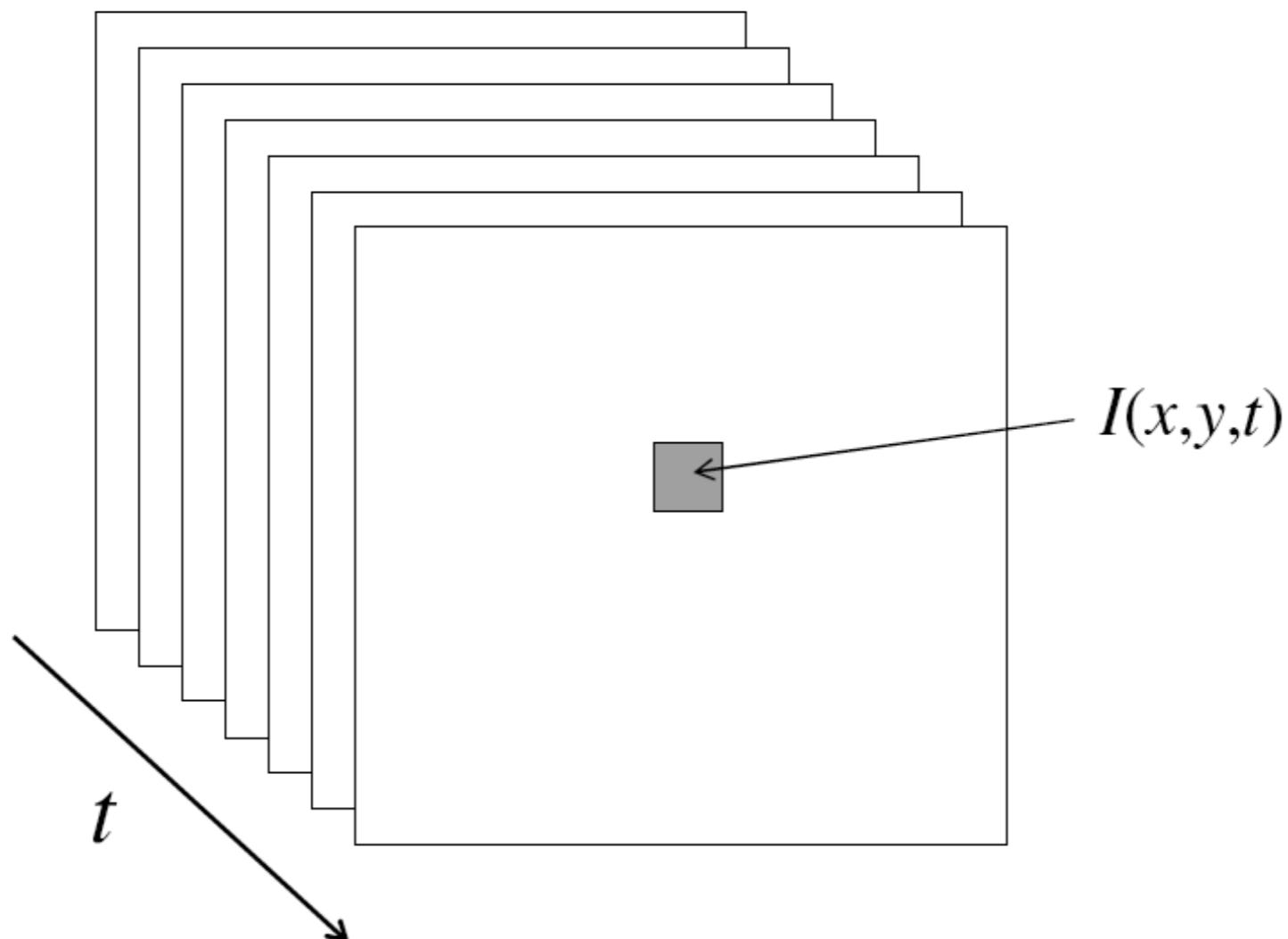


Video + Motion

Last Lecture of CV Course

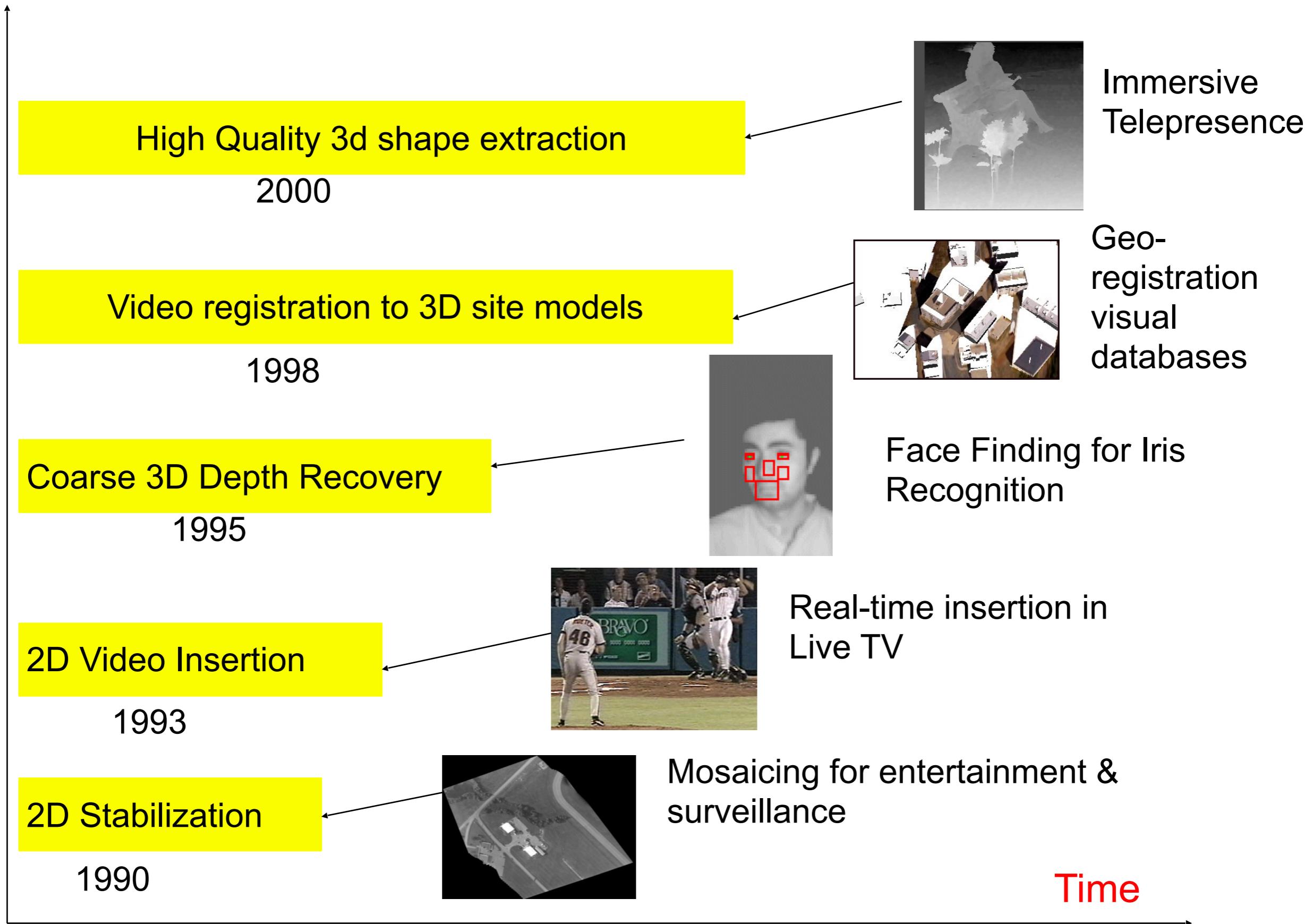
Video

- A video is a sequence of frames captured over time
- Now our image data is a function of space (x, y) and time (t)



Vision algorithm performance over time

Algorithm Complexity



