Question 2 [25]: Tree Freak

A value FL of type (string * int) list is called a frequency list if and only if:

- Every string appearing in the first component of any pair in FL appears in exactly one pair in FL.
- Every integer appearing in the second component of any pair in FL is strictly positive.

For example,

is a frequency list but

is not.

(a) (7 points) Write the function

```
insert: (string * int) -> (string * int) list -> (string * int) list insert takes a frequency list FL and a new pair (s_new,c_new). Conceptually, insert either updates the existing frequency of s_new if there is one or adds it to the list if there isn't. More formally:
```

- If there is some pair (s,c) in FL such that s=s_new then the returned frequency list contains the pair (s_new,c+c_new).
- If there is no such element, then the returned frequency list contains the pair (s_new,c_new) in addition to everything in FL.

Given a valid frequency list and a pair (s_new,c_new) with c_new > 0, insert must evaluate to a valid frequency list.

(b) (6 points) Write the function

combine takes two frequency lists and combines them into one frequency list pairing each string with the sum of its counts in the inputs. More formally, if FL1 and FL2 are two frequency lists, and CFL is the result of calling combine FL1 FL2:

- If (s,c1) appears in FL1 and (s,c2) appears in FL2, then (s,c1 + c2) appears in CFL.
- If (s,c) appears in one of the input list and s does not appear in the other list then (s,c) appears in CFL.
- If s does not appear in either FL1 or FL2, then s does not appear in CFL.

For example, if we have the two frequency lists

```
val FL1 = [("a", 4), ("b", 1)]
val FL2 = [("a", 12), ("b", 4), ("x", 9)]
```

then combine FL1 FL2 should evaluate to the frequency list

While writing this function, you may assume that the insert function satisfies the above specification.

Recall the datatype of trees that carry data only at their leaves

We will now relate frequency lists to trees. Let T be a value of type string tree and FL be a frequency list. We say that FL is a frequency list of T if and only if

- A string appears in a leaf of T if and only if it appears as the first component of a pair in FL.
- If a particular string s appears in k leaves of T, then (s,k) appears in FL.

For example, one frequency list for the tree

is not a frequency list for this tree because "a" appears with the wrong count and "c" appears in no leaf of the tree.

(c) (7 points) Write the function

count takes a tree and builds a frequency list for that tree. While writing this function, you may assume that the combine function satisfies the above specification.

Using mapreduce, write the function

```
count_mr : string tree -> (string * int) list
```

count_mr takes a tree and builds a frequency list for that tree by calling map-reduce with appropriate arguments. count_mr is not a recursive function. While writing this function, you may assume that the combine function satisfies the above specification.

You may not use the function count while writing count_mr.

fun	count_mr	(t	:	string	tree)	:	(string	*	int)	list
ma	apreduce									