A Practical Algorithm for Topic Modling with Provable Guarantees

Sanjeev Arora Rong Ge Yoni Halpern David Mimno Ankur Moitra David Sontag Yihcen Wu Michael Zhu

Presented by: Vanush Vaswani and Kristy Hughes

- Introduction
- Topic Modelling
- 3 Algorithm
- 4 Efficiently Finding Anchor Words
- **5** Topic Recovery via Bayes' Rule
- **6** Experimental Results
- Conclusion

Information Overload





Topic Recovery Results Conclusion

Effective Organisation

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Topics









Introduction

- 2 Topic Modelling
- Algorithm
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Topics

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Topics

```
gene 0.04
dna 0.02
genetic 0.01
```

```
life 0.02
evolve 0.01
organism 0.01
```

```
brain 0.04
neuron 0.02
nerve 0.01
```

```
data 0.02
number 0.02
computer 0.01
```

Topics are distributions over words

Topic Models 000000

Anchor Selection

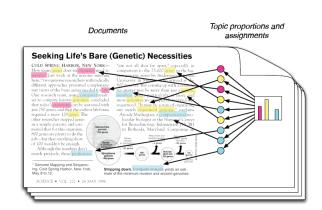
Topic Recovery

Conclusion

Results

Documents

Documents have distribution of topics



Topic Modelling

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Topics

gene dna	0.04 0.02
genetic	0.01

	_

life	0.02
evolve organism	0.01
organism	0.01
	_

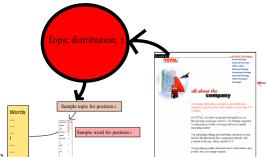
brain	0.04
neuron	0.02
nerve	0.01

Topic proportions and **Documents** assignments Seeking Life's Bare (Genetic) Necessities COLD SPRING HARBOR, NEW YORK-"are not all that far apart," especially in How many genes does an organism need to survive! Last week at the genome meeting comparison to the 75,000 genes in the hu enome, notes Siv Anders here, "two genome researchers with radically University in S different approaches presented complementary views of the basic genes needed for life sus answer may be more than ius One research team, using computer analyses to compare known genomes, concluded that today's organisms can be sustained with just 250 genes, and that the earliest life forms any newly sequenced genome," explains required a mere 128 genes. The other researcher mapped genes lecular biologist at the National Center for Biotechnology Information (NCBI) in a simple parasite and estimated that for this organism. in Bethesda, Maryland, Comparing 800 genes are plenty to do the of 100 wouldn't be enough. Although the numbers don't match precisely, those predictions * Genome Mapping and Sequencing, Cold Spring Harbor, New York, Stripping down. Computer analysis yields an esti-May 8 to 12. mate of the minimum modern and ancient genomes SCIENCE • VOL. 272 • 24 MAY 1996

Task

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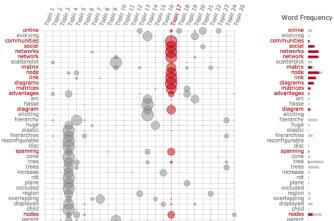
- Assume documents are generated by probabilistic model with unknown variables
- Infer hidden structure onto document
- Situate new document into model



TODO: Redo pic

Word-topic Matrix

Extracted: Word-topic matrix



Aim: Find document-topic matrix

Results

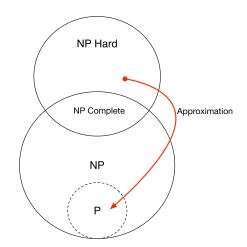
Anchor Words

- Word-topic distributions are separable
- There is a word unique to each topic
- Indicates document is partially about that topic
- Can learn parameters in polynomial time provided there is a large enough number of documents

Approximate Inference & Provable Guarantees

- Document-topic inference:
 - NP-hard

- Approximate techniques
- Provably polynomial-time?



- Topic Recovery

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Algorithm

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Input: Corpus \mathcal{D} , Number of topics K

Output: Word-topic matrix A, topic-topic matrix R

- Compute word-word co-occurrence matrix
- Normalize the matrix
- **3** Find anchor words
- 4 Recover topics

Assumptions:

- Topics may be correlated
- Word-topic distributions are separable

Contributions

- Anchor Selection
 - Combinatorial rather than ILP
 - Stable in the presence of noise
 - polynomial sample complexity
- 2 Recovery step
 - Previous matrix-inversion approach sensitive to noise
 - Replaced with Gradient-based inference
- 3 Empirical comparison of algorithms

Results

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Word-word co-occurrence matrix

	bank	California	Canada	career	careers	employers	employment	federal	human	dot	sqof	listings	openings	opportunities	positions	recruiters	resources	resume	resumes	retirement	search	state	texas	unemployment	work
bank																									Н
California																									П
Canada	1																								
career	3	3																							П
careers			2	9																					П
employers		2		11	7																				П
employment	3	26	22	66	10	16																			
federal	1	1	5		1		11																		
human		4	12	1	1			4																П	П
job	34	14	2	49	8	13	92	13	2																
jobs		18	6	62	11	27	204	19	2	74															
listings		4	2	15	4	9	68	2	55	44															
openings		4		7	2	9	28			49	30														Ш
opportunities	4	8	3	51	9	13	181	9		84	106	25	19												
positions		1		8	2	10	19			16	20	9	13	21											Ш
recruiters				10	4	3	9			5	4	2	2	5	2										
resources		4	12		1			4	74	3	2														Ш
resume		4	3	5		2	3	1	1	10	3			1	2	1									Ш
resumes				8	3	3	11			5	16	1		8	5			15							Ш
retirement		1	1						3			2		1											Ш
search			3	4	6			10			18	6		6	2			3	1						Ш
state			4	1			18		1	12	7	6		3			1			2					Ш
texas	2			1			18			12	6		1	2						9					Ш
unemployment																						2	2		Ш
work			2	1		3	3	2		2	8	2	4	7	5				1			1	2		



o Topic Models

 $\begin{array}{ccc} \operatorname{Algo} & \operatorname{Anchor Selection} \\ \circ \circ & \circ \bullet \circ \circ \end{array}$

