

## ACT03 - Data Mining

Team 7 | Captain: Nadine Rose | Members: Kyle Scott, Lakshya Rathore, Bailey LaRea

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# Problem 1.1

```
library(kableExtra)

Observation <- c(1:12)
True_Status <- c(1, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0)
Posterior_Probability <- c(0.95, 0.85, 0.75, 0.45, 0.35, 0.25, 0.15, 0.05, 0.65, 0.55, 0.5, 0.7)

df <- data.frame(Observation, True_Status, Posterior_Probability)

kable(df, linesep = "\\addlinespace",
      digits = 3, booktabs = T, format = 'latex') %>%
  kable_styling(latex_options = c("striped", "hold_position"))
```

| Observation | True_Status | Posterior_Probability |
|-------------|-------------|-----------------------|
| 1           | 1           | 0.95                  |
| 2           | 1           | 0.85                  |
| 3           | 1           | 0.75                  |
| 4           | 1           | 0.45                  |
| 5           | 1           | 0.35                  |
| 6           | 1           | 0.25                  |
| 7           | 0           | 0.15                  |
| 8           | 0           | 0.05                  |
| 9           | 0           | 0.65                  |
| 10          | 0           | 0.55                  |
| 11          | 0           | 0.50                  |
| 12          | 0           | 0.70                  |

We are given that the cut-off point is 0.72. Using this chart, we know that any Posterior Probability  $\geq 0.72$  will be classified as 1 and any Posterior Probability  $< 0.72$  will be classified as 0.

```
Predicted_Status <- c(1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0)
df <- cbind(df, Predicted_Status)

kable(df, linesep = "\\addlinespace",
      digits = 3, booktabs = T, format = 'latex') %>%
  kable_styling(latex_options = c("striped", "hold_position"))
```

| Observation | True_Status | Posterior_Probability | Predicted_Status |
|-------------|-------------|-----------------------|------------------|
| 1           | 1           | 0.95                  | 1                |
| 2           | 1           | 0.85                  | 1                |
| 3           | 1           | 0.75                  | 1                |
| 4           | 1           | 0.45                  | 0                |
| 5           | 1           | 0.35                  | 0                |
| 6           | 1           | 0.25                  | 0                |
| 7           | 0           | 0.15                  | 0                |
| 8           | 0           | 0.05                  | 0                |
| 9           | 0           | 0.65                  | 0                |
| 10          | 0           | 0.55                  | 0                |
| 11          | 0           | 0.50                  | 0                |
| 12          | 0           | 0.70                  | 0                |

Now we can compare True\_Status to Predicted\_Status to determine the number of True Positives, False Positives, True Negatives and False Negatives.

## Answer Section:

True Positive (True\_Status = 1 && Predicted\_Status = 1) = 3 (Obs. 1, 2, and 3)

False Positive (True\_Status = 0 && Predicted\_Status = 1) = 0

True Negative (True\_Status = 0 && Predicted\_Status = 0) = 6 (Obs. 7, 8, 9, 10, 11, and 12)

False Negative (True\_Status = 1 && Predicted\_Status = 0) = 3 (Obs. 4, 5, and 6)

$$\text{Sensitivity} = \frac{N_{TP}}{N_{TP} + N_{FN}} = \frac{3}{3+3} = 0.5$$

$$\text{Specificity} = \frac{N_{TN}}{N_{TN} + N_{FP}} = \frac{6}{6+0} = 1$$

$$\text{Accuracy} = \frac{N_{TP} + N_{TN}}{N} = \frac{3+6}{12} = 0.75$$

$$\text{Precision} = \frac{N_{TP}}{N_{TP} + N_{FP}} = \frac{3}{3+0} = 1$$

$$\text{F1 Score} = \frac{2 \times (\text{Precision} \times \text{Sensitivity})}{\text{Precision} + \text{Sensitivity}} = \frac{2 \times 1 \times 0.5}{0.5 + 1} = 0.667$$

