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# **Development of new advanced estimation algorithms for improving the resilience of the autonomous and connected vehicle**

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# Chapitre 1

## Resilient State Estimation and Cyber-Attack Reconstruction for Connected Autonomous Vehicles

### Objectifs

The primary objective of this work is to develop a resilient controller and state observers capable of :

- Estimating unmeasured quantities necessary for the SA-ACC.
- Detecting and reconstructing false data injected into the communication channel exactly and in finite time.
- Compensating for these attack signals to maintain vehicle autonomy.

## 1 Introduction

Connected autonomous vehicles (CAVs) have revolutionized conventional transportation systems through the facilitation of wireless communication and interaction among vehicles [Bu, 2012]. A significant stride in this domain is the emergence of Cooperative Adaptive Cruise Control (CACC), which builds upon the capabilities of Adaptive Cruise Control (ACC). While ACC autonomously adjusts vehicle speeds based on preceding traffic, CACC elevates this functionality by integrating inter-vehicle communication. As wireless communication and data exchange become more prevalent in CAVs, there is a growing concern about cyberattacks. It is essential to detect these attacks to maintain the safety, reliability, and integrity of vehicular communication systems. These attacks can take many forms, such as false data injection, Denial of Service (DoS), eavesdropping, or interference, targeting communication channels or sensor systems. Hence, detecting and mitigating these attacks is crucial for ensuring that CAVs function correctly and road safety is maintained [Khalil, 2020 ; Huang, 2022 ; Mousavinejad, 2019 ; Cabelin, 2021].

In prior work, a proportional integral observer was introduced in [Pan, 2023b] for state estimation and spoofing attack detection, and in [Pan, 2023a] for addressing the DoS attack issue by estimating data transmission delays. Nevertheless, these results are limited to scenarios where the attack evolves slowly. Some other work such as [Yamamoto, 2021] and [Cheng, 2023] utilize the concept of unknown input observer (UIO) residual. This residual is used to detect attacks and is enhanced by setting an adaptive threshold that considers the impact of disturbances, thereby improving the accuracy of the attack detector. This UIO-based technique, as utilized also in [Jeon, 2020] within the ACC framework, is specifically designed for constant cyberattack signals.

In this paper, we address the challenge of cyberattack detection by utilizing an UIO to estimate attacks and create an observer-based control to mitigate their adverse effects on platoons with CACC. This algorithm can also be used to monitor cyberattack status with different types of control and modifications. A significant difference in our method is that we transmit data using the acceleration of the preceding vehicle rather than the control input. The advantage of this approach is that in a platoon, we cannot have the same control input, and using acceleration data is more suitable. In contrast to the methodology presented in [Pan, 2023b ; Pan, 2023a ; Jeon, 2020], our proposed approach demonstrates the capability to effectively handle time-varying cyberattack. Unlike the framework outlined in [Pan, 2023b ; Pan, 2023a ; Jeon, 2020], which offers adaptability to dynamic cyberattack scenarios.

On each vehicle, the UIO-based estimator computes the relative state between the preceding and following vehicles while examining any potentially erroneous communication signal data. In the event of a cyberattack, a resilience-controlled system is activated, leveraging the state estimated from UIO. Simulation experiments have demonstrated that the proposed mechanism accurately estimates the system state with a 1-step delay and detects attacks with a 2-step delay. This mechanism not only enhances the system stability but also mitigates safety losses induced by cyberattacks.

## 2 Problem Formulation

### 2.1 General description of the CACC system

The CACC scenario working on a platoon can be illustrated as in Figure 1.1. In Figure 1.1,

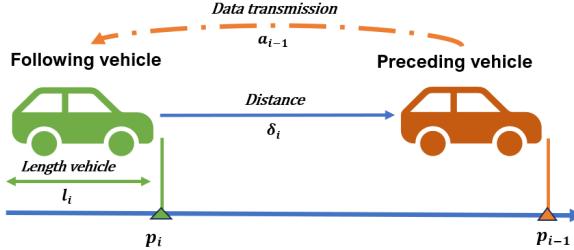


FIGURE 1.1 – Illustration of CACC working on a vehicle platoon.

$a_{i-1}$  represents the acceleration of the preceding vehicle transmitted through a wireless communication channel to the following vehicle;  $\delta_i$  denotes the distance between the rear of the preceding vehicle and the bumper of the following vehicle;  $l_i$  is the length of the following vehicle;  $p_i$  and  $p_{i-1}$  correspond to the positions of the following and preceding vehicles, respectively.

The CACC control system of a vehicle comprises two controllers : an upper-level controller and a lower-level controller. The lower-level controller is responsible for utilizing throttle and/or brake control inputs to achieve the desired acceleration tracking. On the other hand, the upper-level controller is tasked with calculating the desired acceleration to maintain the desired spacing with respect to a preceding vehicle. In line with the approach discussed in [Rajamani, 2002], this paper focuses exclusively on the investigation of the upper-level controller, operating under the assumption that a suitable lower-level controller is already in place.

### 2.2 CACC modeling subject to cyberattack

Basically, the dynamics of  $i^{th}$  vehicle are a Position-Velocity-Acceleration third-order linear model given by the following set of equations :

$$\begin{cases} \dot{p}_i(t) = v_i(t) \\ \dot{v}_i(t) = a_i(t) \\ \dot{a}_i(t) = \frac{1}{\tau_i} u_i(t) - \frac{1}{\tau_i} a_i(t) \end{cases} \quad (1.1)$$

where

- $p_i(t)$ ,  $v_i(t)$  and  $a_i(t)$  denote the position, velocity and acceleration of the  $i^{th}$  vehicle, respectively ;
- $u_i(t)$  is the  $i^{th}$  vehicle control input representing the desired driving/braking force or acceleration ;
- $\tau$  is the engine's constant time lag.

