Prediction of movies popularity

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The purpose of this project is to develop mutliple linear regression model to analyze the factors that will make a movie popular. The dataset contains the information that are extracted from IMDB for random sample movies. For popularity we are going to measure the audience_score as an output variable and the attributes will be the type of movie, genre, runtime, imdb rating, imdb number of votes, critics rating, critics score, audience rating, Oscar awards obtained (actor, actress, director and picture).

if all these attributes are related significantly then we can find the popularity of movie.

Load packages0

```
library(ggplot2)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
       filter, lag
##
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
##
library(statsr)
## Warning: package 'statsr' was built under R version 3.5.2
## Loading required package: BayesFactor
## Warning: package 'BayesFactor' was built under R version 3.5.2
```

```
## Loading required package: coda
## Warning: package 'coda' was built under R version 3.5.2
## Loading required package: Matrix
## *******
## Welcome to BayesFactor 0.9.12-4.2. If you have questions, please contact
Richard Morey (richarddmorey@gmail.com).
## Type BFManual() to open the manual.
## ********
library(gridExtra)
##
## Attaching package: 'gridExtra'
## The following object is masked from 'package:dplyr':
##
##
      combine
library(corrplot)
## corrplot 0.84 loaded
```

Load the data

```
mydata <- load("C://Users//Shwetha Krishna//Downloads//movies.RData")</pre>
movies_new <- movies %>% select(title, title_type, genre, runtime,
imdb rating, imdb num votes, critics rating, critics score, audience rating,
audience score, best pic win, best actor win, best actress win, best dir win)
str(movies_new)
## Classes 'tbl df', 'tbl' and 'data.frame':
                                               651 obs. of 14 variables:
                     : chr "Filly Brown" "The Dish" "Waiting for Guffman"
## $ title
"The Age of Innocence" ...
## $ title_type : Factor w/ 3 levels "Documentary",..: 2 2 2 2 2 1 2 2
1 2 ...
## $ genre
                : Factor w/ 11 levels "Action & Adventure",..: 6 6 4 6
7 5 6 6 5 6 ...
## $ runtime
                     : num 80 101 84 139 90 78 142 93 88 119 ...
## $ imdb_rating : num 5.5 7.3 7.6 7.2 5.1 7.8 7.2 5.5 7.5 6.6 ...
## $ imdb_num_votes : int 899 12285 22381 35096 2386 333 5016 2272 880
12496 ...
## $ critics_rating : Factor w/ 3 levels "Certified Fresh",..: 3 1 1 1 3 2
3 3 2 1 ...
## $ critics score : num 45 96 91 80 33 91 57 17 90 83 ...
```

```
## $ audience_rating : Factor w/ 2 levels "Spilled","Upright": 2 2 2 2 1 2 2
1 2 2 ...
## $ audience score : num 73 81 91 76 27 86 76 47 89 66 ...
                     : Factor w/ 2 levels "no", "yes": 1 1 1 1 1 1 1 1 1 1
## $ best pic win
## $ best_actor_win : Factor w/ 2 levels "no", "yes": 1 1 1 2 1 1 1 2 1 1
## $ best_actress_win: Factor w/ 2 levels "no","yes": 1 1 1 1 1 1 1 1 1 1 1
## $ best dir win
                      : Factor w/ 2 levels "no", "yes": 1 1 1 2 1 1 1 1 1 1
movies_new[c(2,3,7,9,11:14)] \leftarrow lapply(movies_new[c(2,3,7,9,11:14)],
as.numeric)
movies data <- movies new
movies_data <- movies_data %>% select(title_type, genre, runtime,
imdb_rating, imdb_num_votes, critics_rating, critics_score,
audience_rating,best_pic_win, best_actor_win, best_actress_win, best_dir_win)
summary(movies_new)
##
      title
                                                           runtime
                         title_type
                                           genre
## Length:651
                       Min.
                              :1.000
                                       Min.
                                              : 1.000
                                                        Min.
                                                               : 39.0
##
   Class :character
                       1st Qu.:2.000
                                       1st Qu.: 4.000
                                                        1st Qu.: 92.0
##
   Mode :character
                       Median :2.000
                                       Median : 6.000
                                                        Median :103.0
##
                              :1.923
                       Mean
                                       Mean
                                              : 5.545
                                                        Mean
                                                               :105.8
##
                       3rd Qu.:2.000
                                       3rd Qu.: 6.000
                                                        3rd Qu.:115.8
##
                       Max.
                              :3.000
                                       Max.
                                              :11.000
                                                        Max.
                                                               :267.0
                                                        NA's
##
                                                               :1
##
     imdb rating
                    imdb num votes
                                     critics rating
                                                     critics score
## Min.
          :1.900
                    Min. :
                               180
                                           :1.000
                                                               1.00
                                     Min.
                                                     Min.
   1st Qu.:5.900
                    1st Qu.: 4546
                                     1st Qu.:2.000
                                                     1st Qu.: 33.00
##
##
   Median :6.600
                    Median : 15116
                                     Median :2.000
                                                     Median : 61.00
##
                           : 57533
                                                            : 57.69
   Mean
           :6.493
                    Mean
                                     Mean
                                            :2.264
                                                     Mean
    3rd Qu.:7.300
                    3rd Qu.: 58301
                                     3rd Qu.:3.000
                                                     3rd Qu.: 83.00
##
   Max.
           :9.000
                    Max.
                           :893008
                                     Max.
                                            :3.000
                                                     Max.
                                                            :100.00
##
##
    audience rating audience score
                                     best pic win
                                                    best actor win
##
   Min.
           :1.000
                    Min.
                           :11.00
                                    Min.
                                          :1.000
                                                    Min.
                                                          :1.000
##
   1st Ou.:1.000
                    1st Ou.:46.00
                                    1st Ou.:1.000
                                                    1st Ou.:1.000
   Median :2.000
                                                    Median :1.000
##
                    Median :65.00
                                    Median :1.000
##
   Mean
           :1.578
                    Mean
                           :62.36
                                    Mean
                                           :1.011
                                                    Mean
                                                           :1.143
##
    3rd Qu.:2.000
                    3rd Qu.:80.00
                                    3rd Qu.:1.000
                                                    3rd Qu.:1.000
##
   Max.
           :2.000
                    Max.
                           :97.00
                                    Max.
                                          :2.000
                                                    Max.
                                                           :2.000
##
##
   best actress win
                      best dir win
##
   Min.
           :1.000
                     Min.
                            :1.000
   1st Qu.:1.000
                     1st Qu.:1.000
```

```
## Median :1.000 Median :1.000

## Mean :1.111 Mean :1.066

## 3rd Qu.:1.000 3rd Qu.:1.000

## Max. :2.000 Max. :2.000

##

View(movies_new)
```

Drop missing value

```
movies_new <- na.omit(movies_new)</pre>
```

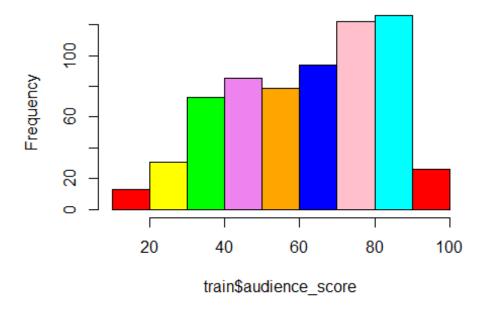
Split data into train and test

```
set.seed(2017)
split <- sample(seq_len(nrow(movies_new)), size = floor(0.999 *
nrow(movies_new)))
train <- movies_new[split, ]
test <- movies_new[-split, ]</pre>
```

histogram

```
colors = c("red", "yellow", "green", "violet", "orange", "blue", "pink",
"cyan")
hist(train$audience_score, col=colors, main = "Histogram for Train score")
```

Histogram for Train score

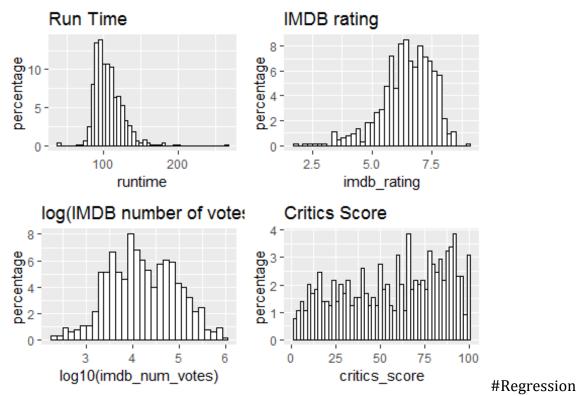


```
summary(train$audience_score)
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 11.0 46.0 65.0 62.3 80.0 97.0
```

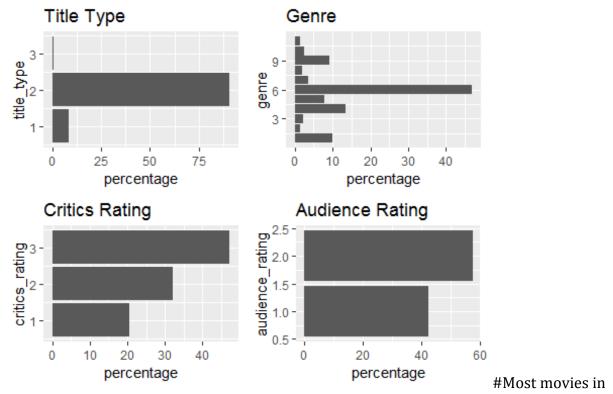
The median of our response variable - audience score distribution is 65; 75% of the movie in the training set have an audience score higher than 80; 25% of the movie in the training set have an audience score lower than 46; very few movie have an audience score lower than 20 or higher than 90

```
p1 <- ggplot(aes(x=runtime), data=train) +
    geom_histogram(aes(y=100*(..count..)/sum(..count..)), color='black',
fill='white', binwidth = 5) + ylab('percentage') + ggtitle('Run Time')
p2 <- ggplot(aes(x=imdb_rating), data=train) +
    geom_histogram(aes(y=100*(..count..)/sum(..count..)), color='black',
fill='white', binwidth = 0.2) + ylab('percentage') + ggtitle('IMDB rating')
p3 <- ggplot(aes(x=log10(imdb_num_votes)), data=train) +
    geom_histogram(aes(y=100*(..count..)/sum(..count..)), color='black',
fill='white') + ylab('percentage') + ggtitle('log(IMDB number of votes)')
p4 <- ggplot(aes(x=critics_score), data=train) +
    geom_histogram(aes(y=100*(..count..)/sum(..count..)), color='black',
fill='white', binwidth = 2) + ylab('percentage') + ggtitle('Critics Score')
grid.arrange(p1, p2, p3, p4, ncol=2)
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.</pre>
```



analysis: Run time, IMDB rating, log(IMDB number of votes) and Critics Scores all have reasonable broad distribution, therefore, they will be considered for the regression analysis.

```
p1 <- ggplot(aes(x=title_type), data=train) +
geom_bar(aes(y=100*(..count..)/sum(..count..))) + ylab('percentage') +
    ggtitle('Title Type') + coord_flip()
p2 <- ggplot(aes(x=genre), data=train) +
geom_bar(aes(y=100*(..count..)/sum(..count..))) + ylab('percentage') +
    ggtitle('Genre') + coord_flip()
p3 <- ggplot(aes(x=critics_rating), data=train) +
geom_bar(aes(y=100*(..count..)/sum(..count..))) + ylab('percentage') +
    ggtitle('Critics Rating') + coord_flip()
p4 <- ggplot(aes(x=audience_rating), data=train) +
geom_bar(aes(y=100*(..count..)/sum(..count..))) + ylab('percentage') +
    ggtitle('Audience Rating') + coord_flip()
grid.arrange(p1, p2, p3, p4, ncol=2)</pre>
```