A FRAMEWORK FOR VIDEO PROCESSING

ALIGN

2D & 3D MODELS OF MOTION & STRUCTURE

MODEL-BASED IMAGE SEQUENCE ALIGNMENT

TEST

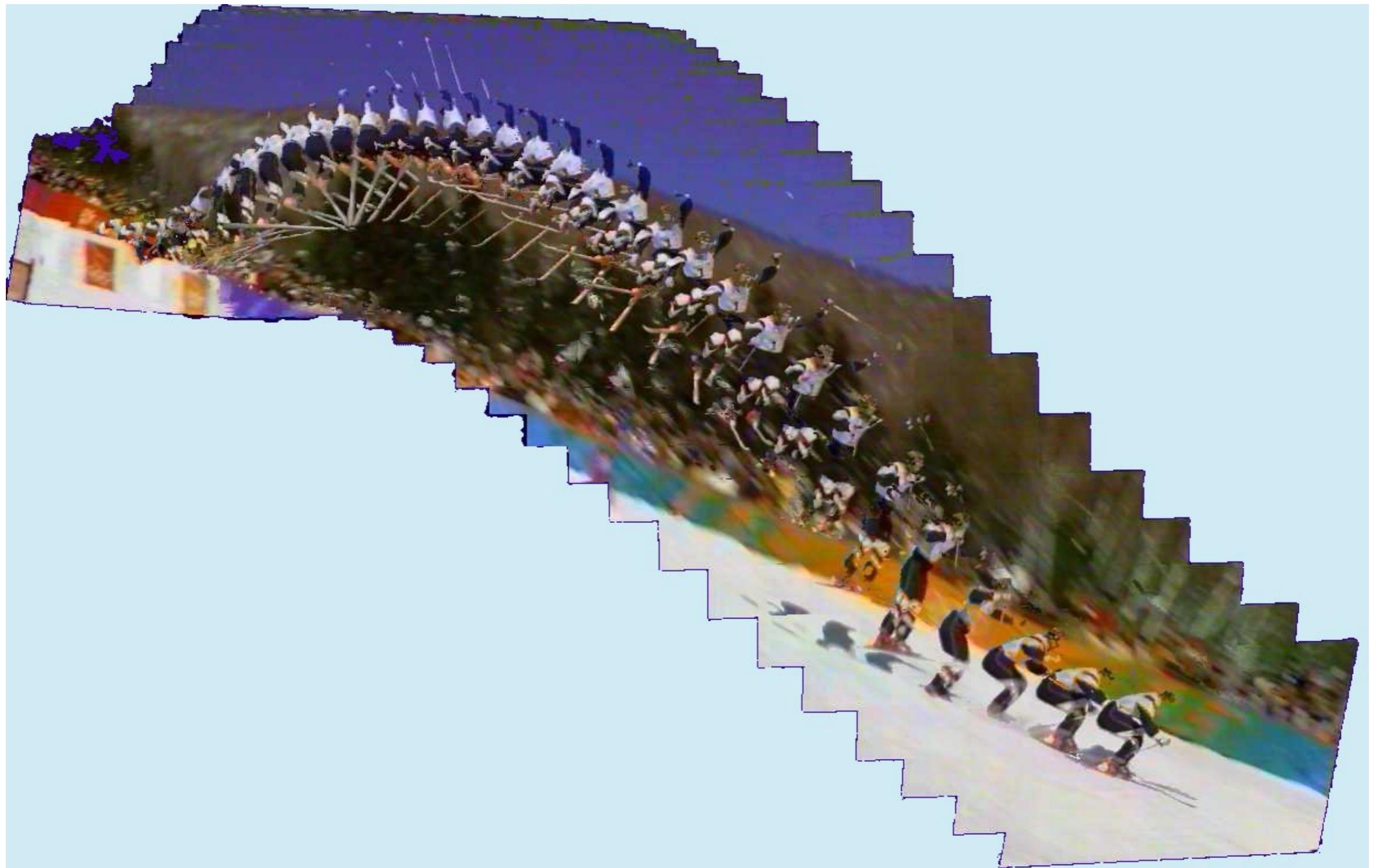
WARP/RENDER WITH 2D/3D MODELS

TEST ALIGNMENT QUALITY

SYNTHESIZE

CREATE OUTPUT REPRESENTATIONS

SYNOPISTIS MOSAICS



Motion: Why is it useful?



