
COMP5111 – Fundamentals of Software Testing and Analysis

Program-based Mutation Testing



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Slides adapted from www.introsoftwaretesting.com by Paul Ammann & Jeff Offutt

Background of Mutation Testing

- Also known as **mutation analysis**

- Proposed by Richard Lipton as a student in 1971.
- Richard DeMillo, Richard Lipton and Fred Sayward. Hints on test data selection: Help for the practicing programmer. IEEE Computer 11(4), 1978.

- Application (mutation testing)

- Generate a pool of mutants by modifying a program slightly
- Measure the adequacy of a test suite by counting the proportion of mutants killed (mutation coverage)

- Alternative applications (mutation analysis)

- Use mutants to seed faults artificially, especially to estimate recall
- Generate mutants for program repair

Using the Syntax to Generate Mutants

- Lots of software artifacts follow strict syntax rules
- Syntactic rules can come from many sources
 - Programs → Program-based
 - Integration elements → Integration
 - Design documents → Model-based
 - Input descriptions → Input-based (a major fuzzing approach)
- Mutants are created with two general goals
 - Cover the syntax in some way
 - Cover various semantic/behavioral differences

Program-based Mutation Testing

Original Method

```
int Min (int A, int B)
{
    int minVal;
    minVal = A;
    if (B < A)
    {
        minVal = B;
    }
    return (minVal);
} // end Min
```

6 mutants

Each represents a
separate program

With Embedded Mutants

```
int Min (int A, int B)
{
```

```
    int minVal;
    minVal = A;
```

```
Δ 1 minVal = B;
```

```
    if (B < A)
```

```
Δ 2 if (B > A)
```

```
Δ 3 if (B < minVal)
```

```
{
```

```
    minVal = B;
```

```
Δ 4 Bomb ();
```

```
Δ 5 minVal = A;
```

```
Δ 6 minVal = failOnZero (B);
```

```
}
```

```
    return (minVal);
```

```
} // end Min
```

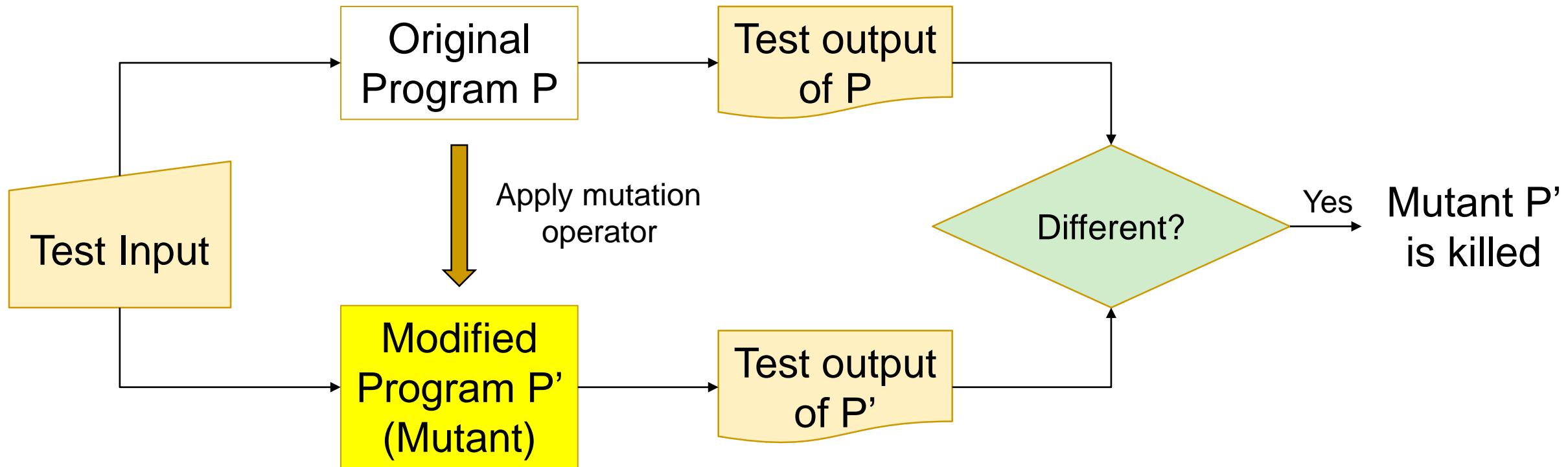
*Replace one variable
with another*

Changes operator

*Immediate runtime
failure ... if reached*

*Immediate runtime
failure if B==0 else
does nothing*

Process of Program-based Mutation Testing



The goal is to check if the test input can detect a syntactic coding mistake in P

Killing Mutants

Given a mutant $m \in M$ for a (ground string) program P and a test t , t is said to kill m if and only if the output of t on P is different from the output of t on m .