The actual spacing between vehicles are  $\varepsilon_{i,act} = p_{i-1} - p_i$  and the desired spacing between vehicles in the constant time-gap spacing policy is given by  $\varepsilon_{i,des} = L + h v_i$ . It follows that the

spacing error can be written as :

$$\varepsilon_{i,des} - \varepsilon_{i,act} \triangleq p_i - p_{i-1} + L + hv_i = \varepsilon_i + hv_i, \quad (1.2)$$

where  $L$  is the minimum safety distance and  $h$  is the time-gap. Then, the controller  $u_i$  is given by [Rajamani, 2002] :

$$\begin{aligned} u_i &= -k_1 a_{i-1} + (k_1 + hk_1 k_2) a_i \\ &\quad - \frac{1}{h} (1 - hk_1 k_2) \dot{\varepsilon}_i - \frac{k_2}{h} \varepsilon_i - k_2 v_i \end{aligned} \quad (1.3)$$

where  $a_{i-1}$  is the acceleration of the preceding vehicle obtained by using inter-vehicle communication. The scalar gains  $k_1$  and  $k_2$  are the controller design parameters to be designed according to the detailed procedure introduced in [Rajamani, 2002].

The controller  $u_i$  defined in (1.3) is convenient in perfect situation where the acceleration of the preceding vehicle,  $a_{i-1}$ , provided through V2V communication channel is not corrupted by intruders. Unfortunately, in CACC platoons, the V2V communication may provide unreliable acceleration due to potential tampering by attackers. To develop a resilient controller to cyber-rattacks, we have to consider the attack signal in the design of the controller. To this purpose, we assume that the following vehicle receives the signal  $\mu(t)$  corrupted by injected false data in the wireless communication channel :

$$\mu(t) = a_{i-1}(t) + f^c(t) \quad (1.4)$$

where  $a_{i-1}(t)$  is the true acceleration and  $f^c(t)$  is the additive cyberattack signal. This cyber-rattack scheme under additive false signals can cover several cyberattack architectures. These may include message falsification attacks, spoofing attacks, and denial of service (DoS) attacks. For instance, in the DoS case, by using the differential mean value theorem, there exists  $\theta_t \in [t - \tau(t), t]$  such that the delayed signal  $a_{i-1}(t - \tau(t))$  can be represented as follows :

$$\begin{aligned} \mu(t) &= a_{i-1}(t - \tau(t)) = a_{i-1}(t) - \underbrace{\frac{da_{i-1}}{dt}(\theta_t) \tau(t)}_{f^c} \\ &= a_{i-1}(t) + f^c. \end{aligned} \quad (1.5)$$

Under a cyberattack, the following vehicle receives  $\mu$  and will utilize it in its controller. Then, instead of (1.3), the controller  $u_i$  will be implemented as follows :

$$\begin{aligned} u_i &= -k_1 \mu(t) + (k_1 + hk_1 k_2) a_i \\ &\quad - \frac{1}{h} (1 - hk_1 k_2) \dot{\varepsilon}_i - \frac{k_2}{h} \varepsilon_i - k_2 v_i. \end{aligned} \quad (1.6)$$

As shown in Figure 1.1, the radar-measured rear-to-bumper distance is defined as follows :

$$\delta_i = p_{i-1} - p_i - l_{i-1}, \quad (1.7)$$

Then, taking the time derivative of  $\delta_i$  results in :

$$\dot{\delta}_i = v_{i-1} - v_i, \ddot{\delta}_i = a_{i-1} - a_i, \ddot{\delta}_i = \dot{a}_{i-1} - \dot{a}_i \quad (1.8)$$

where  $\dot{\delta}_i$ ,  $\ddot{\delta}_i$ , and  $\ddot{\delta}_i$  are the relative speed, acceleration, and jerk (rate of acceleration changes) between two adjacency vehicle. By using (1.7) and (1.8), the controller (1.6) becomes

$$\begin{aligned} u_i &= (hk_1k_2)\mu - (k_1 + hk_1k_2)f^c - k_2v_i - \frac{k_2}{h}(L - l_{i-1}) \\ &\quad - (k_1 + hk_1k_2)\ddot{\delta}_i + \frac{1}{h}(1 - hk_1k_2)\dot{\delta}_i + \frac{k_2}{h}\delta_i. \end{aligned} \quad (1.9)$$

We obtain acceleration information of the preceding vehicle directly through wireless communication. As a result, we assume the jerk of the preceding vehicle to be zero, without considering its lower-order dynamics.

$$\dot{a}_{i-1} = 0 \quad (1.10)$$

Substituting equation (1.9) into (1.1) and using (1.10) and the notation  $x = [\delta_i \ \dot{\delta}_i \ \ddot{\delta}_i]^\top$ , we obtain the model expressed under the following condensed matrix form :

$$\begin{cases} \dot{x} = Ax + Bv_i + F\mu + \Delta - Wf^c \\ y = Cx \end{cases} \quad (1.11)$$

with

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ \frac{-k_2}{\tau h} & \frac{-k_3}{\tau h} & \frac{(k_1 - k_3)}{\tau} \end{bmatrix}, B = \begin{bmatrix} 0 \\ 0 \\ \frac{k_2}{\tau} \end{bmatrix}, F = \begin{bmatrix} 0 \\ 0 \\ \frac{k_3}{\tau} \end{bmatrix},$$

$$\Delta = \begin{bmatrix} 0 \\ 0 \\ \frac{k_2(L - l_{i-1})}{\tau h} \end{bmatrix}, W = \begin{bmatrix} 0 \\ 0 \\ \frac{k_3 - k_1}{\tau} \end{bmatrix}, C = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$$

where  $k_3 \triangleq 1 - hk_1k_2$ .

Notice that to avoid cumbersome equations, the interaction between two cars in the CACC scenario is represented without the subscripts  $i$  and  $i - 1$ . These are deleted from the matrices  $A, B, F, \Delta, W$ , and  $C$  and from the vectors  $x, y$  and  $f_c$ . Only  $v_i$  is kept to avoid confusion with the previous equations.

## 2.3 Problem formulation and objectives

The main objective in the CACC control problem consists in estimating the false data,  $f^c$ , and compensating it in the controller  $u_i$ . The natural solution is the use of the well-known UIO technique to estimate simultaneously the state  $x$  and the false data  $f^c$  as an unknown input.