Motion: Why is it useful?

- Even “impoverished” motion data can evoke a strong percept



G. Johansson, “Visual Perception of Biological Motion and a Model For Its Analysis”, *Perception and Psychophysics* 14, 201-211, 1973.

Tracking: some applications



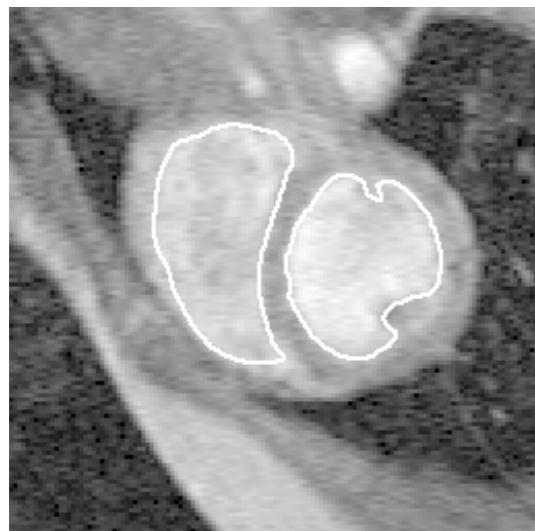
Body pose tracking,
activity recognition



Censusing a bat
population



Video-based
interfaces



Medical apps



Surveillance

Detection vs. tracking



t=1



t=2

...



t=20



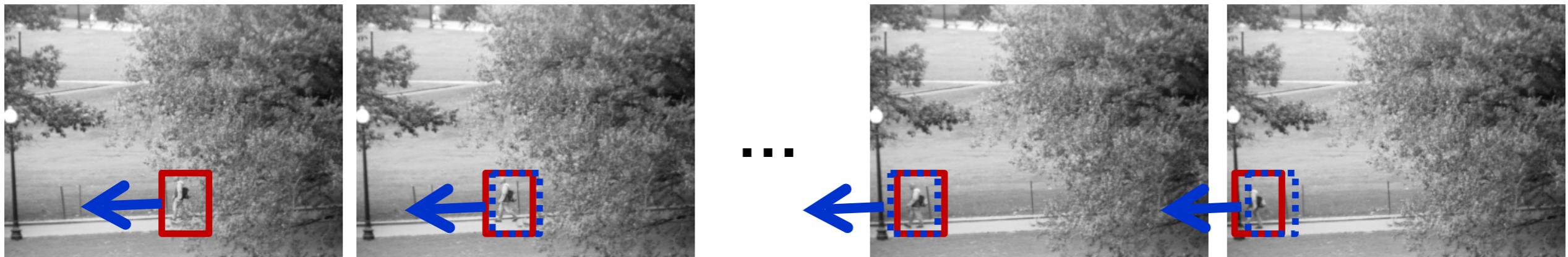
t=21

Detection vs. tracking



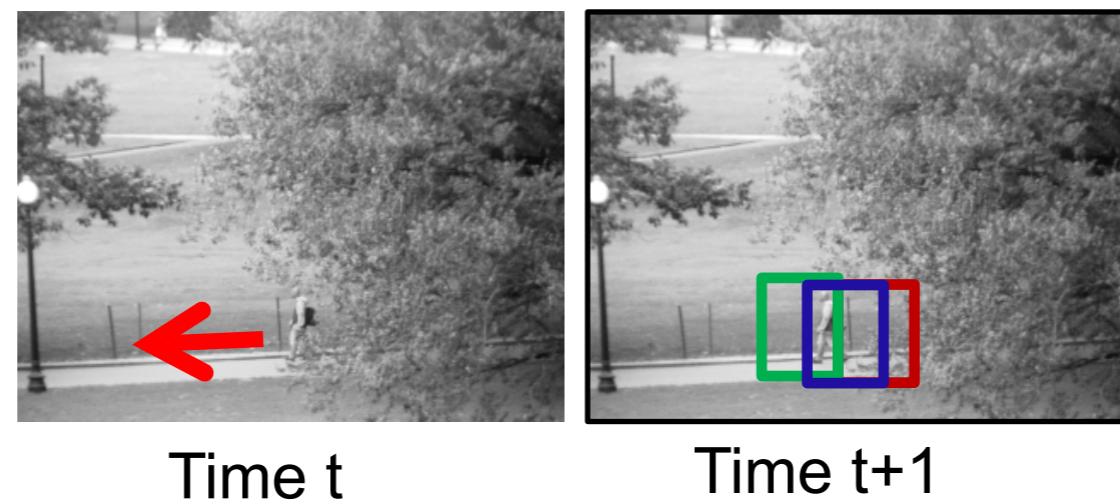
Detection: We detect the object independently in each frame and can record its position over time, e.g., based on detection window coordinates

Detection vs. tracking



Tracking with *dynamics*: We use image measurements to estimate position of object, but also incorporate position predicted by dynamics, i.e., our expectation of the object's motion pattern