- If mutation operators are designed well, the resulting tests will be very powerful
- Different operators must be defined for different programming languages and goals
- Testers can keep adding tests until all mutants have been killed
 - Dead mutant : A test case has killed it
 - Stillborn mutant : **Syntactically illegal**
 - Trivial mutant : Almost every test can kill it
 - Equivalent mutant : No test can kill it (equivalent to original program)

Syntax-Based Coverage Criteria

Mutation Coverage (MC) : For each $m \in M$, TR contains exactly one requirement, to kill m .

- The RIP model from Lecture 1:
 - Reachability : The test causes the faulty statement to be reached (in mutation – the mutated statement)
 - Infection : The test causes the faulty statement to result in an incorrect state
 - Propagation : The incorrect state propagates to incorrect output
- The RIP model leads to two variants of mutation coverage ...

Syntax-Based Coverage Criteria

Reachability
Infection
Propagation

- Strongly Killing Mutants (satisfies RIP):
 - Given a mutant $m \in M$ for a program P and a test t , t is said to strongly kill m if and only if the output of t on P is different from the output of t on m
- Weakly Killing Mutants (satisfies RI):
 - Given a mutant $m \in M$ that modifies a location l in a program P , and a test t , t is said to weakly kill m if and only if the state of the execution of P on t is different from the state of the execution of m immediately on t after l
 - Weakly killing satisfies reachability and infection, but not propagation

Reachability
Infection

Weak Mutation

Weak Mutation Coverage (WMC) : For each $m \in M$, TR contains exactly one requirement, to weakly kill m .

- **Weak mutation** is so named because it is easier to kill mutants under this assumption (e.g., a function that returns void or bool)
- Weak mutation also requires less analysis
- Some mutants can be killed under weak mutation but not under strong mutation (no propagation)
- In practice, there is little difference
 - A test suite that fulfills weak mutation coverage can detect most of the faults detected by a test suite that fulfills strong weak mutation coverage

Strong vs Weak Mutation Example

- Mutant 1 in the Min() example is:
 - The complete test specification to kill Mutant 1:
 - Reachability : *true* // Always get to that statement
 - Infection : $A \neq B$
 - Propagation: $(B < A) = \text{false}$ // Skip the next assignment
 - Full Test Specification : $\text{true} \wedge (A \neq B) \wedge ((B < A) = \text{false})$
 $\equiv (A \neq B) \wedge (B \geq A)$
 $\equiv (B > A)$
- $(A = 5, B = 3)$ will weakly kill mutant 1, but not strongly

Original Method

```
int Min (int A, int B)
{
    int minVal;
    minVal = A;
    if (B < A)
        minVal = B;
    return (minVal);
} // end Min
```

Mutant 1

```
int Min (int A, int B)
{
    int minVal;
    minVal = B;
    if (B < A)
        minVal = B;
    return (minVal);
} // end Min
```

Equivalent Mutation Example

- Mutant 3 in the Min() example is equivalent:
- The infection condition is:
“(B < A) != (B < minVal)”
- However, the previous statement was:
“minVal = A”
 - Substituting, we get: “(B < A) != (B < A)”
- Thus no input can kill this mutant

Original Method

```
int Min (int A, int B)
{
    int minVal;
    minVal = A;
    if (B < A)
        minVal = B;
    return (minVal);
} // end Min
```

Mutant 3

```
int Min (int A, int B)
{
    int minVal;
    minVal = A;
    if (B < minVal)
        minVal = B;
    return (minVal);
} // end Min
```

Strong Versus Weak Mutation

```
1  boolean isEven (int X)
2  {
3      if (X < 0)
4          X = 0 - X;
5      if (float) (X/2) == ((float) X) / 2.0
6          return (true);
7      else
8          return (false);
9  }
```

Reachability : $X < 0$

Infection : $X \neq 0$

$(X = -6)$ will kill mutant 4 under weak mutation

Propagation :

$((\text{float}) ((0-X)/2) == ((\text{float}) 0-X) / 2.0)$

$\neq ((\text{float}) (0/2) == ((\text{float}) 0) / 2.0)$

That is, X is not even ...

