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Hyperons @ HADES

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Oświadczenie

Ja niżej podpisany Krzysztof Nowakowski (nr indeksu: 1078309), doktorant Wydziału Fizyki Astronomii i Informatyki Stosowanej Uniwersytetu Jagiellońskiego, oświadczam, że przedłożona przeze mnie rozprawa doktorska pt. "Hyperons by HADES" jest oryginalna i przedstawia wyniki badań wykonanych przeze mnie osobiście, pod kierunkiem prof. dr. hab. Piotra Salabury. Pracę napisałem samodzielnie.

Oświadczam, że moja rozprawa doktorska została opracowana zgodnie z Ustawą o prawie autorskim i prawach pokrewnych z dnia 4 lutego 1994 r. (Dziennik Ustaw 1994 nr 24 poz. 83 wraz z późniejszymi zmianami).

Jestem świadom, że niezgodność niniejszego oświadczenia z prawdą ujawniona w dowolnym czasie, niezależnie od skutków prawnych wynikających z ww. ustawy, może spowodować unieważnienie stopnia nabytego na podstawie tej rozprawy.

Kraków, dnia	



Abstract

sOME ABSTRACT

Streszczenie

Jakies streszczenie

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Introduction

The HADES detector

Deta analysis

Neural networks

4.1 Introduction into artificial neural networks

4.2 The ROC curve and the optimal classifier

One of the most common problem in machine learning is a binary classification, when a data set has to be divided into two subsets, fulfilling serian requirements. A simple example of such a problem is distinction between signal and bacground events in deta collected by experiment. We would like to have a function which takes as agruments set of physical observables (eg. particles' energy, momentum, coordinates of vertexes), represents by \vec{x} and returns sigle number. More formally, a clasyfier can be call any function $h: \vec{x} \to \mathbb{R}$ designed in such a way, that high $h(\vec{x})$ values correspond signal events and low $h(\vec{x})$ values correspond background event. A threshold value $h(\vec{x})$ =c, which is the value separating signal and background events is called a working point, and has to be set by a user. The signal efficiency will be defined as $\epsilon_S = \int d\vec{x} \rho_S(\vec{x}) \Theta(h(\vec{x}) - c)$ and respectively a background efficiency $\epsilon_B = \int d\vec{x} \rho_B(\vec{x}) \Theta(h(\vec{x}) - c)$.

The problems how to represent a clasyfier performence, how to compare different clasyfiers and how to choose proper working point have been discused since many years.

4.3 The data-driven approach

The original paper by Metodiev, Nachman and Thaler [1] the othors show the idea of a data-driven analysis in details. In this chapter I want to introduce main concepts, necessery to understand how the proposed metode helps in week decays reconstruction.

In a classical approach to supervized machine learning, a model learns its properties usign sets of labeled data. Of course providing good training sets is always a problem. To do this someone can use either experimental data, labeled by a user, or simulation. In first case a user uses his external

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knowledge about the data to describe it. In necond case the user fully rely on simulation. (opisz zagrożenia)

The data-data driven analysis avoids inconveniencees of two mentioned methodes. It requires neither labeling nor simulation. According to Neyman-Pearson lemma [2] the optimal clasyfier for two sets, A and B is a function given by a dencity ratio

$$h_{opt}^{A/B}(\vec{x}) = \frac{\rho_A}{\rho_B} \tag{4.1}$$

or any monotonous function of $\frac{\rho_A}{\rho_B}$. Assuming that both sets A and B contains signal (s) and bacground (b) events and a statistical distribution of s and b is the same in A and B, we can write (4.1) in the following way

$$h_{opt}^{A/B} = \frac{f_1 \rho_s + (1 - f_1)\rho_b}{f_2 \rho_s + (1 - f_2)\rho_b} = \frac{f_1 \rho_s / \rho_b + 1 - f_1}{f_2 \rho_s / \rho_b + 1 - f_2} = \frac{f_1 h_{opt}^{s/b} + 1 - f_1}{f_2 h_{opt}^{s/b} + 1 - f_2}.$$
 (4.2)

It can be proven that $\partial_{h^{s/b}_{opt}} h^{A/B}_{opt} > 0$, what means that optimal clasyfier for both cases is the same. It is important to underline that the reasoning gives no clue about the working points for both cases.

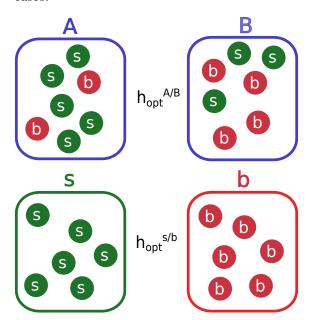


FIGURE 4.1: A data-driven approach visualisation. According to [1] the opitimal clasyfier for sets A and B is equivalent to optimal clasyfier for sets s and b.