Tracking: prediction + correction

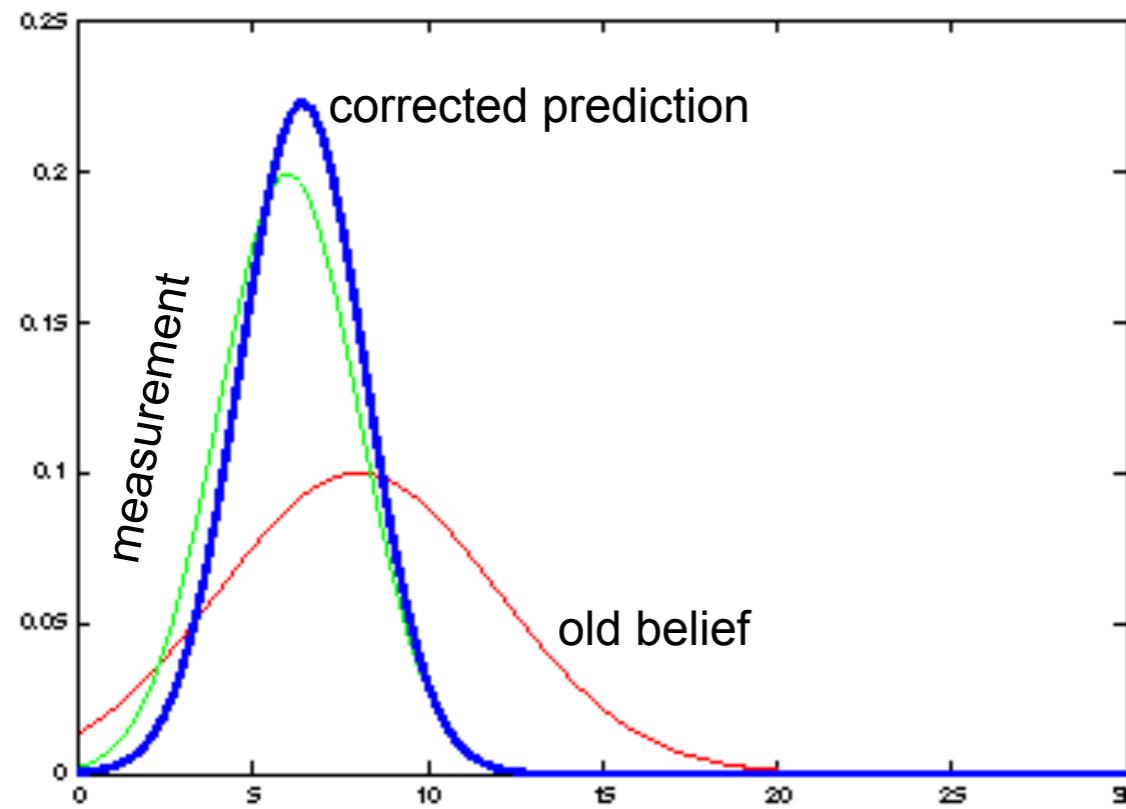
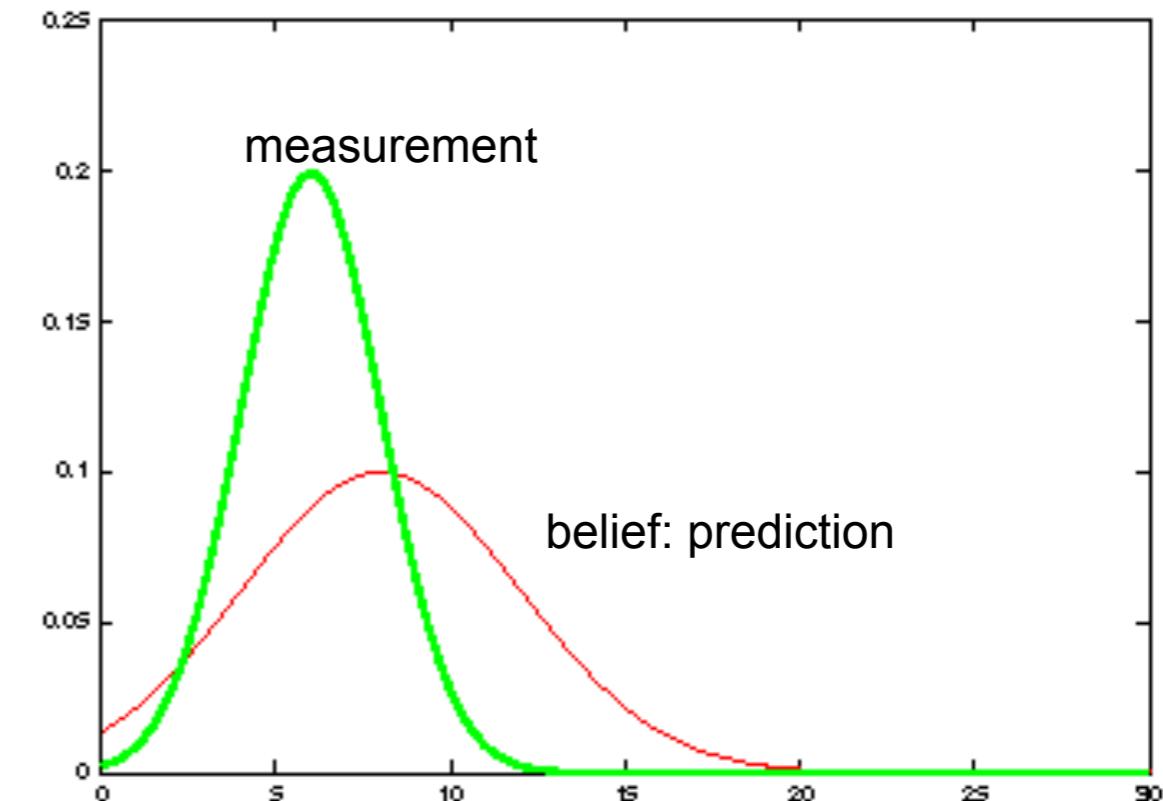
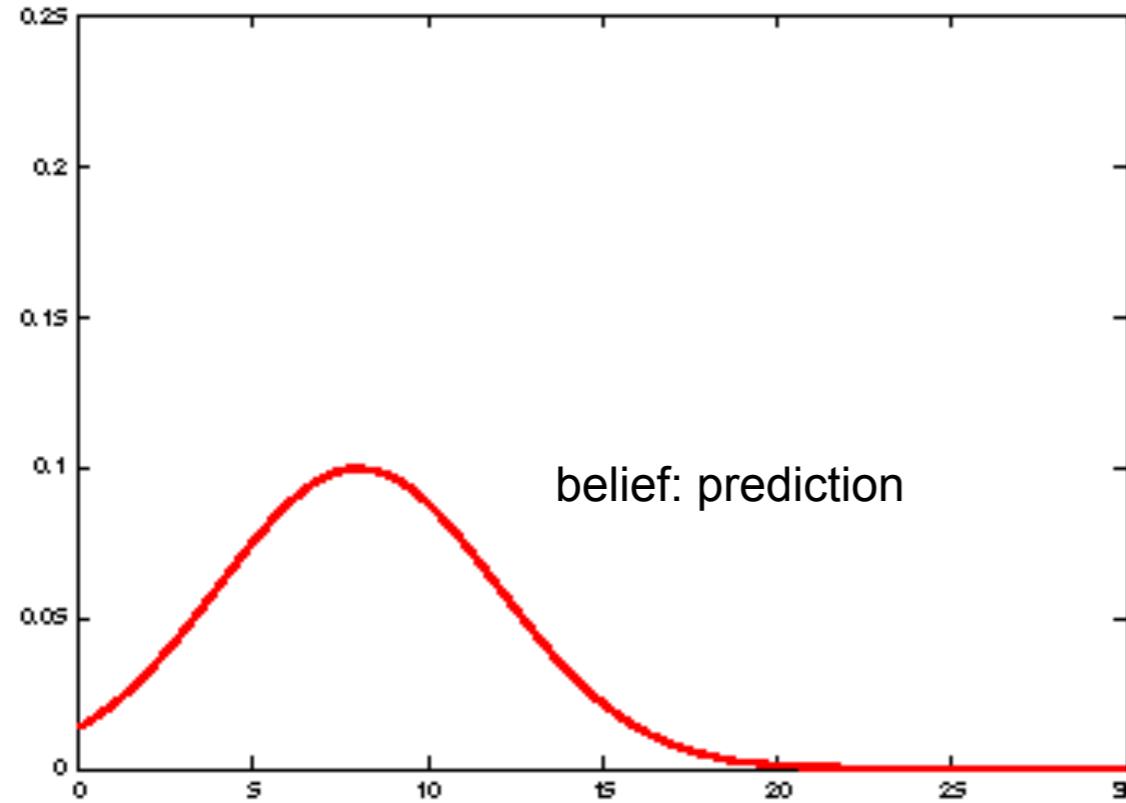