Thus $(X = -6)$ does not kill the mutant under strong mutation

Mutation Coverage as a Stronger Coverage Criterion

```
1 package demo;
2 public class Sample3 {
3     public static void sample3(int y) {
4         int sum = 0;
5         for (int i = y; i < 15; i=i+1) {
6             sum = sum + i;
7         }
8         if (sum > 4 + y)
9             System.out.println("hello");
10        if (sum < 2) {
11            System.out.println("true");
12        } else {
13            System.out.println("false");
14        }
15        System.out.println("--");
16    }
17 }
```

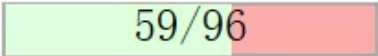
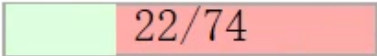
- Randoop can easily generate test cases achieving 100% line coverage.
- Are we done?

Mutation Coverage as a Stronger Coverage Criterion

Pit Test Coverage Report

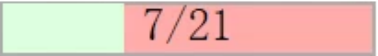
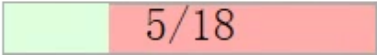
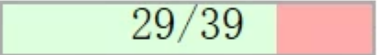
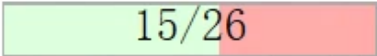
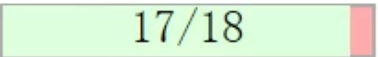
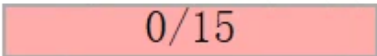
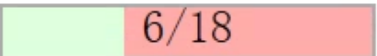
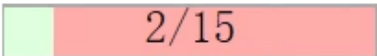
Package Summary

default

Number of Classes	Line Coverage	Mutation Coverage
4	61% 	30% 

Coverage achieved by
tests generated by
Randoop on four classes

Breakdown by Class

Name	Line Coverage	Mutation Coverage
Mono.java	33% 	28% 
Poly.java	74% 	58% 
Sample3.java	94% 	0% 
TestLoop.java	33% 	13% 