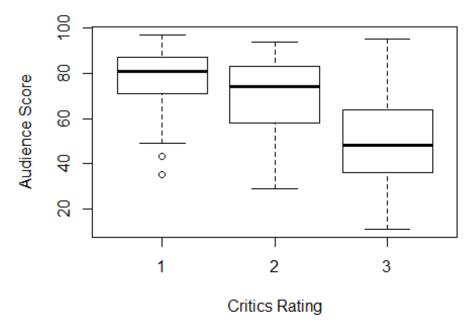
the data are in the "Feature Film" title type and majority of the movies are drama. Therefore, we must be aware that the results could be biased toward drama movies.

```
vars <- names(train) %in% c('runtime', 'imdb_rating', 'imdb_num_votes',
'critics_score')
selected_train <- train[vars]
corr.matrix <- cor(selected_train)
corrplot(corr.matrix, main="\n\nCorrelation Plot of numerical variables",
method="number")</pre>
```

Correlation Plot	of nur	merica mdp_rating	l varial	oles score scritics	
runtime	1	0.27	0.34	0.17	0. 0.
imdb_rating	0.27	1	0.33	0.76	0. 0.
imdb_num_votes	0.34	0.33	1	0.2	-0 -0
critics_score	0.17	0.76	0.2	1	0

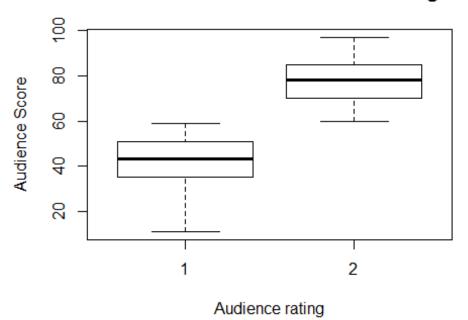
boxplot(audience_score~critics_rating, data=train, main='Audience score vs.
Critics rating', xlab='Critics Rating', ylab='Audience Score')

Audience score vs. Critics rating



```
by(train$audience_score, train$critics_rating, summary)
## train$critics_rating: 1
##
      Min. 1st Qu. Median
                              Mean 3rd Qu.
                                               Max.
                                              97.00
##
     35.00
             71.00
                     81.00
                              79.26
                                      87.00
##
## train$critics_rating: 2
##
      Min. 1st Qu. Median
                              Mean 3rd Qu.
                                               Max.
##
     29.00
             58.00
                     74.00
                              69.96
                                      83.00
                                              94.00
##
## train$critics rating: 3
##
      Min. 1st Qu. Median
                              Mean 3rd Qu.
                                               Max.
##
      11.0
                      48.0
                              49.7
                                               95.0
              36.0
                                       64.0
boxplot(audience_score~audience_rating, data=train, main='Audience Score vs.
Audience Rating', xlab='Audience rating', ylab='Audience Score')
```

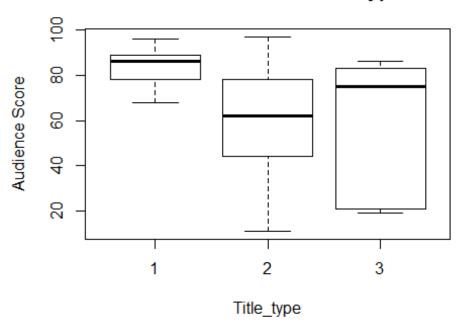
Audience Score vs. Audience Rating



```
by(train$audience_score, train$audience_rating, summary)
## train$audience rating: 1
      Min. 1st Qu. Median
##
                              Mean 3rd Qu.
                                               Max.
##
     11.00
             35.00
                     43.00
                             41.93
                                     51.00
                                              59.00
## train$audience_rating: 2
##
      Min. 1st Qu. Median
                              Mean 3rd Qu.
                                               Max.
##
     60.00
             70.00
                     78.00
                             77.27
                                     85.00
                                             97.00
```

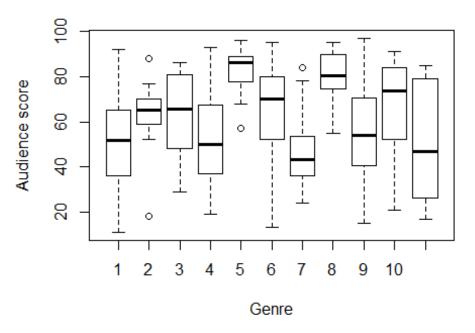
boxplot(audience_score~title_type, data=train, main='Audience score vs. Title
type', xlab='Title_type', ylab='Audience Score')

Audience score vs. Title type



```
by(train$audience_score, train$title_type, summary)
## train$title_type: 1
##
     Min. 1st Qu. Median
                              Mean 3rd Qu.
                                              Max.
##
     68.00
            78.00
                     86.00
                             83.46
                                     89.00
                                             96.00
## train$title_type: 2
##
     Min. 1st Qu. Median
                            Mean 3rd Qu.
                                             Max.
                     62.00
##
     11.00
            44.25
                             60.41
                                     78.00
                                             97.00
## train$title_type: 3
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                              Max.
##
     19.0
             21.0
                     75.0
                              56.8
                                     83.0
                                              86.0
boxplot(audience_score~genre, data=train, main='Audience score vs. Genre',
xlab='Genre', ylab='Audience score')
```

Audience score vs. Genre



```
by(train$audience_score, train$genre, summary)
## train$genre: 1
                          Mean 3rd Qu.
     Min. 1st Qu. Median
                                          Max.
##
    11.00 36.50
                 51.50
                           53.16 65.00
                                          92.00
##
## train$genre: 2
     Min. 1st Qu. Median Mean 3rd Qu.
##
                                          Max.
##
    18.00 59.00
                   65.00
                           62.44 70.00
                                          88.00
## train$genre: 3
##
     Min. 1st Qu. Median Mean 3rd Qu.
                                          Max.
##
    29.00 51.25
                   65.50
                           64.00 80.25
##
## train$genre: 4
     Min. 1st Qu. Median
##
                          Mean 3rd Qu.
                                          Max.
    19.00 37.00 50.00
##
                           52.51 67.50
                                          93.00
## train$genre: 5
##
     Min. 1st Qu. Median
                          Mean 3rd Qu.
                                          Max.
    57.00 77.50
                           82.96 89.00
##
                   86.00
                                          96.00
## train$genre: 6
##
     Min. 1st Qu. Median
                          Mean 3rd Qu.
                                          Max.
##
           52.00
                  70.00
                                          95.00
    13.00
                           65.35
                                  80.00
## train$genre: 7
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
   24.00 36.00 43.00
##
                  45.83 53.50
                            84.00
## -----
## train$genre: 8
 Min. 1st Qu. Median Mean 3rd Qu.
                           Max.
##
   55.00 75.75 80.50 80.17 89.50
                            95.00
## -----
## train$genre: 9
 Min. 1st Qu. Median Mean 3rd Qu.
   15.00 40.50 54.00 55.95 70.50 97.00
##
## -----
## train$genre: 10
  Min. 1st Qu. Median Mean 3rd Qu.
                           Max.
## 21.00 53.00 73.50 66.69 82.50
                            91.00
## -----
## train$genre: 11
## Min. 1st Qu. Median Mean 3rd Qu.
                           Max.
## 17.00 26.00 47.00 50.89 79.00
                           85.00
```

All the categorical variables seems to have reasonable significant correlation with audience score.

