

# **DEPARTMENT OF ELECTRICAL ENGINEERING**

## **CONTROL SYSTEM LABORATORY MANUAL**



**NATIONAL INSTITUTE OF TECHNOLOGY (NIT) ANDHRA PRADESH**  
**(An Institution of National Importance)**  
**DEPARTMENT OF ELECTRICAL ENGINEERING**  
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**NATIONAL INSTITUTE OF TECHNOLOGY (NIT) ANDHRA PRADESH**  
**DEPARTMENT OF ELECTRICAL ENGINEERING**  
**III B. Tech (EEE) II- Semester**  
**EE 356 - Control Systems Lab**

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### List of Experiments

1. Time-response of first and second order systems.
  - a) Simulation of a typical second order system and determination of step response and evaluation of time- domain specifications.
  - b) Evaluation of the effect of additional poles and zeroes on time response of second order system.
2. Frequency-response of second order system.
3. Study of P, PI & PID controller.
4. To study the effect of P, PI, PD and PID controller on the step response of a feedback control system
5.
  - a) Evaluation of effect of pole location on stability
  - b) Effect of loop gain of a negative feedback system on stability
6.
  - a) Effect of open loop and zeroes on root locus contour
  - b) To estimate the effect of open loop gain on the transient response of closed loop system by using Root locus
  - c) Comparative study of Bode, Nyquist and Root locus with respect to Stability.
7. Design and study of lag, lead and Lag-lead compensator networks.
8. DC Position Control
9. DC Motor Speed Control
10.
  - a) Block diagram reduction technique using MATLAB
  - b) State model for classical transfer function & vice versa using MATLAB.

## **Control System Lab**

### **INDEX**

<b>S. No</b>	<b>Experiment Name</b>	<b>Date</b>	<b>Hardware / MATLAB</b>
<b>1.</b>	Time response of second order system a) Simulation of a typical second order system and determination of step response and evaluation of time- domain specifications. b) Evaluation of the effect of additional poles and zeroes on time response of second order system.	20/01/2021	MATLAB
<b>2.</b>	Frequency response of a second order system	27/01/2021	MATLAB
<b>3.</b>	Study of P, PI, PD, PID Controller	03/02/2021	Hardware
<b>4.</b>	Study the effect of P, PI, PD and PID controller on the Step response of a feedback control system	10/02/2021	Hardware & MATLAB
<b>5.</b>	a) Evaluation of effect of pole location on stability. b) Effect of loop gain of a negative feedback system on stability	17/02/2021	MATLAB
<b>6.</b>	a) Effect of open loop and zeroes on root locus contour. b) To estimate the effect of open loop gain on the transient response of closed loop system by using Root locus. c) Comparative study of Bode, Nyquist and Root locus with respect to Stability.	24/02/2021	MATLAB
<b>7.</b>	Design and study of lag, lead and Lag-lead compensator networks	10/03/2021	MATLAB
<b>8.</b>	DC position Control	17/03/2021	Hardware
<b>9.</b>	DC Motor Speed Control	24/03/2021	Hardware
<b>10.</b>	a) Block diagram reduction technique using MATLAB  b) State model for classical transfer function & vice versa using MATLAB	31/04/2021	MATLAB

## **Experiment No:01** **TIME RESPONSE OF FIRST AND SECOND ORDER SYSTEM**

**Aim:** To obtain time response of a First order and second order system in case of under damped, over damped and critically damped systems.

**Apparatus Required:** PC loaded with MATLAB

### Theory:

The time response of control system consists of two parts. Transient response and steady state response.  $C(t) = C_{tr}(t) + C_{ss}(t)$ . Most of the control systems use time as its independent variable. Analysis of response means to see the variation of output with respect to time. The output of the system takes some finite time to reach to its final value. Every system has a tendency to oppose the oscillatory behavior of the system which is called damping. The damping is measured by a factor called damping ratio of the system. If the damping is very high then there will not be any oscillations in the output. The output is purely exponential. Such system is called an over damped system.

If the damping is less compared to over damped case then the system is called a critically damped system. If the damping is very less then the system is called under damped system. With no damping system is undamped.

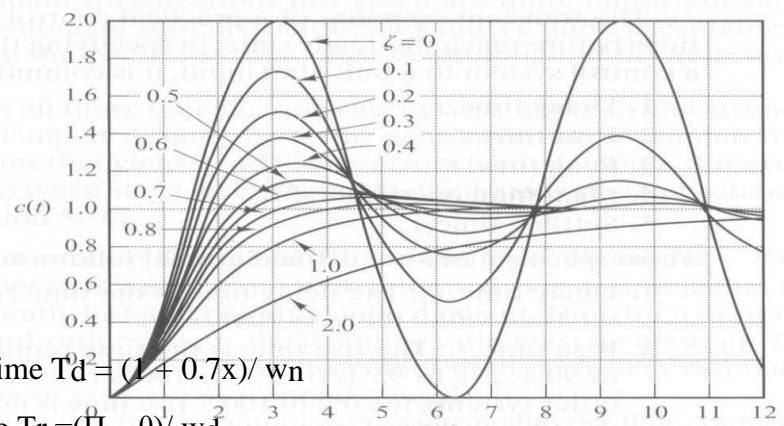
$1 < x < \infty$  --- Over damped system.

$x=1$  --- Critically

damped system.  $0 < x < 1$  ---

Under damped system.

$x=0$  --- Undamped system.



**Time domain specifications:** Delay time  $T_d = (1 + 0.7x)/\omega_n$

$$\text{Rise Time } T_r = (\Pi - \theta)/\omega_d$$

$$\text{Peak overshoot time} = T_p = \Pi/\omega_d$$

$$\% M_p = \exp(-\Pi x / \sqrt{1-x^2})$$

$$\text{Settling Time } T_s = 4/x\omega_n \quad (2\% \text{ tolerance})$$

### Procedure:

Open the MATLAB command window.

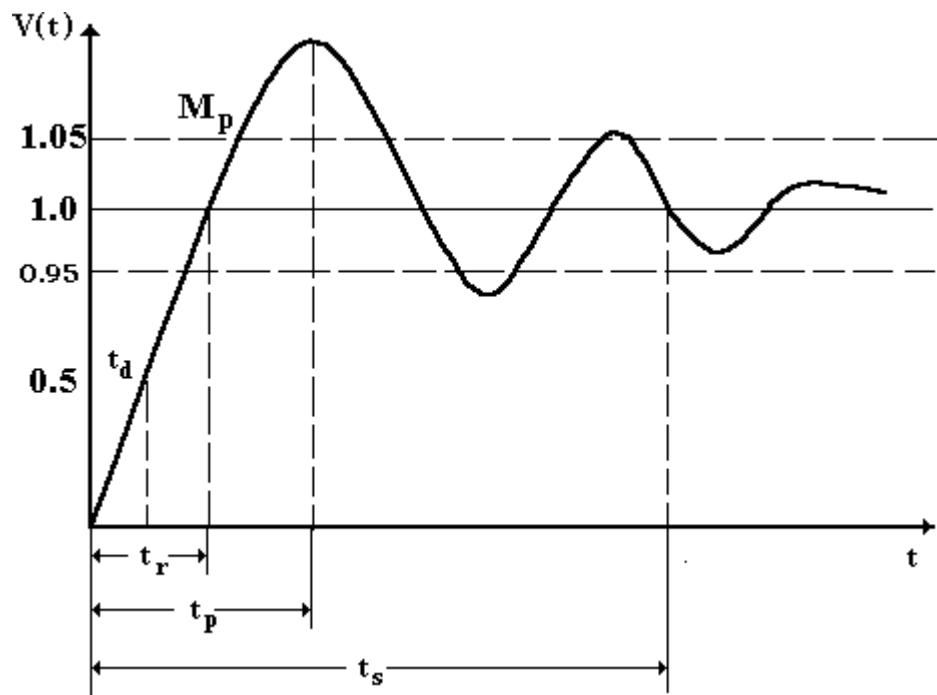
- 1) Click on file-new-M file to open the MATLAB editor window.
- 2) In the given MATLAB editor window enter the program to obtain the step response.

```
% step response of a second order system
wn = input('enter the natural frequency');
x = input('enter damping ratio');
num = [wn*wn];
den = [1 2*x*wn wn*wn];
sys = tf (num, den)
```

```
step(sys);
```

- 3) Save the file in work directory.
- 4) Run the program and enter the respective value for natural frequency, damping ratio and time
- 5) The graphs displayed are according to the above values
- 6) The values of wd, td, theta, tr, ts, Mp can be obtained by
  - a) Right click on the figure window and select grid to get grids on the curve.
  - b) Right click on the figure window and select characteristics and enable peak response, settling time & rise settling
  - c) Repeat the steps 5,6,7 for different values of x.