To this end, it is well-known in the literature [Chaouche, 2022 ; Trinh, 2011] that a necessary rank condition is required, namely  $\text{rank}(CW) = \text{rank}(W)$ . Unfortunately, in the case of the CACC with the matrices given in (1.11) such a rank constraint is not satisfied since we have  $\text{rank}(CW) = 0$  and  $\text{rank}(W) = 1$ . To overcome the fall in rank condition, we need additional information, namely the relative acceleration. This information is typically obtained using a real-time differentiator whose role is to estimate online the derivative of relative velocity. Indeed, since  $CB = CF = C\Delta = CW = 0$ , then with the derivative of  $y$  as a pseudo-measurement, i.e. :

$$\bar{y} \triangleq \dot{y} = CAx = \bar{C}x \quad (1.12)$$

we can construct a UIO to estimate  $x$  and  $f^c$  since  $\text{rank}(\bar{C}W) = \text{rank}(W) = 1$ . Of course, some additional conditions are required to ensure an exponential UIO.

There are numerical differentiators in the literature allowing the online calculation of the derivative of a given signal, such as the famous sliding mode observer [Zhu, 2012], and the high-gain observer [Dabroom, 1997]. However, these numerical differentiators fail in some situations, namely in the presence of sensor noises. An alternative solution to avoid real-time estimation of the derivative of  $y$  consists in investigating the problem by using the discrete-time version of the model, as shown in Figure 1.2 which considers additive sensor noise  $\omega$ .

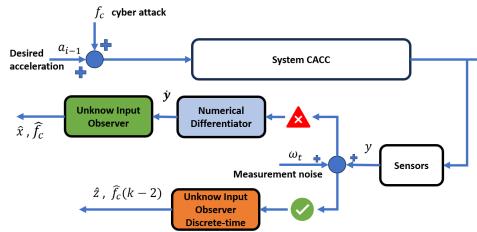


FIGURE 1.2 – Discrete-time model-based UIO.

Indeed, in discrete time, there is no differentiation since the measured signal is a sequence of numbers. The discrete-time version of equation (1.11) is given as follows :

$$\begin{cases} x_{k+1} = \mathcal{A}x_k + \mathcal{B}v_{i,k} + \mathcal{F}\mu_k + \bar{\Delta} - \mathcal{W}f_k^c \\ y_k = Cx_k \end{cases} \quad (1.13)$$

where

$$\mathcal{A} = (\mathbb{I}_3 + TA), \mathcal{B} = TB,$$

$$\mathcal{F} = TF, \mathcal{W} = TW, \bar{\Delta} = T\Delta,$$

and  $T$  being the sampling time. In such case, we need to shift the output equation backward using the state equation in discrete-time (1.13) such that the output  $y_k$  is expressed as a function of delayed state  $x_{k-\tau}$  where  $\tau$  is the smallest positive integer that allows the necessary rank condition to be held. In the next section, we follow this strategy and develop a discrete-time model-based UIO for the studied CACC system to estimate the cyberattack false signal  $f^c$ .

### 3 Discrete-Time Model-Based UIO design for CACC system

This section is devoted to the development of a new unknown input observer based on the discrete-time model (1.13). By introducing the variables

$$z_t \triangleq x_{k-1} \text{ and } \bar{y}_t \triangleq y_{k-1} \quad (1.14)$$

with  $t = k - 1$  and considering additive vector noises,  $\omega_t$ , in both the output measurements and in the process equation, we obtain the following new system

$$\begin{cases} z_{t+1} = \mathcal{A}z_t + \mathcal{B}v_{i,t} + \mathcal{F}\mu_t \\ \quad + \bar{\Delta} - \mathcal{W}f_t^c + E_\omega\omega_t \\ \bar{y}_t = \mathcal{C}z_t + D_\omega\omega_t \end{cases} \quad (1.15)$$

for which the rank condition is satisfied, i.e. :

$$\text{rank}(\mathcal{CW}) = \text{rank}(\mathcal{W}) = 1. \quad (1.16)$$

#### 3.1 UIO structure for the shifted system

By using an UIO corresponding to the shifted system (1.15), we will estimate simultaneously  $z_t$  and  $f_{t-1}^c$ . By using the notation

$$\xi_t \triangleq \begin{bmatrix} z_t \\ f_{t-1}^c \end{bmatrix},$$

$$\mathbb{E} = \begin{bmatrix} \mathbb{I}_3 & \mathcal{W} \end{bmatrix}, \quad A_\xi = \begin{bmatrix} \mathcal{A} & 0 \end{bmatrix}, \quad C_\xi = \begin{bmatrix} \mathcal{C} & 0 \end{bmatrix}$$

the system (1.15) is written under the following descriptor form :

$$\begin{cases} \mathbb{E}\xi_{t+1} = A_\xi\xi_t + \mathcal{B}v_t + \mathcal{F}\mu_t + \bar{\Delta} + E_\omega\omega_t \\ \bar{y}_t = C_\xi\xi_t + D_\omega\omega_t. \end{cases} \quad (1.17)$$

From (1.16), we have

$$\text{rank} \left( \begin{bmatrix} \mathbb{E} \\ C_\xi \end{bmatrix} \right) = n + \text{rank}(\mathcal{CW}) = n + 1.$$

Now, let  $P_z$  and  $Q_z$  be two matrices of appropriate dimensions such that

$$\begin{bmatrix} P_z & Q_z \end{bmatrix} = \left( \begin{bmatrix} \mathbb{E} \\ C_\xi \end{bmatrix}^\top \begin{bmatrix} \mathbb{E} \\ C_\xi \end{bmatrix} \right)^{-1} \begin{bmatrix} \mathbb{E} \\ C_\xi \end{bmatrix}^\top. \quad (1.18)$$

It follows that

$$P_z\mathbb{E} + Q_zC_\xi = \mathbb{I}_p \quad (1.19)$$

where  $p$  is the number of output measurements.

