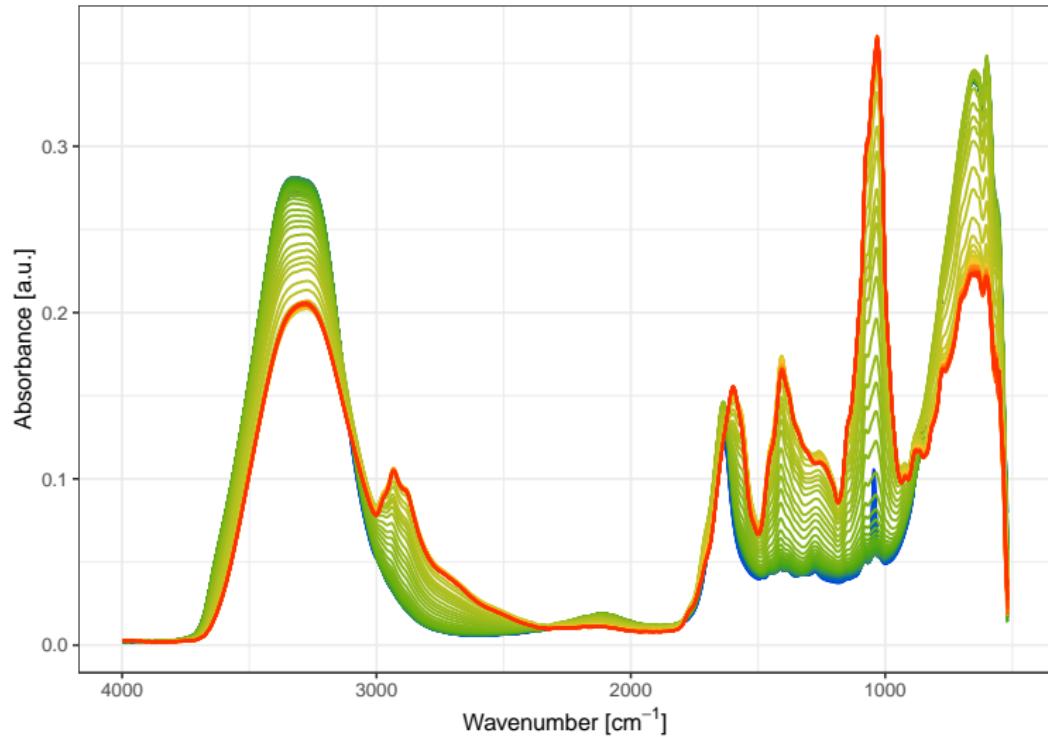
④ Correlation Matrix

⑤ 2D Correlation Spectroscopy



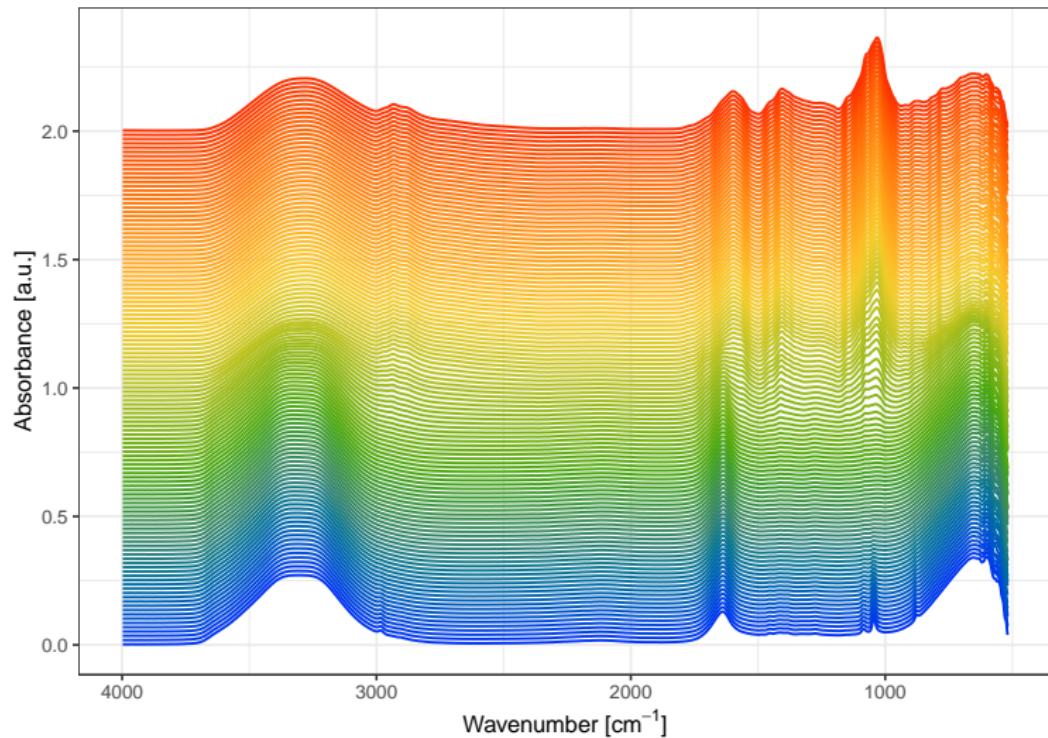
2 All spectra: from blue to red

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2 All spectra with shift

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PCA and HCA