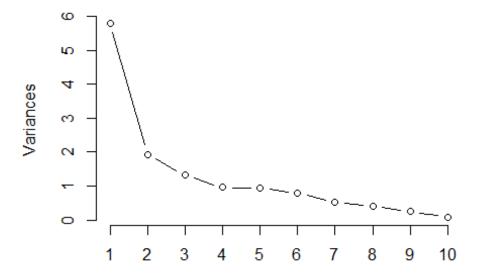
```
x <-
c(movies new$imdb num votes,movies new$best pic win,movies new$best actor win
,movies_new$best_actress_win,movies_new$best_dir_win)
t.test(movies_new$audience_score, x)
##
## Welch Two Sample t-test
##
## data: movies new$audience score and x
## t = -11.841, df = 3249, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -13360.601 -9564.579
## sample estimates:
## mean of x mean of y
## 62.34769 11524.93785
movies_new <- cor(movies_new[2:14])</pre>
movies_pca <- prcomp(movies_new,scale=TRUE)</pre>
str(movies new)
## num [1:13, 1:13] 1 0.0608 0.113 -0.3212 0.1209 ...
##
  - attr(*, "dimnames")=List of 2
     ..$ : chr [1:13] "title_type" "genre" "runtime" "imdb_rating" ...
##
     ..$ : chr [1:13] "title_type" "genre" "runtime" "imdb_rating" ...
summary(movies_pca)
```

```
## Importance of components:
##
                            PC1
                                   PC2
                                          PC3
                                                  PC4
                                                          PC5
                                                                  PC<sub>6</sub>
                                                                          PC7
## Standard deviation
                          2.408 1.3912 1.1453 0.97711 0.96805 0.88458 0.72389
## Proportion of Variance 0.446 0.1489 0.1009 0.07344 0.07209 0.06019 0.04031
## Cumulative Proportion
                          0.446 0.5949 0.6958 0.76924 0.84132 0.90152 0.94182
##
                              PC8
                                      PC9
                                             PC10
                                                     PC11
                                                             PC12
## Standard deviation
                          0.64149 0.49241 0.27999 0.14785 0.04536 2.029e-17
## Proportion of Variance 0.03165 0.01865 0.00603 0.00168 0.00016 0.000e+00
## Cumulative Proportion 0.97348 0.99213 0.99816 0.99984 1.00000 1.000e+00
#movies_pca$x
movies_pca$rotation
##
                            PC1
                                        PC2
                                                    PC3
                                                                PC4
## title_type
                    -0.32269503
                                0.16569082
                                             0.00762755
                                                         0.07160147
## genre
                     0.04310016 -0.14884743
                                             0.40959301
                                                         0.78400436
## runtime
                     0.12008106 0.43703631
                                             0.41396795 -0.10221820
## imdb_rating
                     0.40879921 -0.08153826
                                             0.03391444 -0.04209855
## imdb num votes
                     ## critics_rating
                    -0.39989770 -0.04763634 -0.07801802 -0.07587005
## critics score
                     0.40287506 -0.05311574 0.07044580 0.04430504
## audience rating
                     0.39159825 -0.15609335 -0.05209685 -0.09476602
## audience score
                     0.40387951 -0.12534228 -0.02784244 -0.08589222
## best pic win
                     0.10049013
                                0.50810179 -0.32760853
                                                         0.17924451
                                 0.14026877 0.59959226 -0.49019822
## best actor win
                    -0.06540099
## best_actress_win -0.03611079
                                 0.21856368 0.35021999 0.24038694
                                 0.47901336 -0.23374676
## best dir win
                     0.06247517
                                                         0.11408303
##
                             PC5
                                           PC<sub>6</sub>
                                                       PC7
## title_type
                    -0.029025485
                                  0.4162739801
                                                0.01774850
                                                            0.51653145
## genre
                    -0.360600526
                                  0.0185128933 -0.15853725 -0.02708045
## runtime
                    -0.125209527
                                  0.3030350675
                                                0.46537975 -0.50361627
## imdb_rating
                     0.009515376 -0.0031518082
                                                0.04416907
                                                            0.01586742
## imdb num votes
                     0.045881844
                                  0.5578095682 -0.25858029
                                                            0.25634424
## critics rating
                    -0.008756563
                                  0.0007332718
                                                0.08362822 -0.26251140
## critics_score
                    -0.009920595 -0.0783633052 -0.00368331 0.13927328
## audience rating
                     0.059492939
                                  0.0326932014
                                                0.05748864
                                                            0.04286068
                                                            0.04049258
## audience_score
                     0.034679182
                                  0.0119591729
                                                0.04233168
## best_pic_win
                     0.057484522 -0.1759953771 -0.55336582 -0.37403981
                    -0.239867169 -0.3161240765 -0.41419767
## best actor win
                                                            0.17777832
## best actress win
                     0.810854818 -0.2537922760
                                                0.11764874
                                                            0.14524478
## best_dir_win
                    -0.357782413 -0.4697967748
                                                0.43062643
                                                            0.35843478
                             PC9
##
                                        PC10
                                                    PC11
                                                                 PC12
## title_type
                     0.609588297 -0.11465573
                                              0.17200410
                                                          0.015128057
                    -0.080012638 -0.17041941
                                              0.02631126 -0.010669461
## genre
## runtime
                     0.175141815
                                  0.02540983 -0.05418366 -0.020862999
## imdb_rating
                     0.030334445
                                 0.04925575
                                              0.76774969
                                                          0.460131010
## imdb_num_votes
                    -0.578047291 -0.03061876 -0.03371824
                                                          0.006050424
## critics rating
                    -0.222581327 -0.32914731 0.32309040
                                                          0.052112713
## critics_score
                     0.203730186  0.52445370  -0.15781325
                                                          0.009988180
## audience rating
                     0.171590033 -0.65559527 -0.41486269
                                                          0.395033321
```

```
## audience score
                    0.096642276 -0.31574270
                                             0.26284467 -0.792766840
## best pic win
                    0.317076348 -0.08081960
                                             0.05810095
                                                         0.006167972
## best_actor_win
                    0.008586551 -0.11645863
                                             0.02720766
                                                         0.006469670
## best actress win -0.057200308 -0.08913389
                                             0.03536160 -0.003956082
## best_dir_win
                    -0.150174106 -0.11346573
                                             0.01878072 0.004821782
##
                          PC13
                    0.08616940
## title type
## genre
                    0.03261523
## runtime
                    -0.01884143
## imdb rating
                    -0.12846261
## imdb_num_votes
                    0.09765190
## critics rating
                    0.69642147
## critics score
                    0.67877284
## audience_rating
                    0.11588825
## audience_score
                    0.04050832
## best_pic_win
                    0.03737670
## best_actor_win
                    0.03447072
## best actress win
                    0.03420331
## best dir win
                    0.02357961
print(movies pca)
## Standard deviations (1, .., p=13):
  [1] 2.407948e+00 1.391189e+00 1.145311e+00 9.771066e-01 9.680529e-01
  [6] 8.845760e-01 7.238888e-01 6.414916e-01 4.924064e-01 2.799901e-01
## [11] 1.478504e-01 4.535746e-02 2.029175e-17
##
## Rotation (n x k) = (13 \times 13):
##
                           PC1
                                       PC2
                                                   PC3
                                                               PC4
                                            0.00762755 0.07160147
## title_type
                    -0.32269503 0.16569082
                    0.04310016 -0.14884743
                                            0.40959301
                                                        0.78400436
## genre
## runtime
                    0.12008106 0.43703631
                                            0.41396795 -0.10221820
## imdb rating
                    0.40879921 -0.08153826
                                            0.03391444 -0.04209855
## imdb num votes
                    ## critics_rating
                    -0.39989770 -0.04763634 -0.07801802 -0.07587005
## critics score
                    0.40287506 -0.05311574 0.07044580 0.04430504
## audience_rating
                    0.39159825 -0.15609335 -0.05209685 -0.09476602
## audience_score
                    0.40387951 -0.12534228 -0.02784244 -0.08589222
                    0.10049013 0.50810179 -0.32760853 0.17924451
## best pic win
## best actor win
                    -0.06540099 0.14026877 0.59959226 -0.49019822
## best_actress_win -0.03611079
                                0.21856368 0.35021999 0.24038694
## best dir win
                    0.06247517
                                0.47901336 -0.23374676 0.11408303
                                                      PC7
##
                            PC5
                                          PC6
                                                                  PC8
## title_type
                    -0.029025485
                                 0.4162739801
                                               0.01774850 0.51653145
## genre
                                 0.0185128933 -0.15853725 -0.02708045
                    -0.360600526
## runtime
                    -0.125209527
                                 0.3030350675
                                               0.46537975 -0.50361627
## imdb_rating
                    0.009515376 -0.0031518082
                                               0.04416907
                                                           0.01586742
## imdb num votes
                    0.045881844 0.5578095682 -0.25858029
                                                           0.25634424
## critics_rating
                    -0.008756563 0.0007332718
                                               0.08362822 -0.26251140
## critics score
                   -0.009920595 -0.0783633052 -0.00368331 0.13927328
```

```
## audience rating
                    0.059492939 0.0326932014
                                              0.05748864 0.04286068
## audience score
                    0.034679182 0.0119591729
                                              0.04233168
                                                         0.04049258
## best_pic_win
                    0.057484522 -0.1759953771 -0.55336582 -0.37403981
## best actor win
                   -0.239867169 -0.3161240765 -0.41419767
                                                         0.17777832
## best_actress_win
                    0.810854818 -0.2537922760
                                              0.11764874
                                                         0.14524478
## best_dir_win
                   -0.357782413 -0.4697967748
                                              0.43062643
                                                         0.35843478
##
                           PC9
                                      PC10
                                                  PC11
                                                              PC12
## title type
                    0.609588297 -0.11465573
                                            0.17200410 0.015128057
## genre
                   -0.080012638 -0.17041941
                                            0.02631126 -0.010669461
## runtime
                    ## imdb rating
                    0.030334445 0.04925575
                                            0.76774969
                                                       0.460131010
## imdb num votes
                   -0.578047291 -0.03061876 -0.03371824
                                                       0.006050424
## critics rating
                   -0.222581327 -0.32914731
                                            0.32309040
                                                       0.052112713
## critics_score
                    0.009988180
## audience_rating
                    0.171590033 -0.65559527 -0.41486269
                                                       0.395033321
## audience score
                    0.096642276 -0.31574270
                                            0.26284467 -0.792766840
## best pic win
                    0.317076348 -0.08081960
                                            0.05810095
                                                       0.006167972
## best actor win
                    0.008586551 -0.11645863
                                            0.02720766
                                                       0.006469670
## best actress win -0.057200308 -0.08913389
                                            0.03536160 -0.003956082
## best dir win
                   -0.150174106 -0.11346573
                                            0.01878072
                                                       0.004821782
##
                         PC13
## title_type
                    0.08616940
## genre
                    0.03261523
## runtime
                   -0.01884143
## imdb rating
                   -0.12846261
## imdb num votes
                    0.09765190
## critics rating
                    0.69642147
## critics_score
                    0.67877284
## audience rating
                    0.11588825
## audience score
                    0.04050832
## best pic win
                    0.03737670
## best_actor_win
                    0.03447072
## best actress win
                    0.03420331
## best dir win
                    0.02357961
plot(movies_pca, type='l')
```