**Graph:**



**Tabular Columns :**

Time Domain Specifications	From MATLAB	By Calculation
Rise Time		
Peak Time		
Settling Time		
Max. Overshoot		

**1b) Evaluation of the effect of additional poles and zeros on time response of second order system.**

MATLAB program to evaluate the effect of additional poles and zeros on time response of second order system

For the second order system, if we add a pole it changes to third order.

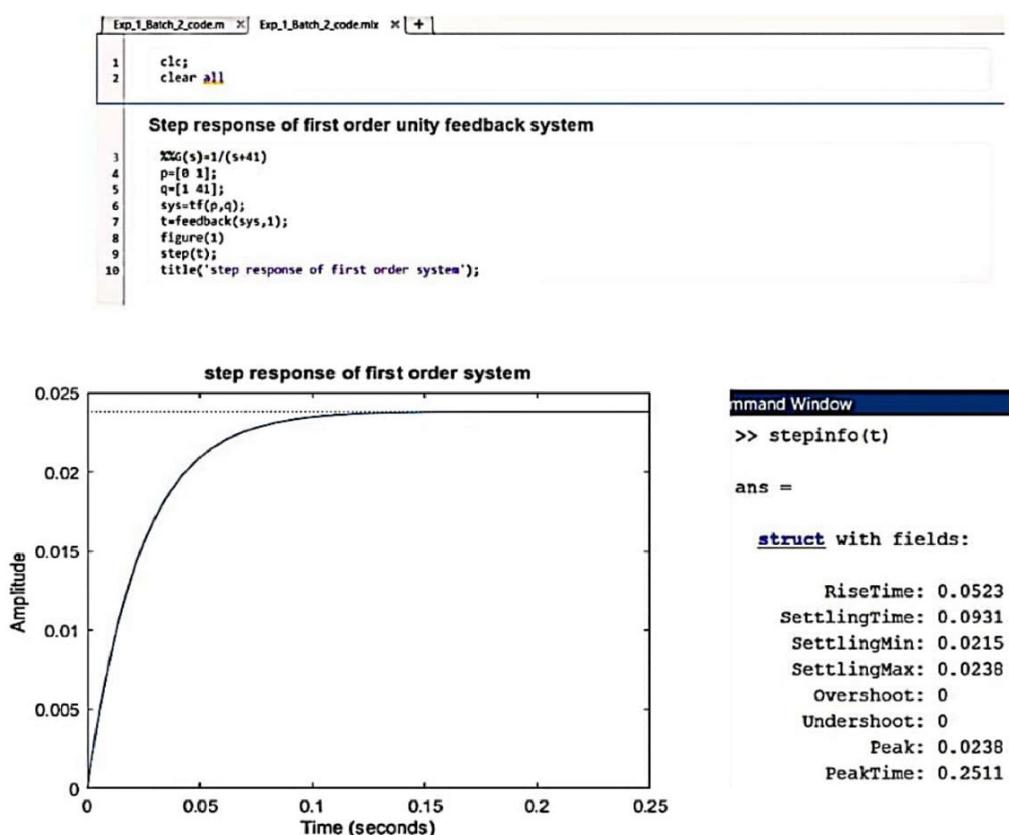
To study the effect of additional poles,

Location of poles	Effect on time response
-R	
-1/R	
-5R	

To study the effect of additional zeros,

Location of zeros	Effect on time response
-R	
-1/R	
-5R	

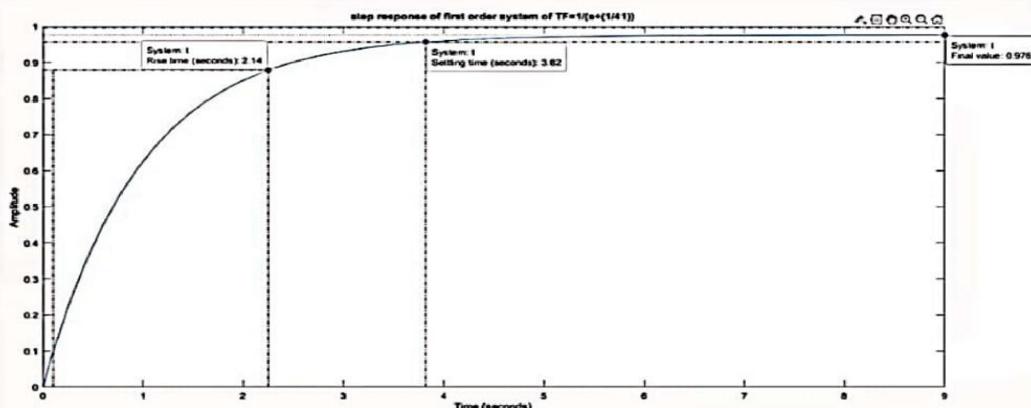
## 1. First Order System: ( $TF=1/s+41$ )



## 2. $TF=1/(s+(1/41))$ :

Step response of first order unity feedback system  $TF=1/(s+(1/41))$

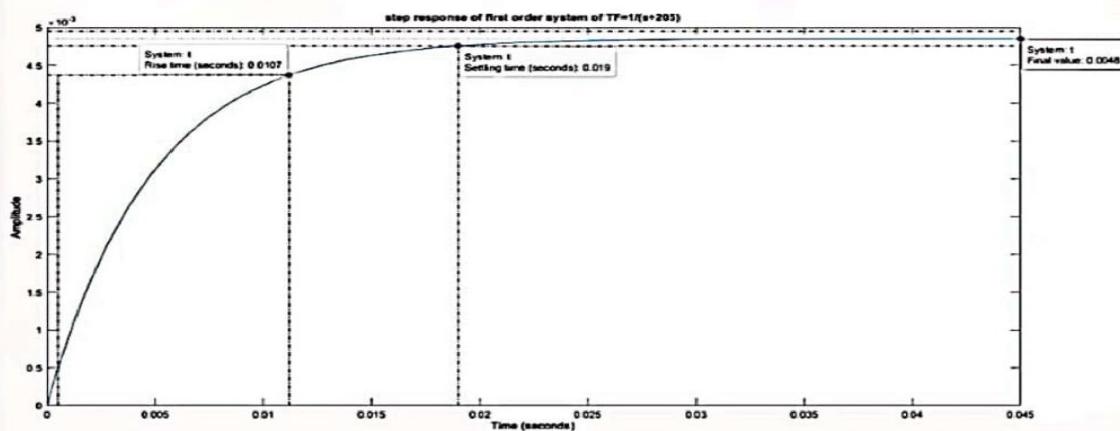
```
12 %%G(s)=1/(s+(1/41))
13 p=[0 1];
14 q=[1 1/41];
15 sys12=tf(p,q);
16 t=feedback(sys12,1);
17 figure(13)
18 step(t);
19 title('step response of first order system of TF=1/(s+(1/41))');
```