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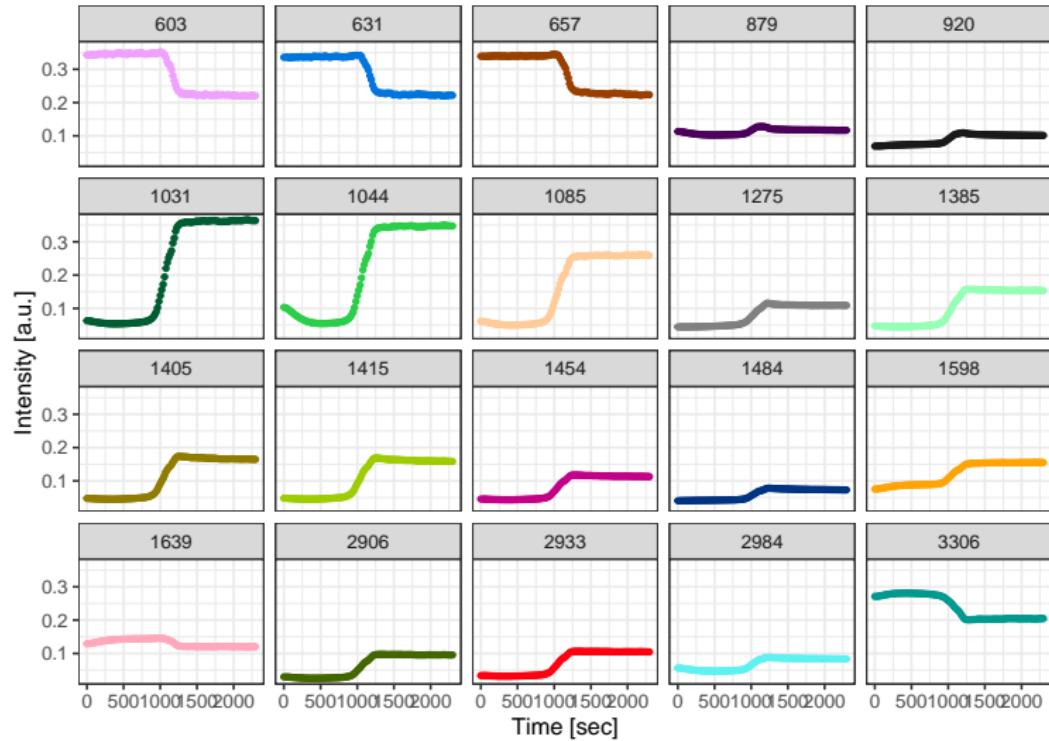
Correlation Matrix
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2D Correlation
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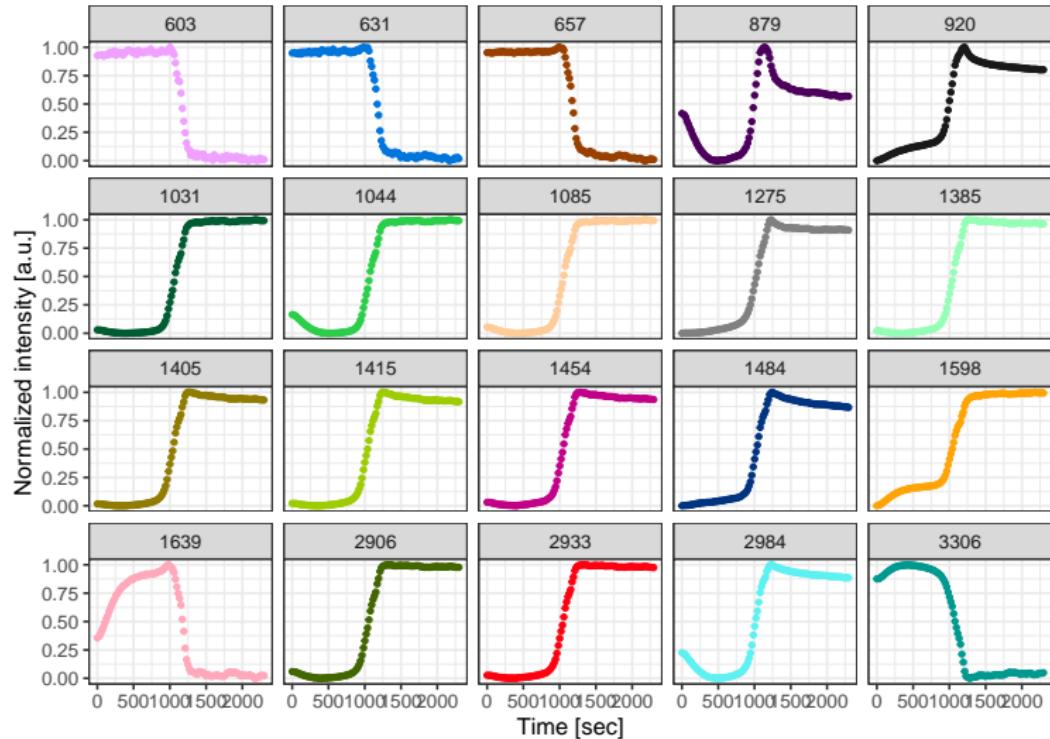
2 Raw Spectra

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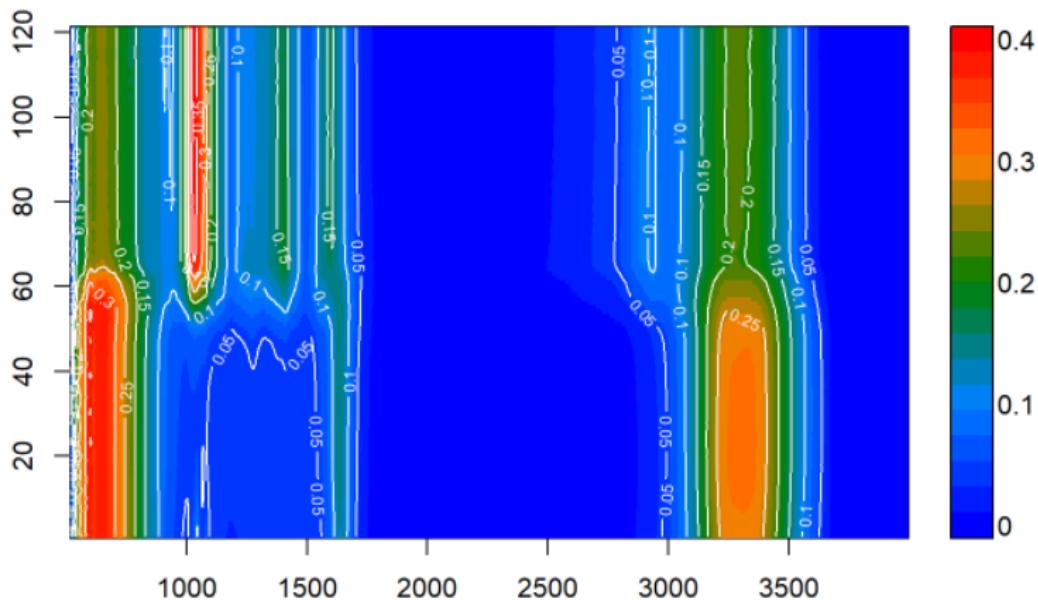
2 Normalized Spectra