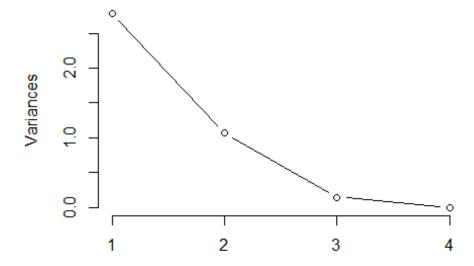
movies_pca



```
(movies_pca_eigens <- movies_pca$sdev^2)</pre>
  [1] 5.798216e+00 1.935407e+00 1.311737e+00 9.547373e-01 9.371265e-01
## [6] 7.824747e-01 5.240150e-01 4.115115e-01 2.424641e-01 7.839445e-02
## [11] 2.185975e-02 2.057299e-03 4.117550e-34
names(movies_pca_eigens) <- paste("PC",1:8,sep="")</pre>
sumlambdas <- sum(movies_pca_eigens)</pre>
sumlambdas
## [1] 13
dim(movies_new)
## [1] 13 13
#corr.matrix
movies_pca_new <- prcomp(corr.matrix, scale = TRUE)</pre>
summary(movies_pca_new)
## Importance of components:
##
                              PC1
                                     PC2
                                              PC3
                                                        PC4
## Standard deviation
                           1.6686 1.0321 0.38787 4.602e-17
## Proportion of Variance 0.6961 0.2663 0.03761 0.000e+00
## Cumulative Proportion 0.6961 0.9624 1.00000 1.000e+00
movies_pca_new$rotation
```

```
##
                      PC1
                                 PC2
                                           PC3
                                                     PC4
## runtime
                -0.4448468 -0.64136349 -0.2684187 0.56454904
## imdb_rating
                ## imdb num votes -0.3647911 0.76594319 -0.1740329 0.49997106
## critics score
                0.5884598 -0.03571694 0.4786108 0.65066974
print(movies_pca_new)
## Standard deviations (1, .., p=4):
## [1] 1.668638e+00 1.032088e+00 3.878682e-01 4.602008e-17
##
## Rotation (n \times k) = (4 \times 4):
##
                                 PC2
                                           PC3
                                                     PC4
## runtime
                -0.4448468 -0.64136349 -0.2684187 0.56454904
## imdb rating
                ## imdb num votes -0.3647911 0.76594319 -0.1740329 0.49997106
## critics score
                0.5884598 -0.03571694 0.4786108 0.65066974
plot(movies_pca_new, type='l')
```

movies pca new

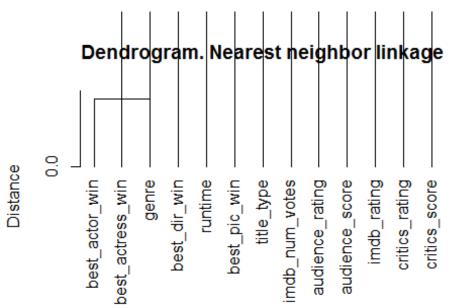


```
(movies_pca_eigens_new <- movies_pca_new$sdev^2)
## [1] 2.784354e+00 1.065205e+00 1.504417e-01 2.117848e-33
names(movies_pca_eigens_new) <- paste("PC",1:2,sep="")
sumlambdas <- sum(movies_pca_eigens_new)
sumlambdas</pre>
```

```
## [1] 4
dim(corr.matrix)

## [1] 4 4

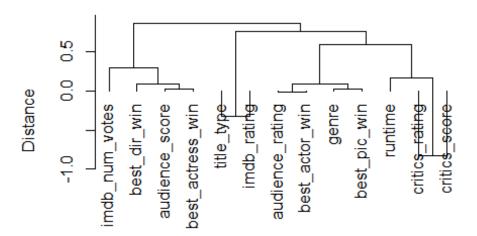
colnames(movies_new) <- rownames(movies_new)
movies_new <- as.dist(movies_new)
mat5.nn <- hclust(movies_new, method = "single")
plot(mat5.nn, hang=-1,xlab="Object",ylab="Distance",
main="Dendrogram. Nearest neighbor linkage")</pre>
```



Object hclust (*, "single")

```
#Default - Complete
mat5.fn <- hclust(movies_new)
plot(mat5.fn,hang=-1,xlab="Object",ylab="Distance",
main="Dendrogram. Farthest neighbor linkage")</pre>
```

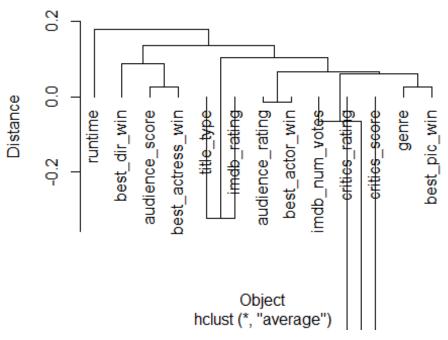
Dendrogram. Farthest neighbor linkage



Object hclust (*, "complete")

```
#Average
mat5.avl <- hclust(movies_new,method="average")
plot(mat5.avl,hang=-1,xlab="Object",ylab="Distance",
main="Dendrogram. Group average linkage")</pre>
```

Dendrogram. Group average linkage



```
# Standardizing the data with scale()
matstd.movies new <- scale(movies new[2:14])</pre>
# K-means, k=2, 3, 4, 5, 6
# Centers (k's) are numbers thus, 10 random sets are chosen
(kmeans2.movies_new <- kmeans(matstd.movies_new,2,nstart = 10))</pre>
## K-means clustering with 2 clusters of sizes 4, 9
##
## Cluster means:
##
           [,1]
## 1 -1.3986451
## 2 0.6216201
##
## Clustering vector:
##
  [1] 2 1 2 2 1 1 1 2 2 2 2 2 2
## Within cluster sum of squares by cluster:
## [1] 0.09262216 0.60484152
  (between_SS / total_SS = 94.2 %)
##
##
## Available components:
##
## [1] "cluster"
                       "centers"
                                      "totss"
                                                      "withinss"
## [5] "tot.withinss" "betweenss"
                                      "size"
                                                      "iter"
## [9] "ifault"
```

```
# Computing the percentage of variation accounted for. Two clusters
perc.var.2 <- round(100*(1 -
kmeans2.movies_new$betweenss/kmeans2.movies_new$totss),1)
names(perc.var.2) <- "Perc. 2 clus"</pre>
perc.var.2
## Perc. 2 clus
##
# Computing the percentage of variation accounted for. Three clusters
(kmeans3.movies_new <- kmeans(matstd.movies_new,3,nstart = 10))</pre>
## K-means clustering with 3 clusters of sizes 4, 3, 6
##
## Cluster means:
##
           [,1]
## 1 -1.3986451
## 2 0.9159192
## 3 0.4744705
## Clustering vector:
## [1] 3 1 3 2 1 1 1 3 3 3 3 2 2
## Within cluster sum of squares by cluster:
## [1] 0.09262216 0.07224741 0.14284023
## (between SS / total SS = 97.4 %)
##
## Available components:
##
## [1] "cluster"
                       "centers"
                                      "totss"
                                                      "withinss"
## [5] "tot.withinss" "betweenss"
                                                      "iter"
                                      "size"
## [9] "ifault"
perc.var.3 <- round(100*(1 -
kmeans3.movies_new$betweenss/kmeans3.movies_new$totss),1)
names(perc.var.3) <- "Perc. 3 clus"</pre>
perc.var.3
## Perc. 3 clus
##
            2.6
# Computing the percentage of variation accounted for. Four clusters
(kmeans4.movies_new <- kmeans(matstd.movies_new,4,nstart = 10))</pre>
## K-means clustering with 4 clusters of sizes 1, 4, 4, 4
##
## Cluster means:
##
           \lceil,1\rceil
## 1 1.1351204
## 2 0.3895597
## 3 0.7253054
```