## Problem 1.2

```
Rank <- c(12, 11, 10, 5, 4, 3, 2, 1, 8, 7, 6, 9)
Rank_Positive <- c(12, 11, 10, 5, 4, 3, 0, 0, 0, 0, 0, 0)
df <- cbind(df, Rank)
df <- cbind(df, Rank_Positive)
kable(df, linesep = "\\addlinespace",
      digits = 3, booktabs = T, format = 'latex') %>%
  kable_styling(latex_options = c("striped", "hold_position"))
```

| Observation | True_Status | Posterior_Probability | Predicted_Status | Rank | Rank_Positive |
|-------------|-------------|-----------------------|------------------|------|---------------|
| 1           | 1           | 0.95                  | 1                | 12   | 12            |
| 2           | 1           | 0.85                  | 1                | 11   | 11            |
| 3           | 1           | 0.75                  | 1                | 10   | 10            |
| 4           | 1           | 0.45                  | 0                | 5    | 5             |
| 5           | 1           | 0.35                  | 0                | 4    | 4             |
| 6           | 1           | 0.25                  | 0                | 3    | 3             |
| 7           | 0           | 0.15                  | 0                | 2    | 0             |
| 8           | 0           | 0.05                  | 0                | 1    | 0             |
| 9           | 0           | 0.65                  | 0                | 8    | 0             |
| 10          | 0           | 0.55                  | 0                | 7    | 0             |
| 11          | 0           | 0.50                  | 0                | 6    | 0             |
| 12          | 0           | 0.70                  | 0                | 9    | 0             |

```
sum_rankpos <- sum(Rank_Positive)
sum_rankpos
```

```
## [1] 45
```

$$\text{AUC} = \frac{\text{sumrankpos} - 0.5 \times \pi N \times (\pi N + 1)}{\pi N (N - \pi N)} = \frac{45 - 0.5 \times 0.5 \times 12 \times (0.5 \times 12 + 1)}{0.5 \times 12 \times (12 - 0.5 \times 12)} = 0.667$$

## Problem 1.3

$$\text{GINI} = 2 \times (\text{AUC} - 0.5) = 2 \times (0.667 - 0.5) = 0.3334$$

# Problem 2

## Calculate KS Statistics

```
# create columns for Decile, Positive, and Negative as given in the Assignment
```

```
Decile <- c(1, 2, 3, 4, 5, 6, 7, 8, 9, 10)
```

```
Positive <- c(100, 98, 96, 90, 85, 80, 75, 66, 51, 41)
```

```
Negative <- c(0, 2, 4, 10, 15, 20, 25, 34, 49, 59)
```

```
# create a data frame with these 3 columns
```

```
ks <- data.frame(Decile, Positive, Negative)
```

```
# create vars for Total Num of Positives and Negatives
```

```
total_pos <- sum(Positive)
```

```
total_neg <- sum(Negative)
```

```
# calculate TPR
```

```
TPR <- Positive / total_pos
```

```
# calculate TNR
```

```
TNR <- Negative / total_neg
```

```
# calculate cumulative TPR
```

```
cumulative_TPR <- cumsum(TPR)
```

```
# calculate cumulative TNR
```

```
cumulative_TNR <- cumsum(TNR)
```

```

# calculate KS statistic
KS <- cumulative_TPR - cumulative_TNR

# bind TPR to the data frame
ks <- cbind(ks, TPR)

# bind TNR to the data frame
ks <- cbind(ks, TNR)

# bind cumulative_TPR to the data frame
ks <- cbind(ks, cumulative_TPR)

# bind cumulative_TNR to the data frame
ks <- cbind(ks, cumulative_TNR)

# bind KS to the data frame
ks <- cbind(ks, KS)

library(kableExtra)

kable(ks, caption = "Calculating KS Statistics", linesep = "\\addlinespace",
      digits = 3, booktabs = T, format = 'latex') %>%
  kable_styling(latex_options = c("striped", "hold_position"))

```

Table 1: Calculating KS Statistics

| Decile | Positive | Negative | TPR   | TNR   | cumulative_TPR | cumulative_TNR | KS    |
|--------|----------|----------|-------|-------|----------------|----------------|-------|
| 1      | 100      | 0        | 0.128 | 0.000 | 0.128          | 0.000          | 0.128 |
| 2      | 98       | 2        | 0.125 | 0.009 | 0.253          | 0.009          | 0.244 |
| 3      | 96       | 4        | 0.123 | 0.018 | 0.376          | 0.028          | 0.348 |
| 4      | 90       | 10       | 0.115 | 0.046 | 0.491          | 0.073          | 0.418 |
| 5      | 85       | 15       | 0.109 | 0.069 | 0.600          | 0.142          | 0.458 |
| 6      | 80       | 20       | 0.102 | 0.092 | 0.702          | 0.234          | 0.468 |
| 7      | 75       | 25       | 0.096 | 0.115 | 0.798          | 0.349          | 0.449 |
| 8      | 66       | 34       | 0.084 | 0.156 | 0.882          | 0.505          | 0.378 |
| 9      | 51       | 49       | 0.065 | 0.225 | 0.948          | 0.729          | 0.218 |
| 10     | 41       | 59       | 0.052 | 0.271 | 1.000          | 1.000          | 0.000 |