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2 Level plot

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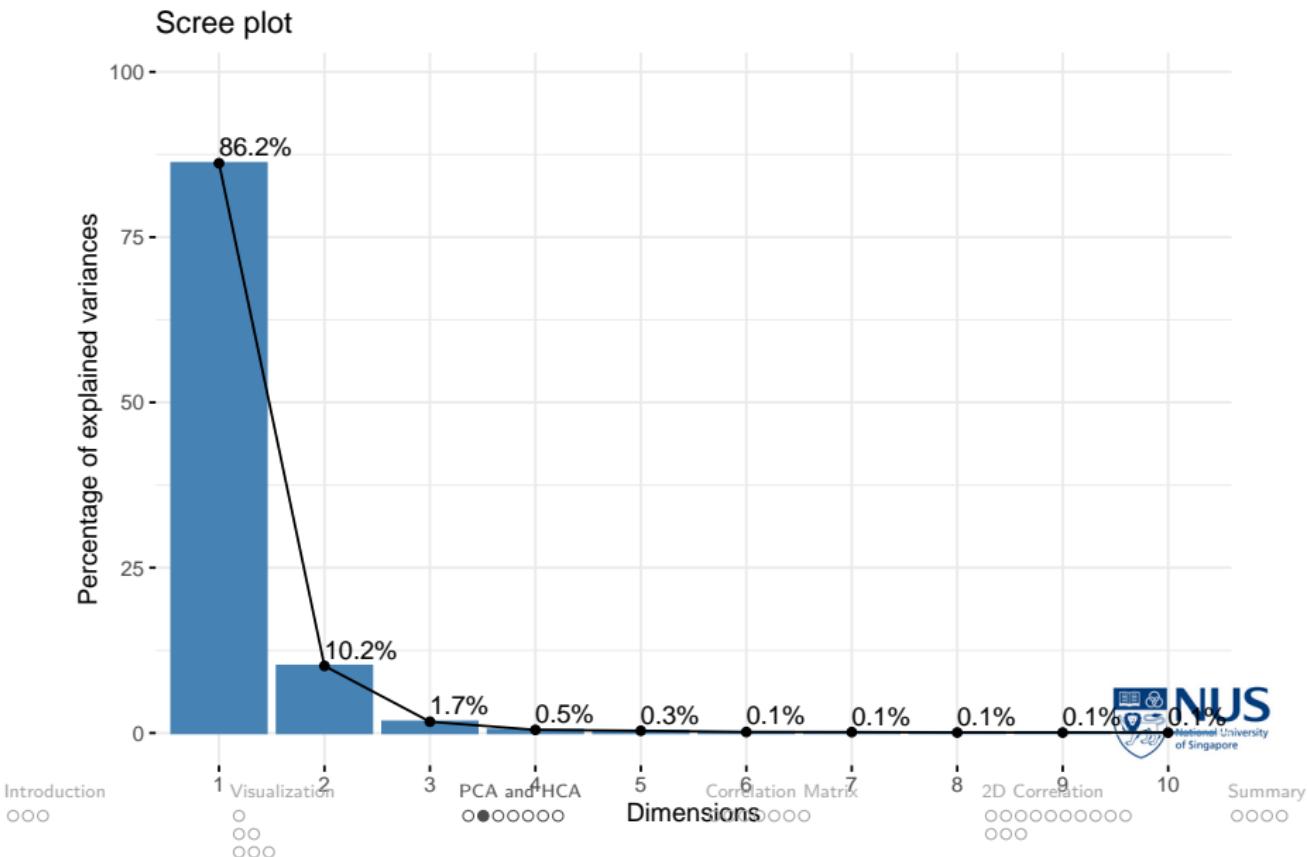
2D Correlation
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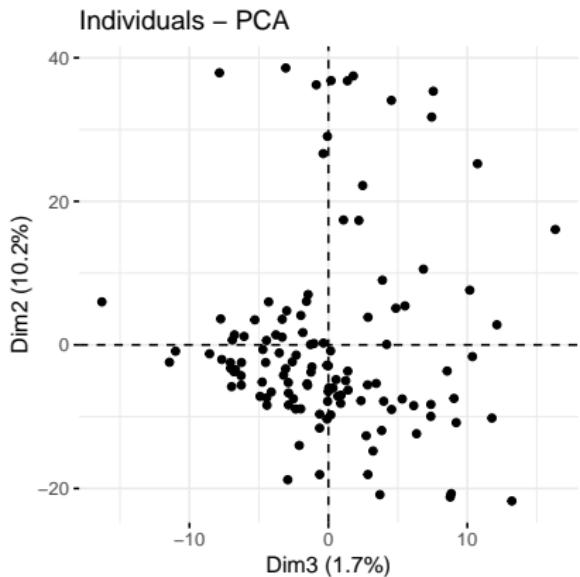
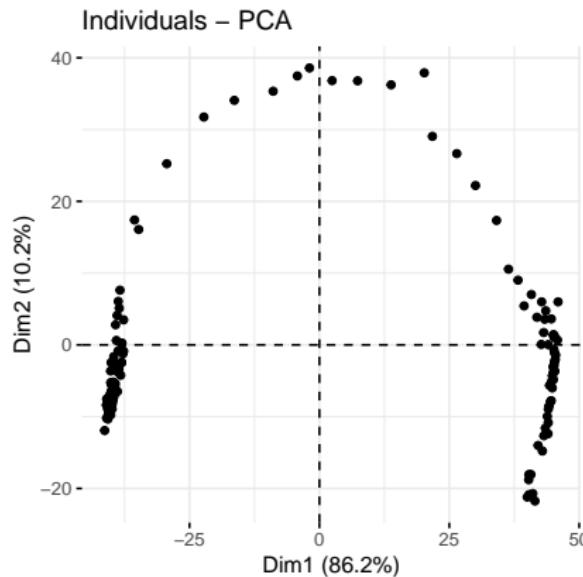
3 PCA Screeplot

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3 PCA Scoreplots

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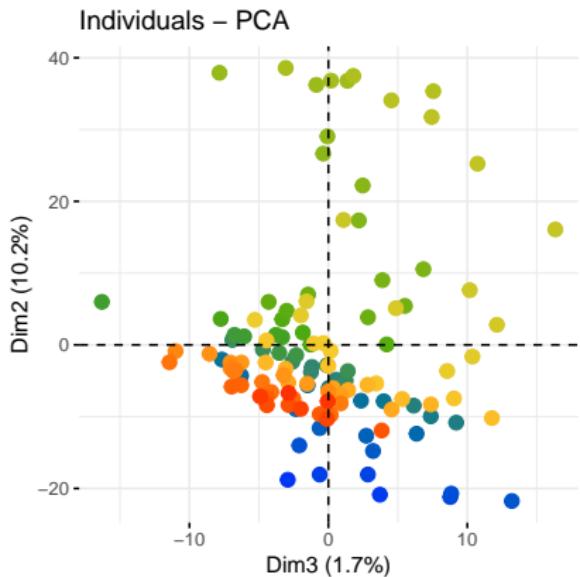
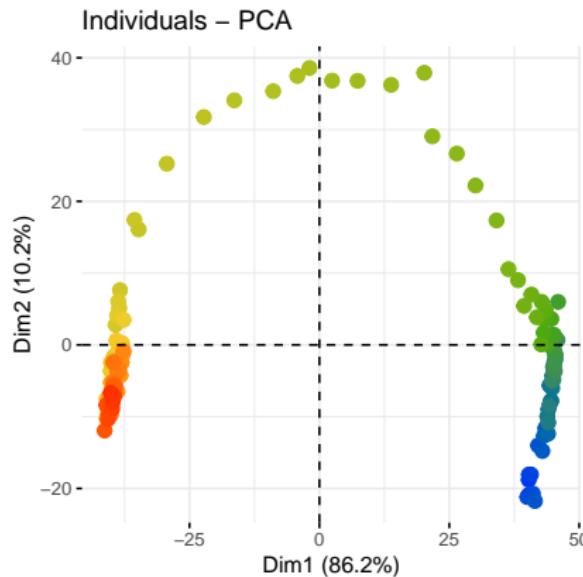
Correlation Matrix
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2D Correlation
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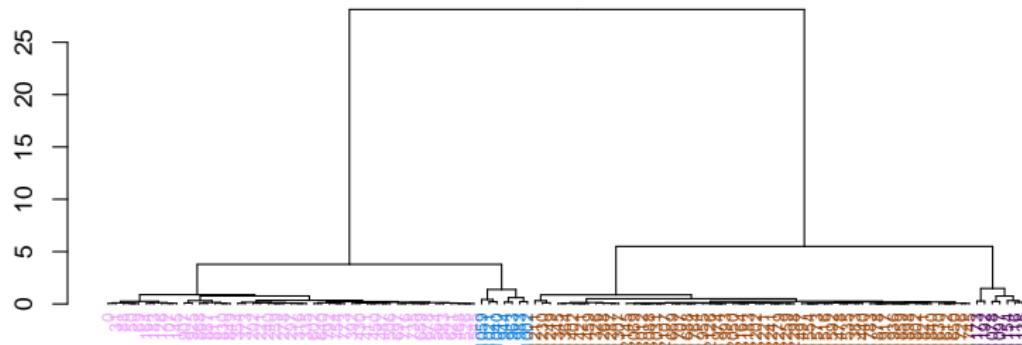
3 PCA Scoreplots with Colours