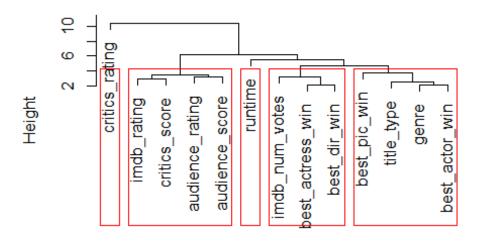
```
## 4 -1.3986451
##
## Clustering vector:
## [1] 3 4 3 1 4 4 4 2 2 2 2 3 3
##
## Within cluster sum of squares by cluster:
## [1] 0.00000000 0.05555089 0.02719733 0.09262216
## (between_SS / total_SS = 98.5 %)
## Available components:
##
## [1] "cluster"
                      "centers"
                                     "totss"
                                                  "withinss"
## [5] "tot.withinss" "betweenss" "size"
                                                   "iter"
## [9] "ifault"
perc.var.4 <- round(100*(1 -
kmeans4.movies new$betweenss/kmeans4.movies new$totss),1)
names(perc.var.4) <- "Perc. 4 clus"</pre>
perc.var.4
## Perc. 4 clus
##
            1.5
# Computing the percentage of variation accounted for. Five clusters
(kmeans5.movies_new <- kmeans(matstd.movies_new,5,nstart = 10))</pre>
## K-means clustering with 5 clusters of sizes 3, 4, 1, 1, 4
##
## Cluster means:
           [,1]
## 1 -1.4848499
## 2 0.3895597
## 3 -1.1400308
## 4 1.1351204
## 5 0.7253054
##
## Clustering vector:
## [1] 5 1 5 4 1 3 1 2 2 2 2 5 5
##
## Within cluster sum of squares by cluster:
## [1] 0.003447006 0.055550893 0.000000000 0.000000000 0.027197330
## (between SS / total SS = 99.3 %)
##
## Available components:
##
## [1] "cluster"
                     "centers"
                                                  "withinss"
                                    "totss"
## [5] "tot.withinss" "betweenss"
                                                    "iter"
                                     "size"
## [9] "ifault"
perc.var.5 <- round(100*(1 -
kmeans5.movies_new$betweenss/kmeans5.movies_new$totss),1)
```

```
names(perc.var.5) <- "Perc. 5 clus"</pre>
perc.var.5
## Perc. 5 clus
            0.7
(kmeans6.movies new <- kmeans(matstd.movies new,6,nstart = 10))
## K-means clustering with 6 clusters of sizes 3, 3, 1, 1, 4, 1
##
## Cluster means:
##
           [,1]
## 1 -1.4848499
## 2 0.4534757
## 3 0.1978115
## 4 -1.1400308
## 5 0.7253054
## 6 1.1351204
##
## Clustering vector:
## [1] 5 1 5 6 1 4 1 3 2 2 2 5 5
## Within cluster sum of squares by cluster:
## [1] 0.003447006 0.006527777 0.000000000 0.000000000 0.027197330
0.000000000
## (between SS / total SS = 99.7 %)
##
## Available components:
##
## [1] "cluster"
                       "centers"
                                      "totss"
                                                      "withinss"
## [5] "tot.withinss" "betweenss"
                                                      "iter"
                                      "size"
## [9] "ifault"
# Computing the percentage of variation accounted for. Six clusters
perc.var.6 <- round(100*(1 -
kmeans6.movies new$betweenss/kmeans6.movies new$totss),1)
names(perc.var.6) <- "Perc. 6 clus"</pre>
perc.var.6
## Perc. 6 clus
            0.3
##
#
movies new <- scale(movies new)</pre>
wss <- (nrow(movies_new)-1)*sum(apply(movies_new,2,var))</pre>
for (i in 1:5) wss[i] <- sum(kmeans(movies_new,centers=i)$withinss)</pre>
fit <- kmeans(movies_new, 5)</pre>
aggregate(movies_new,by=list(fit$cluster),FUN=mean)
```

```
genre
     Group.1 title type
                                         runtime imdb rating imdb num votes
## 1
           1
              0.6552446
                          0.04226622
                                       0.8162421 -0.03810044
                                                                 -0.24881835
## 2
           2
              0.3780973 -0.26494004
                                       0.1309401 -0.45607298
                                                                 -0.03945204
## 3
           3 -1.3828952
                          0.57741865
                                       0.2009378
                                                  0.93213257
                                                                  0.62112031
## 4
              0.7568126
                          1.12858724 -1.3198094
                                                  0.17582146
                                                                  1.06823469
## 5
           5
              1.2966450 -2.50530033 -2.4564286 -1.96575851
                                                                 -2.64845272
     critics rating critics score audience rating audience score best pic win
##
## 1
          0.2629309
                       -0.01309940
                                        -0.12930698
                                                        -0.09763822
                                                                       1.20588787
## 2
          0.7716620
                       -0.31970319
                                        -0.47528871
                                                        -0.47882304
                                                                      -0.62514504
## 3
         -1.2794226
                        0.89219453
                                         1.02579941
                                                         1.00897691
                                                                      0.06420556
## 4
          0.3842178
                        0.07548263
                                        -0.01807412
                                                         0.00538053
                                                                       0.70500306
## 5
          0.8580318
                       -2.32614977
                                        -1.79604772
                                                        -1.83308136
                                                                     -2.07890877
##
     best actor win best actress win best dir win
## 1
          0.5170993
                           -0.1269452
                                        -0.12663683
## 2
         -0.2036942
                            0.5825442
                                         0.31126960
## 3
         -0.5191122
                           -0.4360077
                                        -0.01235528
## 4
          2.5810254
                            1.8312463
                                         1.26181933
## 5
                           -2.0365567
         -1.2410975
                                        -2.07756614
mydata <- data.frame(movies new, fit$cluster)</pre>
mydata
##
                     title_type
                                                 runtime imdb_rating
                                       genre
## title type
                      0.1639182 -0.06215298 -0.42093850
                                                           -1.2489511
## genre
                      0.4831010 -0.86114424 -0.11474062
                                                           -0.1154920
## runtime
                      0.7568126
                                 1.12858724 -1.31980935
                                                            0.1758215
## imdb rating
                     -1.5214408
                                 1.07925282
                                              0.81411896
                                                           -0.4725742
## imdb num votes
                      0.7983436 -0.22189773
                                              1.44238236
                                                            0.3303364
## critics_rating
                      1.2966450
                                -2.50530033 -2.45642864
                                                           -1.9657585
## critics score
                     -1.4659827
                                 1.37334280
                                              0.05246795
                                                            1.3760734
## audience rating
                     -1.1094020 -0.19839699 -0.18263708
                                                            1.2069316
## audience_score
                     -1.4347552
                                 0.05547596
                                              0.11980135
                                                            1.6180995
## best pic win
                      0.3054102 -0.49503085
                                              0.28063492
                                                           -0.1448832
## best actor win
                      0.5599598
                                 0.35856789
                                              0.77880479
                                                           -0.3149656
## best_actress_win
                                 0.42671005
                                              0.34771772
                                                           -0.2986760
                      0.6425379
                      0.5248525 -0.07801366
                                              0.65862615
## best dir win
                                                           -0.1459617
##
                     imdb_num_votes critics_rating critics_score
                                          1.5739081
## title_type
                         -0.1571934
                                                       -1.08058046
## genre
                         -0.5483535
                                          0.4429313
                                                        0.06977534
## runtime
                          1.0682347
                                          0.3842178
                                                        0.07548263
## imdb_rating
                          0.9867322
                                         -1.1905156
                                                        1.49277724
## imdb num votes
                         -0.8118744
                                         -0.2667625
                                                        0.16523268
## critics_rating
                         -2.6484527
                                          0.8580318
                                                       -2.32614977
## critics_score
                                                       -0.33729511
                          0.3252682
                                         -1.8982366
## audience rating
                          0.4124688
                                         -0.8903713
                                                        1.06559223
## audience_score
                          0.7600121
                                         -1.1385670
                                                        1.34770375
## best_pic_win
                          0.9107319
                                          0.2977674
                                                       -0.04151619
## best_actor_win
                         -0.3629931
                                          0.7720413
                                                       -0.22649147
## best_actress_win
                         -0.1537126
                                          0.6279862
                                                       -0.19064690
## best dir win
                          0.2191319
                                          0.4275691
                                                       -0.01388397
```

```
##
                     audience rating audience score best pic win
## title type
                         -1.04110305
                                         -1.13482403
                                                      -0.60536625
## genre
                         -0.26345269
                                         -0.25565727
                                                      -0.59853774
## runtime
                         -0.01807412
                                         0.00538053
                                                       0.70500306
## imdb_rating
                          1.44603725
                                         1.61121240
                                                       0.21147849
## imdb_num_votes
                          0.20256169
                                         0.26207558
                                                       1.58462884
## critics_rating
                         -1.79604772
                                         -1.83308136 -2.07890877
## critics score
                         1.15806169
                                         1.23378457
                                                       0.12152087
## audience_rating
                         -0.39731303
                                         1.61041151
                                                     -0.13613298
## audience score
                          1.89641173
                                         -0.41950083
                                                       0.05995585
## best_pic_win
                         -0.16026498
                                        -0.14850663
                                                      -0.80818282
## best actor win
                         -0.43633413
                                         -0.37630423
                                                      -0.48849334
## best actress win
                                                       0.34371469
                         -0.33251676
                                         -0.35690498
## best_dir_win
                         -0.25796588
                                         -0.19808525
                                                       1.68932009
                     best_actor_win best_actress_win best_dir_win fit.cluster
##
## title_type
                         0.09663716
                                           0.18974833
                                                       -0.32547473
## genre
                         0.32594753
                                           0.28448204
                                                       -0.40632841
                                                                              2
                                                                              4
## runtime
                         2.58102537
                                          1.83124630
                                                        1.26181933
                                                                              3
## imdb rating
                                          -0.07742750
                                                        0.25977475
                        -0.03888245
## imdb_num_votes
                                           0.61031855
                                                                              1
                         0.19456281
                                                        0.74753935
## critics rating
                                                                              5
                        -1.24109754
                                          -2.03655670
                                                       -2.07756614
                                                        0.26007161
                                                                              3
## critics_score
                        -0.28818236
                                          -0.22518295
                                                                              3
## audience_rating
                        -1.09305950
                                          -0.73621677
                                                       -0.46894130
## audience score
                                          -0.70520373
                                                                              3
                        -0.65632455
                                                       -0.10032617
                                                                              2
## best_pic_win
                        -0.33833093
                                           1.04839758
                                                        1.99720881
## best_actor_win
                        -0.89903054
                                          0.80754895
                                                       -0.02032727
                                                                              2
                                                                              1
## best actress win
                                         -1.07482430
                         0.89209531
                                                       -0.19510588
## best dir win
                         0.46463970
                                          0.08367019
                                                       -0.93234395
                                                                              1
d <- dist(mydata, method = "euclidean") # distance matrix</pre>
fit <- hclust(d, method="complete")</pre>
plot(fit)
# cut tree into 5 clusters
groups <- cutree(fit, k=5)</pre>
# draw dendogram with red borders around the 5 clusters
rect.hclust(fit, k=5, border="red")
```

Cluster Dendrogram



d hclust (*, "complete")

Factor Analysis

```
head(movies_data)
## # A tibble: 6 x 12
     title_type genre runtime imdb_rating imdb_num_votes critics_rating
          <dbl> <dbl>
##
                         <dbl>
                                     <dbl>
                                                     <int>
                                                                     <dbl>
## 1
              2
                                        5.5
                                                       899
                                                                         3
                     6
                            80
## 2
              2
                                        7.3
                                                     12285
                                                                         1
                     6
                           101
## 3
              2
                     4
                            84
                                        7.6
                                                     22381
                                                                         1
              2
## 4
                     6
                           139
                                        7.2
                                                     35096
                                                                         1
## 5
              2
                     7
                            90
                                                       2386
                                                                         3
                                        5.1
                     5
                            78
## 6
                                        7.8
                                                       333
## # ... with 6 more variables: critics_score <dbl>, audience_rating <dbl>,
       best_pic_win <dbl>, best_actor_win <dbl>, best_actress_win <dbl>,
       best dir win <dbl>
#Loading the required library
library(psych)
## Warning: package 'psych' was built under R version 3.5.3
## Attaching package: 'psych'
## The following objects are masked from 'package:ggplot2':
##
##
       %+%, alpha
```

```
#Applying Factor Analysis on the data with 4 factors
fit pc <- principal(movies data, nfactors = 4, rotate = "varimax")</pre>
#Printing the results of Factor Analysis
fit_pc
## Principal Components Analysis
## Call: principal(r = movies data, nfactors = 4, rotate = "varimax")
## Standardized loadings (pattern matrix) based upon correlation matrix
##
                     RC1
                           RC3
                                 RC2
                                       RC4
                                             h2
                                                  u2 com
## title_type
                    -0.51 0.27
                                0.13
                                      0.38 0.49 0.51 2.6
## genre
                    0.13 -0.07 0.10 0.90 0.85 0.15 1.1
                    0.14 0.38 0.61 0.14 0.55 0.45 1.9
## runtime
                    0.87 0.14 0.13 0.04 0.80 0.20 1.1
## imdb rating
## imdb num votes
                    0.25 0.63 0.17 0.09 0.49 0.51 1.5
## critics rating
                   -0.82 -0.20 -0.01 -0.11 0.72 0.28 1.2
                    0.90 0.09 0.05 0.11 0.83 0.17 1.1
## critics_score
## audience rating
                    0.78 0.08 0.01 -0.03 0.62 0.38 1.0
## best pic win
                    0.06 0.77 0.00 -0.05 0.60 0.40 1.0
## best_actor_win
                    0.00 -0.09 0.86 -0.11 0.75 0.25 1.1
## best_actress_win 0.00 0.16 0.46 0.19 0.28 0.72 1.6
                    0.03 0.65 0.11 -0.01 0.44 0.56 1.1
## best dir win
##
##
                         RC1 RC3 RC2 RC4
## SS loadings
                        3.21 1.74 1.41 1.06
## Proportion Var
                        0.27 0.14 0.12 0.09
## Cumulative Var
                        0.27 0.41 0.53 0.62
## Proportion Explained 0.43 0.23 0.19 0.14
## Cumulative Proportion 0.43 0.67 0.86 1.00
##
## Mean item complexity = 1.4
## Test of the hypothesis that 4 components are sufficient.
##
## The root mean square of the residuals (RMSR) is 0.09
## with the empirical chi square 694 with prob < 4.5e-131
##
## Fit based upon off diagonal values = 0.88
#rounding the values to 3 decimal places
round(fit_pc$values, 3)
## [1] 3.500 1.866 1.133 0.923 0.899 0.884 0.690 0.680 0.545 0.501 0.268
## [12] 0.110
#Printing the loading data to console for the
fit_pc$loadings
##
## Loadings:
##
                   RC1
                          RC3
                                 RC2
                                        RC4
## title type
                   -0.506 0.273 0.133 0.382
```

```
## genre
                                    0.104
                     0.132
                                           0.902
## runtime
                     0.137
                            0.378
                                    0.606
                                           0.135
## imdb_rating
                     0.873
                             0.142
                                    0.132
## imdb num votes
                     0.245
                            0.628
                                    0.170
## critics_rating
                     -0.818 -0.202
                                          -0.112
## critics score
                     0.900
                                           0.107
## audience rating
                     0.785
## best_pic_win
                             0.769
## best_actor_win
                                    0.857 -0.106
## best actress win
                             0.162
                                    0.461 0.194
## best_dir_win
                             0.650
                                   0.115
##
##
                    RC1
                           RC3
                                 RC2
                                       RC4
                  3.215 1.740 1.406 1.063
## SS loadings
## Proportion Var 0.268 0.145 0.117 0.089
## Cumulative Var 0.268 0.413 0.530 0.619
```

