

Lecture 22

Iteration vs Recursion

FIT 1008
Introduction to Computer Science



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WARNING

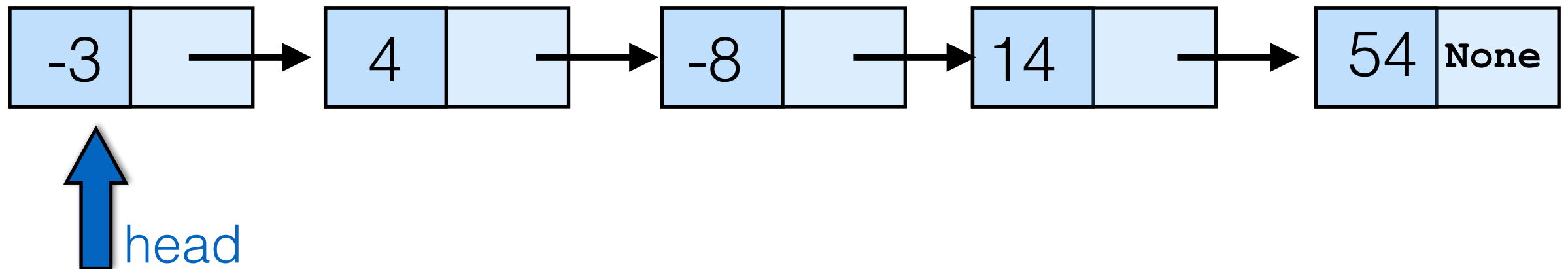
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Operation	Class Method
str(obj)	__str__(self)
len(obj)	__len__(self)
item in obj	__contains__(self,item)
y = obj[ndx]	__getitem__(self,ndx)
obj[ndx] = value	__setitem__(self,ndx,value)
obj == rhs	__eq__(self,rhs)
obj < rhs	__lt__(self,rhs)
...	
obj + rhs	__add__(self,rhs)
...	

```
class List:
    def __init__(self):
        self.head = None
        self.count = 0
```

```
def __len__(self):
    return self.count
```

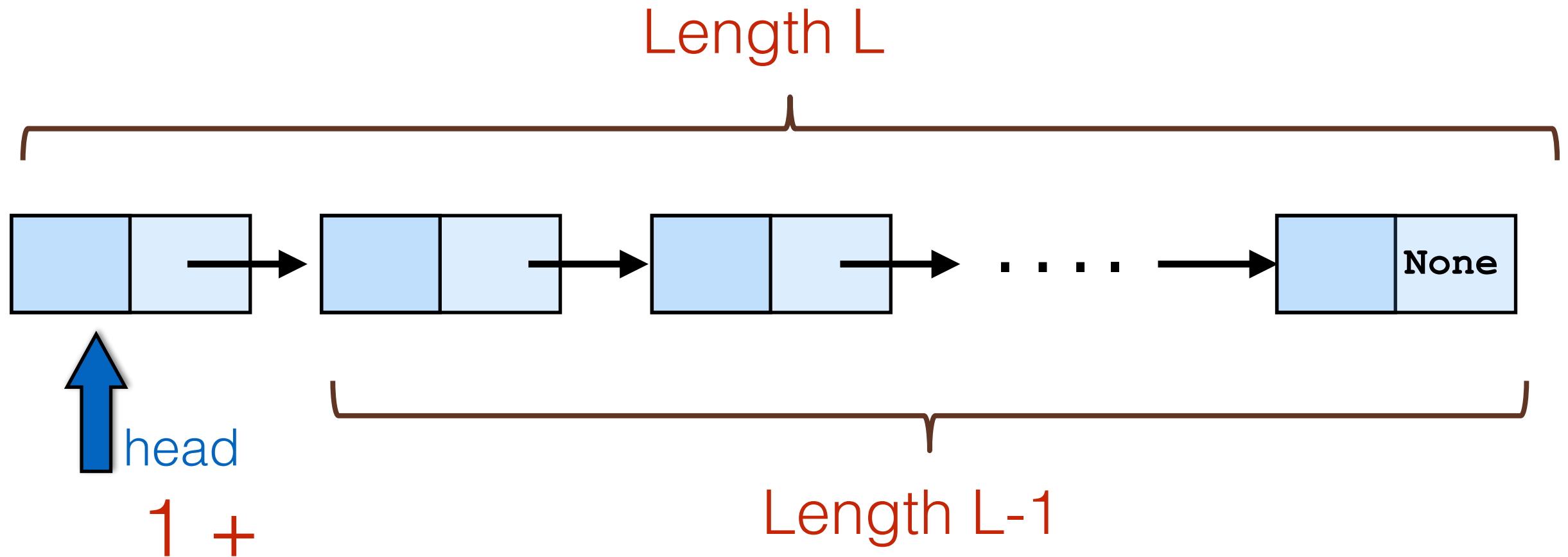
 ?