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3 HCA Dendrogram 4 Clusters

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Correlation Matrix
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2D Correlation
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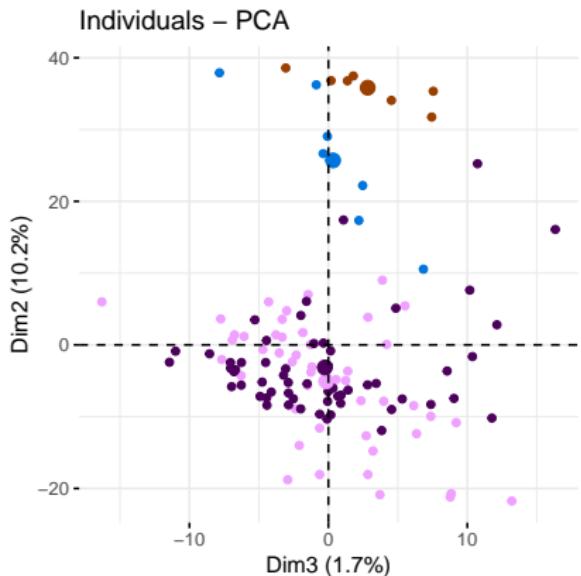
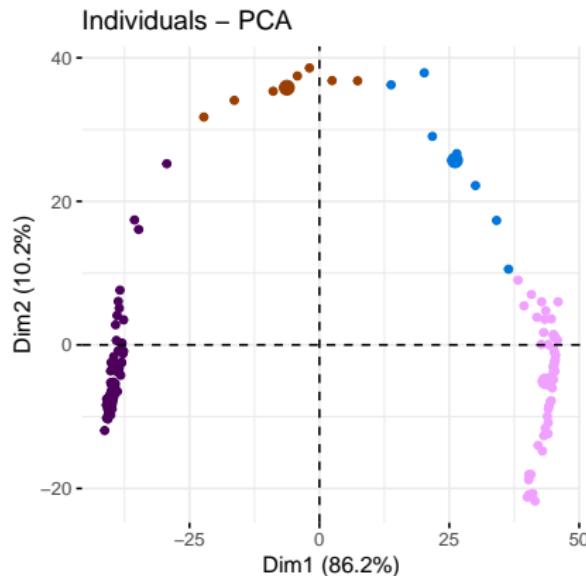
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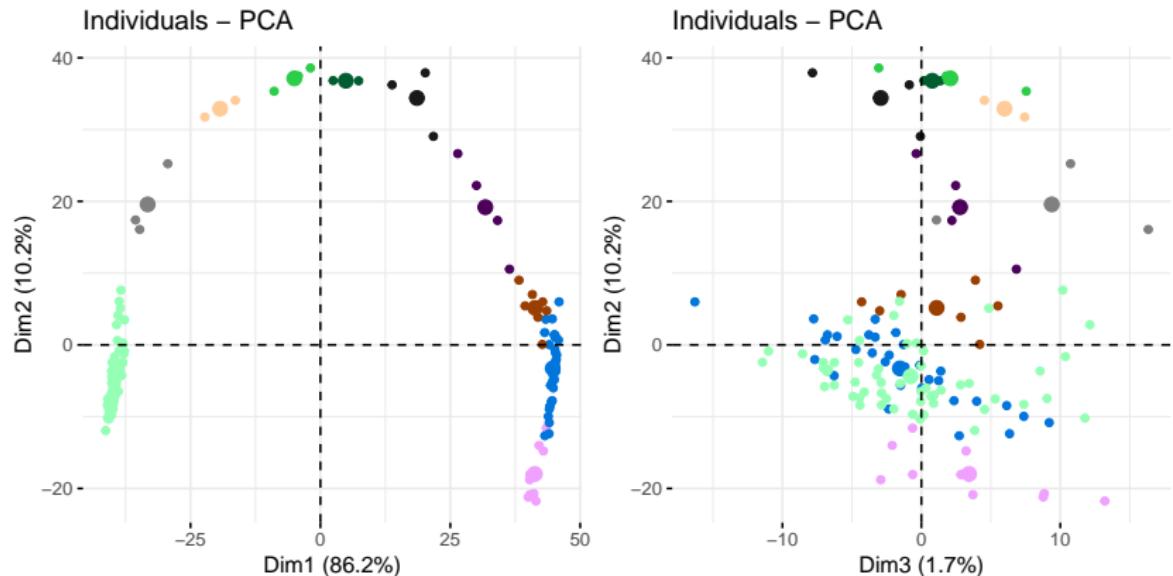
3 PCA Scoreplots with 4 Clusters Membership

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3 PCA Scoreplots with 10 Clusters Membership

