# Package 'logdensity'

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Title Estimate the (Logarithm) of the Density and its Derivatives

Type Package

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<b>Description</b> This package contains functions that estimate the logarithm of an unknown density function from iid data. The estimation strategy is based on a local polynomial appoximation to the log-density. The estimates behave well near the boundary of the support of the density and can be guaranteed to be nonnegative. Details can be found in Pinske and Schurter (2020) "Estimates of derivatives of (log) densities and related objects."
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logdensity-package The logdensity package

## **Description**

A package for estimating (log) densities and their derivatives

## **Details**

This package contains functions that estimate the logarithm of an unknown density function from iid data. The estimation strategy is based on a local polynomial appoximation to the logarithm of the density. The estimates behave well near the boundary of the support of the density and can be guaranteed to be nonnegative. Details can be found in Pinske and Schurter (2020).

## Author(s)

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#### References

Pinkse, J. and Schurter, K. (2020) "Estimates of derivatives of (log) densities and related objects."

bellpoly

Evaluate partial Bell polynomials

# Description

Evaluates the partial Bell polynomials, also known as the incomplete Bell polynomials. The complete Bell polynomial is the sum of the partial Bell polynomials over k = 1, ..., n. The partial polynomials are evaluated using the recurrence relation

$$k B_{n,k}(x_1, \dots, x_{n-k+1}) = \sum_{r=k-1}^{n-1} \binom{n}{r} x_{n-r} B_{r,k-1}(x_1, \dots, x_{r-k+2})$$

where the sum is over r = k - 1, ..., n - 1, and  $B_{0,0} = 1$ ,  $B_{0,k} = 0$  for  $k \ge 1$ , and  $B_{n,0} = 0$  for  $n \ge 1$ .

## Usage

```
bellpoly(x, n = nrow(x), k = min(1, n):n)
```

## **Arguments**

- x a matrix or object that can be coerced into one by as.matrix
- n nonnegative integer representing the number of elements
- k vector of integers no greater than n representing the sizes of partition

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## Value

bellpoly returns a vector or matrix depending on the dimensions of x that contains the value of the partial Bell polynomial(s) evaluated at columns of as.matrix(x).

## **Examples**

```
n <- 5
k <- 1:n

## Idempotent numbers
bellpoly(k)
choose(n, k) * k^(n - k) # equivalent

## Stirling numbers (unsigned) of the first kind
bellpoly(x = factorial(k-1))

## Stirling numbers of the second kind
bellpoly(x = rep(1, n))</pre>
```

evalkernel

Evaluate a kernel function

# Description

Evaluate a kernel function

# Usage

```
evalkernel(
   u,
   kernel = c("epanechnikov", "gaussian", "triweight", "uniform", "triangle", "co
        "quartic")
)
```

# Arguments

u **numeric array** 

kernel character string specifying name of kernel

## Value

array with same dimensions as u containing kernel evaluated at u. Note: NA values of u evaluate to 0.

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logdensity

A local polynomial log-density estimator

# Description

logdensity.fit is intended to be called from within logdensity, after performing basic argument verification. Use caution when calling logdensity.fit directly.

# Usage

```
logdensity(
  data,
  x,
  h,
  g,
  dg,
  m = "epanechnikov",
  minx = -Inf,
  maxx = Inf,
  S = 1,
  logf = TRUE,
  mc.cores = 1L,
  ...
)

logdensity.fit(data, x, h, g, dg, m, minx, maxx, logf, exact, ...)
```

# Arguments

data	numeric vector of observations
х	points at which to estimate (if shorter than h, recycled to length of h)
h	bandwidth (if shorter than x, recycled to the length of x)
g	function of u, zl, and zr that must be equal to an S-length vector of 0's at zl = $\max((\min x-x)/h,-1)$ and zr = $\min((\max x-x),1)$ , where S is the order of the local polynomial approximation to the log-density. Function must be vectorized so that g(u, zl, zr) returns a matrix that is length(u) by S.
dg	function that evaluates derivative of $g$ with respect to $u$ . Must be vectorized and return a matrix that is $length(u)$ by $S$ .
m	kernel function used to compute the density. Can be a function, symbol, or character string that matches the name of a function or one of the kernels allowed in evalkernel. If m == "epanechnikov" and the polynomial order is 1, an exact solution is computed. Otherwise, the estimate of the log-density involves numerical integration.
minx	lower bound of support of x
maxx	upper bound of support of $x$
S	degree of polynomial expansion of log-density to be used with default $g$ . If user supplies $g$ and $dg$ , this argument is ignored without warning.