By considering the following two-stage observer

$$\begin{cases} \kappa_{t+1} = (P_z A_\xi - K C_\xi) \kappa_t + P_z \mathcal{B} v_{i,t} \\ \quad + [(P_z A_\xi - K C_\xi) Q_z + K] \bar{y}_t \\ \quad + P_z \mathcal{F} \mu_t + P_z \Delta \\ \hat{\xi}_t = \kappa_t + Q_z \bar{y}_t \end{cases} \quad (1.20)$$

the estimation error  $\tilde{\xi}_t = \hat{\xi}_t - \xi_t$  satisfies the equation :

$$\begin{aligned} \tilde{\xi}_{t+1} &= (P_z A_\xi - K C_\xi) \tilde{\xi}_t \\ &\quad + [(K D_\omega - P_z E_\omega) \quad Q_z D_\omega] \bar{\omega}_t, \end{aligned} \quad (1.21)$$

where  $\bar{\omega}_t$  is defined as follows :

$$\bar{\omega}_t \triangleq [\omega_t^\top \quad \omega_{t+1}^\top]^\top. \quad (1.22)$$

**Remark 1.** The central focus of this paper does not lie in the details of designing controller parameters  $k_1$  and  $k_2$ . Rather, our attention is directed towards the development of a novel cyberattack detection algorithm. It is crucial to note that in the proposed methodology, we make an assumption that the control design phase, specifically ensuring the string stability of the controller (1.3), is considered as a distinct and independent process from the estimation design procedure outlined in this paper. As demonstrated in [Rajamani, 2002], the controller (1.3) achieves string stability under specific conditions. This stability depends on the transfer function  $H(s) = \frac{\bar{\varepsilon}_i}{\bar{\varepsilon}_{i-1}}$ , where  $\bar{\varepsilon}_i$  is defined in (1.2), satisfying the inequality  $|H(j\omega)| \leq 1$ . Detailed analysis in [Rajamani, 2002] reveals that such a condition is met when two critical parameters adhere to certain criteria. Specifically, the condition holds when  $-k_1 h > \tau$  and  $k_2 > 0$ , as meticulously explained in the calculations provided in [Rajamani, 2002, Eqs.(32)-(34)].

### 3.2 LMI-Baed ISS design method

The objective consists in determining the observer gain  $K$  such that the estimation error  $\tilde{\xi}_t$  is exponentially robust with respect to the bounded disturbance  $\omega_t$ . The next theorem provides sufficient conditions expressed in terms of LMIs ensuring the robust exponential stability of  $\tilde{\xi}_t$ . For the sake of brevity, we put  $\mathcal{A}_z \triangleq P_z A_\xi$ ,  $\mathcal{D}_z \triangleq Q_z D_\omega$ , and  $\mathcal{E}_z \triangleq P_z E_\omega$ .

**Theorem 1.** Assume there exist two symmetric and positive definite matrices  $\mathcal{P}$  and  $\mathcal{S}$ , a matrix  $\mathcal{Z}$  of appropriate dimension, and a scalar  $\alpha$ , with  $\alpha \in ]0, 1[$ , such that the following LMI condition holds :

$$\begin{array}{ccc} -\alpha \mathcal{P} & 0 & \mathcal{A}_z^\top \mathcal{P} - C_\xi^\top \mathcal{Z} \\ (\star) & -\mathcal{S} & \left[ \begin{array}{c} \mathcal{D}_\omega^\top \mathcal{Z} - \mathcal{E}_z^\top \mathcal{P} \\ \mathcal{D}_z^\top \mathcal{P} \end{array} \right] \\ (\star) & (\star) & -\mathcal{P} \end{array} < 0 \quad (1.23)$$

Then the estimation error  $\tilde{\xi}_k$ , with  $K = \mathcal{P}^{-1} \mathcal{Z}^\top$ , satisfies the following exponential Input-to-

*State Stable (ISS) bound :*

$$\|\tilde{\xi}_t\| \leq \sqrt{\frac{\lambda_{\max}(\mathcal{P})}{\lambda_{\min}(\mathcal{P})}} \|\tilde{\xi}_0\| \alpha^{\frac{t}{2}} + \sqrt{\frac{\lambda_{\max}(\mathcal{S})}{(1-\alpha)\lambda_{\min}(\mathcal{P})}} \max_{0 \leq k \leq t} \|\bar{\omega}_k\|. \quad (1.24)$$

*Proof.* The proof is based on the Lyapunov function  $\vartheta_t \triangleq \tilde{\xi}_t^\top \mathcal{P} \tilde{\xi}_t$ . By expanding the expression of  $\vartheta_{t+1}$  along the trajectories of (1.21), we can deduce easily that under the LMI condition (1.23), we have

$$\vartheta_{t+1} - \alpha \vartheta_t \leq \bar{\omega}_t^\top \mathcal{S} \bar{\omega}_t.$$

Hence, by induction technique and backward substitution, we deduce that

$$\vartheta_t \leq \vartheta_0 \alpha^t + \frac{\lambda_{\max}(\mathcal{S})}{1-\alpha} \max_{0 \leq k \leq t} \|\bar{\omega}_k\|^2.$$

Consequently, we can conclude by using the double inequality

$$\lambda_{\min}(\mathcal{P}) \|\tilde{\xi}_t\|^2 \leq \vartheta_t \leq \lambda_{\max}(\mathcal{P}) \|\tilde{\xi}_t\|^2.$$

□

### 3.3 Defense strategy

The key idea consists of developing a Resilient, Robust, and Reliable CACC (3R-CACC) controller able to cope with cyberattacks, external disturbances, and data loss. The 3R-CACC defense mechanism is as depicted in Figure 1.3. As soon as an attack or a significant external disturbance is detected, the CACC controller (1.3) will switch to the ACC controller to forget the false data in communication data.

$$u_i = -\frac{1}{h}(v_i - v_{i-1} + \lambda \bar{\epsilon}_i) \quad (1.25)$$

with the condition  $h > 2\tau$  and  $\lambda > 0$  in order to ensure the string stability. After implementing the controller (1.25), the system no longer remains the same as (1.13). Therefore, we need to transform the controller (1.25) in terms of  $x$  and rewrite a new system similar to (1.13). This enables the system to detect cyberattacks, which will be treated as unknown inputs.

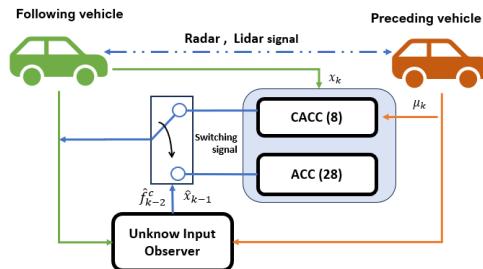


FIGURE 1.3 – Resilient control for CACC system.