Mutation Coverage as a Stronger Coverage Criterion

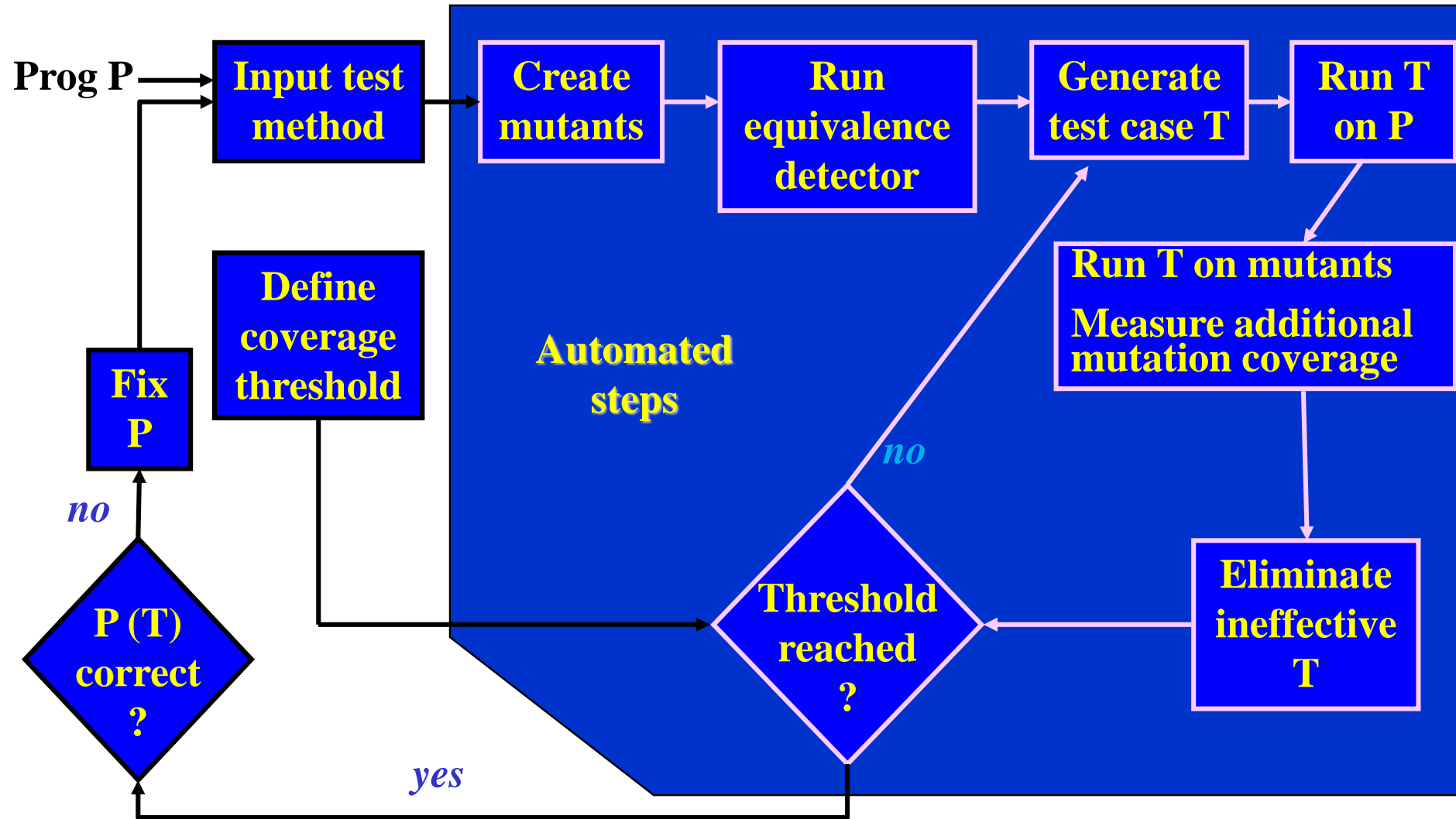
```
1  package demo;
2  public class Sample3 {
3      public static void sample3(int y) {
4          int sum = 0;
5          3 for (int i = y; i < 15; i=i+1) {
6              1 sum = sum + i;
7          }
8          3 if (sum > 4 + y)
9              1 System.out.println("hello");
10         2 if (sum < 2) {
11             1 System.out.println("true");
12         } else {
13             1 System.out.println("false");
14         }
15         1 System.out.println("--");
16     }
17 }
```

Mutation Coverage by Randoop and Evosuite

	Name	Line Coverage	Mutation Coverage
Coverage achieved by Randoop	TestLoop.java	33% 	12% 
Coverage achieved by Evosuite	TestLoop.java	95% 	24% 

Mutation coverage is generally considered the finest coverage criterion in practice.

Testing Programs with Mutation



Why Mutation Works

Fundamental Premise of Mutation Testing

If the software contains a fault, there will usually be a set of mutants that can only be killed by a test case that also detects that fault

- This is not absolute !
- The mutants guide the tester to a very effective set of tests
- A very challenging problem :
 - Find a fault and a set of mutation-adequate tests that do not find the fault
- Of course, its effectiveness depends on the mutation operators ...

Designing Mutation Operators

- At the method level, mutation operators for different programming languages are similar
- Mutation operators do one of two things:
 - Mimic typical programmer mistakes (incorrect variable name)
 - Encourage common test heuristics (cause expressions to be 0)
- Researchers design lots of operators, then experimentally select the most useful

Effective Mutation Operators

If tests that are created specifically to kill mutants created by a collection of mutation operators $O = \{o1, o2, \dots\}$ also kill mutants created by all remaining mutation operators with very high probability, then O defines an effective set of mutation operators