.....▶
count from head to access elements

```
class List:
    def __init__(self):
        self.head = None

    def __len__(self):
        current = self.head
        count = 0
        while current is not None:
            current = current.next
            count += 1
        return count
```

Complexity: $O(n)$ where n is the size of the list.



Convergence: Call recursion with $L-1$. Use variable *current*.

Base case: Empty? Size of empty list is 0.

Combining solutions: Add up result of recursive call +

```
def _length(self, current):  
    if self.current is None: # base case  
        return 0  
    else:  
        return 1 + self._length(current.next)
```

Base case

Convergence

```
def __len__(self):  
    return self._length(self.head)
```

Combination

Auxiliary method sets up the initial
parameters

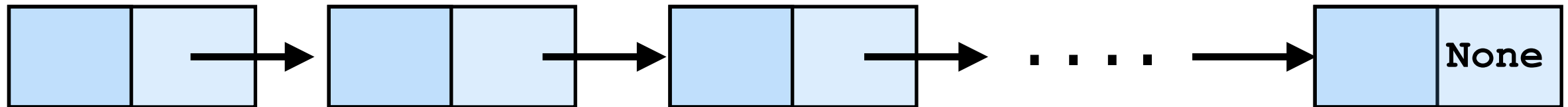
Recursion vs Iteration

- Can every **iterative function** be implemented using **recursion**?
Yes, it is straightforward.
- Can every **recursive function** be implemented using **iteration**?
Yes, but you might also need to store past results.

Operation	Class Method
str(obj)	__str__(self)
len(obj)	__len__(self)
item in obj	__contains__(self,item)
y = obj[ndx]	__getitem__(self,ndx)
obj[ndx] = value	__setitem__(self,ndx,value)
obj == rhs	__eq__(self,rhs)
obj < rhs	__lt__(self,rhs)
...	
obj + rhs	__add__(self,rhs)
...	

__contains__

current



head

__contains__

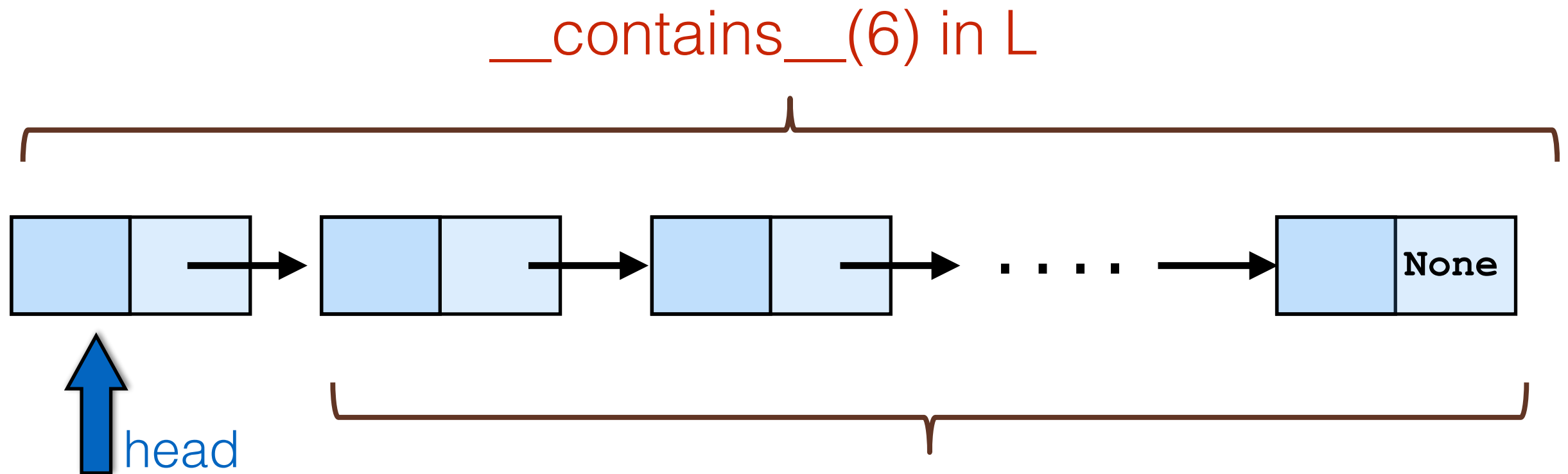
```
def __contains__(self, item):  
    current = self.head  
    while current is not None:  
        if current.item == item:  
            return True  
        current = current.next  
    return False
```

