

$$\lambda = 1$$

$$A - E = \begin{pmatrix} 12 & 14 & 4 \\ 14 & 23 & 18 \\ 4 & 18 & 28 \end{pmatrix} \xrightarrow[\substack{\text{III} \div 2 \\ \text{I} \leftrightarrow \text{II}}]{\substack{\text{III} \div 2 \\ \text{I} \leftrightarrow \text{II}}} \begin{pmatrix} 2 & 9 & 14 \\ 14 & 23 & 18 \\ 12 & 14 & 4 \end{pmatrix} \xrightarrow[\substack{\text{III} - 6\text{I}}]{\substack{\text{II} - 4\text{I}}} \begin{pmatrix} 2 & 9 & 14 \\ 0 & -40 & -80 \\ 0 & -40 & -80 \end{pmatrix} \xrightarrow[\substack{\text{III} = \text{II} \\ \lambda_0}]{\substack{\text{II} \div -40}} \begin{pmatrix} 2 & 9 & 14 \\ 0 & 1 & 2 \\ 0 & 0 & 0 \end{pmatrix} \rightarrow$$

$$\begin{aligned} &\xrightarrow{\text{I} - 9\text{II}} \begin{pmatrix} 1 & 0 & -2 \\ 0 & 1 & 2 \\ 0 & 0 & 0 \end{pmatrix} \Rightarrow V_1 = \left\langle \begin{pmatrix} 2 \\ -2 \\ 1 \end{pmatrix} \right\rangle \Rightarrow v_3 = \begin{pmatrix} 2/3 \\ -2/3 \\ 1/3 \end{pmatrix} \\ &\text{I} \div 2 \end{aligned}$$

Ответ : разложение

$$A = C D C^T = \underbrace{\begin{pmatrix} 1/3 & -2/3 & 2/3 \\ 2/3 & -1/3 & -2/3 \\ 2/3 & 2/3 & 1/3 \end{pmatrix}}_C \underbrace{\begin{pmatrix} 49 & 0 & 0 \\ 0 & 16 & 0 \\ 0 & 0 & 1 \end{pmatrix}}_D \underbrace{\begin{pmatrix} 1/3 & 2/3 & 2/3 \\ -2/3 & -1/3 & 2/3 \\ 2/3 & -2/3 & 1/3 \end{pmatrix}}_{C^T}$$