4.4 Application for analysis

Simulations of a new experiment

The HADES collaboration is one of the leading forces of a FAIR Phase-0 project. Within the scope of FAIR project a pp@4.5GeV experiment is going to be pervormed. It gives a great opportunity to measure hyperons' Dalitz decays (see Chapter 1). One of the goals of my work was to carry out a simulation of such an experiment.

5.1 An estimation of cross-sections

In energy range of $1GeV < \sqrt{S} < 6GeV$ an inclusive cross section for $\Lambda(1116)$ and $\Sigma(1193)$ were measured for many different energys [ref]. Also an inclusive cross section for $\Lambda(1405)$ production was measured for two different energys [ref], and a cross section for $\Lambda(1520)$ in known for one energy [ref] in this range. In contrast to the exclusive production cross section , inclusive cross sections for hyperons' production are poorly known.

5.1.1 $\Lambda(1116)$ inclusive cross section

The first step for all estimations is a parametrization of a $\Lambda(1116)$ inclusive production. In a given energy range there are four measured values. More over I made two additional assumptions i) the cross section is equal 0 for threshold energy, ii) for energy below one pion mass (140MeV) the inclusive and the exclusive cross sections are the same, so for the parametrization I can use cross section measured for $pp \to pK^+\Lambda(1116)$ for \sqrt{S} below ??. To the chosen data points I fitted a 3th order polynomial

$$\sigma_{\text{pp}\to\Lambda(1116)X}(\sqrt{S}) = 48 \cdot (\sqrt{S} - 2.55) + 292.6 \cdot (\sqrt{S} - 2.55)^2 - 45.4 \cdot (\sqrt{S} - 2.55)^3. \tag{5.1}$$

Fit result, together with residual plot is show in ??.

5.1.2 $\Sigma(1193)$ inclusive cross section

According to PDG [ref] almost all $\Sigma(1193)$ s decay into $\Lambda(1116)$. I means that the inclususive $\Lambda(1116)$ signal contains a fraction deriving from Sz decays. However knowing a relation between $\Lambda(1116)$ and $\Sigma(1193)$ it is possible to disantanle both contributions.

A $\Sigma(1193)/\Lambda(1116)$ ratio was measured by COSY and others [ref], see ??. Additionally the COSY collaboration proposed a parametrization of the ratio for eccess energy $\epsilon < 200 MeV$. Above this energy ($\epsilon > 200 MeV$) a linear parametrization

$$\frac{\Lambda(1116)}{\Sigma(1193)}(\epsilon) = 2.215 - 2.7 \cdot 10^{-5} \epsilon \tag{5.2}$$

describes data quite well ($\chi^2=0.89$). In fact for $\epsilon>200MeV$ the ratio is almost constant and does not depend on energy.

Knowing the $\Lambda(1116)/\Sigma(1193)$ I was able to disantagle a $\Lambda(1116)$ and $\Sigma(1193)$ production. Using determinated ratio and the $\Lambda(1116)$ production parametrization (eq. 5.1) I created following set of equations,

$$P_1(\epsilon) = \frac{L(\epsilon)}{S(\epsilon)} = \frac{L(\sqrt{S} - \Lambda(1116)_{thr})}{S(\sqrt{S} - \Sigma(1193)_{thr})} = P_1(\sqrt{S}), \tag{5.3}$$

$$P_2(\sqrt{S}) = \Lambda(\sqrt{S}) + \Sigma(\sqrt{S}). \tag{5.4}$$

Solving the first equation and shifting an argument by $\Sigma(1385)_{thr}$ I obtained an equation,

$$\Sigma(\sqrt{S}) \cdot P_1(\sqrt{S} + \Sigma(1193)_{thr}) = \Lambda(\sqrt{S} - \Lambda(1116)_{thr} + \Sigma(1193)_{thr}). \tag{5.5}$$

Now, using eq. 5.5 and 5.4 I got a recurrence relation

$$\Lambda(\sqrt{S} - \Lambda(1116)_{thr} + \Sigma(1193)_{thr}) = P_1(\sqrt{S} + \Sigma(1193)_{thr}) \left(P_2(\sqrt{S}) - \Lambda(Sqs)\right).$$
 (5.6)

Assuming that $\Lambda(\Lambda(1116)_{thr})=0$ and $\Sigma(\Sigma(1193)_{thr})=0$, the above equation can be solved with any given precision. For the purpuse of cross sections estimation a single step was set $\Delta M=\frac{\Sigma(1193)_{thr}-\Lambda(11116)_{thr}}{10}$, obtained decomposition is shown in ref??.

5.1.3 $\Lambda(1520)$ and $\Sigma(1385)$ production cross sections

5.1.4 $\Xi^{-}(1322)$

5.2 Background channels selection

5.3 Simulations results

TABLE 5.1: List of signal (S) and background (B) channels for simulated benchmark reactions. Channels marked with * have estimated cross-sections, as described in Chapter ??. Each channel containing Δ Dalitz decay is listed below reference channel, used for cross section estimation.