**Remark 2.** The LMI conditions (1.23) correspond to the system without uncertainties, which guarantee certain robustness with respect to the parameter uncertainties in the sense of the exponential ISS criterion (1.24). Indeed, with the proposed method, if we have uncertainties, i.e. :  $A + \delta A$  and  $C + \delta C$  instead of  $A$  and  $C$ , for instance, we can add  $\delta Ax(t)$  and  $\delta Cx(t)$  in the disturbance vector  $\omega$  and then the LMIs ensure the exponential ISS bound with respect to the new vector of disturbances,  $\omega$ , containing the parameter uncertainties. However, such a technique does not ensure exponential convergence of the estimation and tracking errors to zero in the free-disturbance case (with the initial vector of disturbances without including the uncertain parameters), and the boundedness of  $\delta A$  and  $\delta C$  does not imply necessarily the boundedness of  $\delta Ax(t)$  and  $\delta Cx(t)$ . To overcome this issue, we need to develop an extended LMI condition that consider both the structure and magnitude of uncertainties.

## 4 Simulation results by Using Matlab and Carla Platform

We demonstrate the effectiveness of the proposed observer by conducting MATLAB and CARLA simulations with two cyberattack scenarios. The parameters of the CACC system and its controller are given in Table 1.1.

Parameter	$\tau$	$L$	$l_i$	$h$	$k_1$	$k_2$	$t_s$
Value	0.4	7.3	5	0.5	-0.8	2.5	0.01
Unit	s	m	m	s	-	-	-

TABLE 1.1 – Parameters of CACC system and the controller gains.

It is assumed that two vehicles are driving longitudinally on the road, and each vehicle is equipped with a cruise control system. The preceding vehicle should pursue the following desired trajectory :  $a_{i-1}(t) = 3 \sin(\frac{2\pi}{10})t$ . The two simulation scenarios of cyberattacks explored here are outlined below :

**Case 1 :** Sparse attack, DoS, packet-loss :

$$f^c(t) = \begin{cases} X(t) & 6 \leq t < 8 \\ a_{i-1}(t) & 10 \leq t < 15 \\ 0 & \text{otherwise} \end{cases} \quad (1.26)$$

**Case 2 :** False data injected :

$$f^c(t) = \begin{cases} -5 & 6 \leq t < 8 \\ 2(t-4) & 10 \leq t < 15 \\ 0 & \text{otherwise} \end{cases} \quad (1.27)$$

where  $X(t) \sim U(-5, 5)$  is a random variable following a uniform distribution, with probability  $P(X(t)) = 0.2$ .

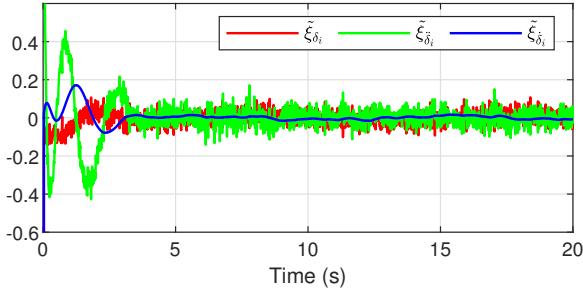


FIGURE 1.4 – State estimation case 1.

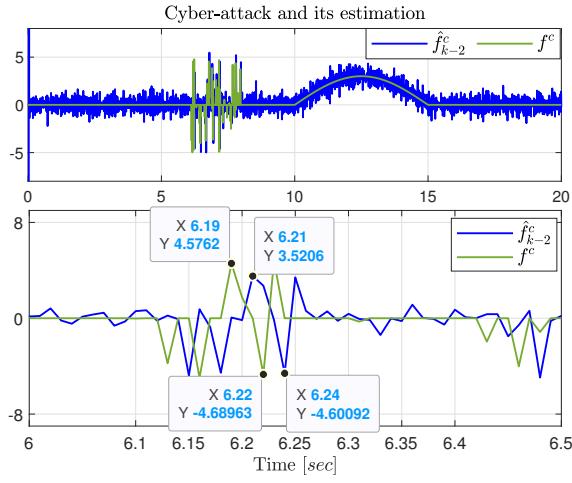


FIGURE 1.5 – Attack estimation using UIO case 1.

#### 4.1 Simulation result using Matlab

By solving the LMI condition (1.23), we obtain the observer gain  $K$  given by :

$$K = \begin{bmatrix} 0.5000 & -0.005 & 0.0498 & -8.9295 \\ -0.005 & 1.000 & -99.9950 & 1427.22 \end{bmatrix}^\top.$$

The proposed observer is designed to estimate the state vector, including relative position, relative velocity, and relative acceleration, as well as provide an accurate estimation of any cyberattacks even in the presence of a Gaussian noise  $\omega_t = \mathcal{N}(0.02^2[m])$  for both system and measurement. For both attack scenarios, we set the initial conditions of the actual system as  $\xi_0 = [5 \ 10 \ 0 \ 0]^\top$ , while the initial state of the observer is set to  $\hat{\xi}_0 = [0 \ 0 \ 0 \ 0]^\top$ .

Simulation results for the first scenario of cyberattack (1.26) are presented in Figure 1.4 and Figure 1.5. In Figure 1.4, we can see the error of the relative position, relative velocity, and relative acceleration along with their estimates. The observer demonstrates similar good performance in accurately reconstructing a random cyberattack and packet-loss, as depicted in Figure 1.5. As we can see, the estimated delay attack is exactly 2 steps.

For the second case of time-varying and bounded attack signal (1.27), it can be observed from the Figure 1.6 that the cyberattack signal is accurately estimated, and the estimation error

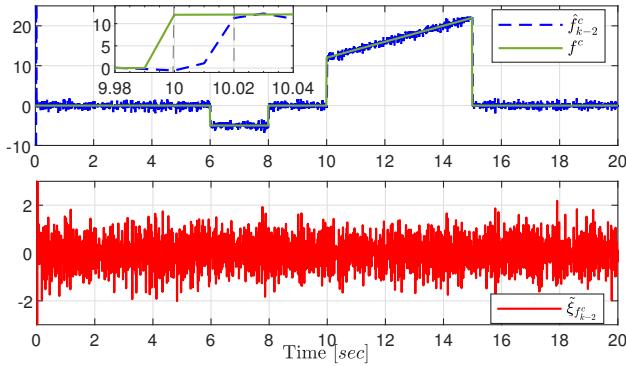


FIGURE 1.6 – Attack estimation and the errors case 2.

is bound.