Complexity: Worst case - $O(n)$ where n is the size of the list.

__contains__

```
def __contains__(self, item):  
    current = self.head  
    while current is not None:  
        if current.item == item:  
            return True  
        current = current.next  
    return False
```

- **Best case** complexity when found first: **$O(1)$** *CompEq where CompEq is the complexity of == (or __eq__)
- **Worst case** when not found: **$O(n)$** *CompEq where n is the length of the list.



$6 == \text{head.item}$ **or** $\text{__contains__}(6)$ in L-1

Convergence: Call recursion with L-1. Use variable *current*.

Base case: Empty or Element Found. We need both.

Combining solutions: it's in the head **or** in the remaining list.

Auxiliary method sets up the initial parameters

```
def __contains__(self, item):  
    return self._contains_aux(self.head, item)
```

```
def _contains_aux(self, current, item):  
    if current is None:  
        return False  
    return current.head == item or self._contains_aux(current.next, item)
```

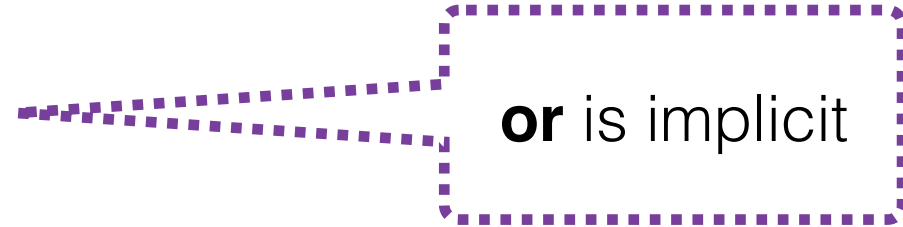
Base case

Convergence

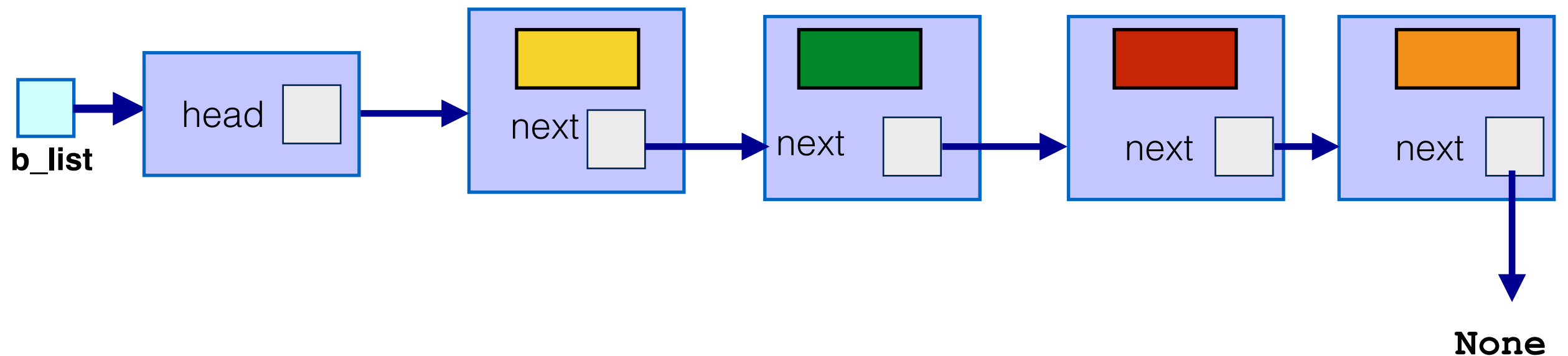
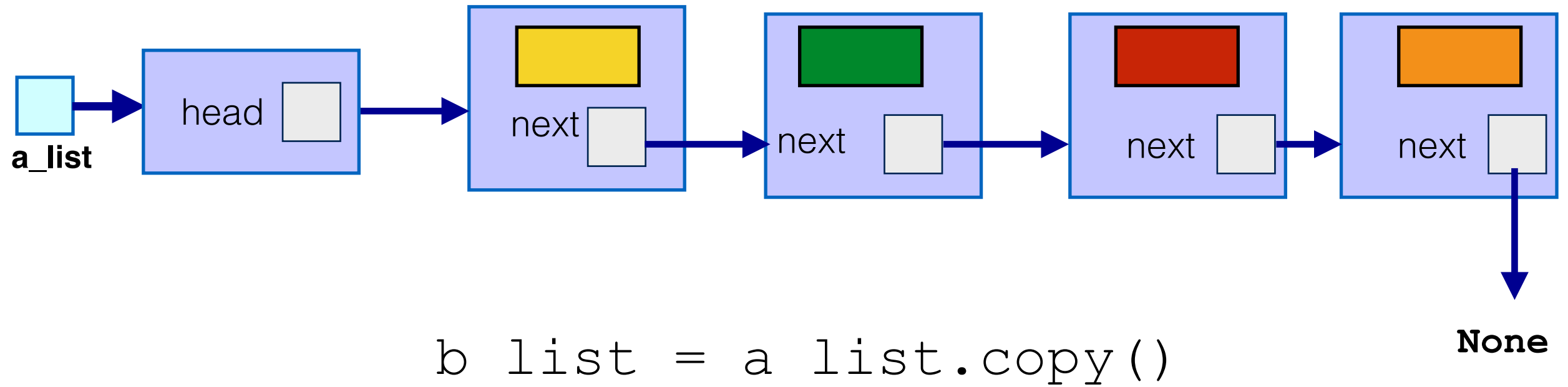
Combination

Alternative coding

```
def __contains__(self, item):  
    return self._contains_aux(self.head, item)
```

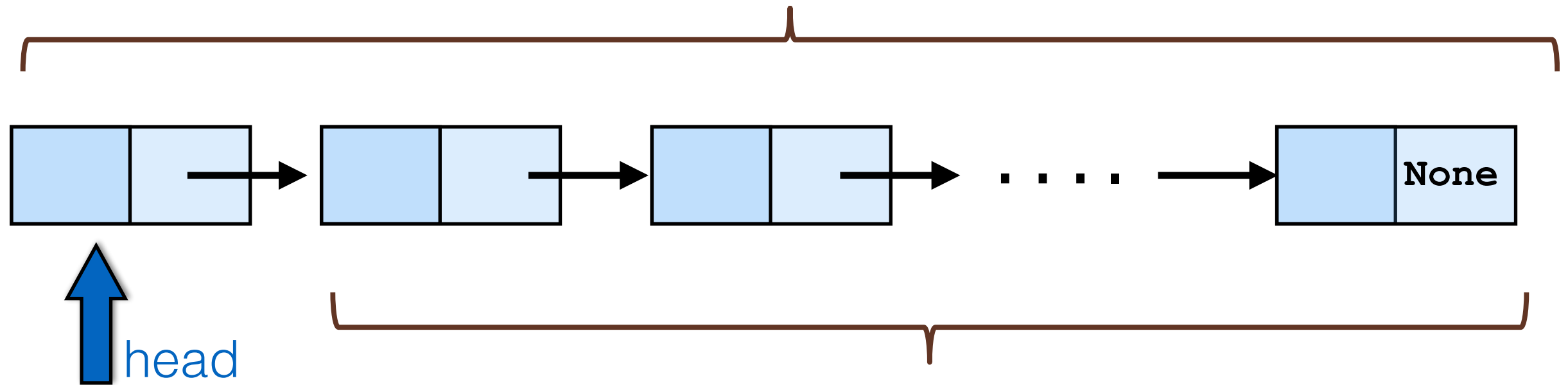
```
def _contains_aux(self, current, item):  
    if current is None:  
        return False  
    elif current.head == item:   
        return True  
    else:  
        return self._contains_aux(current.next, item)
```