- Refer to Appendix for 11 commonly used mutation operators

Subsumption of Other Criteria

- Mutation is widely considered the **strongest** test criterion
 - And most **expensive** !
- Mutation **subsumes** the following criteria by including specific mutation operators
 - Node coverage
 - Edge coverage
 - Clause coverage
 - General active clause coverage
 - Correlated active clause coverage
 - All-defs data flow coverage
- Recent studies find that strong mutation is more correlated to fault detection than weak mutation

Mutation Testing

- The number of test requirements for mutation depends on two things
 - The syntax of the artifact being mutated
 - The set of mutation operators
- Mutation testing is difficult to apply **manually**
- Mutation testing is very effective – considered the “**golden standard**” of testing
- Mutation testing is often used to **evaluate** the adequacy of test suites selected for other criteria
 - By mutation coverage of the test suites satisfying a criterion C

Questions About Mutation

- Should more than one operator be applied at the same time ?
 - ❑ Should a mutated string contain one mutated element or several?
 - ❑ Almost certainly not – multiple mutations can interfere with each other
 - ❑ Extensive experience with program-based mutation indicates not
- Should every possible application of a mutation operator be considered ?
 - ❑ Necessary with program-based mutation
- Mutation operators exist for several **languages**
 - ❑ Several programming languages (*Fortran, Lisp, Ada, C, C++, Java*)
 - ❑ Specification languages (*SMV, Z, Object-Z, algebraic specs*)
 - ❑ Modeling languages (*Statecharts, activity diagrams*)
 - ❑ Input grammars (*XML, SQL, HTML*)

How well are mutation faults coupled with real faults?

EMPIRICAL STUDY

Are mutants valid substitutes of real faults?

A study was published in FSE14

- 357 real faults (480 reproducible failing tests) in 5 open-source projects
 - Chart, Closure, Math, Time, Lang (Defect4J)
 - A total of 211K lines of code were tested
- 230,000 mutants generated for these faulty program versions
- 35,141 generated test suites detecting 198 of the real faults
 - 28,318 test suites generated by Evosuite (avg. size 68), detecting 182 faults
 - 3,387 test suites generated by Randoop (avg. size 6,929), detecting 90 faults
 - 3,436 test suites generated by JCrasher (avg. size 47,928), detecting 2 faults

Rene Just, et al.: Are Mutants a Valid Substitute for Real Faults in Software Testing? FSE 2014: 654-665.

Are mutants valid substitutes of real faults?

■ Findings:

- ❑ 263 (73%) real faults are coupled to some mutants, i.e., tests killing these mutants can expose the coupled real faults
 - Real faults are more often coupled to mutants generated by **conditional/relational operator replacement** and **statement deletion**
- ❑ 32 (10%) real faults requires stronger or new mutation operators
- ❑ 63 (17%) real faults involve algorithmic changes or code deletion. They are not coupled to any mutants even with an extended set of mutation operators
- ❑ 258/480 failing tests kill 2 new mutants beyond those killed by passing tests written by developers
- ❑ 222/480 failing tests kill more than 2 new mutants (avg. 28) beyond those killed by passing tests written by developers

Implication?

Rene Just, et al.: Are Mutants a Valid Substitute for Real Faults in Software Testing? FSE 2014: 654-665.

How about using mutation scores on C programs?

- [Chekam et al., ICSE17]

- Mutation testing provides valuable guidance for improving test suites and revealing real faults
- There is a strong connection between mutation score increase and fault detection at higher score levels

- [Papadakis et al., ICSE18]

- When the mutation score is low, its correlation with fault detection is weak
- When the mutation score is high, its correlation with fault detection is strong