## 3. $TF=1/s+205$ :

Step response of first order unity feedback system  $TF=1/(s+205)$

```
20 %%G(s)=1/(s+205)
21 p=[0 1];
22 q=[1 205];
23 sys11=tf(p,q);
24 t=feedback(sys11,1);
25 figure(14)
26 step(t);
27 title('step response of first order system of TF=1/(s+205)');
```



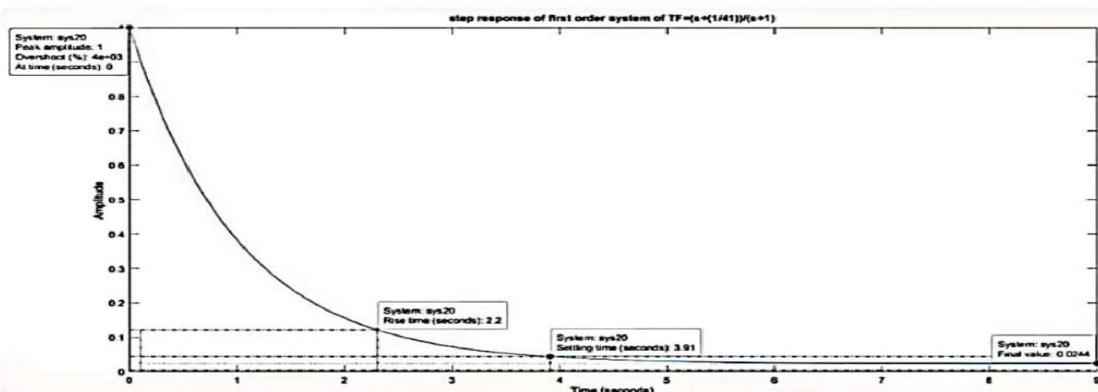
# Effect of Zeroes on first order system:

## 1. Pole at -1, Zero at -1/41:

### Effect of zeroes on first order system

#### Step response of first order system (pole at -1 and zero at -1/41)

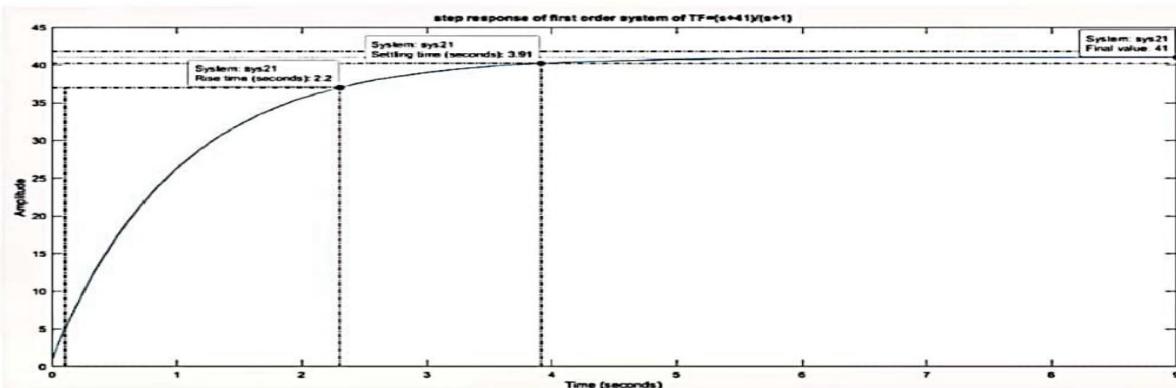
```
28 %%G(s)=(s+(1/41))/(s+1)
29 p=[1 1/41];
30 q=[1 1];
31 sys20=tf(p,q);
32 t=feedback(sys20,1);
33 figure(20);
34 step(sys20);
35 title('step response of first order system of TF=(s+(1/41))/(s+1)');
```



## 2. Pole at -1, Zero at -41:

#### Step response of first order system (pole at -1 and zero at -41)

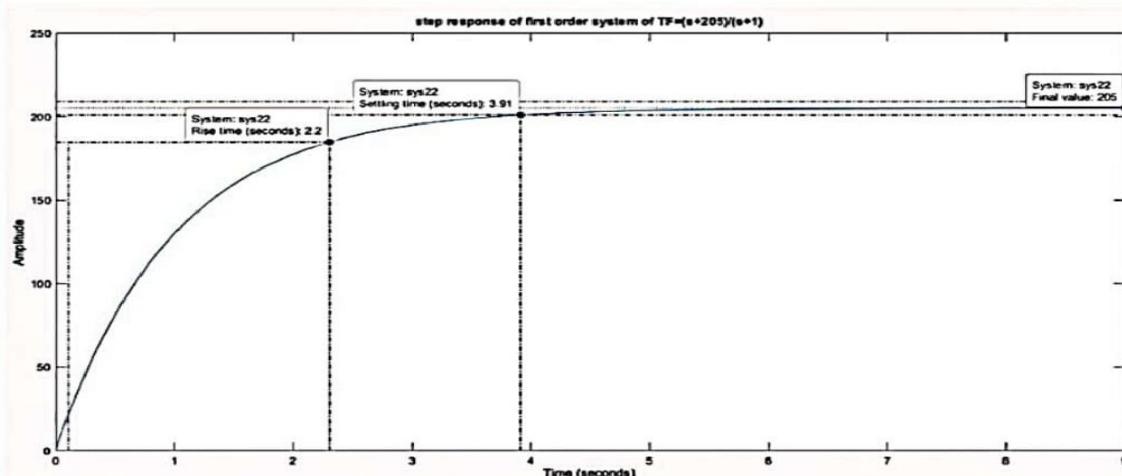
```
36 %%G(s)=(s+41)/(s+1)
37 p=[1 41];
38 q=[1 1];
39 sys21=tf(p,q);
40 t=feedback(sys21,1);
41 figure(21);
42 step(sys21);
43 title('step response of first order system of TF=(s+41)/(s+1)');
```



### 3.Pole at -1, Zero at -205(-5\*41):

Step response of first order system (pole at -1 and zero at -205)

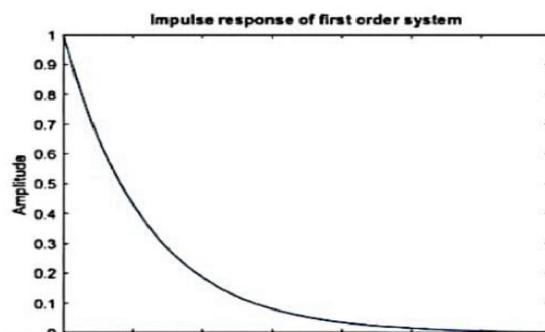
```
44 %%G(s)=(s+205)/(s+1)
45 p=[1 205];
46 q=[1 1];
47 sys22=tf(p,q);
48 t=feedback(sys22,1);
49 figure(22)
50 step(sys22);
51 title('step response of first order system of TF=(s+205)/(s+1)');
```



### Impulse Response of 1<sup>st</sup> order system:

Impulse response of first order unity feedback system

```
11 %%G(s)=1/(s+41)
12 p=[0 1];
13 q=[1 41];
14 sys=tf(p,q);
15 t=feedback(sys,1);
16 figure(2)
17 impulse(t);
18 title('impulse response of first order system');
```