Belief

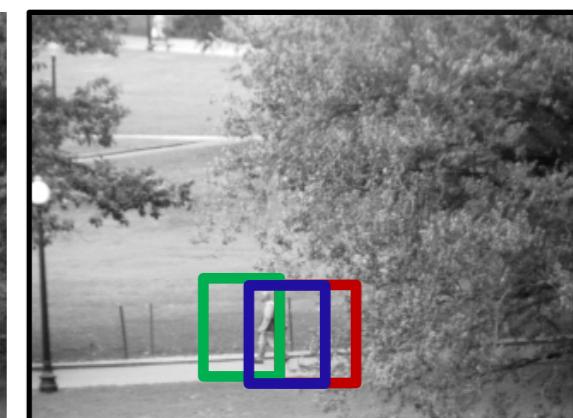
Measurement

Corrected prediction

Tracking: prediction + correction



Time t



Time $t+1$

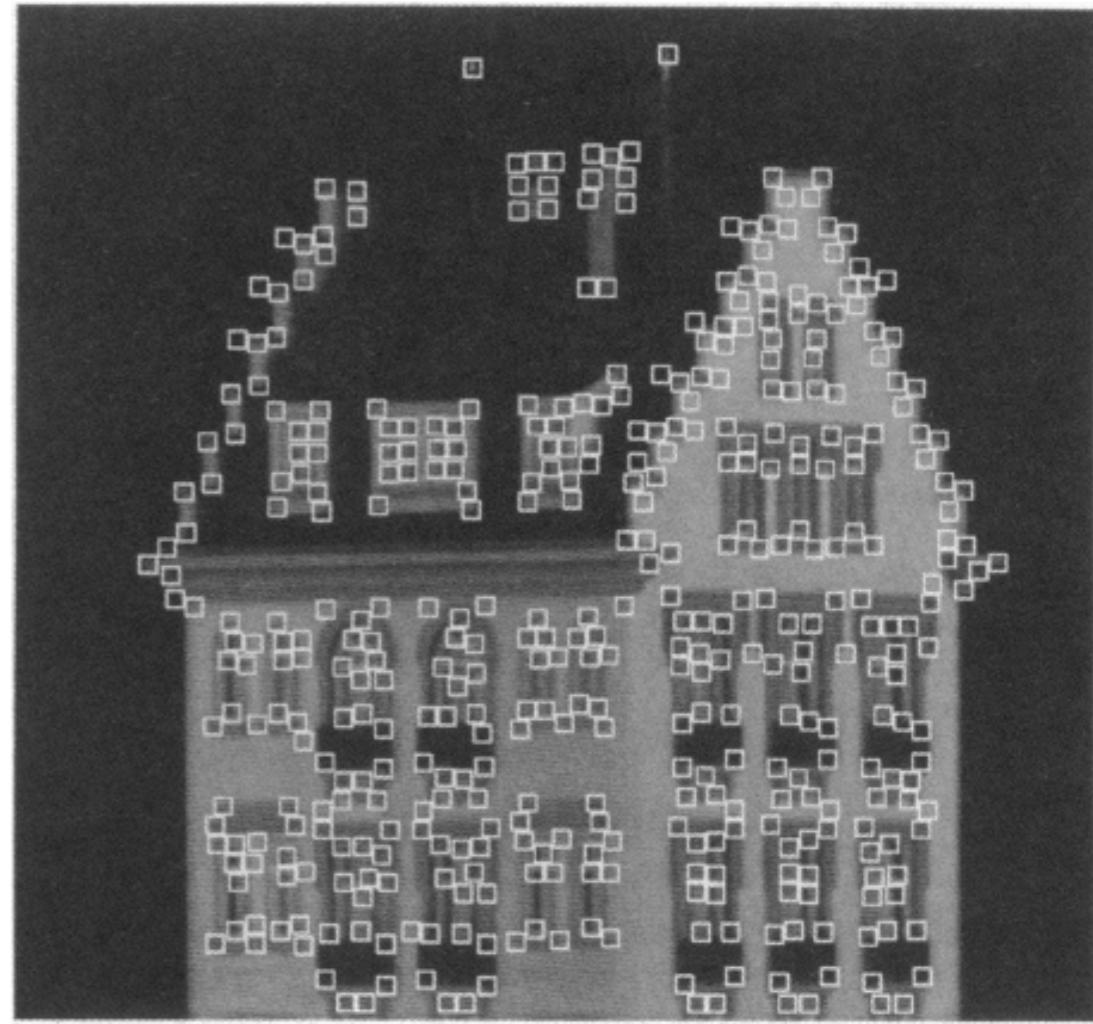
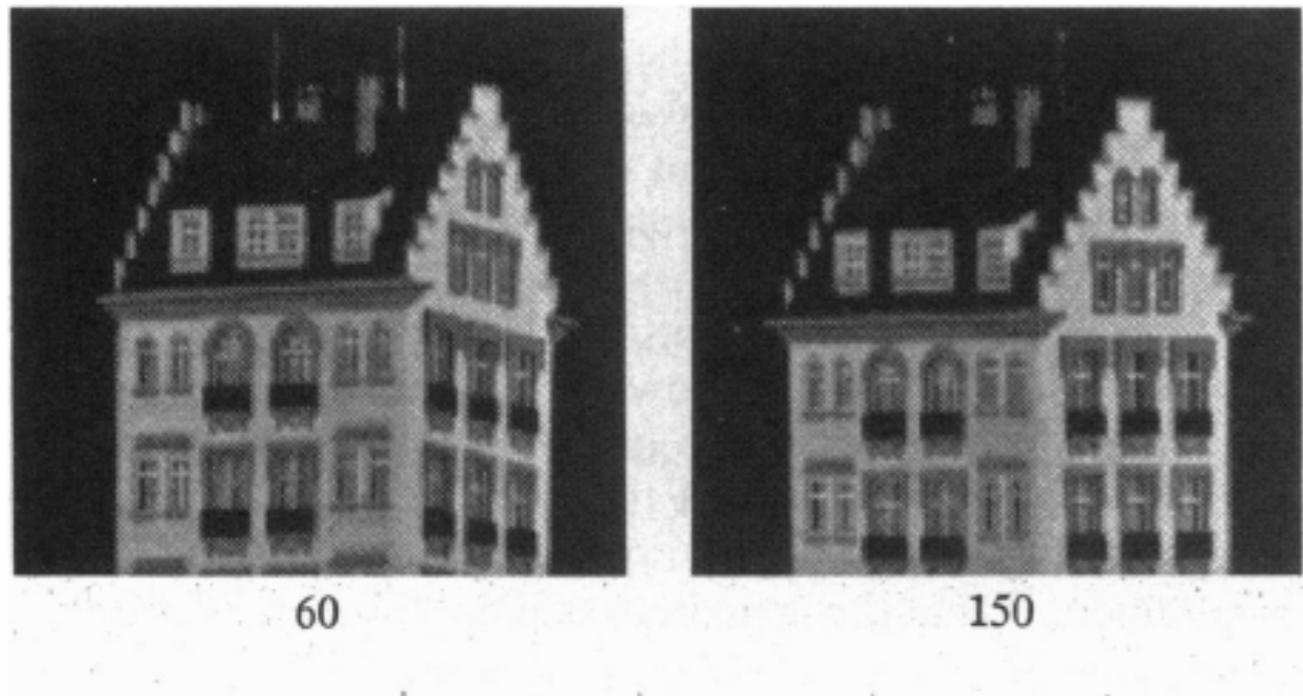
Recovering motion

- Feature-tracking
 - Extract visual features (corners, textured areas) and “track” them over multiple frames
- Optical flow