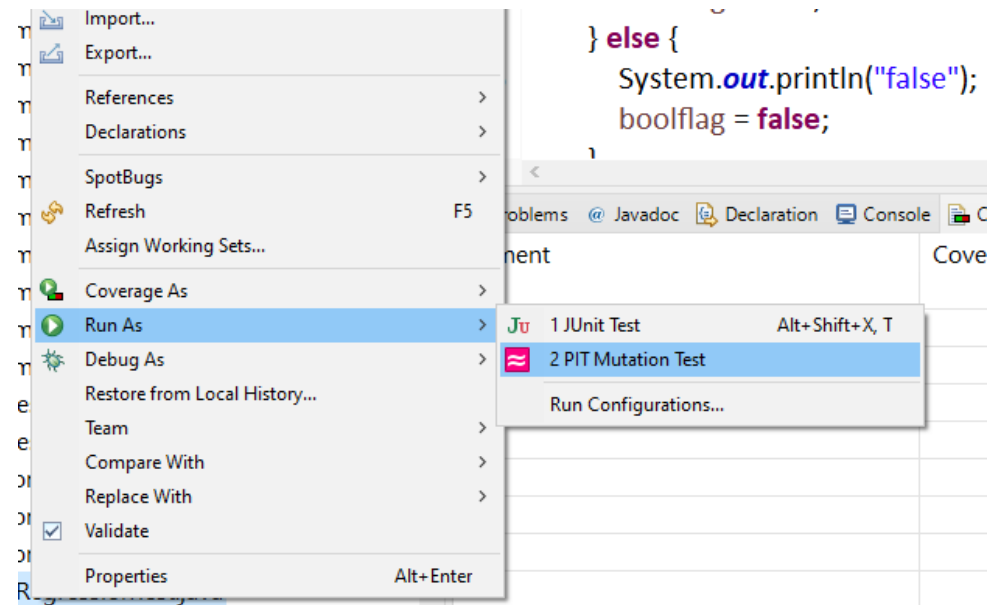
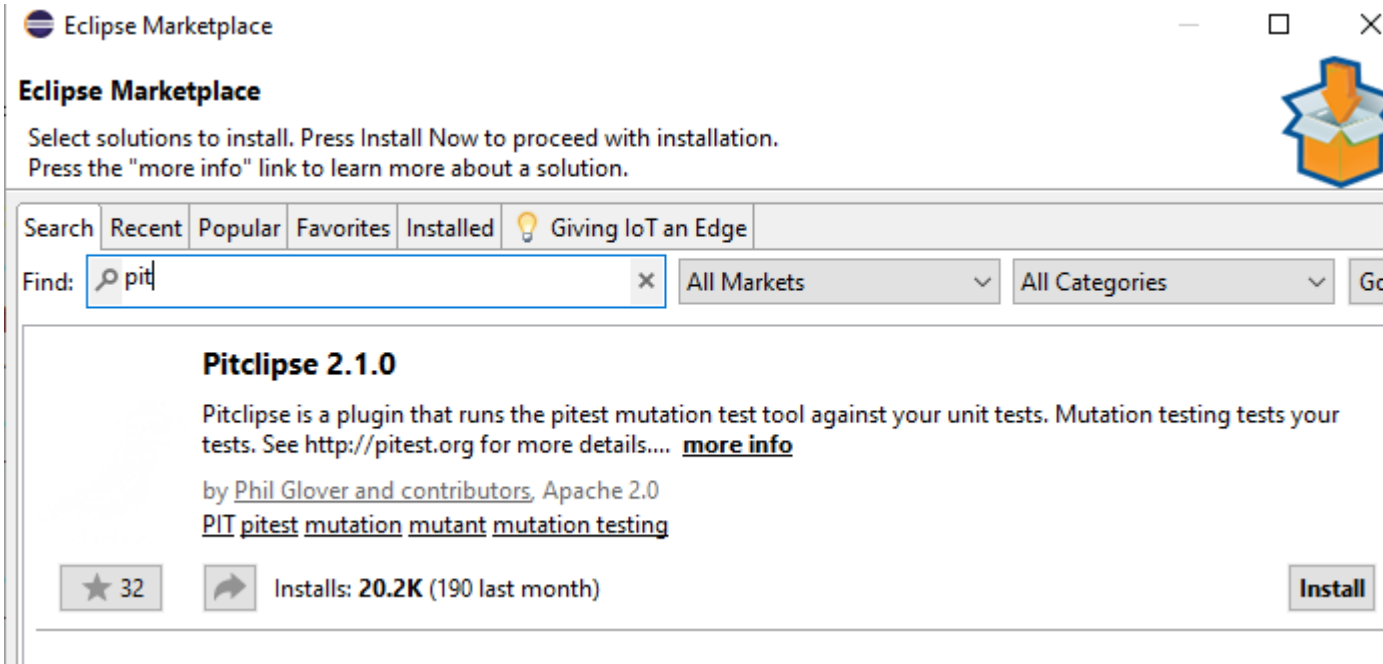
- Threat to validity

