# 15-381 Assignment 01

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## 1: Task 1.1

## Formulation one:

Variables:

B, M, S, H, P, C, where each variable has domain  $\{1, 2, 3, 4, 5, 6\}$ 

Constraints:

 $(\text{define } m(n) = (n \mod 6) + 1)$ 

- 1. BMSHPC must be distinct values
- 2. m(B M) = 1
- 3. m(S H) = 1
- 4. m(H P) = 1
- 5.  $m(P-C) \neq 1$ ,  $m(S-C) \neq 1$ ,  $m(H-C) \neq 1$
- 6. C = 1

### Formulation two:

Variables:

 $A_1, A_2, A_3, A_4, A_5, A_6$ , where each variable  $A_i$  represents the person or animal sitting in seat i, and has domain  $\{A, B, C, D, E, F\}$ 

Constraints:

 $(\text{define } m(n) = (n \mod 6) + 1)$ 

TODO

Lastly, (TODO Why inefficient to run AC3 with more constraints?)

## 2: Task 1.2

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3: Task 1.3

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4: Task 1.4

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## 5: Task 1.5

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### 6: Task 2.1

If  $X_i$  has constraint  $X_i = c$ , let its domain  $D_i = \{c\}$  (the singleton set containing c) Then the constraint is no longer necessary.

### 7: Task 2.2

$$X_1 + X_2 = X_3$$

Make a variable called Z, and let its domain be a pair of values, where the first value may be in the domain of  $X_1$  and the second in the domain of  $X_2$ . Then the three equivalent binary constraints are:

- 1.  $Z[1] = X_1$
- 2.  $Z[2] = X_2$
- 3.  $Z[1] + Z[2] = X_3$

### 8: Task 2.3

$$X_1 + X_2 + \dots + X_{n-1} = X_n$$

Let Z be an n-1 tuple. ¡TODO domain; Then you need a minimum of n constraints:

- 1. Z[1] = X1
- 2. Z[2] = X2
- 3. ...
- 4.  $Z[n-1] = X_{n-1}$
- 5.  $Z[1] + Z[2] + ... + Z[n-1] = X_n$

(Not good at latex but that should be 1 - n.

## 9: Task 2.4

Given an n-ary constraint, stuff n-1 of the variables into a new variable, let that be Z in this discussion. Then, create n-1 constraints, where  $Z[i] = X_i$  for i=1 to n-1 Then create an additional constraint, which is the original constraint, but substitute the variables with Z and a positional index.  $(X_i - > Z[i])$ 

Why? TODO