 - Recover image motion at each pixel from spatio-temporal image brightness variations (optical flow)

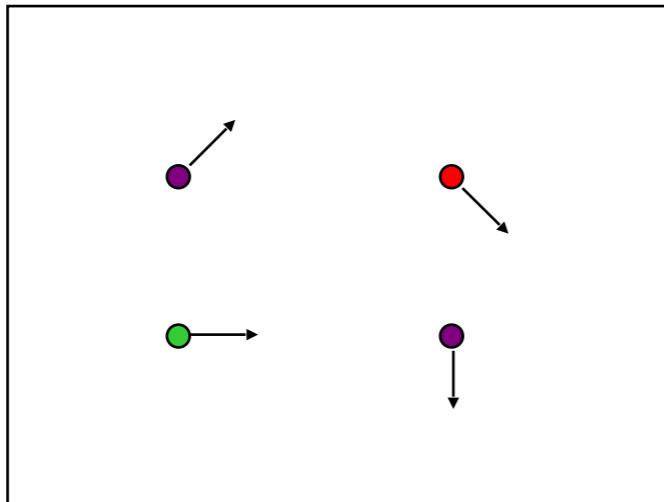
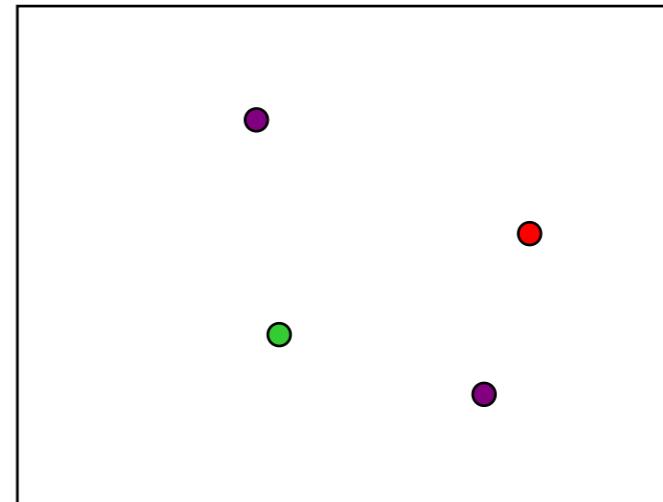
B. Lucas and T. Kanade. [An iterative image registration technique with an application to stereo vision.](#) In *Proceedings of the International Joint Conference on Artificial Intelligence*, pp. 674–679, 1981.