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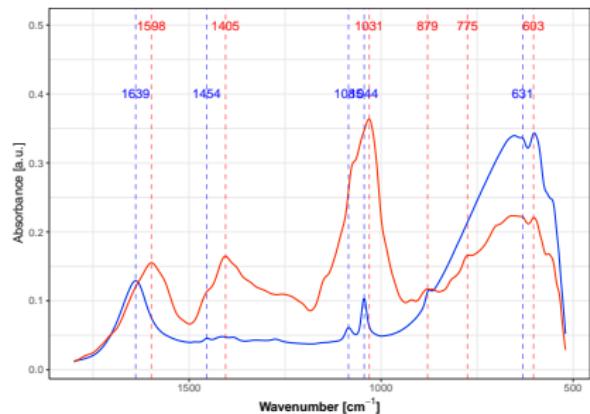
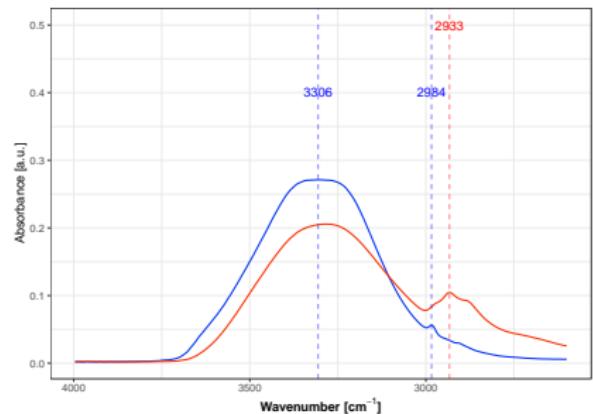
2D Correlation
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4 Spectra Inspection

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Correlation Matrix
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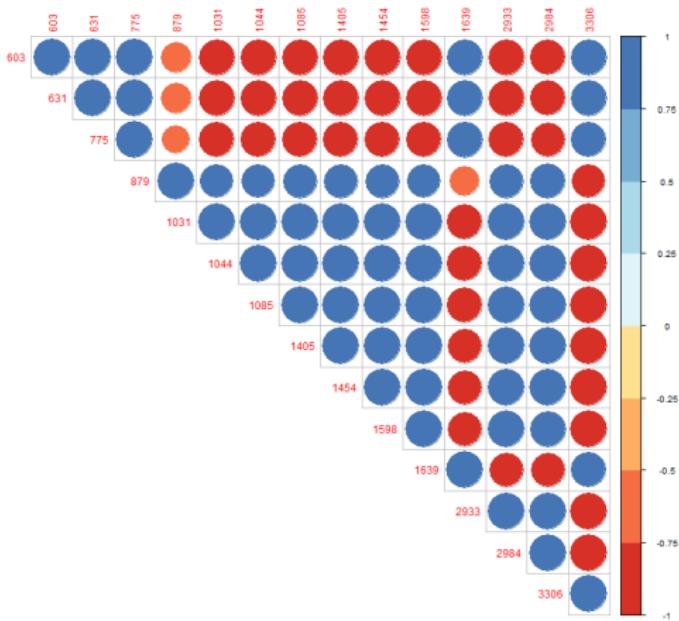
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4 Correlation Matrix - Original Order

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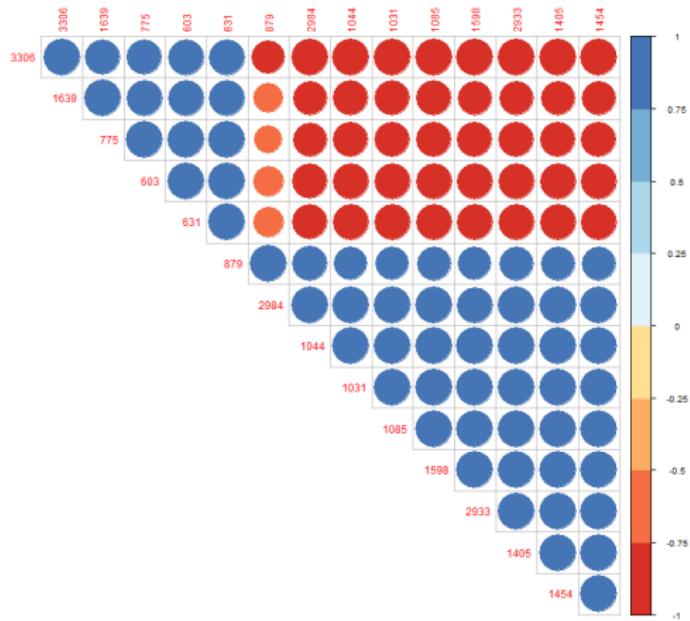
Correlation Matrix
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2D Correlation
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4 Correlation Matrix - Clustering Order