Channel	σ (μb)	Type
$\Xi^{-}(1322)$ production		
$pK^{+}K^{+}\Xi^{-}(1322)$	3.6/0.35	S*
$pp\pi^{+}\pi^{+}\pi^{-}\pi^{-}$	600	B^{\dagger}
$\mathrm{p}\Lambda(1116)\mathrm{K_S^0}\pi^+$	100	B^{\dagger}
$p\Lambda(1116)K^{+}\pi^{+}\pi^{-}$	30	B^{\dagger}
$n\Lambda(1116)K_{S}^{0}\pi^{+}\pi^{+}$	30	${f B}^{\dagger}$
$\mathrm{p}\Sigma(1193)\mathrm{K}_\mathrm{S}^0\pi^+$	20	B^{\dagger}
$\mathrm{ppK_S^0K_S^0}$	20	B^{\dagger}
background channels the same like for $\Xi^-(132)$	2) plus below	
ppK ⁺ K ⁻	20	B [†]
Dalitz decays of hyperons		
$pK^{+}\Lambda(1405)[\Lambda(1116)e^{+}e^{-}]$	69.6 , BR = 8.4×10^{-5}	S*
$pK^{+}\Lambda(1520)[\Lambda(1116)e^{+}e^{-}]$	32.2 , BR = 5.3×10^{-6}	S*
$pK^{+}\Sigma(1385)[\Lambda(1116)e^{+}e^{-}]$	56.24 , BR = 1.1×10^{-4}	S*
$pK^{+}\Lambda(1405)[X]$	69.6	B^{\dagger}
$pK^+\Lambda(1520)[X]$	32.2	B^{\dagger}
$\mathrm{pK}^+\Sigma(1385)[X]$	56.24	B^{\dagger}
$\mathrm{pp}\pi^+\pi^-\pi^0$	1840	В
$p\pi^+\pi^-\Delta^+[pe^+e^-]$	$2760, BR = 4.5 \times 10^{-5}$	${ m B}^{\dagger}$
$pn\pi^+\pi^+\pi^-\pi^0$	300	\mathbf{B}^{\dagger}
$p\pi^{+}\pi^{+}\pi^{-}\Delta^{0}[ne^{+}e^{-}]$	$450, BR = 4.5 \times 10^{-5}$	\mathbf{B}^{\dagger}
$pp\pi^{+}\pi^{-}\pi^{0}\pi^{0}$	300	\mathbf{B}^{\dagger}
$p\Lambda(1116)K^{+}\pi^{0}$	43	${f B}^{\dagger}$
$K^{+}\Lambda(1116)\Delta^{+}[pe^{+}e^{-}]$	$64, BR = 4.5 \times 10^{-5}$	В
$n\Lambda(1116)K^{+}\pi^{+}\pi^{0}$	20	${f B}^{\dagger}$
$\pi^{+} K^{+} \Lambda(1116) \Delta^{0} [\text{ne}^{+} \text{e}^{-}]$	$30, BR = 4.5 \times 10^{-5}$	В
$p\Lambda(1116)K^{+}\pi^{0}\pi^{0}$	10	$\mathrm{B}_{_{_{\perp}}}^{\dagger}$
$\mathrm{p}\Sigma(1193)\mathrm{K_{S}^{0}}\pi^{+}$	18	$_{-}^{\dagger}$
$p\Lambda(1116)K^{+}\pi^{0}\pi^{0}\pi^{0}$	7	B [†]
Real photon decays of hyperons		
$pK^+\Lambda(1405)[\Lambda(1116)\gamma]$	$69.6, BR = 1.3 \times 10^{-2}$	S*
$pK^{+}\Lambda(1520)[\Lambda(1116)\gamma]$	32.2 , BR = 5.0×10^{-4}	S*
$pK^{+}\Sigma(1385)[\Lambda(1116)\gamma]$	56.24 , BR = 1.1×10^{-2}	S*
$\mathrm{pp}\pi^+\pi^-\pi^0$	1840	\mathbf{B}^{\dagger}
$p\Lambda(1116)K^+$	54.5	\mathbf{B}^{\ddagger}
$\mathrm{p}\Lambda(1116)\mathrm{K}^+\pi^0$	35	\mathbf{B}^{\dagger}
$p\Lambda(1116)K^{+}\pi^{+}\pi^{-}$	20	\mathbf{B}^{\dagger}
$p\Sigma(1193)K^+$	23.5	\mathbf{B}^{\ddagger}
$p\Sigma(1193)K^{+}\pi^{0}$	20	\mathbf{B}^{\ddagger}
$p\Sigma(1193)K^{+}\pi^{+}\pi^{-}$	2	B^{\ddagger}

Conclusions

Appendix A

The data-driven approach for a neural network training

The original paper by Metodiev, Nachman and Thaler [1] shows the idea of a data-driven analysis in details. In this chapter I want to introduce main concepts, necessery to understand how the proposed metode helps in week decays reconstruction.

In a classical approach to supervized machine learning, a model learns its properties usign sets of labeled data.

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