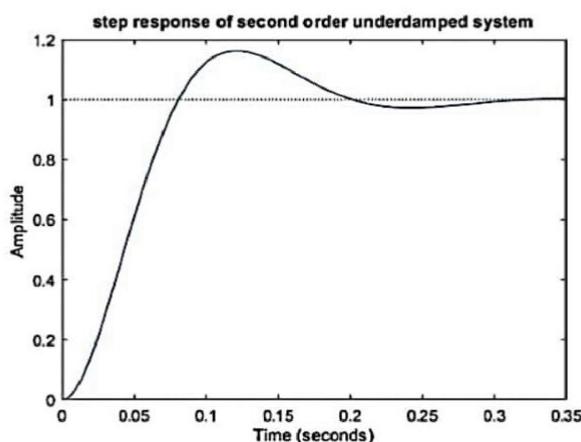
## 2. Second Order System:

### 1.Underdamped:

```
Exp_1_Batch_2_code.m  × Exp_1_Batch_2_code mlx *  + |
```

Step response of second order underdamped system

```
19 %%G(s)=w^2/(s^2+2*e*w*s+w^2)
20 w=30;
21 e=0.5;
22 p=[0 0 w*w];
23 q=[1 2*e*w w*w];
24 sys=tf(p,q);
25 figure(3)
26 step(sys);
27 title('step response of second order underdamped system');
```



```
>> stepinfo(sys)

ans =
```

struct with fields:

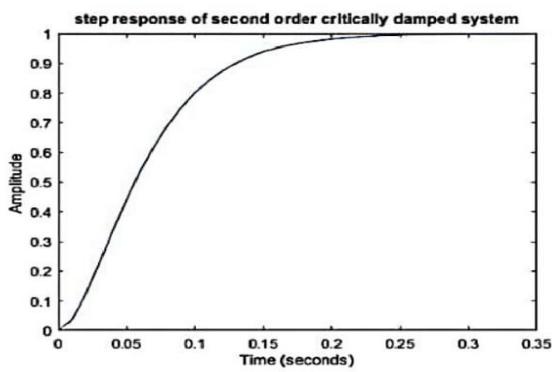
```
RiseTime: 0.0546
SettlingTime: 0.2692
SettlingMin: 0.9315
SettlingMax: 1.1629
Overshoot: 16.2929
Undershoot: 0
Peak: 1.1629
PeakTime: 0.1197
```

### ii. Critically Damped:

```
Exp_1_Batch_2_code.m  × Exp_1_Batch_2_code mlx *  + |
```

Step response of second order critically damped system

```
28 %%G(s)=w^2/(s^2+2*e*w*s+w^2)
29 w=30;
30 e=1;
31 p=[0 0 w*w];
32 q=[1 2*e*w w*w];
33 sys1=tf(p,q);
34 figure(4)
35 step(sys1);
36 title('step response of second order critically damped system');
```



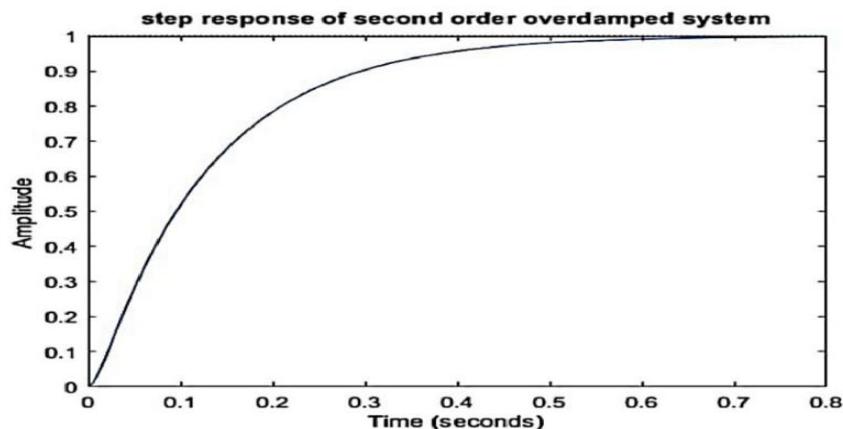
```
>> stepinfo(sys1)
ans =
struct with fields:
    RiseTime: 0.1123
    SettlingTime: 0.1948
    SettlingMin: 0.9008
    SettlingMax: 1.0000
    Overshoot: 0
    Undershoot: 0
    Peak: 1.0000
    PeakTime: 0.7900
```

### iii. Over Damped:

Exp\_1\_Batch\_2\_code.m Exp\_1\_Batch\_2\_code.mlx +

Step response of second order over damped system

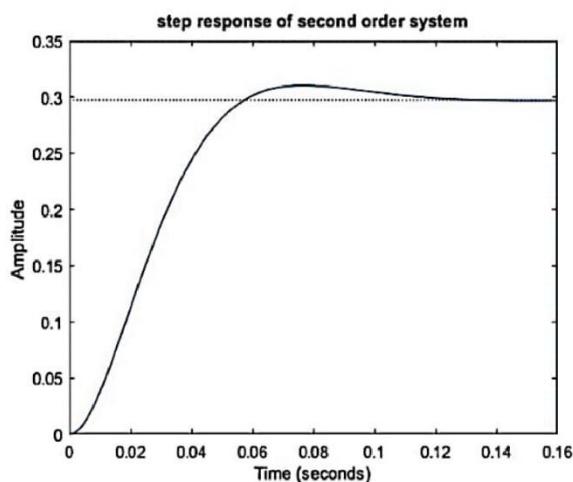
```
37 %%G(s)=w^2/(s^2+2*e*w*s+w^2)
38 w=30;
39 e=2;
40 p=[0 0 w*w];
41 q=[1 2*e*w w*w];
42 sys2=tf(p,q);
43 figure(5)
44 step(sys2);
45 title('step response of second order overdamped system');
```



```
>> stepinfo(sys2)
ans =
struct with fields:
    RiseTime: 0.2744
    SettlingTime: 0.4960
    SettlingMin: 0.9017
    SettlingMax: 0.9993
    Overshoot: 0
    Undershoot: 0
    Peak: 0.9993
    PeakTime: 0.9109
```

# Effect of Poles And Zeroes On second order system:

```
Exp_1_Batch_2_code.m  Exp_1_Batch_2_code.mlx  +  
  
Effect of poles and zeroes  
46 z=[];  
47 p=[-41+41i -41-41i];  
48 k=1000;  
49 sys3=zpk(z,p,k)  
  
sys3 =  
1000  
-----  
(s^2 + 82s + 3362)  
Continuous-time zero/pole/gain model.  
50 figure(5)  
51 step(sys3);  
52 title('step response of second order system');
```



```
>> stepinfo(sys3)  
ans =  
  
struct with fields:  
  
    RiseTime: 0.0371  
    SettlingTime: 0.1028  
    SettlingMin: 0.2687  
    SettlingMax: 0.3103  
    Overshoot: 4.3210  
    Undershoot: 0  
    Peak: 0.3103  
    PeakTime: 0.0764
```