Now we look at the cummunality

```
fit_pc$communality
##
         title_type
                               genre
                                               runtime
                                                            imdb_rating
##
          0.4942891
                           0.8469119
                                             0.5472540
                                                              0.8019189
##
                      critics_rating
     imdb num votes
                                         critics_score
                                                        audience rating
##
          0.4903074
                           0.7223572
                                             0.8328603
                                                              0.6227920
##
       best pic win
                      best actor win best actress win
                                                           best dir win
##
          0.5962795
                           0.7545185
                                             0.2764227
                                                              0.4373098
#Printing the scores
fit pc$scores
##
                                                            RC4
                   RC1
                                 RC3
                                               RC2
##
     [1,] -0.404943531 -0.4151740232 -0.905785630
                                                    0.183028231
##
     [2,]
           1.183523750 -0.2402690540 -0.587002215
                                                    0.495744916
##
           1.197150675 -0.1926766799 -0.872858317 -0.318041246
     [3,]
##
     [4,]
          0.746040312 1.0958964542 2.125086117 -0.420175510
##
     [5,] -1.130877722 -0.3332576205 -0.701393500
                                                    0.677958210
##
          1.646426936 -1.0411545451 -0.943452605 -1.248228614
     [6,]
##
     [7,]
          0.115330935 -0.0830649033 0.424679213
                                                    0.246007375
##
     [8,] -1.221370095 -0.8606384500 1.470345946 -0.413625812
##
     [9,]
          1.557306445 -0.9740526972 -0.756253960 -1.238763747
##
    [10,]
          0.870677078 -0.1027570390 -0.253094461
                                                    0.487940159
##
    [11,]
          0.917157157 -0.2144559166 2.079492782 -2.107898399
##
    [12,] -0.264092157 -0.1524256600 -0.374463777
                                                    0.468097194
##
    [13,]
          0.977543238 -0.0441425619 2.709930400 -0.596375459
##
    [14,] -1.041590787 -0.0317207272 -0.396299403 -0.516393889
    [15,] -1.724143498  0.0220824465  -0.284788381  -0.508662769
##
    [16,]
                        2.1455205480 0.173358702 0.588359711
          0.636538238
##
    [17,] -0.126275790 1.7372819920 0.264676679 -0.009345918
                                                    0.324577627
##
    [18,]
          0.412590116 -0.2315886569 -0.404510697
## [19,] -1.442241194 -0.1831500494 -0.710171808 0.658661506
```

```
[20,] -1.553467876 -0.1859099761 -0.754671897
##
                                                   0.294794439
##
    [21,] -0.110220238 -0.6170993913 2.123001738 -0.458591696
##
    [22,]
           1.605183665 -1.0058476245 -0.873200491 -1.239825111
##
    [23,] -0.222799785 -0.1378870489 -0.384236067
                                                   0.463762683
##
    [24,] -0.325981723 -0.1609200827 0.844553942
                                                   0.569636528
##
           1.789950915 -0.8936148244 -0.852732356 -1.169996042
    [25,]
    [26,] -1.042998018 -0.1373646959 -0.493312776 -0.480541136
##
          0.016352617
##
    [27,]
                        0.0223692741 3.212115808 -0.371823584
##
    [28,] -0.145955511
                       1.3653595674 -1.109924104
                                                   0.710462956
    [29,]
           0.554998513 -0.0527066393 -0.201190740 -0.770545341
##
##
    [30,]
           1.702105894 -1.0748775919 -0.555014366 -0.049130236
##
    [31,]
           1.128321685 -0.2707342639 -0.977846709
                                                   1.661847704
##
    [32,]
           0.482848145
                        0.0288407209 -0.706210618 -1.240209990
##
    [33,]
           0.753901850 -0.5792897380 -0.891776025
                                                   2.285494620
                        0.4908771494 -0.095964440
##
    [34,]
           0.596929860
                                                   1.573303898
##
    [35,] -0.713959267 -0.1176432936 -0.145736063 -0.088640959
##
    [36,] -0.619852633
                        0.9724109738 -0.158047553 -1.591356536
##
    [37,]
           0.795996289
                        0.1352959636 1.082613768
                                                   0.843553775
##
    [38,] -1.101572469 -0.1172888498 -0.118252976
                                                   0.248030081
##
                        3.3035117397 0.170582024 -1.633180854
    [39,]
          1.252315938
##
    [40,]
          0.436643694 4.8841208263 -1.005004910 -0.043948127
                                                   0.346740761
##
          0.417789274 -0.2387149869 -0.423027946
    [41,]
##
    [42,]
           0.908301482 -0.5476560817 2.175742855 -0.245015201
    [43,] -0.396986840 -0.1398715253 -0.482298267
                                                   0.137799151
##
##
    [44,] -0.844772921 -0.1447284815 -0.556391929 -0.442238990
##
    [45,]
          0.675018268
                       1.7950841584
                                     0.476001513
                                                   0.171311610
    [46,] -0.096762967 -0.1096696809 -0.154095528 -0.563133853
##
##
    [47,]
          0.095136079
##
    [48,] -0.588365444 -0.0541964400 0.298885649
                                                   0.346349086
##
    [49,] -1.908100068 -0.1238390254 -0.471456305
                                                   0.286730598
##
    [50,] -0.856051850 0.0077529771
                                     0.078647409
                                                   0.312165232
##
    [51,]
          1.346248066 -1.0833202995 -1.222765658 -1.296356386
##
    [52,] -0.024672116 0.5370712055
                                      0.078604178
                                                   0.186579966
##
    [53,] -0.575091337 -0.1379372919 -0.094987068
                                                   1.526957657
##
    [54,] -0.985936914
                       1.5617144728 -0.122444679
                                                   0.043289887
##
    [55,]
         0.312358468
                       6.4499838962 1.217880837 -1.245858022
##
    [56,] -0.333702213
                       1.5815134624 0.249349549 -0.037024136
    [57,] -0.666074826 -0.0599235893 -0.112982293
##
                                                   0.327006646
##
    [58,] -0.815048419 -0.2488453477 -0.429469947
                                                   0.345107214
##
    [59,] -1.277093281 -0.4682141631 -0.931401962
                                                   1.386747347
    [60,] -0.184240558 -0.9539269325 1.651097856
##
                                                   0.975810577
##
    [61,]
          0.252844342 -0.0665702658 -0.613564746 -0.200366072
##
    [62,] -0.869816696 -0.8271453487 2.611957677
                                                   0.023492930
##
    [63,]
          2.177341975 -0.8286792071 -0.431933953 -1.123859103
##
          2.008049606 -0.9007787898 -0.749353550 -1.128151792
##
    [65,] -0.651601314 -0.6163996990 1.897256985
                                                   0.849379834
##
    [66,] -1.561784995 0.0356970982 -0.687795457 -1.328227750
##
    [67,]
          1.803125109 -0.8678307146 -0.428124509 -1.206939067
##
    [68,] -0.266936958 1.4680000708 -0.130374221
                                                   1.028083129
  [69,] -0.195196561 -0.2211479616 -0.715914697 0.440833107
```

```
##
   [70,] -0.148001343 -0.1653767581 0.958150480
                                                 0.543980929
##
   [71,] -0.827222715 -0.5132129906 2.342314675 -0.324398603
##
   [72,] -1.363194701 -0.0967942947
                                    0.397519008 -0.193437635
##
   [73,] -1.025015125 -0.9985122768
                                    1.588688953
                                                 0.784144613
##
   [74,]
         0.553973287 -0.2181630681 -0.639755952 -0.428544516
##
   [75,] -0.144513678 -0.2079515094 -0.509874151
                                                 0.847156007
##
   [76,] -0.721411017 -0.0826442740
                                    0.161280006
                                                 0.358973009
##
   [77,] -0.721225559 -0.4814961582
                                    1.742737813 -1.907135940
##
   [78,] -0.683712975 -0.2780350191 -0.471332482
                                                 0.345272438
   [79,] -1.459357239 -0.0646616835 -0.469389230 -0.512518166
##
##
   [80,]
         0.719008349 1.3515772326 -0.505701178
                                                 0.144494326
##
   [81,] -0.208666792
                       0.4393024742 -0.156540444
                                                 1.542404897
##
   [82,]
         0.475682416 -0.2067060262 -0.696775528 -0.449171801
##
   [83,] -1.053420173
                       0.3407411963 -0.006609313 -1.656789796
    [84,] -1.126452896 -0.0266358242 -0.700980209 -1.698809783
##
##
                       0.9525986464 0.249627530
                                                 0.531323640
   [85,]
         1.290467923
##
   [86,] -0.846783580 0.0451969025 -0.322966447
                                                 0.323217459
##
   [87,] -0.203798794 -0.2559092565 -0.653218164
                                                 0.461523772
##
   [88,] -1.675883731 -0.2035746543 -0.729146067
                                                 0.265324079
##
          0.697416441 -0.2695839394 -0.382824423
                                                 0.400356405
   [89,]
##
   [90,] -1.254342686 -0.0615751058 -0.399154708
                                                -0.554721089
##
         1.077653467 -0.0812805110 -0.072335075
                                                 0.487276804
   [91,]
##
   [92,]
          [93,] -0.168432148 -0.4130569204 -0.731713130
##
                                                 1.663349289
##
         0.401821063 -0.8374417472 -0.571992410 -1.826283777
   [94,]
##
   [95,] -0.270425017 -0.2445333884 -0.608109711
                                                 0.469235308
   [96,] -0.702455918 -0.1948833584 -0.250647320
##
                                                 0.329963141
##
   [97,] -1.036799826 -0.2045279340 -0.367211688
                                                 0.280622389
##
          0.511314241 -0.7653277486 1.835925483
                                                 0.861988196
   [98,]
          0.559363688 6.9181788671 -1.179819027 -1.041033816
##
   [99,]
## [100,]
          1.714280113 -0.7297902794
                                    0.154213850 -1.195072606
## [101,]
          1.031591224 -0.1655498520
                                    0.278163963
                                                 0.845903556
  [102,] -0.875366202 -0.2289629034 -0.402431058
                                                 0.303070994
## [103,] -0.396924154 -0.7680083834
                                   2.533034822
                                                 0.164976251
## [104,]
         0.157555143 0.3517507145 -0.369979445
                                                 1.591224158
## [105,] -1.647551524 -0.1227996539 -0.801900535 -0.550530597
## [106,] -0.861083536 -0.1664946496
                                   0.612927390
                                                 0.654854338
         0.830473945 -0.3697482695 -0.721010477
                                                 0.380322477
## [107,]
## [108,] -1.003935762 -0.6026413658 2.088036793 -0.379826134
## [109,] -1.236968601 0.2443390401 -0.218412342 -1.690776275
## [110,] -1.648093891 -0.0621924268 -0.558132399 -0.517769644
         1.508844207 2.0687741161 2.748054251
## [111,]
                                                 1.562727950
## [112,] -0.191450251 -0.2553102811 -0.287958339
                                                 0.212171902
## [113,]
         0.493595523
                       0.2293368594
                                    0.001287262
                                                 0.368962107
## [114,] -1.339239878 -0.7623825255
                                    1.409625797 -1.198376990
## [115,] -1.127926374 -0.2636431524 -0.456040213
                                                 1.425950062
## [116,] -0.482853794 -0.1217675219
                                    0.013151231
                                                 0.150014629
## [117,] 1.678487349 -1.1108241368 -0.652894160 -0.037906608
## [118,] -0.112453954 0.5057944327
                                    0.193677906 -1.718638984
```

```
## [120,]
          1.582634724 -0.8387814526 -0.275477630 -1.232049268
## [121,] -0.755126992 -0.3463488707 2.030797645 -0.304523480
## [122,]
         0.446423375
                      0.0281966979 -0.821179661
                                                 0.342166167
## [123,] -1.521204746 -0.1195195061 -0.580769821
                                                 0.318668086
## [124,] -1.173920024 0.0768948450 -0.376386229 -0.536427966
## [125,]
          0.657784827 -0.1555570116 -0.100746690
                                                 0.383349333
## [126,] -1.339715786 -0.1268806225 -0.725756014 -0.667770335
## [127,]
         0.289862963 -0.2725021756 -0.800886432
                                                 0.981547057
## [128,] -0.895317495 -0.1018220916 -0.485237775 -0.508560883
## [129,]
          0.450694704 -0.2543789140 -0.680391838
                                                 0.337601954
## [130,]
          1.063302362 -0.2607945139 -0.630000870
                                                 0.449677064
## [131,]
          1.627843765 -1.2751196220 -1.759224113
                                               -1.254524165
## [132,]
          0.468457047
## [133,] -1.898569092 -0.5272914085 1.370973458 -1.202958877
## [134,]
          1.629116358 -0.5795701239 0.631395681 -1.156520888
         0.572582217 -0.1869442874 -0.151383247
                                                 0.352377734
## [135,]
## [136,] -0.088378132 -0.6888059860 3.072133684
                                                 0.204042853
## [138,] -0.431320365
                       0.0780661776 -0.691860911
                                                 0.475727819
## [139,] -0.999539388
                       0.6455513007 -0.518819020 -1.643349906
## [140,]
         1.188744242 1.6230021102 -0.537148130 -0.254030067
## [141,] -0.840205665 -0.1942316598 -0.598788257 -0.466359632
## [142,] -1.196316482 -0.2300066948 -0.608162075
                                                 0.239541894
         0.456532342 -0.2321060440 -0.515177269
## [143,]
                                                 0.316688714
## [144,]
         0.706816842 -0.3372822182 -0.594639132
                                                 0.356070665
## [145,] -0.449553604
                      1.1686126546 3.542185801
                                               -0.056276732
                                                 1.977276699
## [146,]
         0.773795629 -0.6219644070 -0.839410927
## [147,] -0.280828278
                       0.1456932756 -0.156898139 -1.505653196
## [148,] -0.411961696
                      1.7795043224 0.142972018
                                                 0.220412174
## [149,]
                       0.3420116289 -0.216628326
         1.250591085
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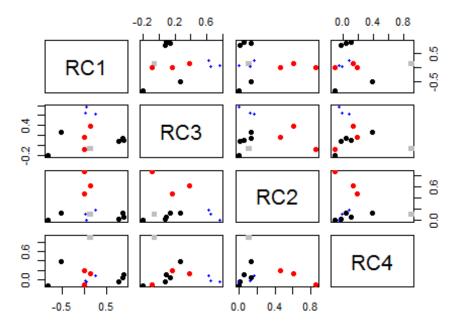
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           0.872744676 -0.3555355840 -0.603803791
## [587,]
                                                    0.373502392
## [588,] -1.236795366 -0.0428821310 -0.307600608
                                                  -0.488232540
## [589,] -0.050520056 -0.8414199571
                                     2.925103952
                                                    1.389621714
## [590,]
           0.948889421
                        0.1408634762
                                      0.570169464
                                                    0.840615347
## [591,]
           1.624030406 -0.7604557883
                                      0.512704271 -0.773916952
## [592,]
           1.630236108 -0.9484493260 -0.644617045 -1.208795889
## [593,] -0.204156999
                        1.3050690253 -0.521600752
                                                    1.423766910
## [594,]
           1.079235135
                        0.5419290896
                                     0.183740902
                                                    0.527674409
## [595,]
           0.233755295 -0.1254987278 -0.328122127
                                                    0.224241931
                                     2.736423883
## [596,]
           0.802811225 -0.8155912806
                                                    0.092532554
                        0.2482380591 -0.779361219 -1.625137413
## [597,]
           0.674288987
## [598,]
           0.435260247 -0.0825846950 0.931245069
                                                    2.295847997
                        0.3493780709 -0.854114013 -1.081644559
## [599,]
           1.205530302
## [600,] -0.746915697 -0.5611149979
                                     1.616192237 -2.307038188
## [601,]
           1.004970587
                        0.0245004672 -0.317049944 -0.686224102
## [602,]
           1.830368138 -0.9685403243 -0.612617314 -1.232598607
## [603,] -0.077352941 -0.3670827377 -0.632657088
                                                    0.565690858
## [604,] -0.843877044
                        0.2671617785 -0.035996947
                                                  -1.609748385
## [605,] -0.716907578 -0.3037740218 -0.678769591
                                                    0.707608046
           0.085108091 -0.2283280446 0.011917607
## [606,]
                                                    1.019667472
## [607,] -0.160415849 -0.3353248979 -0.561191424
                                                    0.170464479
## [608,] -0.973540613 -0.0088080167 -0.359595104
                                                    0.267249616
## [609,]
           1.184010141 -0.3099979969 -0.998102276
                                                    0.463885263
           0.409632018 9.2351971688 0.799778851
## [610,]
                                                  -0.102832872
## [611,]
           1.977395651 -0.8780763958 -0.707689473
                                                  -1.133238702
## [612,] -0.792130577 -0.1257738515 -0.198409321
                                                    0.327235648
## [613,]
           0.482942379 -0.2219414097 -0.387443365
                                                    0.342636843
           0.004767950 -0.2596629694 -0.553155870
                                                    0.457391304
## [614,]
## [615,]
           1.930044775 -0.8821992686 -0.806383029
                                                  -1.148441147
           1.171823907 -0.3058948038 -0.769771058
                                                    0.462016535
## [616,]
## [617,] -1.547682750 -0.1657314029 -0.822231364
                                                  -0.557749428
## [618,]
          0.960010382 -0.4024376953 -0.714522727
                                                    0.396215403
## [619,] -0.808385961 -0.8699595253 1.623757286 -0.344582037
```

