

# FIT1045 Intro to Algorithms and Programming – Workshop 12

## Objectives

The **objectives of this workshop** are:

- To get used to NP-completeness.
- To create a certificate checker for CLIQUE and INDEPENDENT-SET problem.

## Useful Links:

For this workshop, you may find it useful to review some of the following concepts:

- Some known NP-complete problems. (<https://en.wikipedia.org/wiki/NP-completeness>)
- Lecture materials to develop intuition.

In particular, you may find it useful in proving the membership of a problem in class NP.

## Task 0 (To be completed before class):

Review workshop 4 (tasks 1 – 3) and how to represent a graph as an adjacency list and adjacency matrix from there:

1. Write up a function which accepts a graph in adjacency list format and determines whether any two vertices (Ex. 5 and 2) are adjacent (joined via an edge) in the given graph
2. Repeat this process for an adjacency matrix.

## Task 1:

This task will have you verifying that a certificate to the Max-Clique problem. The Max-Clique: Given a graph  $G$ , find the largest clique (set of nodes such that all pairs in the set are neighbors).

The decision version of the Problem is: Does  $G$  have a clique of size  $K$ ? Write a python program that takes a graph  $G$ , a number  $k$  and a possible certificate  $C$  to this problem.

Your program returns “yes”, if  $C$  is a clique of size  $k$  in the graph  $G$  and “no” otherwise. The graph is given in a file testGraph.txt. A file named cliqueList.txt is also given which contains group of possible cliques of vertices which you will need to check.

For this question you can assume  $k = 4$

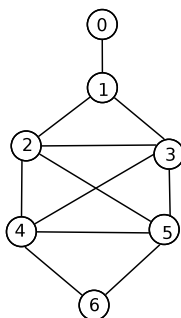


Figure 1: Graph G

**For example:** Your program might do the following:

Enter the filename for graph: testGraph.txt

Enter the filename for possible cliques: cliqueList.txt

[2, 3, 4, 5] : Yes

[1, 2, 3, 6] : No

[1, 2, 3] : No

[1, 3, 6] : No

[0, 1, 5, 6] : No

[1, 2, 3, 4] : No

## Task 2:

This task will have you verifying that a certificate to the Max-Independent Set problem. An Independent Set in a graph is a set of nodes with no two of which have an edge.

The decision version of the Problem is: Does  $G$  have an independent set of size  $K$ ?

Write a python program that takes a graph  $G$ , a number  $k$  and a possible certificate to this problem  $I$ . Your program returns "yes", if  $I$  is an independent set of size  $k$  in the graph  $G$  and "no" otherwise.

The graph is given in a file testGraph.txt. A file named independentSet.txt is also given which contains a group of possible independent vertex sets. For this question you can assume  $k = 3$ .

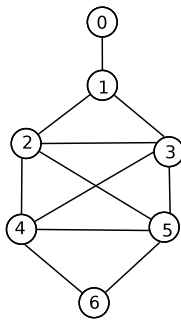


Figure 2: Graph G

**For example:** Your program might do the following:

Enter the filename for graph: testGraph.txt

Enter the filename for independent set: independentSet.txt

[1, 3, 5] : No

[1, 2, 6] : No

[3, 6] : No

[0, 2, 6] : Yes

[0, 3, 6] : Yes

### Task 3:

The complement of a graph  $G$  is a graph  $H$  on the same vertices such that two distinct vertices of  $H$  are adjacent if and only if they are not adjacent in  $G$  (Refer Figure 3). Write a program to find the complement of a graph. Use this program to find the complement of the graph discussed in the previous questions. Repeat Task 1 and Task 2 with the complement graph. Discuss your observations with your neighbor/tutor. Try to convince yourself about the observations you make.

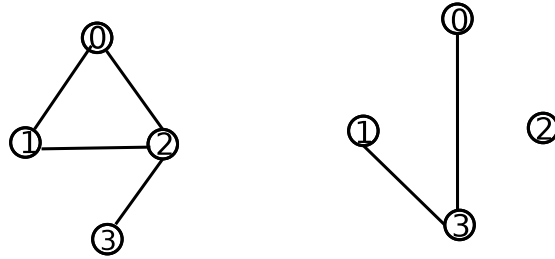


Figure 3: Graph  $G$  and its complement