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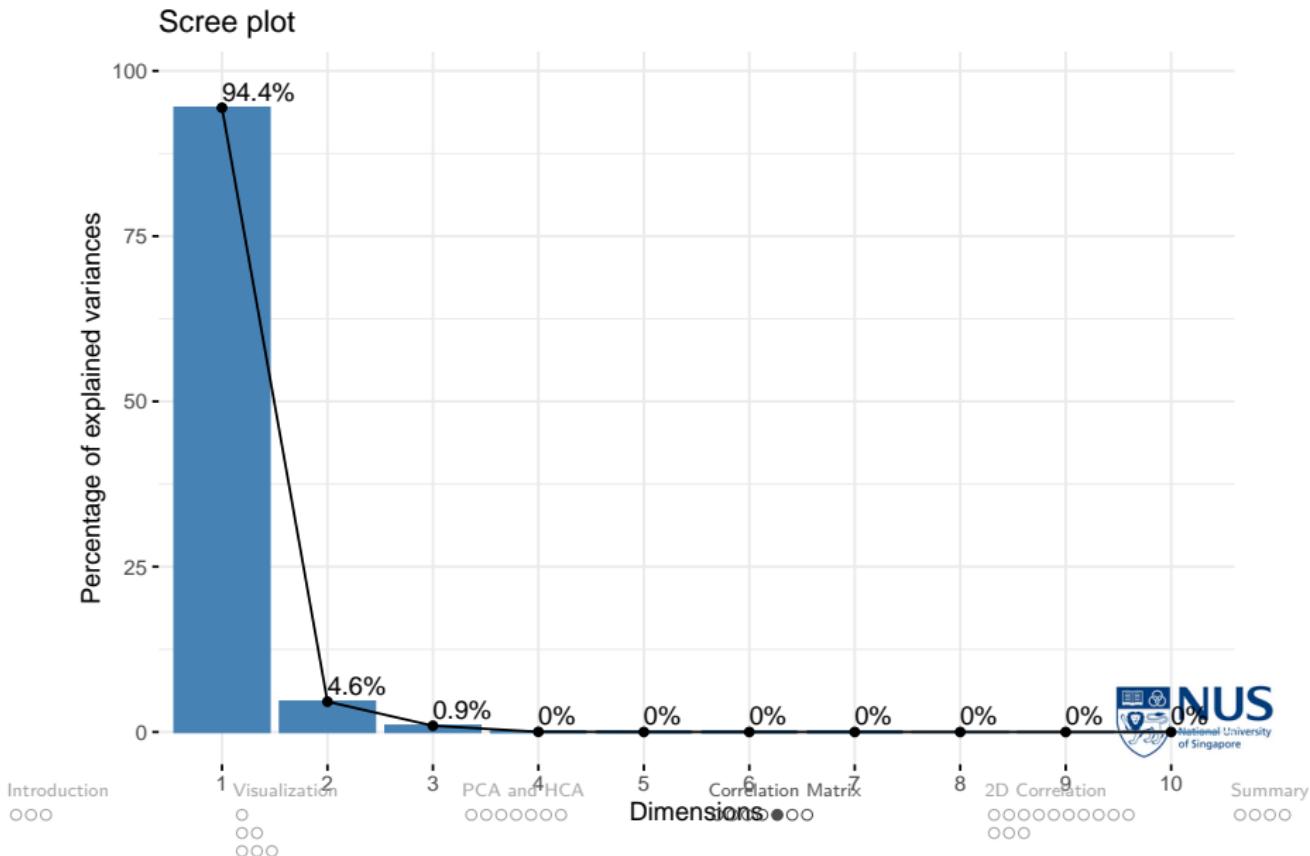
Correlation Matrix
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2D Correlation
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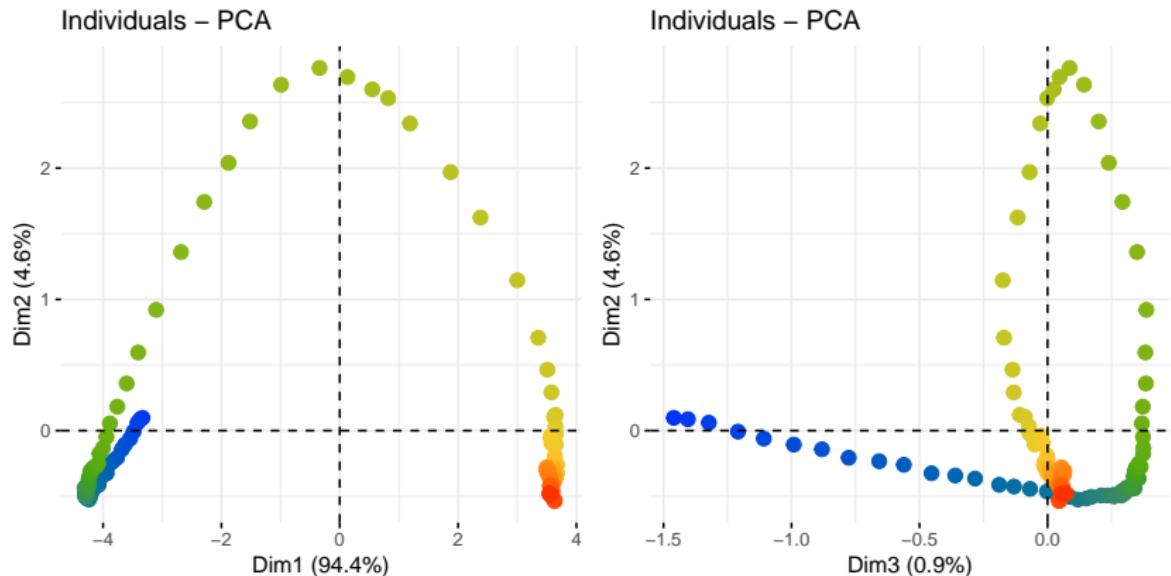
4 PCA on selected wavenumbers

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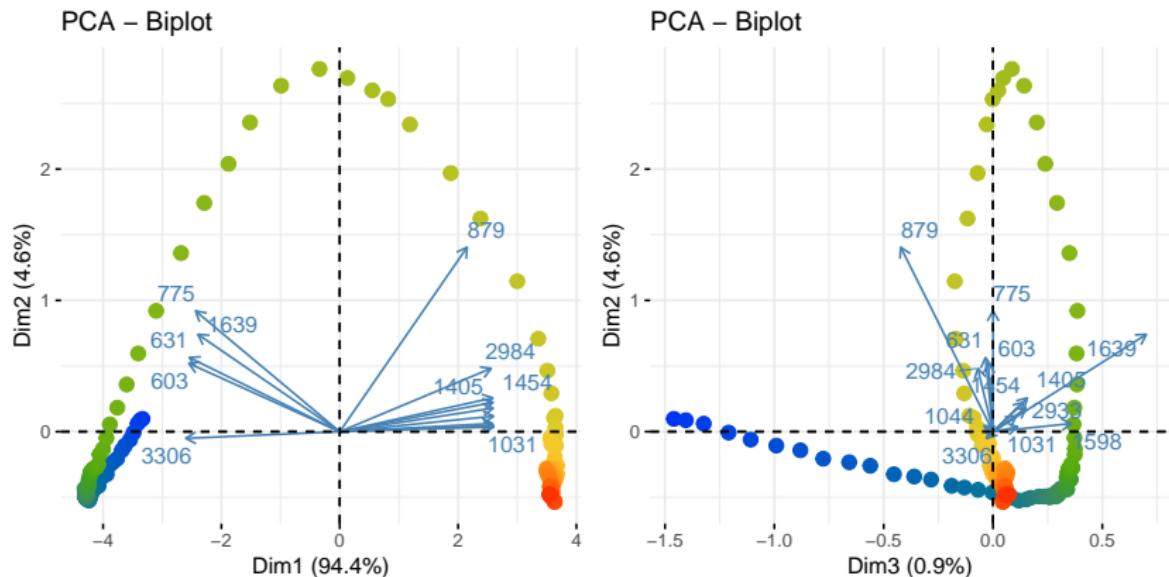
4 PCA Scoreplots with Colours

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4 PCA Biplots

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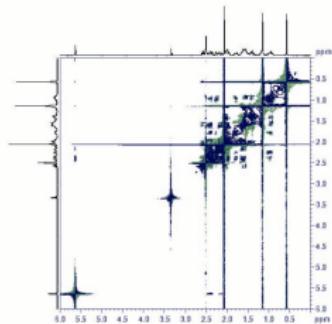
Correlation Matrix
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2D Correlation
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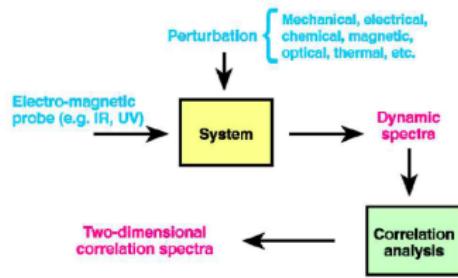
Summary
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- ▶ 1971 Jean Jeener AMPERE Summer School Basko Polje (Yugoslavia)
- ▶ 1976 Richard Ernst first experimental demonstration of the technique
- ▶ 1980 Isao Noda sinusoidal perturbations based 2D spectroscopy
- ▶ 1993 generalized 2D correlation analysis based on Fourier transformation
- ▶ 2D correlation analysis is used for the interpretation of many types of spectroscopic data (including XRF, UV/VIS spectroscopy, fluorescence, infrared, and Raman spectra)