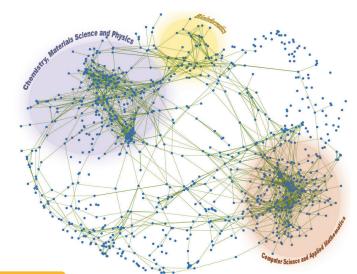
Topic Recovery

Results

onclusion

Words as vertices

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Algo Anchor Selection

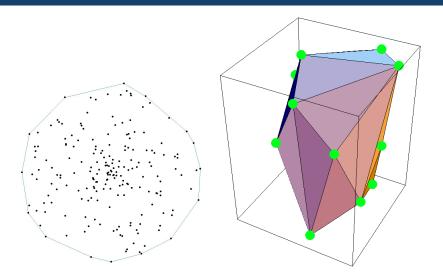
Topic Recovery

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onclusion

Convex Hull

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- Efficient for 2 dimensions $O(n \log n)$
- Inefficient for n > 2 dimensions
- Complexity depends on method and approximation used
- Previous method: ILP
- New method: Recursive greedy
 - Compute subspace span of current convex hull
 - 2 Find point furthest from this sub-span
 - Add point to convex hull
 - Repeat until K points found

TODO: Work out how the whole convex hull - words as vertices work. I think what we have here is wrong because there is no approximation

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Topic Recovery Task

- Recovers the topics
- Represented as topic-word distributions
- · Topic uniquely identified by anchor word

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1 Discard rows not containing anchor words from word-word co-occurrence matrix (O)

- 2 Permute matrix into a diagonal matrix
- **3** We know that $Q = ARA^T$ where A is the word-topic matrix and R is the topic-topic matrix
- **4** Solve $Q = ARA^T$ using matrix inversion

Word-word co-occurrence probability matrix

For an anchor word (row) in the co-ocurrence matrix

$$Q_{s_k,j} = \sum_{k'} p(z_1 = k'|w_1 = s_k) p(w_2 = j|z_1 = k')$$
= 1 because of the anchor word property

$$= p(w_2 = j|z_1 = k) = C_{i,k}$$

For any other row
$$\bar{Q}_{i,j} = \sum_k p(z_1 = k|w_1 = i)p(w_2 = j|z_1 = k)$$
 But this is clearly a convex combination of anchor

words

$$\bar{Q}_{i,j} = \sum_{i} C_{i,k} \bar{Q}_{s,k}$$

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New method

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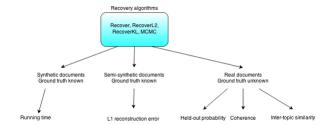
- Row normalize Q into Q
- Recover A and R using Bayes rule

$$p(w_1 = i|z_1 = k) = \frac{p(z_1 = k|w_1 = i)p(w_1 = i)}{\sum_i p(z_1 = k|w_1 = i')p(w_1 = i')}$$

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Experiments

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Metrics

- Ground truth known
 - Reconstruction error
- Ground truth unknown
 - Held out probability probability of an unseen document under the learned model
 - Coherence measure of semantic quality
 - Inter-topic similarity measure of uniqueness of topics

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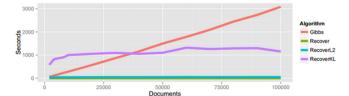


Figure 1. Training time on synthetic NIPS documents.

Results

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Results - Reconstruction error

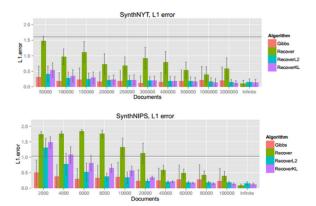


Figure 2. ℓ_1 error for learning semi-synthetic LDA models with K = 100 topics (**top**: based on NY Times, **bottom**: based on NIPS abstracts). The horizontal lines indicate the ℓ_1 error of K uniform distributions.

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Results - Held out probability, coherence and unique words

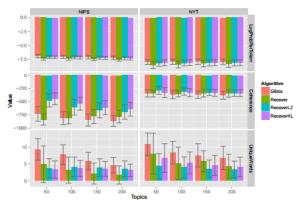


Figure 5. Held-out probability (per token) is similar for RecoverKL, RecoverL2, and Gibbs sampling. RecoverKL and RecoverL2 have better coherence, but fewer unique words than Gibbs. (Up is better for all three metrics.)

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Summary

- New algorithms for topic recovery have been presented
 - Empirical results compare to MCMC
 - Uses anchor word assumption and Bayes' rule for theoretical and empirical performance improvements
- Simple to implement, maintains provable guarantees
- Attractive feature: Running time independent of the size of the corpus

Future Work

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- Use output of algorithms for further optimization
- Parallel implementations

Comments

- Main contribution: algorithms for topic inference with provable guarantees for running time
 - Effect: running time effectively independent of corpus size

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Results

Thanks!

Any questions please email either of us:

Vanush Vaswani

vvas9619@uni.sydney.edu.au

Kristy Hughes

khug2372@uni.sydney.edu.au