

# FIT3155: Week 2 tutorial

## Covering concepts from Week 1

**Objectives:** The tutorials, in general, give practice in problem solving, in analysis of algorithms and data-structures, and in mathematics and logic useful in the above.

**Instructions to the class:** Prepare your answers to the questions **before** the tutorial. It will probably not be possible to cover all questions unless the class has prepared them all in advance.

**Instructions to Tutors:**

- i. The purpose of the tutorials is not to solve the practical exercises.
- ii. The purpose is to check answers, and to discuss particular sticking points, not to simply make answers available.

1. Revise Gusfield's  $Z$ -value based linear-time exact matching algorithm
2. In the above  $Z$ -algorithm, for any given input string if we found that  $Z_2 = q$  (where  $q > 0$ ), then the values of  $Z_3, Z_4, \dots, Z_{q+1}, Z_{q+2}$  can be immediately obtained without additional character comparisons. Reason why?
3. Stare at the lecture slide handling the preprocessing CASE 2b of the  $Z$ -algorithm. When  $Z_{k-l+1} \geq r - k + 1$ , the algorithm does explicit comparisons until it finds a mismatch. This is a reasonable way to organize the algorithm, but in fact CASE 2b can be refined so as to eliminate an unneeded character comparison. Argue that when  $Z_{k-l+1} > r - k + 1$ , then  $Z_k = r - k + 1$ , and hence no character comparisons are necessary. Therefore, explicit character comparisons are needed only in the case when  $Z_{k-l+1} = r - k + 1$ .
4. Reason a potential linear-time solution for the following problem: Given two equal-length strings  $\alpha$  and  $\beta$  from a fixed alphabet, determine if  $\alpha$  is a circular (or cyclic) rotation of  $\beta$ . For example,  $\alpha = \text{defabc}$  is a circular rotation of  $\beta = \text{abcdef}$ .
5. Similar to the above exercise, give a linear-time algorithm to determine whether a linear string  $\alpha$  is a SUBstring of a circular string  $\beta$ . Note:

a circular string `str[1..n]` is such that the character `str[n]` precedes character `str[1]`.

6. Give an algorithm that takes in two string  $\alpha$  and  $\beta$  of lengths  $m$  and  $n$ , and finds the longest suffix of  $\alpha$  that exactly matches a prefix of  $\beta$ . Reason the run-time of your algorithm.
7. Given a string `str[1..n]`, let `len(i)` denote the length of the largest suffix of `str[i..n]` that is also a prefix of `str`. Give an algorithm that computes `len(i)` values. Reason the run-time of your algorithm.

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    END  
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