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## **Assignment 3**

**AI1110**: Probability and Random Variables Indian Institute of Technology Hyderabad

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**12.13.5.12: Question**. Find the probability of throwing at most 2 sixes in 6 throws of a single die.

**Answer:**  $\frac{35}{18}(\frac{5}{6})^4$ .

**Solution**: According to the question:

n	Number of throws	6
p	Probability of getting 6	1/6
q	Probability of getting other than 6	<u>5</u>

TABLE 0: Given Information

Let X: Number of times we get number in 6 throws of a die. Throwing a die and getting 6 or a number other tha 6 is a bernoulli event. So, X has a binomial distribution.

$$\Pr(X = k) = P_X(k) = {}^{n}C_k q^{n-k} p^k$$
 (1)

$$P_X(k) = {}^{6}C_k(\frac{5}{6})^{6-k}(\frac{1}{6})^k \tag{2}$$

We are supposed to find probability of throwing at most 2 sixes i.e.  $Pr(X \le 2)$ .

$$\Pr\left(X \le 2\right) = F_X(2) \tag{3}$$

$$= P_X(0) + P_X(1) + P_X(2)$$
 (4)

Using (2) in (4):

$$= {}^{6}C_{0}(\frac{5}{6})^{6}(\frac{1}{6})^{0} + {}^{6}C_{1}(\frac{5}{6})^{5}(\frac{1}{6})^{1} + {}^{6}C_{2}(\frac{5}{6})^{4}(\frac{1}{6})^{2}$$
 (5)

$$= (\frac{5}{6})^6 + (\frac{5}{6})^5 + \frac{5}{12} \times (\frac{5}{6})^4 \tag{6}$$

$$= \left(\frac{5}{6}\right)^4 \left(\frac{25}{36} + \frac{5}{6} + \frac{5}{12}\right) \tag{7}$$

$$= (\frac{5}{6})^4 (\frac{70}{36}) \tag{8}$$

$$=\frac{35}{18}(\frac{5}{6})^4\tag{9}$$

So,the required probability is  $\frac{35}{18}(\frac{5}{6})^4$ .