Feature tracking

- Many problems, such as structure from motion require matching points
- If motion is small, tracking is an easy way to get them

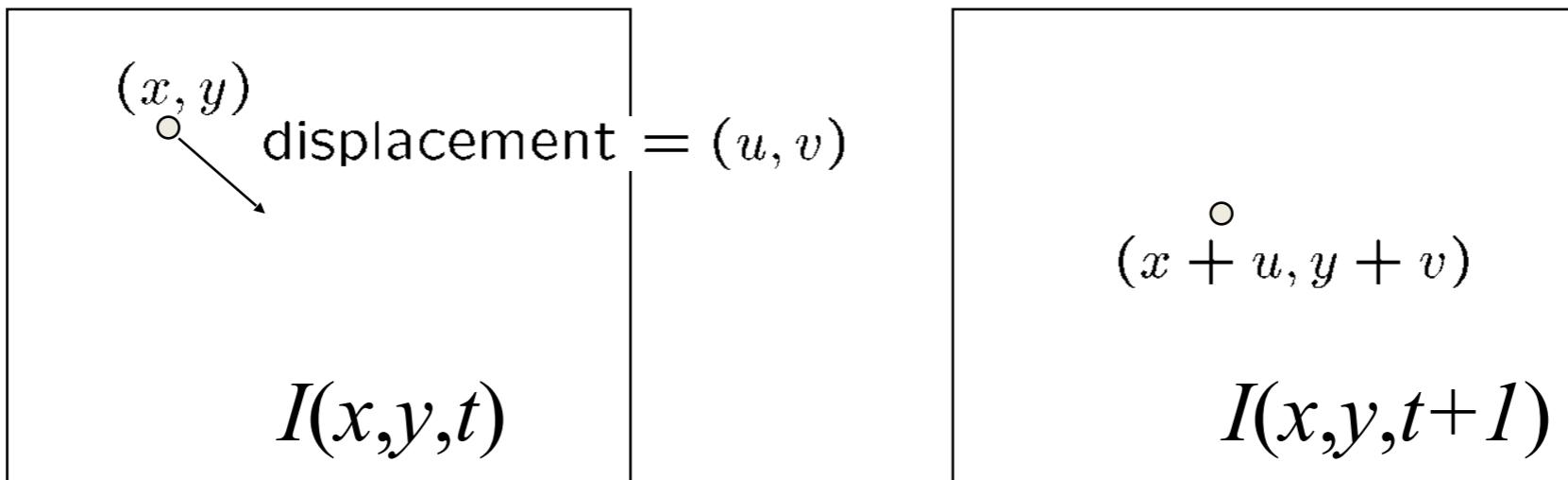


Feature tracking

 $I(x,y,t)$  $I(x,y,t+1)$

- Given two subsequent frames, estimate the point translation
- Key assumptions of Lucas-Kanade Tracker
 - **Brightness constancy:** projection of the same point looks the same in every frame
 - **Small motion:** points do not move very far
 - **Spatial coherence:** points move like their neighbors

Feature tracking



- Brightness Constancy Equation:

$$I(x, y, t) = I(x + u, y + v, t + 1)$$

Take Taylor expansion of $I(x + u, y + v, t + 1)$ at (x, y, t) to linearize the right side:

$$I(x + u, y + v, t + 1) \approx I(x, y, t) + I_x \cdot u + I_y \cdot v + I_t$$

Image derivative along x Difference over frames

$$I(x + u, y + v, t + 1) - I(x, y, t) = +I_x \cdot u + I_y \cdot v + I_t$$

So: $I_x \cdot u + I_y \cdot v + I_t \approx 0 \rightarrow \nabla I \cdot \begin{bmatrix} u & v \end{bmatrix}^T + I_t = 0$

Feature tracking

B. Lucas and T. Kanade. An iterative image registration technique with an application to stereo vision. In *Proceedings of the International Joint Conference on Artificial Intelligence*, pp. 674–679, 1981.

How many variables and equations?

- How to get more equations for a pixel?
- **Spatial coherence constraint**
- Assume the pixel's neighbors have the same (u,v)
 - If we use a 5x5 window, that gives us 25 equations per pixel

$$0 = I_t(\mathbf{p}_i) + \nabla I(\mathbf{p}_i) \cdot [u \ v]$$

$$\begin{bmatrix} I_x(\mathbf{p}_1) & I_y(\mathbf{p}_1) \\ I_x(\mathbf{p}_2) & I_y(\mathbf{p}_2) \\ \vdots & \vdots \\ I_x(\mathbf{p}_{25}) & I_y(\mathbf{p}_{25}) \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} = - \begin{bmatrix} I_t(\mathbf{p}_1) \\ I_t(\mathbf{p}_2) \\ \vdots \\ I_t(\mathbf{p}_{25}) \end{bmatrix}$$

Feature tracking

- Least squares problem:

$$\begin{bmatrix} I_x(p_1) & I_y(p_1) \\ I_x(p_2) & I_y(p_2) \\ \vdots & \vdots \\ I_x(p_{25}) & I_y(p_{25}) \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} = - \begin{bmatrix} I_t(p_1) \\ I_t(p_2) \\ \vdots \\ I_t(p_{25}) \end{bmatrix}$$

$A \quad d = b$
 $25 \times 2 \quad 2 \times 1 \quad 25 \times 1$

Matching patches across images

- Overconstrained linear system

$$\begin{bmatrix} I_x(p_1) & I_y(p_1) \\ I_x(p_2) & I_y(p_2) \\ \vdots & \vdots \\ I_x(p_{25}) & I_y(p_{25}) \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} = - \begin{bmatrix} I_t(p_1) \\ I_t(p_2) \\ \vdots \\ I_t(p_{25}) \end{bmatrix}$$

$A \quad d = b$
 $25 \times 2 \quad 2 \times 1 \quad 25 \times 1$

Least squares solution for d given by $(A^T A)^{-1} A^T b$

$$\begin{bmatrix} \sum I_x I_x & \sum I_x I_y \\ \sum I_x I_y & \sum I_y I_y \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} = - \begin{bmatrix} \sum I_x I_t \\ \sum I_y I_t \end{bmatrix}$$