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logf	logical indicating whether the log-density should be compute, in addition to its derivative(s).
mc.cores	integer number of cores to use with $mcmapply$ . If equal to 1 (default), $mapply$ will be used to loop over $x$ , instead.
	Further arguments supplied to g and dg
exact	logical indicating whether an exact solution should be used (if available) or numerical integration. Exact solution currently only available with epanechnikov kernel and local linear approximation.

#### Value

an object of class logdensity which inherits from matrix. The S+1 by length (x) matrix of estimated log-densities (NA unless logf is TRUE) and derivatives has the following additional attributes: x vector of points at which the estimates were computed n number of non-missing observations used in estimation h bandwidth(s) used call matched call

A numeric vector containing the log-density (if logf == TRUE) and its derivatives

#### References

Pinkse, J. and Schurter, K. (2020) "Estimates of derivatives of (log) densities and related objects."

#### See Also

```
mapply, mcmapply, integrate, bellpoly
```

#### **Examples**

```
dat \leftarrow rchisq(n = 100, df = 2)
x \leftarrow seq(from = 0, to = 2, length.out = 20)
## fixed bandwidth
ld <- logdensity(data = dat, x = x, h = 0.5, minx = 0, S = 1)
print(ld)
plot(ld)
## variable bandwidth
h <- pmax(1-x, 0.5)
1d \leftarrow 1ogdensity(data = dat, x = x, h = h, minx = 0, S = 2)
ld
plot(ld)
## Faa di Bruno's formula for the density and its derivatives
deriv <- 0L # integer between 0 and S (=2 for most recent estimation)
\exp(\operatorname{ld}[1,]) \star \operatorname{colSums}(\operatorname{bellpoly}(\operatorname{ld}[-1,], n = \operatorname{deriv}))
### verify formula for deriv = 0, 1, and 2
\exp(\text{ld}[1,]) \star \text{colSums}(\text{bellpoly}(\text{ld}[-1,], n = 0L)) # density (0th derivative)
exp(ld[1, ]) # equivalent
\exp(\operatorname{ld}[1,]) * \operatorname{colSums}(\operatorname{bellpoly}(\operatorname{ld}[-1,], n = 1L)) # 1st derivative of density
exp(ld[1, ]) * ld[2,] # equivalent
\exp(\mathrm{ld}[1,]) \star \mathrm{colSums}(\mathrm{bellpoly}(\mathrm{ld}[-1,], n = 2L)) # 2nd derivative of density
\exp(1d[1, ]) * (1d[2,]^2 + 1d[3, ]) # equivalent
```

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```
plot.logdensity Plot density and log-density estimates
```

## **Description**

Plot density and log-density estimates

## Usage

```
## S3 method for class 'logdensity'
plot(x, density = FALSE, type = "l", xlab, ylab, ...)
```

## **Arguments**

```
x a logdensity object
density logical indicating whether to plot density or log-density
type what type of plot should be drawn
xlab a title for the x axis
ylab a title for the y axis
... further arguments passed to plot.default
```

## See Also

```
plot.default
```

```
print.logdensity Print log-density estimates
```

# Description

Print log-density estimates

# Usage

```
## S3 method for class 'logdensity'
print(
    x,
    digits = max(3L, getOption("digits") - 3L),
    max = 100,
    quote = FALSE,
    ...
)
```

## **Arguments**

```
x a logdensity object
digits minimal number of significant digits
max approximate max number of entries to be printed
quote logical, indicating whether strings should be printed with surrounding quotes
... further arguments passed to print.default
```

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# Value

invisibly returns x

# See Also

print.default

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