Project overview/update

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Project goal

- Automatic generation of {expression equality checker, normalizer, property inference}
- Current code is fragile and hard to extend
- Something easier to add to would be nice

Initial approach: rewrite rules

- Use completion algorithm to make a confluent rewrite system
- ▶ Confluence: apply rules in any order and get some results
 - Consider $y + x + -x \rightarrow y$ on x + -x + -(-x).
 - ▶ Can get -(-x) or x as final result
 - ▶ Need to add -(-x) = x to fix
- ▶ (Done) Base Knuth-Bendix algorithm and syntactic unification
- ► (Near done) Associative-commutative completion and unification
 - One small bug in there somewhere maybe
- ▶ (Failed) Rewrite rules conditioned on properties
 - Trying to represent these as unconditional equations gets unwieldy and prevents sensible results
 - ▶ Also, associativity only sort of works $((AB)C \rightarrow A(BC))$ does not cover all cases)

The future: theorem provers?

- ▶ Property inference and equality checking are all first-order logic things
- ▶ We could delegate that to a theorem prover, potentially
- ► Could also enable more stuff like bandwidth properties (generalization of diagonal, triangular, etc.)
- Potential tools
 - Prolog (might not be expressive enough)
 - ightharpoonup E (first order logic, but nothing else we'd need to roll our own \mathbb{N})
 - SMT solvers like z3 (seem to be very well developed, may not solve our problem)
 - Coq et al don't fit our problem type