- Since mutation coverage is very fine, a higher mutation score often require a larger test suite
- The correlation between mutation score and fault detection is partially derived from the large test suite size

Tool – PIT / Pitclipse

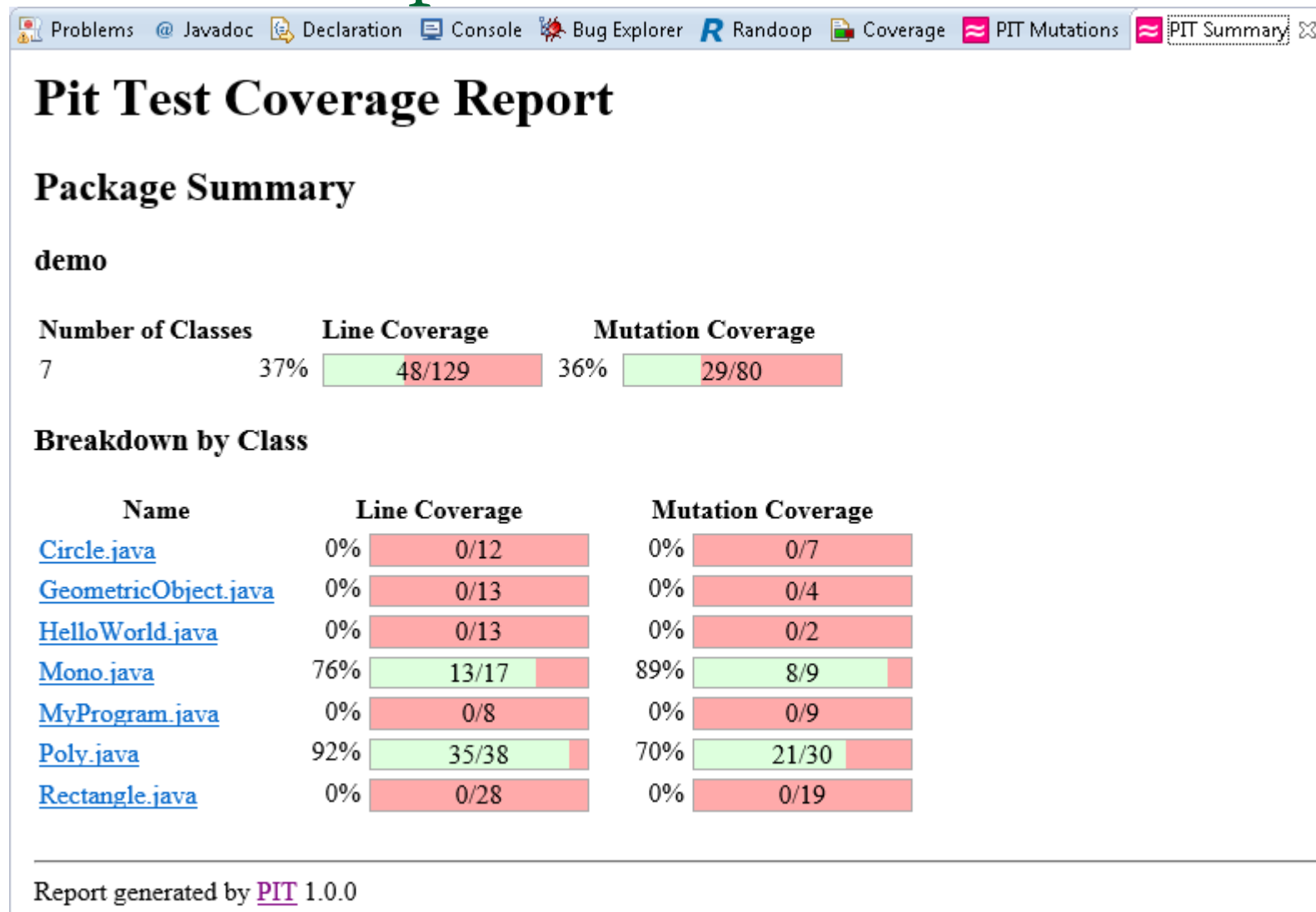
- Check mutation coverage of a given test suite.
- Install Pitclipse at Eclipse Market Place.
- Select the test suite and run as PIT Mutation Test.
- Click **PIT Mutations** to list all generated mutants.
- Click **PIT Summary** to find out proportion of mutants killed by the selected test suite.
- More information: <https://pitest.org/>
- Video: <https://www.taringamberini.com/en/blog/presentation/mutation-testing-with-pit/>