# Problem 3.1

Read in the CSV file for Microsoft

```
library(readr)

microsoft <- read.csv("Microsoft_Results.csv")
```



## Problem 3.2

First Step is to create a function that will calculate all the required values which can be passed to the function parameter called ‘cutoff’

```
stats <- function(cutoff){  
  
  predicted_detections <- ifelse(microsoft$P_HasDetections >= cutoff, 1, ifelse(microsoft$P_HasDetections < cutoff, 0, 1))  
  
  TP <- sum(ifelse((microsoft$HasDetections == 1 & predicted_detections == 1), 1, 0))  
  
  TruePos <- c(TruePos, TP)  
  
  FP <- sum(ifelse((microsoft$HasDetections == 0 & predicted_detections == 1), 1, 0))  
  
  FalsePos <- c(FalsePos, FP)  
  
  TN <- sum(ifelse((microsoft$HasDetections == 0 & predicted_detections == 0), 1, 0))  
  
  TrueNeg <- c(TrueNeg, TN)  
  
  FN <- sum(ifelse((microsoft$HasDetections == 1 & predicted_detections == 0), 1, 0))  
  
  FalseNeg <- c(FalseNeg, FN)  
  
  Sensitivity <- c(Sensitivity, TP / (TP + FN))  
}
```

```

Specificity <- c(Specificity, TN / (TN + FP))

Accuracy <- c(Accuracy, (TP + TN) / (TP + TN + FP + FN))

Precision <- c(Precision, TP / (TP + FP))
}

```

Now that the function is created, we can call the function for whichever desired values we have. For the purpose of simplicity and demonstration, here we have chosen to display a table with all the desired statistics at the five percent level

```

TP <- vector()
FP <- vector()
TN <- vector()
FN <- vector()
TruePos <- vector()
FalsePos <- vector()
TrueNeg <- vector()
FalseNeg <- vector()
Sensitivity <- vector()
Specificity <- vector()
Accuracy <- vector()
Precision <- vector()

cutoff <- seq(0.05, 1, by = 0.05)
mapply(stats, cutoff)

```

```

stats_df <- data.frame(cutoff, TruePos, FalsePos, TrueNeg, FalseNeg, Sensitivity, Specificity, Accuracy, Precision)

kable(stats_df, caption = "Statistics for the five percentile level", linesep = "\\addlinespace",
      digits = 3, booktabs = T, format = 'latex') %>%
  kable_styling(latex_options = c("striped", "hold_position"))