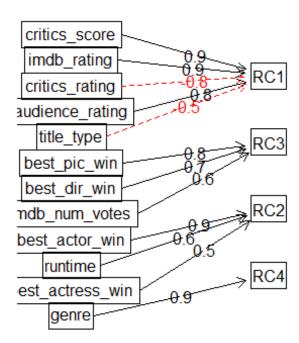
```
## [620,] -0.253848572 -0.1412237283 -0.362718828 0.456872319
## [621,] -0.608270740 -0.0387789784 -0.585316534 -1.822090441
## [622,] -1.402782568 -0.0840117380 -0.522022743 -0.537799123
## [623,] 0.529553291 -0.2615502200 -0.668063391 -0.080136683
## [624,] 1.084738778 -0.7701969208 1.716481562 -0.163430178
## [625,] 0.391000277 1.5008650490 -0.704346951 -0.687033960
## [626,] 1.308587973 0.2714506814 2.172948035 -0.104293792
## [627,] -1.321787845 -0.2020043480 -0.392508892 0.625836144
## [628,] 0.452572950 -0.1526105304 -0.174708061
                                               1.540248296
## [629,] -1.306360726 -0.2841444302 1.960985726 -2.369060103
## [631,] -1.091042163 -0.7034141883 2.000885579 -0.371520639
## [632,] -1.687039473 -0.2827769220 0.402107037 1.775353621
## [633,] 1.028186627 2.1478526846 1.232533009 0.959449491
## [634,] -1.122580288 -0.2549239837 -0.593615177
                                                0.307977870
## [635,] -0.276320752   0.0685239002   0.536404763   0.535597389
## [636,] 1.240519039 -0.3622954280 3.153223409 0.221790267
## [637,] -1.053776187 -0.1750346818 -0.422691077 0.246503533
## [638,] -1.149898664 -0.1624377763 0.476080568 1.796513291
## [639,] 0.700883443 -0.2330303293 -0.284059102
                                                0.384294870
## [640,] -0.886647655 -0.0007959968 1.299363659
                                                0.679595070
## [641,] -0.672801798  0.0812856784 -0.586041423 -1.410751857
## [642,] 1.998992509 -0.9737070359 -0.591975687 0.059994570
## [643,] 1.134692248 -0.5075791485 1.746730431 -0.154858371
## [644,] 0.586137849 -0.4979088082 -0.839706349
                                              1.528443065
## [645,]
         ## [646,] -1.095168827 -0.1001961450 -0.153231987
                                                0.314479459
## [647,] -0.832445523 -0.2460363668 -0.505095277
                                                0.309154292
## [648,] -0.279907451 -0.1412668325 -0.758658516 -0.645098173
## [649,] -0.198902263 -0.0087295117 -0.708952273 -1.482335287
## [650,] -1.038959928      0.3763020872      0.059327449      -1.656843374
## [651,] -1.543419462 0.0469533267 -0.538308589 -0.516637025
# See Correlations within Factors
fa.plot(fit pc)
```