Pitclipse at Eclipse Marketplace



If you fail to install Pitclipse plugin directly at Eclipse Market, use the Pitclipse software update site address under installation of new software: <https://pitest.github.io/pitclipse-releases/>

Tool – PIT / Pitclipse



Appendix

For reference only

Mutation Operators for Java

1. ABS — Absolute Value Insertion:

Each arithmetic expression (and subexpression) is modified by the functions *abs()*, *negAbs()*, and *failOnZero()*.

2. AOR — Arithmetic Operator Replacement:

Each occurrence of one of the arithmetic operators $+$, $-$, $*$, $/$, and $\%$ is replaced by each of the other operators. In addition, each is replaced by the special mutation operators *leftOp*, and *rightOp*.

3. ROR — Relational Operator Replacement:

Each occurrence of one of the relational operators ($<$, \leq , $>$, \geq , $=$, \neq) is replaced by each of the other operators and by *falseOp* and *trueOp*.

Mutation Operators for Java (2)

4. *COR* — *Conditional Operator Replacement*:

Each occurrence of one of the logical operators (and - &&, or - || , and with no conditional evaluation - &, or with no conditional evaluation - |, not equivalent - ^) is replaced by each of the other operators; in addition, each is replaced by falseOp, trueOp, leftOp, and rightOp.

5. *SOR* — *Shift Operator Replacement*:

Each occurrence of one of the shift operators <<, >>, and >>> is replaced by each of the other operators. In addition, each is replaced by the special mutation operator leftOp.

6. *LOR* — *Logical Operator Replacement*:

Each occurrence of one of the logical operators (bitwise and - &, bitwise or - |, exclusive or - ^) is replaced by each of the other operators; in addition, each is replaced by leftOp and rightOp.

Mutation Operators for Java (3)

7. *ASR* — *Assignment Operator Replacement*:

Each occurrence of one of the assignment operators (`+=`, `-=`, `*=`, `/=`, `%=`, `&=`, `|=`, `^=`, `<<=`, `>>=`, `>>>=`) is replaced by each of the other operators.

8. *UOI* — *Unary Operator Insertion*:

Each unary operator (arithmetic `+`, arithmetic `-`, conditional `!`, logical `~`) is inserted in front of each expression of the correct type.

9. *UOD* — *Unary Operator Deletion*:

Each unary operator (arithmetic `+`, arithmetic `-`, conditional `!`, logical `~`) is deleted.

Mutation Operators for Java

10. SVR — Scalar Variable Replacement:

Each variable reference is replaced by every other variable of the appropriate type that is declared in the current scope.

11. BSR — Bomb Statement Replacement:

Each statement is replaced by a special Bomb() function.

Further Reading

- Ming Wen, Yepang Liu, Rongxin Wu, Xuan Xie, Shing-Chi Cheung and Zhendong Su: Exposing Library API Misuses via Mutation Analysis. In International Conference on Software Engineering, Technical Research Paper, 2019
- Xiangjuan Yao, Mark Harman, Yue Jia: A study of equivalent and stubborn mutation operators using human analysis of equivalence. ICSE 2014: 919-930
- Yue Jia, Mark Harman: An Analysis and Survey of the Development of Mutation Testing. IEEE Trans. Software Eng. 37(5): 649-678 (2011)
- David Schuler, Valentin Dallmeier, Andreas Zeller: Efficient mutation testing by checking invariant violations. ISSTA 2009: 69-80
- Rene Just, et al.: Are Mutants a Valid Substitute for Real Faults in Software Testing? FSE 2014: 654-665.