```

Table 2: Statistics for the five percentile level

| cutoff | TruePos | FalsePos | TrueNeg | FalseNeg | Sensitivity | Specificity | Accuracy | Precision |
|--------|---------|----------|---------|----------|-------------|-------------|----------|-----------|
| 0.05   | 499001  | 500999   | 0       | 0        | 1.000       | 0.000       | 0.499    | 0.499     |
| 0.10   | 498968  | 500789   | 210     | 33       | 1.000       | 0.000       | 0.499    | 0.499     |
| 0.15   | 498711  | 498998   | 2001    | 290      | 0.999       | 0.004       | 0.501    | 0.500     |
| 0.20   | 497610  | 492899   | 8100    | 1391     | 0.997       | 0.016       | 0.506    | 0.502     |
| 0.25   | 492989  | 474524   | 26475   | 6012     | 0.988       | 0.053       | 0.519    | 0.510     |
| 0.30   | 478925  | 432025   | 68974   | 20076    | 0.960       | 0.138       | 0.548    | 0.526     |
| 0.35   | 451667  | 370007   | 130992  | 47334    | 0.905       | 0.261       | 0.583    | 0.550     |
| 0.40   | 413742  | 303093   | 197906  | 85259    | 0.829       | 0.395       | 0.612    | 0.577     |
| 0.45   | 367764  | 239301   | 261698  | 131237   | 0.737       | 0.522       | 0.629    | 0.606     |
| 0.50   | 306004  | 170809   | 330190  | 192997   | 0.613       | 0.659       | 0.636    | 0.642     |
| 0.55   | 225532  | 99644    | 401355  | 273469   | 0.452       | 0.801       | 0.627    | 0.694     |
| 0.60   | 156745  | 51740    | 449259  | 342256   | 0.314       | 0.897       | 0.606    | 0.752     |