# Addition of pole at -1/41:

Exp\_1\_Batch\_2\_code.m Exp\_1\_Batch\_2\_codemlx +

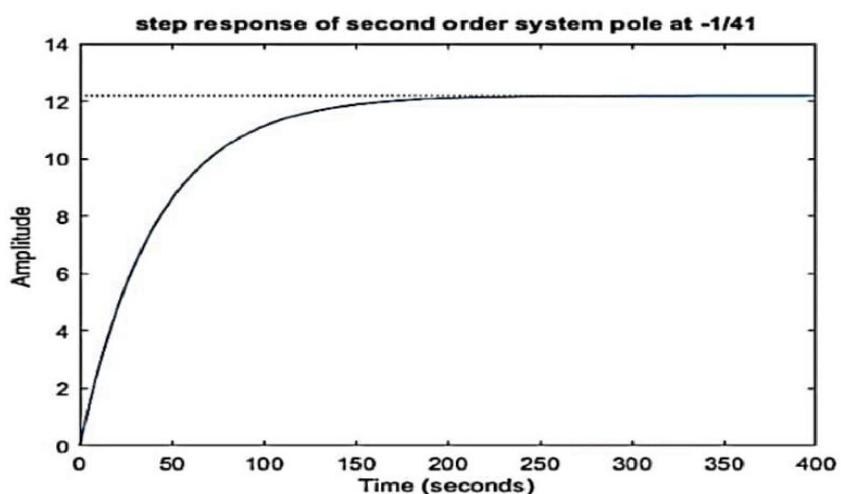
## Addition of pole at -1/41

```
53 z=[];
54 p=[-41+41i -41-41i -1/41];
55 k=1000;
56 sys4=zpk(z,p,k)

sys4 =
1000
(s+0.02439) (s^2 + 82s + 3362)

Continuous-time zero/pole/gain model.

57 figure(7);
58 step(sys4);
59 title('step response of second order system pole at -1/41');
```



```
>> stepinfo(sys4)

ans =

struct with fields:

    RiseTime: 90.0776
    SettlingTime: 160.4189
    SettlingMin: 11.0298
    SettlingMax: 12.1948
    Overshoot: 0
    Undershoot: 0
    Peak: 12.1948
    PeakTime: 432.3794
```

## Addition of pole at -41:

```

Addition of pole at -41

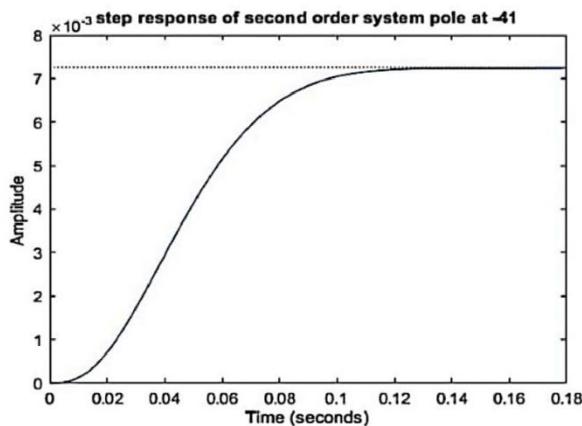
60 z=[];
61 p=[-41+41i -41-41i -41];
62 k=1000;
63 sys5=zpk(z,p,k)

sys5 =
 
 1000
 -----
 (s+41) (s^2 + 82s + 3362)

Continuous-time zero/pole/gain model.

64 figure(8)
65 step(sys5);
66 title('step response of second order system pole at -41');

```



```
>> stepinfo(sys5)
```

```

ans =

struct with fields:

    RiseTime: 0.0610
    SettlingTime: 0.1050
    SettlingMin: 0.0066
    SettlingMax: 0.0072
    Overshoot: 0
    Undershoot: 0
    Peak: 0.0072
    PeakTime: 0.2011

```

## Addition of pole at -205(-5\*41):

```

Addition of pole at -205

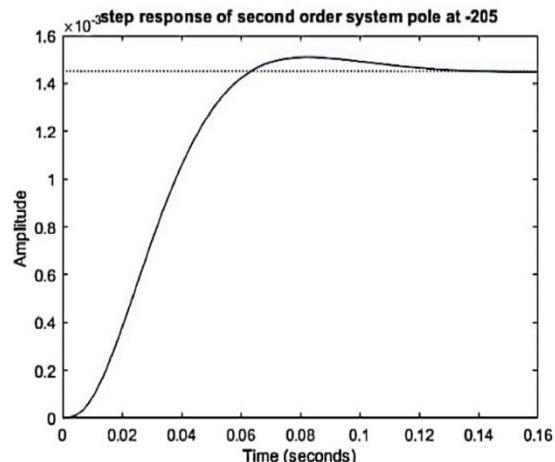
67 z=[];
68 p=[-41+41i -41-41i -205];
69 k=1000;
70 sys6=zpk(z,p,k)

sys6 =
 
 1000
 -----
 (s+205) (s^2 + 82s + 3362)

Continuous-time zero/pole/gain model.

71 figure(9)
72 step(sys6);
73 title('step response of second order system pole at -205');

```



```
>> stepinfo(sys6)
```

```

ans =

struct with fields:

    RiseTime: 0.0387
    SettlingTime: 0.1078
    SettlingMin: 0.0013
    SettlingMax: 0.0015
    Overshoot: 4.1000
    Undershoot: 0
    Peak: 0.0015
    PeakTime: 0.0831

```

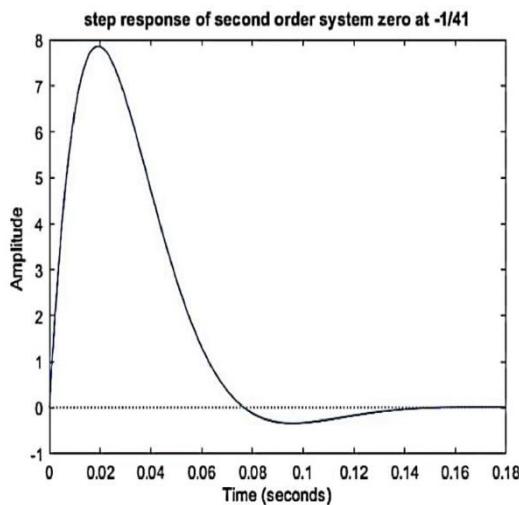
## Addition of zero at -1/41:

```
Addition of zero at -1/41
74 z=[-1/41];
75 p=[-41+41i -41-41i];
76 k=1000;
77 sys7=zpk(z,p,k)

sys7 =
1000 (s+0.02439)
-----
(s^2 + 82s + 3362)

Continuous-time zero/pole/gain model.

figure(10)
step(sys7);
title('step response of second order system zero at -1/41');
```



```
>> stepinfo(sys7)
```

```
ans =
```

struct with fields:

```
RiseTime: 6.0793e-06
SettlingTime: 0.1220
SettlingMin: -0.3323
SettlingMax: 7.8659
Overshoot: 1.0832e+05
Undershoot: 4.5804e+03
Peak: 7.8659
PeakTime: 0.0191
```

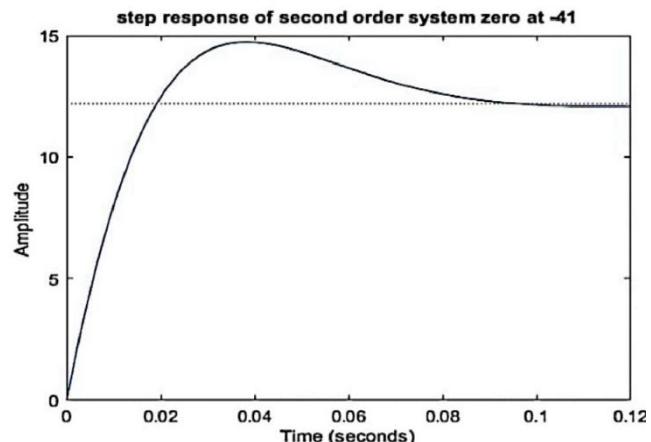
## Addition of zero at -41:

```
Addition of zero at -41
81 z=[-41];
82 p=[-41+41i -41-41i];
83 k=1000;
84 sys8=zpk(z,p,k)

sys8 =
1000 (s+41)
-----
(s^2 + 82s + 3362)

Continuous-time zero/pole/gain model.

figure(11)
step(sys8);
title('step response of second order system zero at -41');
```



```
>> stepinfo(sys8)
```

```
ans =
```

struct with fields:

```
RiseTime: 0.0146
SettlingTime: 0.0844
SettlingMin: 11.3784
SettlingMax: 14.7302
Overshoot: 20.7874
Undershoot: 0
Peak: 14.7302
PeakTime: 0.0382
```