We can see that the proposed observer can estimate the full state with good accuracy, while the unknown input is reconstructed with a fixed delay of two units based on the available output measurements.

## 4.2 Simulation result using Carla

To evaluate the system under more realistic conditions, we conducted simulations within the CARLA simulator. Specifically, we simulated a scenario where a leading vehicle utilized a PID controller for cruise control, aiming to maintain a velocity of  $10m/s$ . We kept the parameters consistent with those listed in Table 1.1 and adopted a time step of  $t_s = 0.04$ . We also implemented a deterministic attack signal that varies over time and is defined by equation (1.27). As depicted in Fig 1.8, the error state vectors for relative position and relative velocity exhibit good tracking, but the third vector  $\tilde{\xi}_a$  falls short of perfection. This is because the acceleration of the preceding vehicle in Fig 1.9 sent to the network is inconsistent, which affects the attack estimation performance. Fig 1.9 illustrates the observer taking at least 5 seconds to converge to the actual state, and the estimated value being influenced by noise and imperfection of the model. However, the leading vehicle retains its ability to detect the cyberattack signal, ensuring a safe distance effectively. A video showcasing the simulation scenario is provided in [GitHub repository](#). Fig. 1.7 displays a thumbnail from the video.


 FIGURE 1.7 – Carla Simulator platform ([GitHub repository](#)).

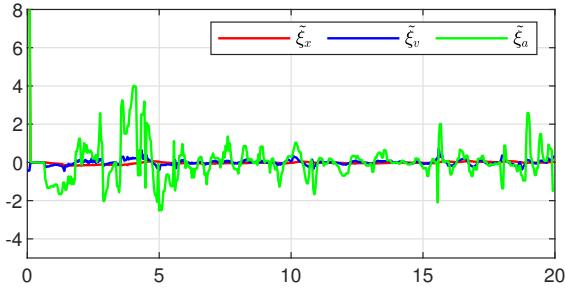


FIGURE 1.8 – State estimation using CARLA under attack case 2.

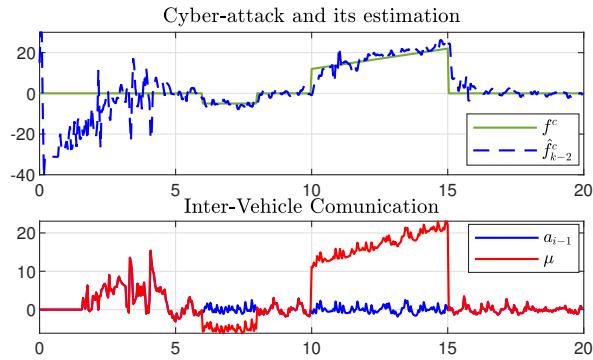


FIGURE 1.9 – Cyberattack signal and inter-vehicle communication case 2.

## 5 Conclusion

In this paper, we proposed a novel UIO design technique ensuring a theoretical ISS bound on the cyberattack detection error in the context of the CACC system. To guarantee such an ISS bound, a new LMI condition is proposed. The key idea consists in shifting the original output measurement to satisfy the well-known matching condition. The theoretical result is validated through two simulation scenarios of cyberattacks by using the Matlab software and the Carla simulator.

Our future endeavors will focus on exploring the challenge in the presence of model parameter uncertainties. This will entail designing a robust observer-based controller, necessitating simultaneous synthesis of the observer and controller gains by addressing a unified LMI condition.

## 6 Use Exact discretization

To overcome the above limitation, we propose discretizing the system. Previous studies [Nguyen, 2024] have applied state discretization with a delay that satisfies the necessary rank condition. This approach represents an alternative solution to the rank condition problem. However, the introduction of delays can affect control system performance and stability, leading to reduced responsiveness and complicating the design of the observer and controller, especially in the presence of measurement noise. To address these challenges, we propose the use of an exact

discretization method, as suggested in the literature [Zhang, 2021] allowing us to estimate both the state and cyberattacks using an UIO. Additionally, we will introduce conditions to ensure the exponential convergence of the estimation error, which will be discussed in the next section.

Figure fig. 1.10 illustrates the structure of the proposed observer-based cyberattack estimation framework.

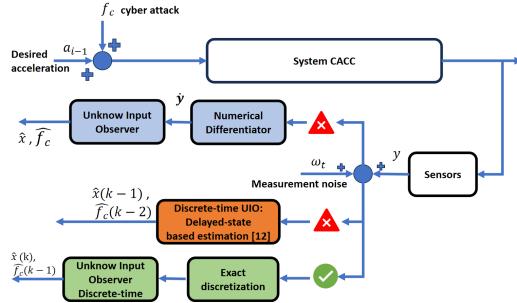


FIGURE 1.10 – Discrete-time model-based UIO

The discrete-time version of equation is presented as follows, according to the approach detailed in reference [Zhang, 2021] :

$$\begin{cases} x_{k+1} = A_d x_k + B_d v_{i,k} + F_d \mu_k + \hat{\Delta} - W_d f_k^c \\ y_k = C_d x_k \end{cases} \quad (1.28)$$

where

$$A_d = e^{A_c T_s}, B_d = \int_0^{T_s} e^{A_c \eta} B_c d\eta, C_d = C_c$$

$$F_d = \int_0^{T_s} e^{A_c \eta} F_c d\eta, W_d = \int_0^{T_s} e^{A_c \eta} W_c d\eta,$$

$$\hat{\Delta} = \int_0^{T_s} e^{A_c \eta} \Delta \eta$$

and  $T_s$  is a sampling period

We verify the rank condition of the newly discretized system (6) :

$$C_d W_d = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} 1.14e^{-06} \\ 3.41e^{-04} \\ 6.75e^{-02} \end{pmatrix} = 1e^{-03} \begin{pmatrix} 0.0011 \\ 0.3419 \end{pmatrix}$$

The rank condition is satisfied :

$$\text{rank}(CW) = \text{rank}(W)$$

## 6.1 Simulation results and comparaison

To demonstrate the effectiveness of the exact discretization method used in our study and the developed observer, we conducted simulations in MATLAB and CARLA, following the same procedures outlined in the paper by [Nguyen, 2024]. This section will be divided into two parts : Matlab results and Carla results. In each part, we will present our findings and compare them with those from the study by [Nguyen, 2024].