- ▶ mathematical technique used to study changes in measured signals
- ▶ Spectra measured with perturbation
 - > time
 - > temperature
 - > pressure
 - > incidence angle
 - > magnetic field
 - > position in space
- ▶ measured spectra show systematic variations that are processed with 2D correlation analysis for interpretation
- ▶ synchronous and asynchronous matrix



5 Applications

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- ▶ determine the events that are occurring at the same time (in phase) and those events that are occurring at different times (out of phase)
- ▶ determine the sequence of spectral changes
- ▶ identify various inter- and intra-molecular interactions
- ▶ band assignments of reacting groups
- ▶ to detect correlations between spectra of different techniques, for example infrared spectroscopy and Raman spectroscopy

5 Foundation of 2D correlation spectroscopy

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$$C_{\text{auto}}(\tau) = \int_{-\infty}^{\infty} f^*(u) \cdot f(u + \tau) du \quad (1)$$

$$C_{\text{cross}}(\tau) = \int_{-\infty}^{\infty} f^*(u) \cdot \mathbf{g}(u + \tau) du \quad (2)$$

5 Dynamic spectra and reference spectrum

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$$\tilde{y}(\nu, t) = \begin{cases} y(\nu, t) - \bar{y}(\nu) & \text{for } T_{\min} \leq t \leq T_{\max} \\ 0 & \text{otherwise} \end{cases} \quad (3)$$

$$\bar{y}(\nu) = \frac{1}{T_{\max} - T_{\min}} \int_{T_{\min}}^{T_{\max}} y(\nu, t) dt \quad (4)$$



5 Complex cross-correlation function

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$$\tilde{Y}(\nu, \omega) = \mathcal{F}(\tilde{y}(\nu, t)) = \int_{-\infty}^{\infty} \tilde{y}(\nu, t) \cdot e^{-i\omega t} dt \quad (5)$$

$$\Phi(\nu_1, \nu_2) + i\Psi(\nu_1, \nu_2) = \frac{1}{2\pi(T_{\max} - T_{\min})} \int_{-\infty}^{\infty} \tilde{Y}(\nu_1, \omega) \cdot \tilde{Y}^*(\nu_2, \omega) d\omega \quad (6)$$

5 Equations 6

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$$\Phi(\nu_1, \nu_2) = \frac{1}{m-1} \sum_{j=1}^m \tilde{y}(\nu_1, t_j) \cdot \tilde{y}(\nu_2, t_j) \quad (7)$$

$$\tilde{z}(\nu_2, t_j) = \sum_{k=1}^m N_{jk} \cdot \tilde{y}(\nu_2, t_k) \quad (8)$$

$$N_{jk} = \begin{cases} 0 & \text{if } j = k \\ \frac{1}{\pi(k-j)} & \text{otherwise} \end{cases} \quad (9)$$

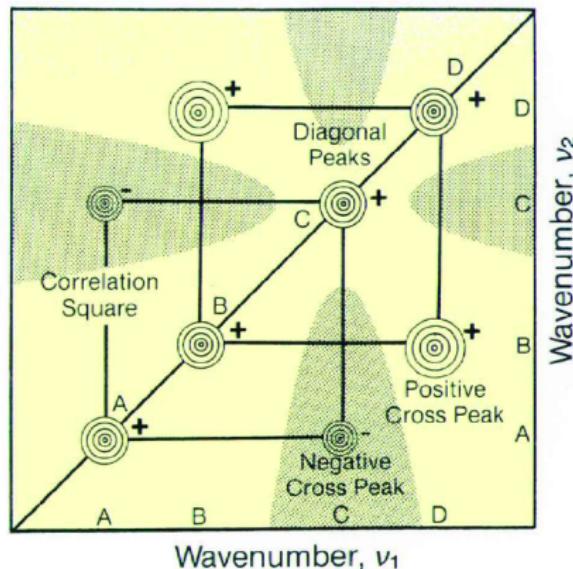
$$\Psi(\nu_1, \nu_2) = \frac{1}{m-1} \sum_{j=1}^m \tilde{y}(\nu_1, t_j) \cdot \tilde{z}(\nu_2, t_j) \quad (10)$$



5 Synchronous Spectrum

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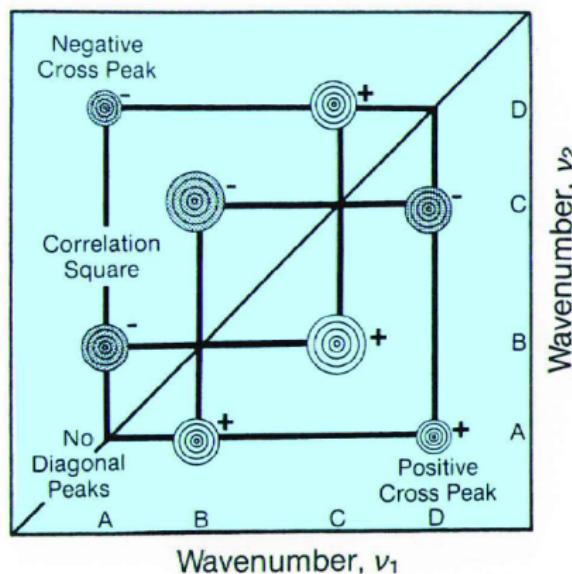
- ▶ peaks at diagonal - auto-correlation function
- ▶ magnitude of autopeaks (>0) - the overall intensity variation
- ▶ off-diagonal cross peaks - simultaneous changes of spectral intensities for two spectral variables
- ▶ the sign of synchronous cross peaks is positive if the intensities at two different spectral variables are either increasing or decreasing together



5 Asynchronous Spectrum

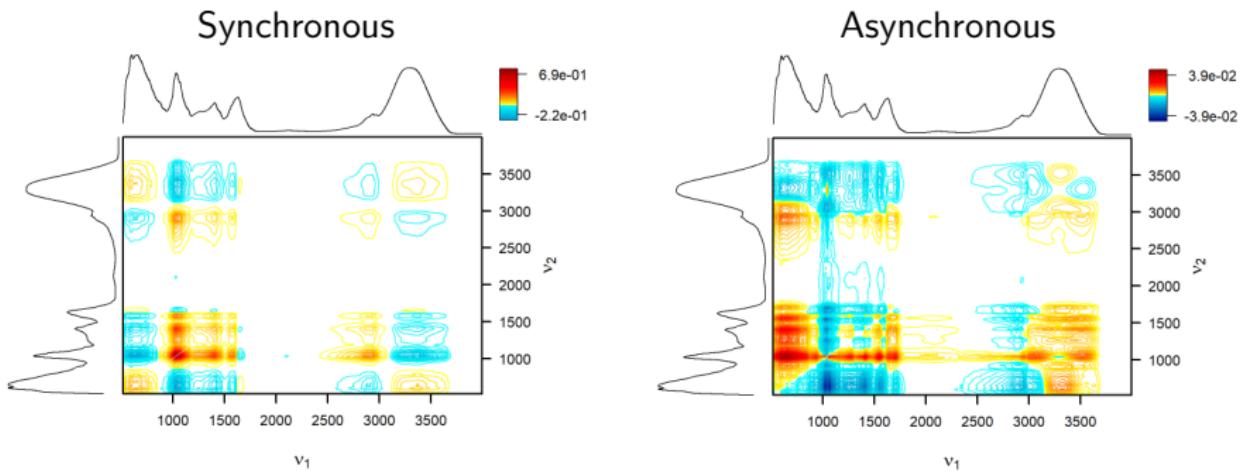
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- ▶ antisymmetric with respect to the diagonal line
- ▶ asynchronous peak develops only if the intensities of two spectral features change out of phase (delayed or accelerated) with each other
- ▶ the sign of an asynchronous peak becomes positive if the intensity change at ν_1 occurs predominately before ν_2 in the sequential order of t



