Bootstrap Method

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1 Algorithm

Data: $y_1, \ldots, y_n \sim i.i.d \ (\mu, \sigma_Y^2)$

Step1: Calculate mean and deviation

$$\overline{\mu_Y} = \frac{1}{n} \sum_{i=1}^{n} y_i \\ \widehat{S_Y^2} = \frac{1}{n-1} (y_i - \overline{\mu_Y})^2$$

Step2: Repeat below S times $(s=1,2,...,S)^{-1}$

$$\begin{array}{l} 1.\ \underline{y_1^B},\dots,y_m^B\sim(y_1,\dots y_m) \text{ duplicated samples} \\ 2.\overline{\mu_s^B}=\frac{1}{n}\sum_{i=1}^ny_i^B \\ \text{After repeat S times, we get } \overline{\mu_1^B},\dots,\overline{\mu_S^B} \end{array}$$

Step3: Sort
$$\overline{\mu_1^B} < \overline{\mu_2^B}, \ldots, < \overline{\mu_S^B}^{\; 2}$$

95% Confidence interval is between $\overline{\mu_2^B}$ and $\overline{\mu_{S-1}^B}$

 $^{^1\}mbox{Usually, }1000$ times needed. If could, 10000 times is better. Bigger number of repeat is better.

²Here, normal distribution is not assumed.