

# Indian Institute of Technology Jodhpur

## Signals and Systems

### EEL2010 Assignment 2

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1. Consider a scenario where we want to transmit (send) an digital image  $f(m, n)$  (where  $m, n \in \mathbb{Z}$ ) over a communication channel (link)  $C$ . Let  $f$  be of size full HD i.e.  $1920 \times 1080$  samples (1920 columns and 1080 rows), and it is provided as a png file (“f.png”). However, due to constraints, we can only transmit  $960 \times 540$  samples via the said channel  $C$ . Thus, we need to reduce the number of samples in  $f$  by a factor of 2 along row and column. This operation is known as downsampling. Let the downsampled image be denoted by  $g(m, n)$  which is sent over the channel. On the receiver side, the received image  $g$  is upsampled i.e. the number of samples are increased by a factor 2 along rows and columns. Let  $g_u$  denote the upsampled signal. Now, consider the following tasks:
  - (a) Task 1: Obtain  $g$ , by simply taking every alternate sample along rows and columns of  $f$ . Obtain,  $g_u$  by upsampling  $g$  (use interpolation). Now compare  $f$  and  $g$  visually.
  - (b) Task 2: Apply a moving average filter on  $f$ . That is, replace each sample value in  $f$  by the average of samples in a  $3 \times 3$  block. Let the resultant image be  $f_m$  which is still full HD in resolution. Now, obtain  $g$  by simply taking every alternate sample along rows and columns of  $f_m$ . Obtain,  $g_u$  by upsampling  $g$  (use interpolation). Now compare  $f$  and  $g$  visually.

In which task, Task 1 or Task2, does the upsampled image  $g_u$  is visually closer to  $f$  and why? Does your answer hold for any arbitrary image  $f$ ? Explain. [10]