### 6.1.1 Using Matlab

The observer developed based on the descriptor system for cyber-attack detection, along with the controllers described in the previous section, has been evaluated through simulations. For the CACC system, the system and controller parameters are as follows :  $\tau = 0.4s$ ,  $L = 7.3m$ ,  $l_i = 5m$ ,  $h = 0.5s$ ,  $k_1 = -0.8$ ,  $k_2 = 2.5$ ,  $t_s = 0.01$

We solve (11) for the observer gain using YALMIP Toolbox, with the exponential stability parameter  $\alpha = 0.5$ . By solving the LMI condition, we obtain the observer gain  $K$  :

$$K = \begin{pmatrix} 0.5 & -0.005 \\ -0.001 & 0.7 \\ -0.2 & -68.0 \\ 2.2 & 1004.2 \end{pmatrix}$$

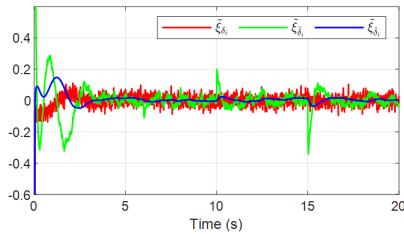


FIGURE 1.11 – The error state estimation

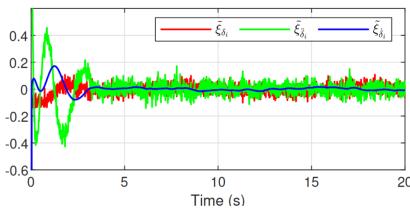


FIGURE 1.12 – The error state estimation [Nguyen, 2024]

The figures (Fig. 1.11 and Fig. 1.12) illustrate the estimation errors of system states within the CACC framework, including position, velocity, and acceleration. These figures allow a comparison between the method applied in our study (Fig. 1.11) and the method used in the study referenced as [Nguyen, 2024] (Fig. 1.12). In Fig. 1.12, which represents the results from [Nguyen, 2024], the estimation errors for position, velocity, and acceleration exhibit significant initial oscillations. These oscillations persist for about 5 seconds before the system

stabilizes around zero. Additionally, the amplitude of the noise affecting these errors is substantial, indicating a less accurate state estimation under the influence of cyberattacks and noise. Conversely, Fig. 1.11, derived from our study, demonstrates that the estimation errors using an exact discretization method show less pronounced initial oscillations. The system stabilizes more rapidly, within approximately 3 seconds, and the noise amplitudes in both position and velocity errors are significantly reduced. This highlights the superiority of our method in improving state estimation accuracy, effectively mitigating the impact of cyberattacks and noise. Moreover, a notable difference in velocity error can be observed : the method from [Nguyen, 2024] results in larger velocity estimation errors compared to our method, where the errors are less significant. This further supports the conclusion that our exact discretization method offers a more robust and precise approach to state estimation in the CACC system.

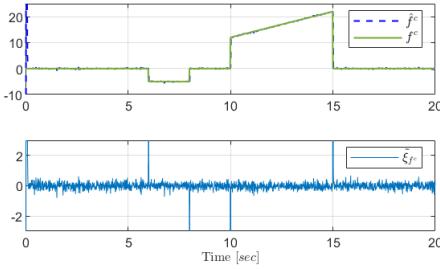


FIGURE 1.13 – Cyber-attack estimation and error

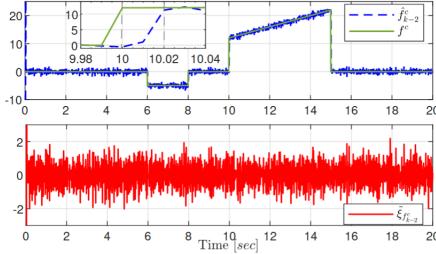


FIGURE 1.14 – Cyber-attack estimation and error[Nguyen, 2024]

The figures presented depict the actual cyberattacks (in blue) and the estimated values (in green). In the second subfigure, the estimation error for cyberattacks is compared between our study (Fig. 6) and the study in [Nguyen, 2024] (Fig. 7). Both methods demonstrate a rapid and accurate capacity to detect cyberattacks, as evidenced by the alignment of the estimated cyberattack curves with the actual value. However, a more detailed comparative analysis reveals significant differences in terms of accuracy and noise.

First, our method exhibits superior performance in terms of estimation accuracy for cyberattacks. As illustrated in Fig. 6, the estimates obtained with our approach show reduced fluctuations and greater stability compared to the method from [Nguyen, 2024], represented in Fig. 7. This difference indicates that our method is more robust and less sensitive to variations.

Second, the figures also highlight a notable difference in the estimation errors of cyberattacks. In our method (Fig. 6), the estimation error is primarily centered around zero, with minimal fluctuations up to approximately 0.6. In contrast, the method from study [Nguyen, 2024] (Fig.

7) shows an estimation error reaching an amplitude of around 2. This higher level of noise in the results from [Nguyen, 2024] could lead to less reliable performance, where precise and stable responses are critical for maintaining security.

### 6.1.2 Using CARLA Simulator

To evaluate the effectiveness of the discretization method applied to the system, which will subsequently enable the development of an observer to estimate states (position, speed, and acceleration) as well as detect cyberattacks, it is imperative to conduct tests under realistic conditions. This validation was carried out using the CARLA simulator.

We implemented the same simulation scenario [Nguyen, 2024] on the CARLA platform, including two vehicles : a lead vehicle and a following vehicle. The objective was to test the system under real conditions, which allowed us to confirm our theoretical results previously obtained with MATLAB and to compare our discretization method with that developed in [Nguyen, 2024]. The speed of the lead vehicle is maintained using a PID controller to stabilize the reference speed at 10 m/s. To ensure the reproducibility of the results and the precise tracking of the following vehicle, we strictly adhered to the CACC system parameters defined in the previous section (MATLAB simulation). Additionally, we discretized the system with a simulation time step of 0.04 seconds, which allowed us to accurately capture the dynamic evolutions of the vehicles in real-time on CARLA.