Copy Linked Lists



```
def copy(self):  
    new_list = List()  
    for item in self:  
        new_list.insert(len(new_list), item)  
    return new_list
```


`_copy(self.head, new_list)`



`_copy(self.head.next, new_list)`

`new_list.insert(0, head.item)`

copy

```
def copy(self):  
    new_list = List()  
    self._copy_aux(self.head, new_list)  
    return new_list
```

Auxiliary method sets up the initial parameters

```
def _copy_aux(self, node, new_list):  
    if node is not None:  
        self._copy_aux(node.next, new_list)  
        new_list.insert(0, node.item)
```

Convergence

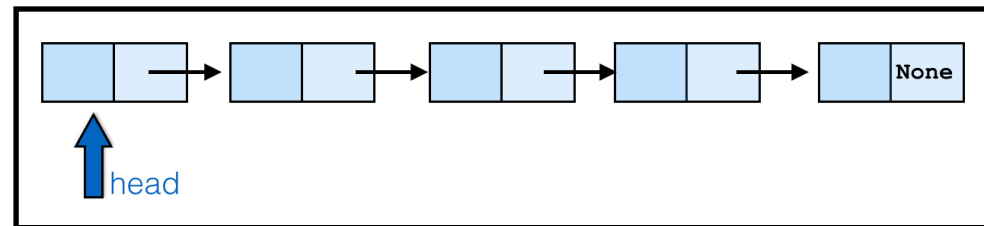
Base case

Combination

```
def copy(self):
    new_list = List()
    self._copy_aux(self.head, new_list)
    return new_list

def _copy_aux(self, node, new_list):
    if node is not None:
        self._copy_aux(node.next, new_list)
        new_list.insert(0, node.item)
```

$O(n)$



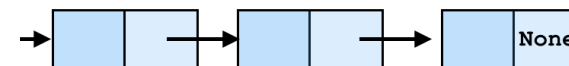
_copy_aux $O(1)$



_copy_aux $O(1)$



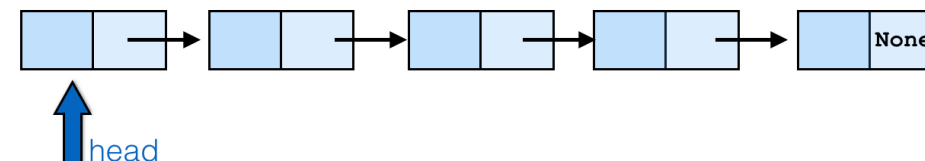
_copy_aux $O(1)$



_copy_aux $O(1)$



_copy_aux $O(1)$



n times

Using iterators...

```
def copy(a_list):  
    new_list = List()  
    copy_aux(iter(a_list), new_list)  
    return new_list
```

```
def copy_aux(iter, new_list):  
    try:  
        item = next(iter)  
        copy_aux(iter, new_list)  
        new_list.insert(0, item)  
    except StopIteration:  
        pass
```



Used when a statement is required
no code needs to be executed.

copy

```
def copy(self):  
    new_list = List()  
    for item in self:  
        new_list.insert(len(new_list), item)  
    return new_list
```

$O(n^2)$

```
def copy(self):  
    new_list = List()  
    self._copy_aux(self.head, new_list)  
    return new_list  
  
def _copy_aux(self, node, new_list):  
    if node is not None:  
        self._copy_aux(node.next, new_list)  
        new_list.insert(0, node.item)
```

$O(n)$

Advantages/Disadvantages of Recursion

- Advantages:
 - More natural
 - Easier to prove correct
 - Easier to analyse
- Disadvantages:
 - Run-time overhead depending on the quality of the compiler
 - Memory overhead (fewer local variables versus stack space for function call)