| 0.65   | 111830  | 27026    | 473973  | 387171   | 0.224       | 0.946       | 0.586    | 0.805     |
| 0.70   | 84108   | 14959    | 486040  | 414893   | 0.169       | 0.970       | 0.570    | 0.849     |
| 0.75   | 66583   | 9018     | 491981  | 432418   | 0.133       | 0.982       | 0.559    | 0.881     |
| 0.80   | 51056   | 5406     | 495593  | 447945   | 0.102       | 0.989       | 0.547    | 0.904     |
| 0.85   | 33312   | 2738     | 498261  | 465689   | 0.067       | 0.995       | 0.532    | 0.924     |
| 0.90   | 3961    | 248      | 500751  | 495040   | 0.008       | 1.000       | 0.505    | 0.941     |
| 0.95   | 3       | 0        | 500999  | 498998   | 0.000       | 1.000       | 0.501    | 1.000     |
| 1.00   | 0       | 0        | 500999  | 499001   | 0.000       | 1.000       | 0.501    | NaN       |

## Problem 3.3

```
library(pROC)

AUC <- auc(microsoft$HasDetections, microsoft$P_HasDetections)
AUC

## Area under the curve: 0.6938

GINI <- 2*(AUC - 0.5)
GINI

## [1] 0.3875789
```

## Problem 3.4

Call our function from 3.2 but this time only for deciles

```
TP <- vector()
FP <- vector()
TN <- vector()
FN <- vector()
TruePos <- vector()
FalsePos <- vector()
TrueNeg <- vector()
FalseNeg <- vector()
Sensitivity <- vector()
Specificity <- vector()
Accuracy <- vector()
Precision <- vector()

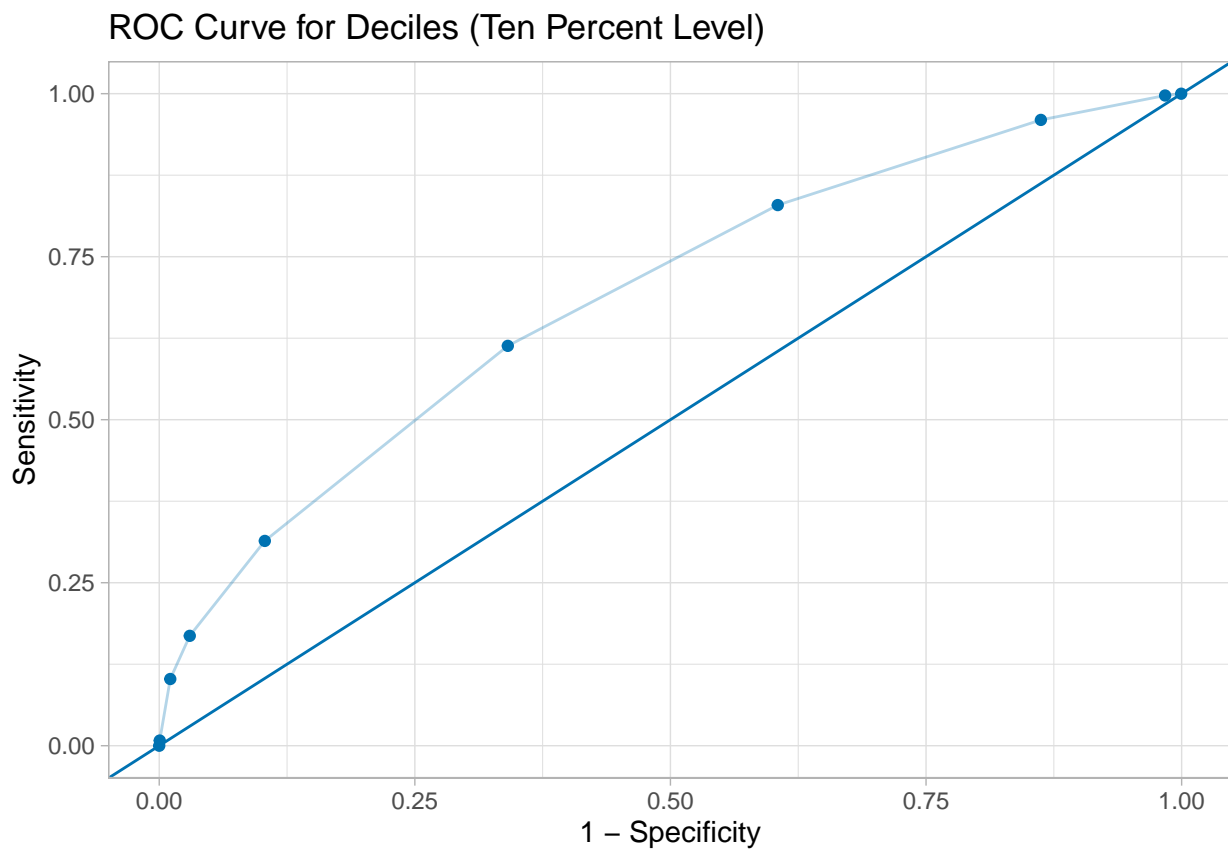
cutoff <- seq(0.1, 1, by = 0.1)
mapply(stats, cutoff)
```

