

Bootstrap Method

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1 Algorithm

Data: $y_1, \dots, y_n \sim i.i.d. (\mu, \sigma_Y^2)$

Step1: Calculate mean and deviation

$$\overline{\mu_Y} = \frac{1}{n} \sum_{i=1}^n y_i$$
$$\widehat{S_Y^2} = \frac{1}{n-1} \sum_{i=1}^n (y_i - \overline{\mu_Y})^2$$

Step2: Repeat below S times (s=1,2,...,S) ¹

1. $y_1^B, \dots, y_m^B \sim (y_1, \dots, y_m)$ duplicated samples

2. $\overline{\mu_s^B} = \frac{1}{n} \sum_{i=1}^n y_i^B$

After S times repeat, we get $\overline{\mu_1^B}, \dots, \overline{\mu_S^B}$

Step3: Sort $\overline{\mu_1^B} < \overline{\mu_2^B}, \dots, < \overline{\mu_S^B}$ ²

95% Confidence interval is between $\overline{\mu_2^B}$ and $\overline{\mu_{S-1}^B}$

¹Usually, 1000 times needed. If could, 10000 times is better. Bigger number of repeat is better.

²Here, normal distribution is not assumed.