Principal Component Analysis



#Visualize the relationship
fa.diagram(fit_pc)

Components Analysis



```
fit1 <- lm(audience score~., data = train[,-1])
g1 <- step(fit1)
## Start: AIC=2523.57
## audience score ~ title type + genre + runtime + imdb rating +
       imdb_num_votes + critics_rating + critics_score + audience_rating +
##
       best_pic_win + best_actor_win + best_actress_win + best_dir_win
##
##
                      Df Sum of Sq
                                      RSS
                                             AIC
## - best_pic_win
                                  1 30449 2521.6
                       1
## - best dir win
                       1
                                  1 30449 2521.6
## - best actor win
                       1
                                  3 30451 2521.6
## - critics_rating
                       1
                                 7 30454 2521.7
## - title_type
                       1
                                22 30469 2522.0
## - critics_score
                       1
                                46 30494 2522.6
## - imdb_num_votes
                       1
                                48 30496 2522.6
## - best actress win 1
                                69 30517 2523.0
## <none>
                                    30448 2523.6
## - runtime
                       1
                                152 30600 2524.8
## - genre
                       1
                                205 30653 2525.9
## - imdb_rating
                       1
                             17711 48159 2819.1
## - audience_rating
                       1
                             32608 63056 2994.1
##
## Step: AIC=2521.59
## audience_score ~ title_type + genre + runtime + imdb_rating +
##
       imdb_num_votes + critics_rating + critics_score + audience_rating +
       best_actor_win + best_actress_win + best_dir_win
##
##
##
                      Df Sum of Sa
                                      RSS
                                             AIC
## - best_dir_win
                       1
                                  2 30450 2519.6
                                  3 30451 2519.7
## - best_actor_win
                       1
## - critics_rating
                       1
                                 7 30455 2519.7
## - title type
                       1
                                22 30470 2520.1
                       1
                                46 30495 2520.6
## - critics score
                       1
## - imdb num votes
                                53 30502 2520.7
## - best_actress_win 1
                                68 30517 2521.0
                                    30449 2521.6
## <none>
## - runtime
                       1
                                151 30600 2522.8
## - genre
                       1
                                205 30654 2523.9
## - imdb rating
                       1
                             17717 48165 2817.2
## - audience rating
                       1
                             32609 63058 2992.1
## Step: AIC=2519.62
## audience_score ~ title_type + genre + runtime + imdb_rating +
##
       imdb_num_votes + critics_rating + critics_score + audience_rating +
##
       best actor win + best actress win
##
##
                      Df Sum of Sq
                                      RSS
                                             AIC
## - best actor win
                       1
                                  3 30453 2517.7
                       1
                                 7 30457 2517.8
## - critics_rating
```

```
1
                                 21 30471 2518.1
## - title type
## - critics score
                       1
                                 47 30497 2518.6
## - imdb_num_votes
                       1
                                 55 30505 2518.8
## - best actress win 1
                                68 30518 2519.1
## <none>
                                    30450 2519.6
## - runtime
                       1
                                150 30600 2520.8
                       1
                                205 30655 2522.0
## - genre
## - imdb rating
                       1
                             17726 48176 2815.4
## - audience_rating
                             32665 63115 2990.7
##
## Step: AIC=2517.69
## audience score ~ title type + genre + runtime + imdb rating +
##
       imdb num votes + critics rating + critics score + audience rating +
##
       best actress win
##
##
                      Df Sum of Sa
                                      RSS
                                             ATC
## - critics_rating
                       1
                                 7 30460 2515.8
## - title type
                       1
                                21 30474 2516.1
## - critics score
                       1
                                48 30501 2516.7
## - imdb_num_votes
                       1
                                55 30508 2516.8
                                66 30519 2517.1
## - best actress win 1
## <none>
                                    30453 2517.7
## - runtime
                       1
                                148 30601 2518.8
## - genre
                       1
                                204 30657 2520.0
## - imdb rating
                       1
                             17754 48208 2813.8
## - audience_rating
                       1
                             32759 63213 2989.7
##
## Step: AIC=2515.83
## audience_score ~ title_type + genre + runtime + imdb_rating +
##
       imdb num votes + critics score + audience rating + best actress win
##
##
                      Df Sum of Sa
                                      RSS
                                             AIC
## - title_type
                       1
                                 20 30480 2514.3
## - best actress win 1
                                65 30525 2515.2
## - imdb num votes
                       1
                                77 30536 2515.5
## <none>
                                    30460 2515.8
                                155 30614 2517.1
## - runtime
                       1
## - critics_score
                       1
                                164 30624 2517.3
## - genre
                       1
                                205 30665 2518.2
                       1
## - imdb rating
                             18166 48625 2817.4
## - audience_rating
                       1
                             33435 63895 2994.6
##
## Step: AIC=2514.26
## audience_score ~ genre + runtime + imdb_rating + imdb_num_votes +
       critics score + audience rating + best actress win
##
##
##
                      Df Sum of Sq
                                      RSS
                                             AIC
                                64 30544 2513.6
## - imdb_num_votes
                       1
## - best_actress_win 1
                                71 30551 2513.8
## <none>
                                    30480 2514.3
```

```
## - runtime
                                 172 30652 2515.9
                        1
## - critics score
                                 177 30658 2516.0
## - genre
                        1
                                 221 30702 2517.0
                      1 19195 49675 2829.2
1 33431 63911 2992.8
## - imdb rating
## - audience_rating
##
## Step: AIC=2513.63
## audience_score ~ genre + runtime + imdb_rating + critics_score +
       audience_rating + best_actress_win
##
                       Df Sum of Sq
##
                                       RSS
                                               AIC
                                  63 30608 2513.0
## - best_actress_win 1
## <none>
                                     30544 2513.6
## - runtime
                        1
                                 130 30675 2514.4
## - critics_score
                        1
                                 165 30709 2515.1
## - genre
                        1
                                 226 30771 2516.4
## - imdb_rating
                        1
                               20291 50836 2842.2
## - audience rating 1 33506 64050 2992.2
##
## Step: AIC=2512.97
## audience_score ~ genre + runtime + imdb_rating + critics_score +
##
       audience_rating
##
##
                      Df Sum of Sq
                                      RSS
                                              AIC
## <none>
                                    30608 2513.0
## - critics_score
                       1
                                162 30769 2514.4
                                173 30781 2514.6
## - runtime
                      1
                                242 30850 2516.1
## - genre
                       1
## - genre 1 242 30850 2516.1

## - imdb_rating 1 20277 50885 2840.9

## - audience_rating 1 33586 64194 2991.7
library(car)
## Warning: package 'car' was built under R version 3.5.2
## Loading required package: carData
## Attaching package: 'car'
## The following object is masked from 'package:psych':
##
##
       logit
## The following object is masked from 'package:dplyr':
##
##
       recode
compareCoefs(fit1,g1,se=FALSE)
## Calls:
## 1: lm(formula = audience_score ~ ., data = train[, -1])
```

```
## 2: lm(formula = audience score ~ genre + runtime + imdb rating +
     critics_score + audience_rating, data = train[, -1])
##
##
##
                     Model 1 Model 2
## (Intercept)
                       -24.0
                               -27.4
## title_type
                      -0.701
## genre
                     -0.262 -0.282
## runtime
                     -0.0290 -0.0279
## imdb_rating
                        9.18
                                9.30
## imdb num votes
                    3.02e-06
## critics_rating
                       -0.25
## critics_score
                      0.0217 0.0276
## audience rating
                                20.5
                        20.4
## best_pic_win
                       0.363
## best_actor_win
                         0.2
## best_actress_win
                       -1.08
## best dir win
                       0.171
fit_final <- lm(audience_score ~</pre>
genre+runtime+imdb_rating+critics_score+audience_rating, data=train[,-1])
summary(fit_final)
##
## Call:
## lm(formula = audience score ~ genre + runtime + imdb rating +
       critics_score + audience_rating, data = train[, -1])
##
##
## Residuals:
##
        Min
                  10
                       Median
                                    30
                                            Max
## -21.0752 -4.7253
                       0.6766
                                4.3219 24.4640
##
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
##
                                                  <2e-16 ***
## (Intercept)
                   -27.43046
                              2.25795 -12.148
## genre
                                0.12495 -2.255
                   -0.28172
                                                  0.0245 *
## runtime
                                0.01463 -1.907
                   -0.02790
                                                  0.0569 .
                                                  <2e-16 ***
## imdb_rating
                     9.30480
                                0.45083 20.639
## critics_score
                                0.01500
                                        1.842
                                                  0.0659 .
                     0.02764
## audience rating 20.47743
                                0.77092 26.562
                                                  <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.899 on 643 degrees of freedom
## Multiple R-squared: 0.8844, Adjusted R-squared:
## F-statistic: 983.6 on 5 and 643 DF, p-value: < 2.2e-16
newmovie <- test %>% select(genre, imdb_rating,
audience rating,critics score,runtime)
predict(fit final, newmovie)
```

```
## 1
## 90.28938

predict(fit_final, newmovie, interval = "prediction", level = 0.95)

## fit lwr upr
## 1 90.28938 76.61211 103.9666

test$audience_score
## [1] 94
```