$A^T A \qquad \qquad \qquad A^T b$

The summations are over all pixels in the $K \times K$ window

Conditions for solvability

Optimal (u, v) satisfies Lucas-Kanade equation

$$\begin{bmatrix} \sum I_x I_x & \sum I_x I_y \\ \sum I_x I_y & \sum I_y I_y \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} = - \begin{bmatrix} \sum I_x I_t \\ \sum I_y I_t \end{bmatrix}$$

$A^T A$ $A^T b$

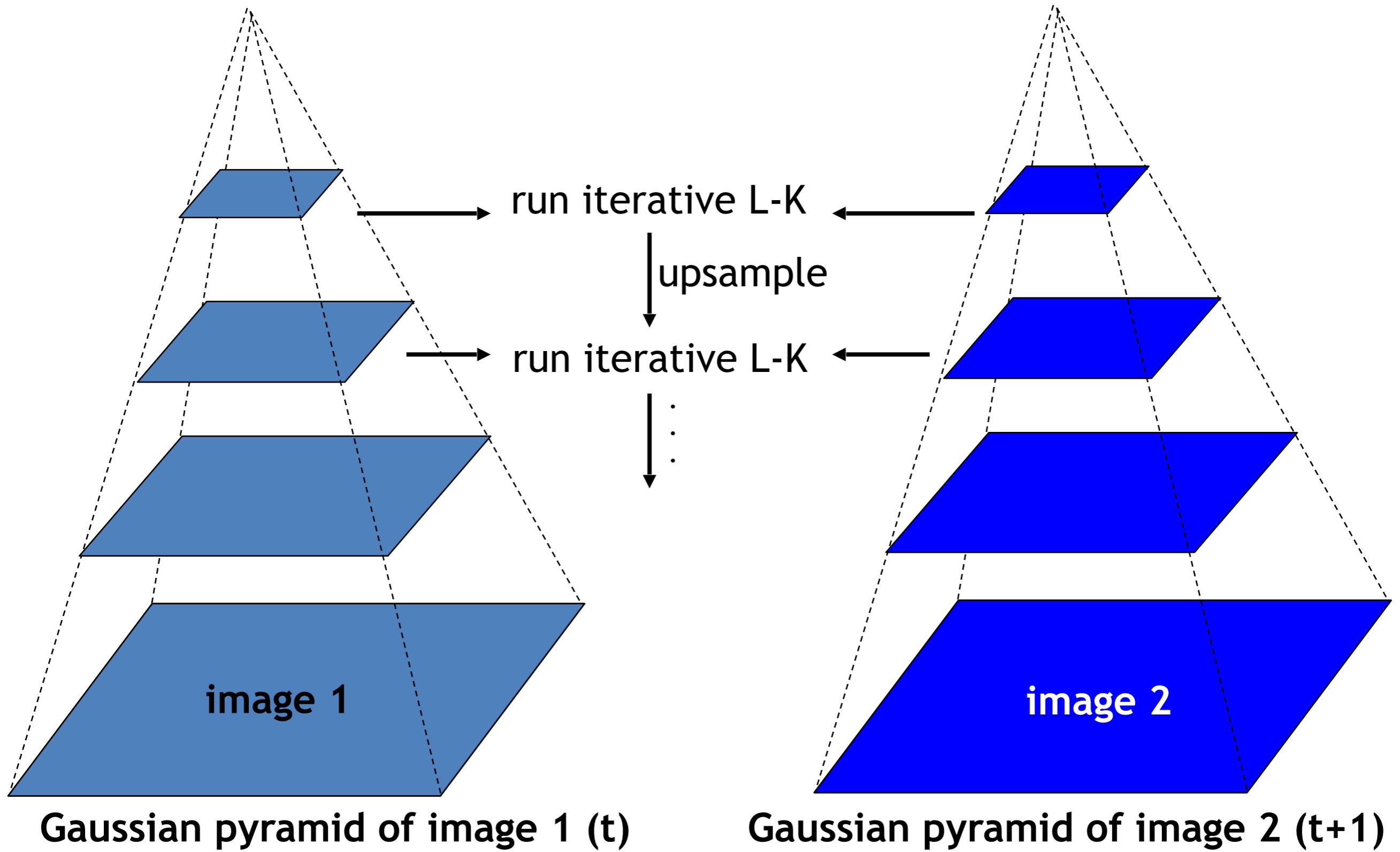
When is this solvable? I.e., what are good points to track?

- $\mathbf{A}^T \mathbf{A}$ should be invertible
- $\mathbf{A}^T \mathbf{A}$ should not be too small due to noise
 - eigenvalues λ_1 and λ_2 of $\mathbf{A}^T \mathbf{A}$ should not be too small
- $\mathbf{A}^T \mathbf{A}$ should be well-conditioned
 - λ_1 / λ_2 should not be too large (λ_1 = larger eigenvalue)

Does this remind you of anything?

Criteria for Harris corner detector

Dealing with larger movements: coarse-to-fine registration



There are several other algorithms that you should know

- Optical flow (Lucas Kanade)
- Other advanced versions of motion and tracking

Let us look back

[Lecture:1](#): Introduction to Computer Vision

[Lecture:2](#): Basics of Image Processing

[Lecture:3-4](#): Affine Transformations

[Lecture:5-6](#): Image Filtering

Lecture 7: Learning to code with opencv+python

[Lecture 8](#): Discrete Wavelet Transform [+[PyWavelets](#)]

[Lecture 9](#): Camera Calibration

[Lecture 10](#): Corner Detection

[Lecture 11](#): Line+boundary detection (Hough) + Calibration (cont.)

[Lecture 12](#): Camera Calibration (Cont.)

[Lecture 13](#): Image Registration

[Lecture 14](#): Segmentation

[Lecture 15-20](#): Segmentation + Recognition

[Lecture 21-23](#): Stereo + Mosaic

[Lecture 24](#): Video+Motion

About End-Sem

- Two parts
 - Closed book (24th)- 1 hr
 - Open book/resources (on 24th)- 3 hrs + 1hr (bonus) - you can use any resource but should not discuss with any person (friend, senior, batch-mate, TAs, or professor)
 - Syllabus - entire course (but more emphasis on post exam-3)