Create the ROC plot by graphing 1 - Specificity vs Sensitivity with some of the data provided by our function

```
library(ggplot2)
Specificity <- 1 - Specificity
df <- data.frame(Specificity, Sensitivity)
plt <- ggplot(data = df, aes(x = Specificity, y = Sensitivity)) +
  geom_point(color = '#0072B2') +
```

```
geom_line(alpha = 0.3, color = '#0072B2') +  
geom_abline(slope = 1, intercept = 0, color = '#0072B2') +  
ggtitle(label = "ROC Curve for Deciles (Ten Percent Level)") +  
xlab("1 - Specificity") +  
ylab("Sensitivity") +  
theme_light()
```

plt



## Problem 3.5

Same process as 3.4 except this time we are working at the fifth percentile level

```
TP <- vector()
FP <- vector()
TN <- vector()
FN <- vector()
TruePos <- vector()
FalsePos <- vector()
TrueNeg <- vector()
FalseNeg <- vector()
Sensitivity <- vector()
Specificity <- vector()
Accuracy <- vector()
Precision <- vector()

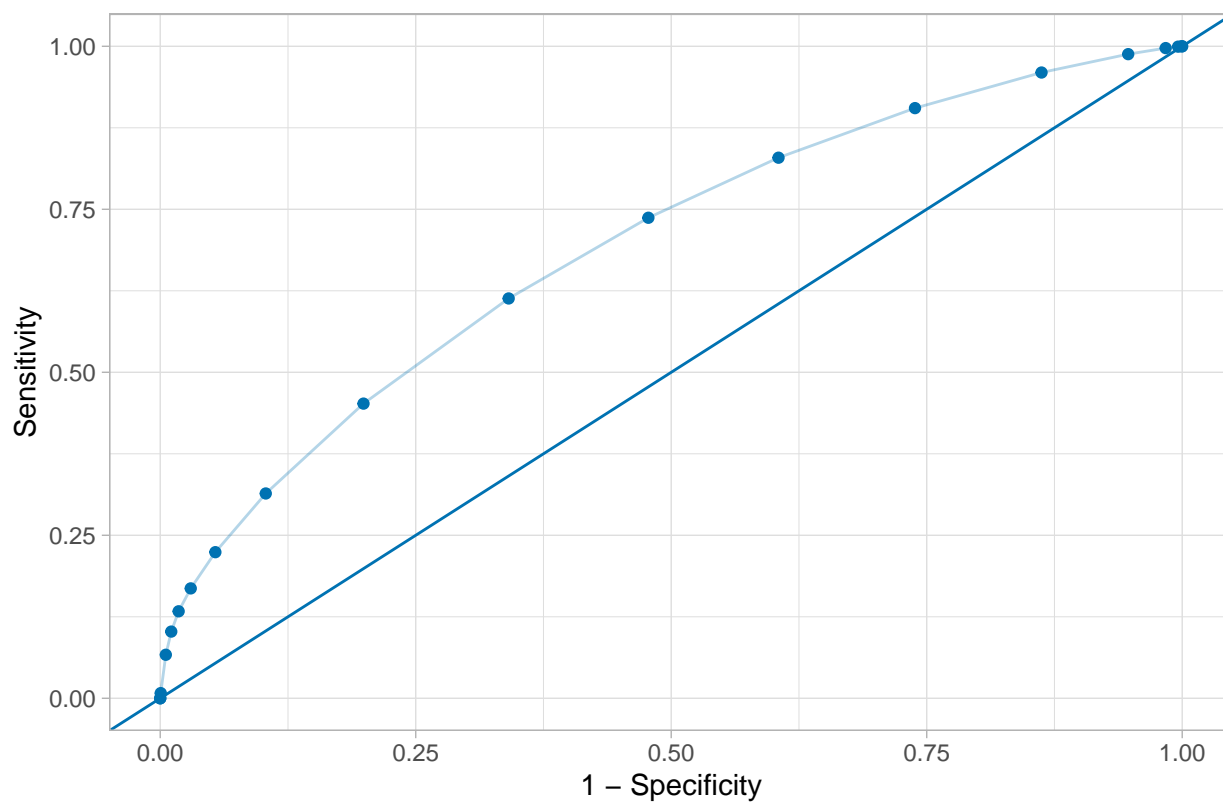
cutoff <- seq(0.05, 1, by = 0.05)
mapply(stats, cutoff)
```

```
library(ggplot2)
Specificity <- 1 - Specificity
df <- data.frame(Specificity, Sensitivity)
plt <- ggplot(data = df, aes(x = Specificity, y = Sensitivity)) +
  geom_point(color = '#0072B2') +
  geom_line(alpha = 0.3, color = '#0072B2') +
  geom_abline(slope = 1, intercept = 0, color = '#0072B2') +
  ggtitle(label = "ROC Curve for the Five Percent Level") +
```

```
xlab("1 - Specificity") +  
ylab("Sensitivity") +  
theme_light()
```