5 Synchronous and asynchronous matrix for propolis

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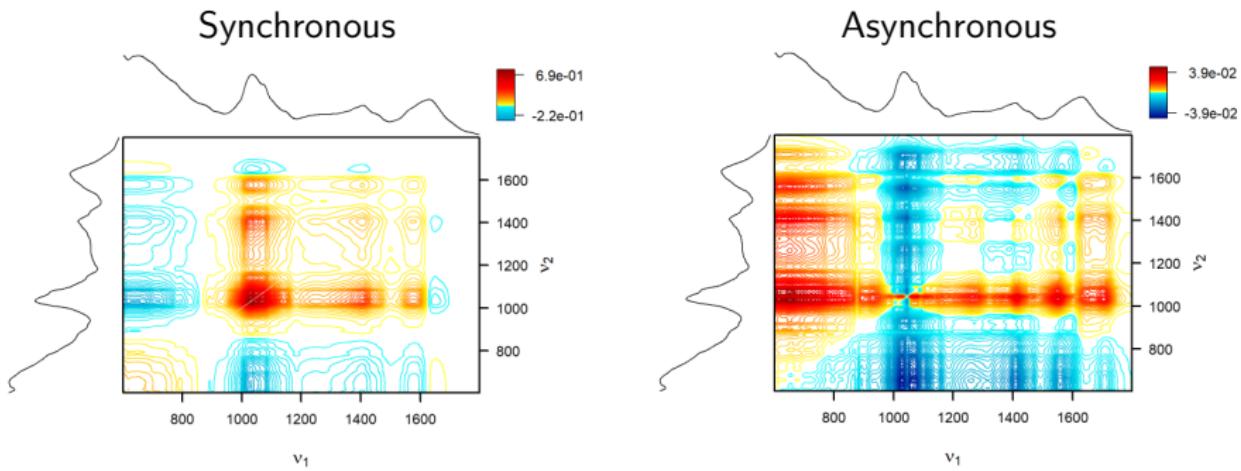
Correlation Matrix
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2D Correlation
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5 Close-up

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PCA and HCA
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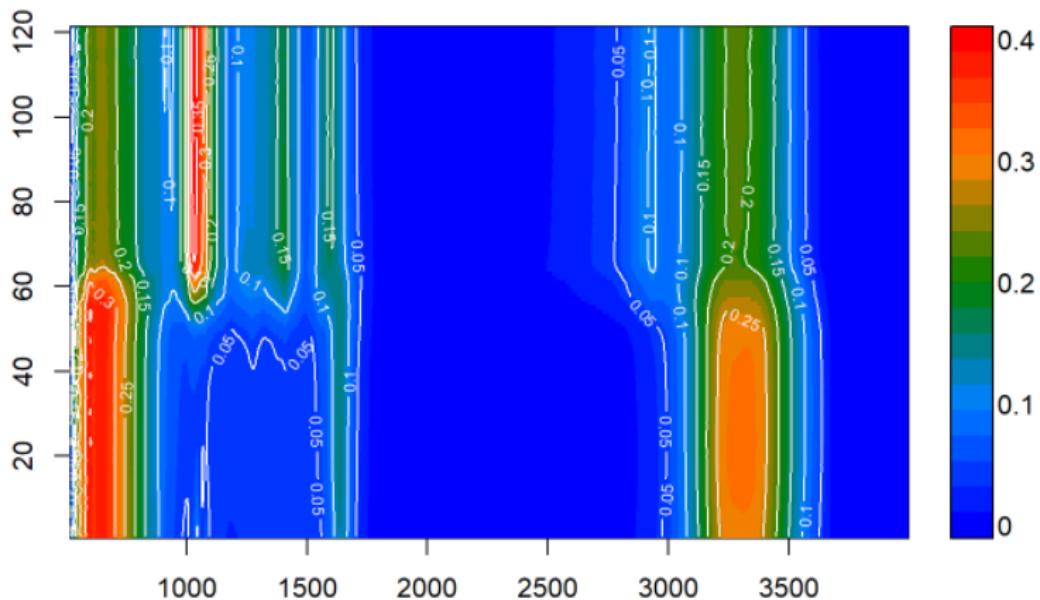
Correlation Matrix
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2D Correlation
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5 Level plot

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2D Correlation
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Summary
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- ▶ for the spectral datasets measured with external perturbation (time, temperature, pressure, pH, concentration, position in space) we can look for correlations
- ▶ dimension reduction is helpful in finding the important wavenumbers (energies, frequencies)
- ▶ 2D correlation analysis and investigation of synchronous and asynchronous matrices may help in finding relationships between spectral bands and clearly visualise the changes under the perturbation



A grayscale photograph of a modern library interior. The perspective is looking down a central aisle between two long rows of floor-to-ceiling bookshelves. The shelves are filled with books of various sizes and colors. The ceiling is made of large, white, angular steel beams and glass panels, allowing natural light to filter through.

Thank you!

6 2D correlation spectra based on the Hilbert Transform

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$$\Phi(\nu_1, \nu_2) = \frac{1}{T_{\max} - T_{\min}} \int_{T_{\min}}^{T_{\max}} \tilde{y}(\nu_1, t) \cdot \tilde{y}(\nu_2, t) dt \quad (11)$$

$$\tilde{z}(\nu_2, t) = \mathcal{H}(\tilde{y}(\nu_2, t)) = \frac{1}{\pi} \text{PV} \int_{-\infty}^{\infty} \frac{\tilde{y}(\nu_2, t')}{t' - t} dt \quad (12)$$

$$\Psi(\nu_1, \nu_2) = \frac{1}{T_{\max} - T_{\min}} \int_{T_{\min}}^{T_{\max}} \tilde{y}(\nu_1, t) \cdot \tilde{z}(\nu_2, t) dt \quad (13)$$

