## FIT3155: Tute+Lab sheet for week 9

Objectives: Concepts from weeks 8

## Tute questions:

- 1. Revise the fast divide-and-conquer approach for large integer multiplication.
- 2. Prove that the above divide-and-conquer-approach for integer multiplication has a time-complexity of  $O(d^{\log_2(3)})$ , when multiplying two 2d bit integers. This requires you to solve the following time recurrence relationship:

$$T(2d) = 3T(d) + cd$$

where c is a constant.

- 3. Compute  $7^{330}$  mod 13 by hand using the repeated squaring method.
- 4. Revise Miller-Rabin's randomized algorithm for primality testing.

## Lab questions:

- 1. Implement the divide-conquer approach for multiplication of two integers.
- 2. Implement modular exponentiation using the method of repeated squaring.
- 3. Implement Miller-Rabin's randomized method of primality testing. Generate the the first 10,000 primes using this method.