plt

ROC Curve for the Five Percent Level





## Problem 3.6

```
true_pos <- function(decile){  
  
  vec <- microsoft$HasDetections[microsoft$P_HasDetections > decile - 0.1 & microsoft$P_HasDetections <= decile + 0.1]  
  
  n <- length(vec)  
  
  count <- sum(vec == 1)  
  
  TPC <- c(TPC, count)  
  
  N <- c(N, n)  
}
```

```
total_pos <- sum(microsoft$HasDetections == 1)  
prop_pos <- total_pos / 1000000  
  
vec <- vector()  
n <- vector()  
count <- vector()  
TPC <- vector()  
N <- vector()  
  
decile <- seq(1, 0.1, -0.1)  
  
mapply(true_pos, decile)
```

```

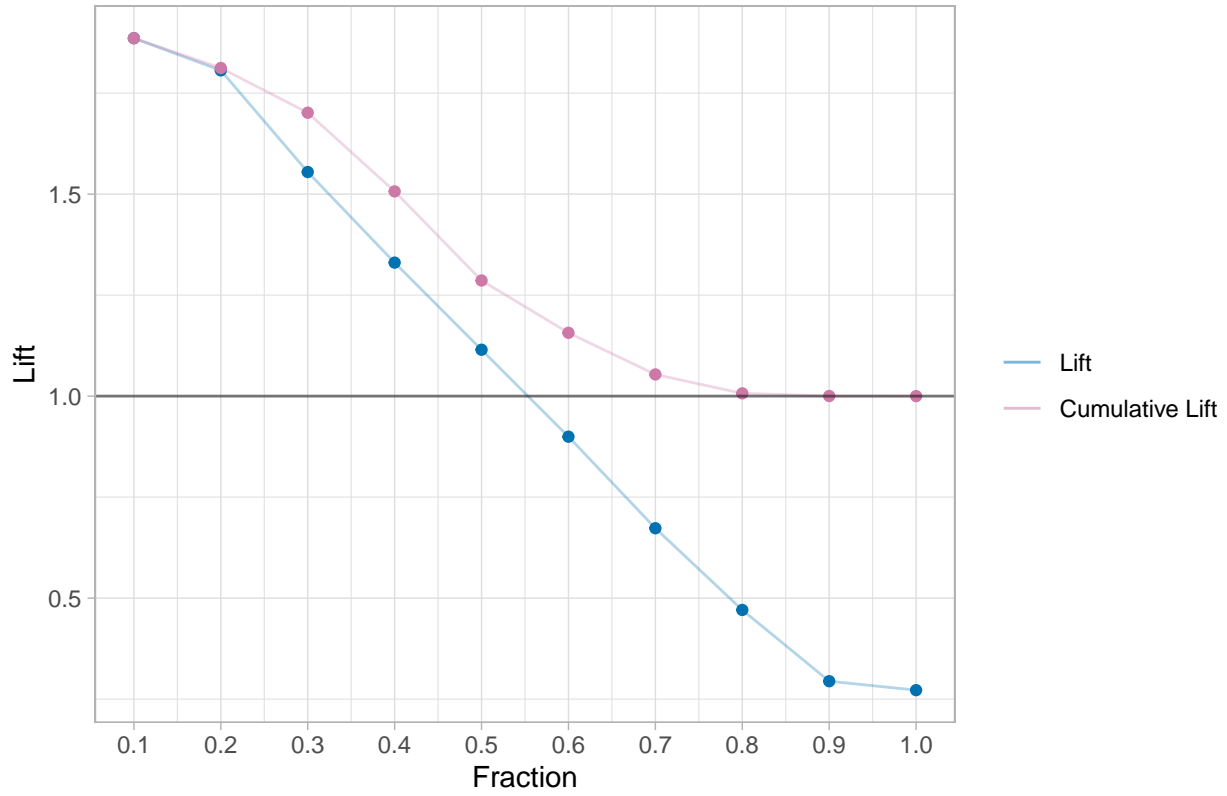
library(ggplot2)

lift <- (TPC / N) / prop_pos
new_seq <- seq(0.1, 1, 0.1)
lift_cum <- (cumsum(TPC) / cumsum(N)) / prop_pos
df <- data.frame(lift, lift_cum, new_seq)
plt <- ggplot(data = df, aes(x = new_seq)) +
  geom_point(aes(y = lift), color = '#0072B2') +
  geom_line(aes(y = lift, color = "Lift"), alpha = 0.3) +
  geom_point(aes(y = lift_cum), color = '#CC79A7') +
  geom_line(aes(y = lift_cum, color = "Cumulative Lift"), alpha = 0.3) +
  geom_hline(yintercept = 1, alpha = 0.5) +
  scale_color_manual("", breaks = c("Lift", "Cumulative Lift"), values = c('#0072B2', '#CC79A7')) +
  ggtitle(label = "Lift Chart") +
  xlab("Fraction") +
  ylab("Lift") +
  scale_x_continuous(n.breaks = 10) +
  theme_light()

plt

```

Lift Chart



## Chapter IV Exercises

### Problem 1

$$(4.2) \quad p(x) = \frac{e^{\beta_0 + \beta_1 x}}{1 + e^{\beta_0 + \beta_1 x}}$$

$$\text{So, } \frac{p(x)}{1 - p(x)}$$

$$= \frac{e^{\beta_0 + \beta_1 x}}{1 + e^{\beta_0 + \beta_1 x}} \div \frac{e^{\beta_0 + \beta_1 x}}{1 + e^{\beta_0 + \beta_1 x}}$$

$$= \frac{e^{\beta_0 + \beta_1 x}}{1 + e^{\beta_0 + \beta_1 x}} \div \frac{1 + e^{\beta_0 + \beta_1 x}}{1 + e^{\beta_0 + \beta_1 x}} - \frac{e^{\beta_0 + \beta_1 x}}{1 + e^{\beta_0 + \beta_1 x}}$$

$$= \frac{\frac{e^{\beta_0 + \beta_1 x}}{1 + e^{\beta_0 + \beta_1 x}}}{\frac{1}{1 + e^{\beta_0 + \beta_1 x}}}$$

$$(4.3) \quad \frac{p(x)}{1 - p(x)} = e^{\beta_0 + \beta_1 x}$$

## Problem 9

(a) (i)  $\frac{p(X)}{1-p(X)} = 0.37$

(ii)  $p(X) = 0.37(1 - p(X))$

(iii)  $1.37 \times p(X) = 0.37$

(iv)  $p(X) = 0.37/1.37 = 27\%$

(b) Odds =  $\frac{p(X)}{1-p(X)} = 0.16/0.84 = 0.19$