The comparison between Figures 9 and 10 highlights the performance differences between our system, simulated in the CARLA environment, and the one described in reference [Nguyen, 2024]. These figures illustrate the estimation errors of the system states. In our study, the estimation errors for speed and position converge more rapidly to zero compared to the study conducted in [Nguyen, 2024]. However, the estimation of acceleration takes approximately 5 seconds to stabilize around zero, a delay similar to that observed in [Nguyen, 2024].

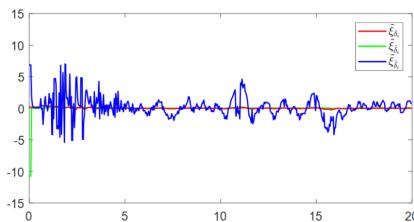


FIGURE 1.15 – The error state estimation

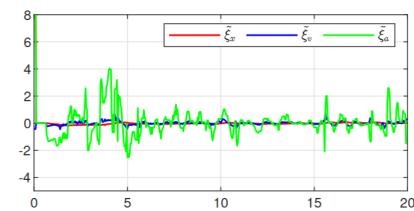


FIGURE 1.16 – The error state estimation [Nguyen, 2024]

The Figures 11 and 12 present a comparison of the cyberattack estimation results obtain-

ned respectively with our discretization method applied in the CARLA environment and with the reference approach described in [Nguyen, 2024]. A detailed analysis highlights significant differences in terms of robustness, convergence speed, and accuracy.

Firstly, Figure 12 shows larger initial fluctuations, illustrating a notable transient instability in the method of [Nguyen, 2024]. Conversely, Figure 11 demonstrates a transient phase with more limited fluctuations, reflecting better initial error management. This difference highlights the ability of our method to better dampen disturbances at the startup phase.

Secondly, convergence speed is a key factor in this comparison. Our method achieves rapid convergence and begins to accurately estimate the cyberattack within 3 seconds. In contrast, the method in [Nguyen, 2024] requires more than 5 seconds to stabilize the estimations, which can be a critical limitation in applications requiring high responsiveness, particularly in dynamic and complex environments.

Finally, in terms of long-term accuracy, our method demonstrates a better ability to track the actual variations of the cyberattack, with a close match between  $f^c$  (the actual value) and  $\hat{f}_c$  (the estimation). In comparison, although the approach in [Nguyen, 2024] manages to stabilize errors, it provides lower accuracy, limiting its effectiveness in scenarios requiring precise estimation.

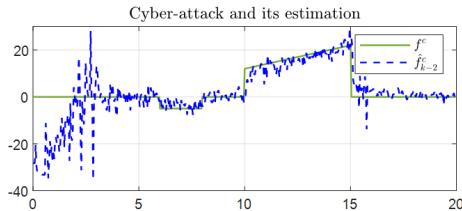


FIGURE 1.17 – Cyber-attack estimation

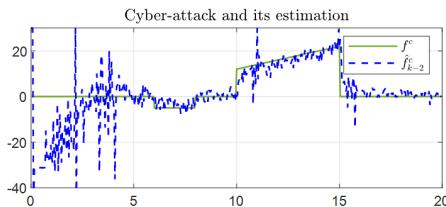


FIGURE 1.18 – Cyber-attack estimation [Nguyen, 2024]

## 6.2 Conclusion

In our study, we introduced a new exact discretization technique that guarantees the rank condition for UIO existence and developed an LMI-based observer ensuring an ISS bound on cyberattack detection error in a CACC system. The method was compared with a previous discretization approach that introduced output delay. Simulations in MATLAB and CARLA confirmed the improved performance and effectiveness of the proposed method.

Future work includes extending the approach to multi-vehicle platoons for greater realism and applying it to other systems such as Mixed Traffic Flow, highlighting its adaptability and potential to enhance the safety and resilience of autonomous vehicle control against cyberattacks.

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## RÉSUMÉ

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## MOTS CLÉS

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Estimation, mot clé 2, mot clé 3, mot clé 4

## ABSTRACT

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The reliability and safety of Connected and Autonomous Vehicles (CAVs) rely heavily on the real-time availability of precise dynamic variables. However, equipping vehicles with high-end sensors to measure every necessary variable—such as sideslip angles or vehicle trajectories—is often economically unfeasible or physically impossible. Furthermore, CAVs are increasingly vulnerable to sensor faults and cyber-attacks targeting inter-vehicle communications (V2V/V2I), which can lead to critical failures. To address these challenges without incurring the high cost of physical hardware redundancy, this thesis proposes the development of an embedded electronic board functioning as a resilient "soft sensor" based on analytical redundancy.

The research adopts a hybrid modeling methodology that integrates physical differential equations with online learning-based neuro-adaptive neural networks. This approach allows for the accurate representation of complex, time-varying parameters and unknown inputs within the vehicle's dynamics. Based on these models, advanced nonlinear estimation algorithms—specifically Unknown Input Observers (UIO) and neuro-adaptive observers—are developed to reconstruct missing state variables and ensure system resilience against data loss and malicious signal injection.

The proposed estimation strategies are applied to two primary control challenges:

- Resilience to Cyber-Attacks in Adaptive Cruise Control (ACC): The thesis investigates specific architectures for detecting and mitigating cyber-attacks, such as Denial of Service (DoS) and False Data Injection (FDI), within autonomous and cooperative ACC systems.
- Vehicle Tracking and Platooning: Novel estimation algorithms are proposed to handle the nonlinear dynamics and unknown forces inherent in tracking surrounding vehicles, which is essential for decision-making in maneuvers like lane changes and platooning.

The final contribution of this work is the design and fabrication of a prototype embedded electronic board. This hardware integrates the developed algorithms, validating the theoretical contributions and demonstrating a cost-effective, scalable solution for enhancing the autonomy, security, and fault tolerance of next-generation vehicles.

## KEYWORDS

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State Estimation, keyword 2, keyword 3, keyword 4