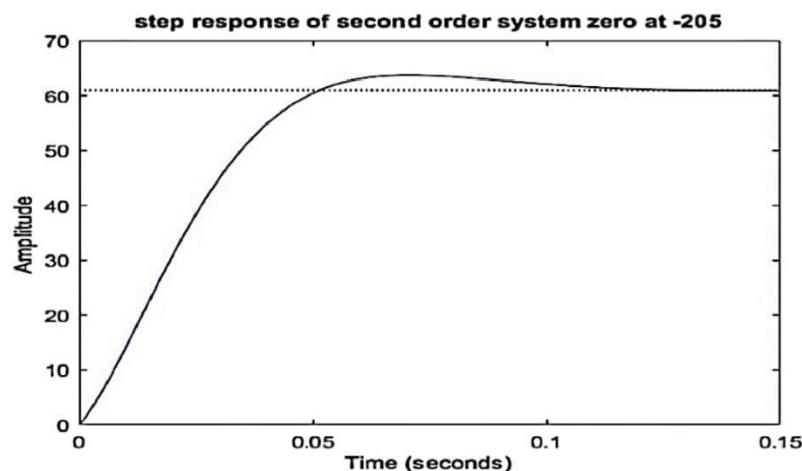
## Addition of zero at -205(-5\*41):

```
88      Addition of zero at -205
89
90
91      z=[-205];
92      p=[-41+41i -41-41i];
93      k=1000;
94      sys9=zpk(z,p,k)

      sys9 =
      1000 (s+205)
      -----
      (s^2 + 82s + 3362)

      Continuous-time zero/pole/gain model.

92      figure(12)
93      step(sys9);
94      title('step response of second order system zero at -205');
```



```
>> stepinfo(sys9)

ans =

    struct with fields:

        RiseTime: 0.0354
        SettlingTime: 0.0978
        SettlingMin: 55.0411
        SettlingMax: 63.7516
        Overshoot: 4.5526
        Undershoot: 0
        Peak: 63.7516
        PeakTime: 0.0708
```

**Result:**

## **Experiment No.2**

### **FREQUENCY RESPONSE OF A SECOND ORDER SYSTEM**

**Aim:** To determine frequency response of a second order system and evaluation of Frequency domain specifications using MATLAB.

#### **Theory:**

The frequency response of a system or a component is normally performed by keeping the amplitude A fixed and determining B and  $\Phi$  for a suitable range of frequencies where steady state output may be represented as  $c(t) = B \sin(\omega t + \Phi)$ . The ease and Accuracy of measurements are some of the advantages of the frequency response method. Without the knowledge of transfer function, the frequency response of stable open loop system can be obtained experimentally or the systems with very large time constants, the frequency response test is cumbersome to perform. We can use the data obtained from measurements on the physical system without deriving its mathematical model. Nyquist, bode, Nichols etc are some of the frequency response methods. For difficult cases, such as conditionally stable systems, Nyquist Plot is probably the only method to analyse stability.

$$G(s) = \frac{w_n^2}{s^2 + 2gw_n s + w_n^2}$$

$$\text{Resonance Frequency } \omega_r = \omega_n \sqrt{1 - 2\zeta^2}$$

$$\text{Resonance Peak M R} = 1/2\zeta \sqrt{1 - \zeta^2}$$

$$\text{Bandwidth } \omega_b = \omega_n \sqrt{1 - \zeta^2} + \sqrt{1 - \zeta^2} + 1$$

#### **Procedure:**

#### **Procedure:**

- 1) Open the MATLAB command window.
- 2) Click on file/new/M file to open the MATLAB editor window. In MATLAB editor window enter the program
- 3) Save the program as .M file.
- 4) Execute the program by selecting run.
- 5) Obtain the Specifications from the plot.

#### **Theoretical Calculations:**

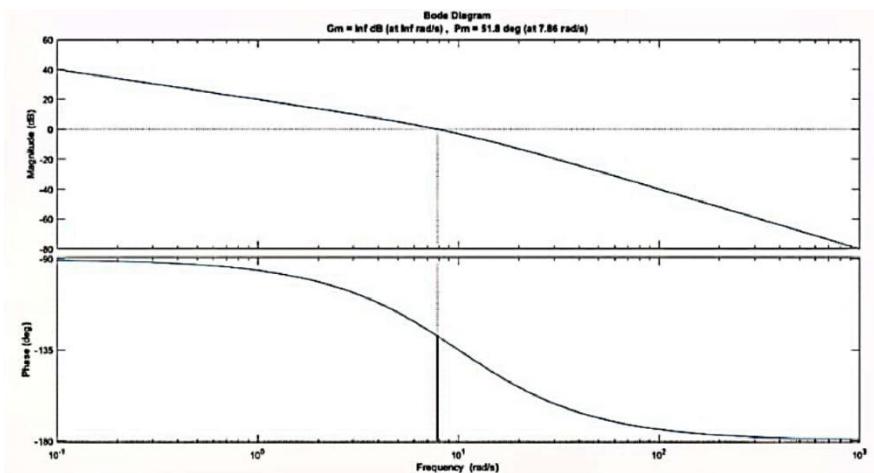
#### **Program:**

```
numerator= [100]
denominator= [1 10 100]
sys=tf(numerator, denominator)
```

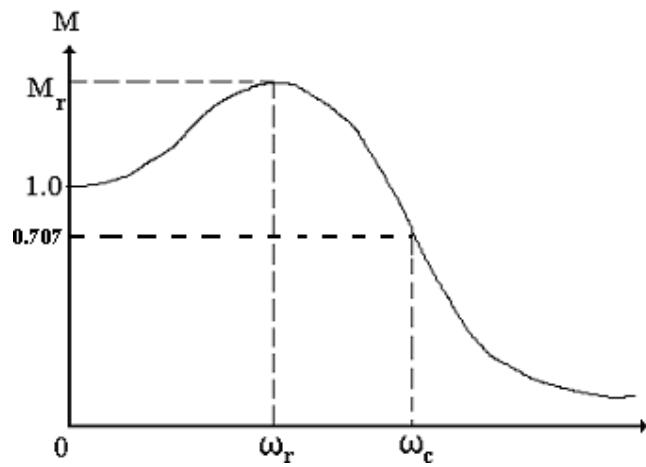
```
[Mr,wr]=getPeakGain(sys);
wb=bandwidth(sys)
bode(sys)
margin(sys)
grid
```

## 1. $TF = 100/s^2 + 10s + 100$

<b>Command Window</b> <pre>&gt;&gt; %frequency response of second order system w=input('enter natural frequency'); enter natural frequency10 &gt;&gt; e=input('enter damping ratio'); enter damping ratio0.5 &gt;&gt; num=w*w; &gt;&gt; den=[1,2*e*w,w*w]; &gt;&gt; openlooptf=tf([100],[1,10,0])  openlooptf =  100 ----- s^2 + 10 s  Continuous-time transfer function.  &gt;&gt; g=tf(num,den)  g =  100 ----- s^2 + 10 s + 100  Continuous-time transfer function.</pre>	<b>Command Window</b> <pre>&gt;&gt; [mr,wr]=getPeakGain(g)  mr =  1.1547  wr =  7.0610  &gt;&gt; wb=bandwidth(g)  wb =  12.7119  &gt;&gt; bode(openlooptf) &gt;&gt; margin(openlooptf) &gt;&gt; figure(1)</pre>
--	---



Graph:



Observations

Parameter	Practical Values	Theoretical values
$\omega_r$		
$M_r$		
$\omega_b$		
$\omega_{gc}$		
$\omega_{pc}$		
PM		
GM		

Result:

**Experiment No: 03**  
**Study of P, PI, PD, PID Controller**

**Objective:** Study of P, PI, PD, PID Controller

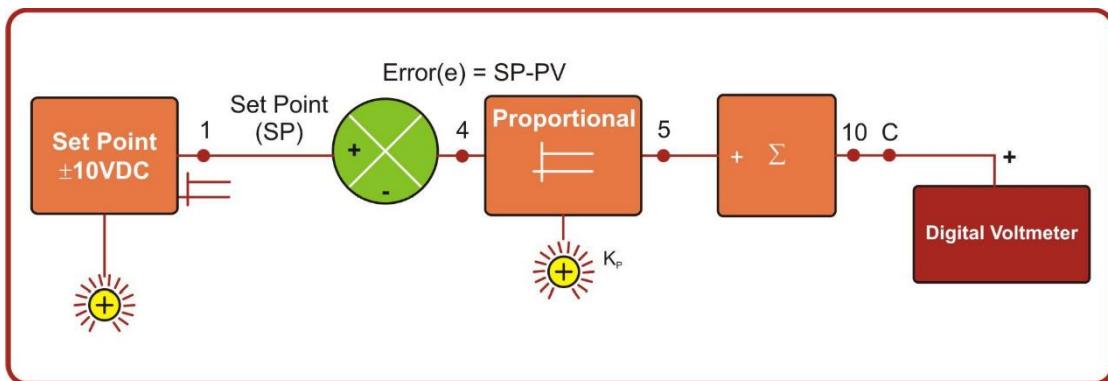
**Apparatus Required**

- |                          |        |
|--------------------------|--------|
| 1. PID kit               | 1 No.  |
| 2. Patch Cord 16"        | 20 No. |
| 3. Mains Cord            | 1 No.  |
| 4. TechBook Power Supply | 1 No   |

**Objective:** Study of Proportional controller.

**Procedure:**

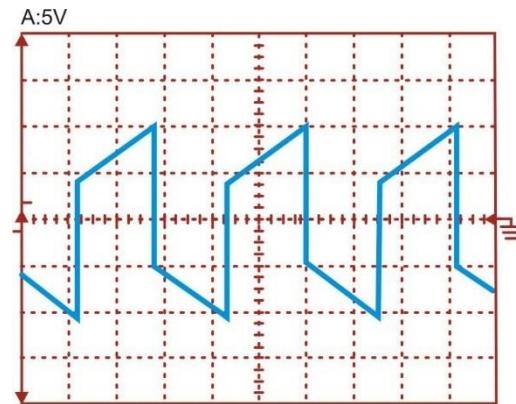
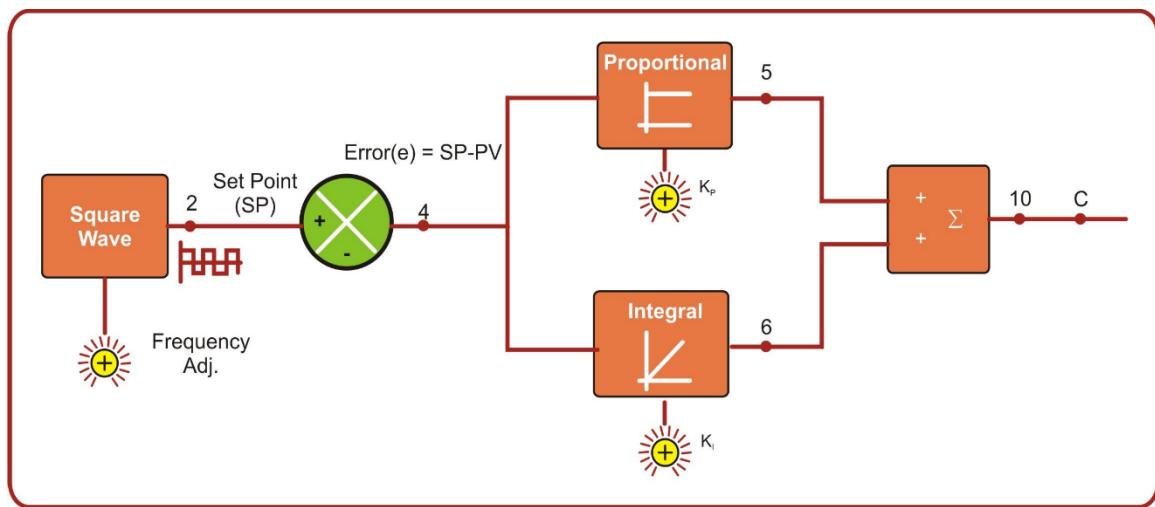
1. Connections for Proportional controller are as shown in the figure.
2. After making, all required connection on board which on the power supply and start the experiment.
3. Ground PV and inputs of summing block which are not in use.
4. Set  $\pm 1.0V$  at test point  $\pm 10V$  set point output.
5. Apply set point to proportional input.
6. Check the output of proportional block with digital voltmeter given on board.
7. Vary slowly the  $K_p$  value, observe the change in the output, and find out the proportional band that is  $PB = 100/K_p$ .



**Objective:** Study of Proportional + Integrator (PI)

**Procedure:**

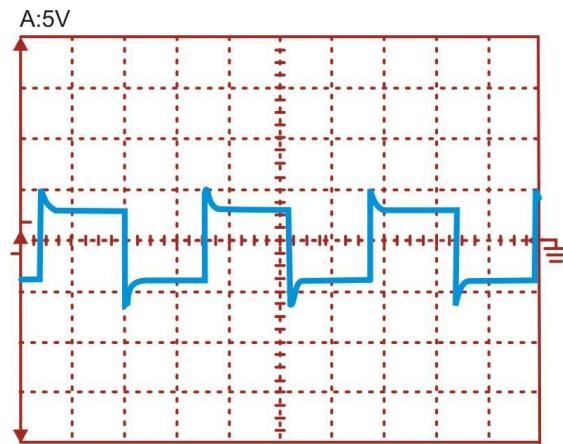
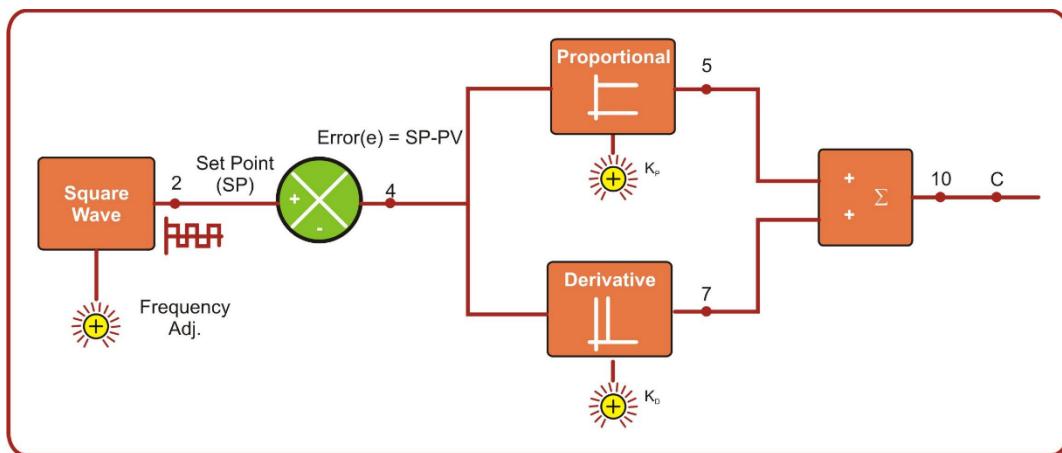
1. Connections for Proportional + Integrator (PI) controller are as shown in the figure.
2. After making, all required connection on board which on the power supply and start the experiment.
3. Ground PV and inputs of summing block which are not in use.
4. Apply square wave to the set point (SP).
5. Check the output of summer block  $\Sigma$  of summing block on CRO that will look like as shown in figure.
6. Vary slowly the KP & KI value and observe the changes in the output.



## **Objective:** Study of Proportional + Derivative (PD)

### **Procedure:**

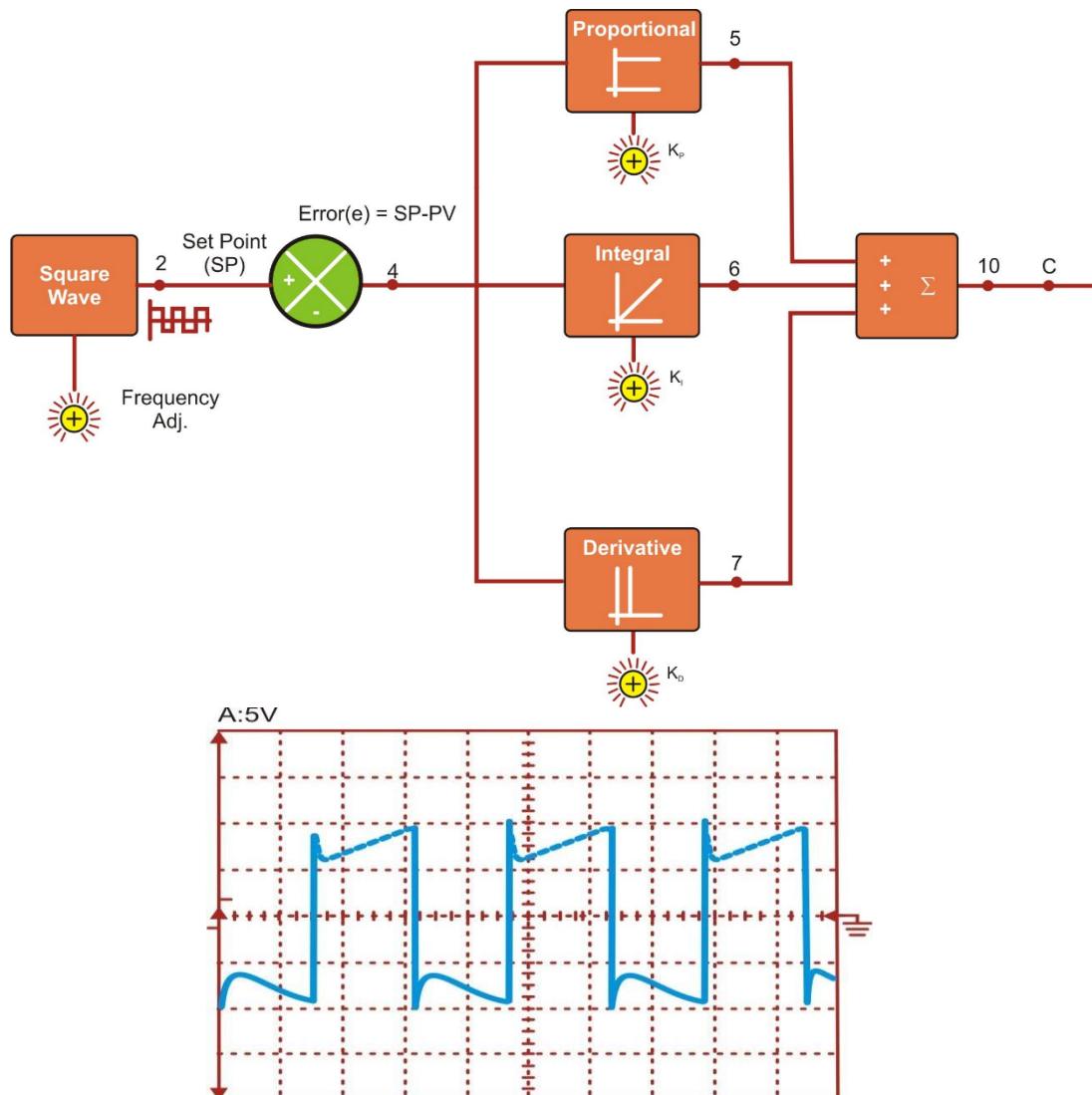
1. Connections for Proportional + Derivative (PD) controller are as shown in the figure.
2. After making, all required connection on board which on the power supply and start the experiment.
3. Ground PV and inputs of summing block which are not in use.
4. Apply square wave to the set point (SP).
5. Check the output of summer block  $\Sigma$  of summing block on CRO that will look like as shown in figure.
6. Vary slowly the KP & KD value and observe the changes in the output.



**Objective:** Study of Proportional + Integrator + Derivative (PID)

**Procedure:**

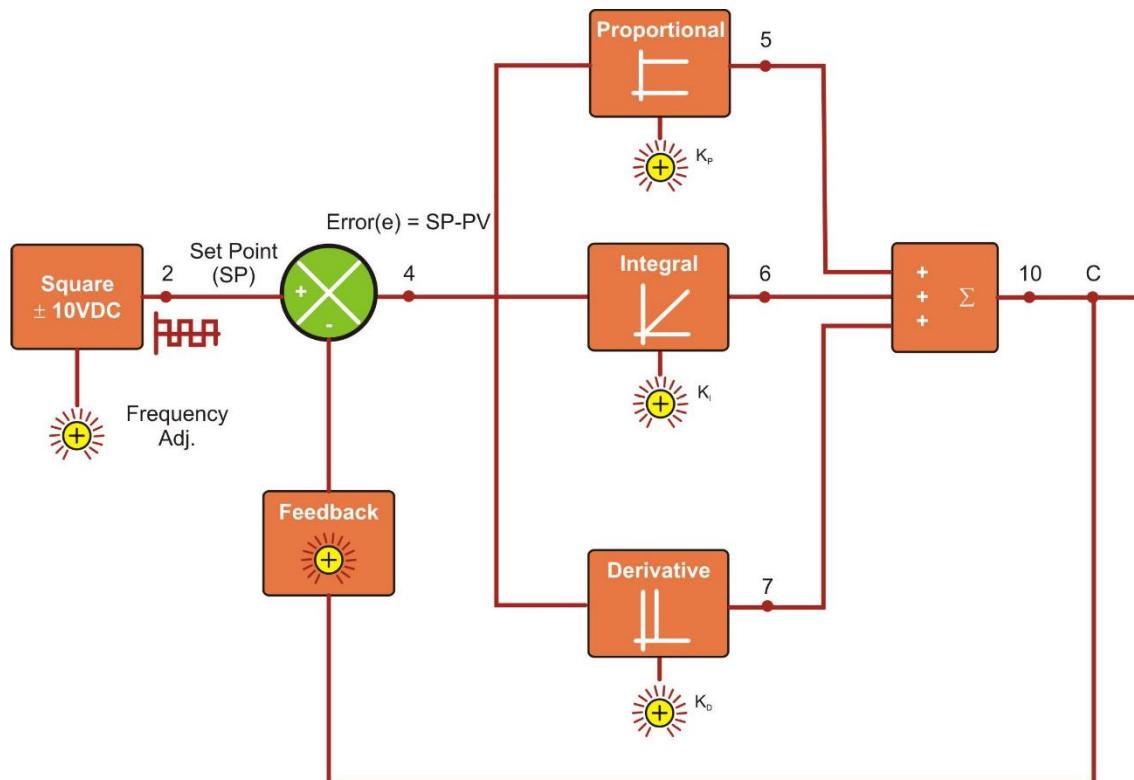
1. Connections for Proportional + Integrator + Derivative (PID) controller are as shown in the figure.
2. After making, all required connection on board switch on the power supply and start the experiment.
3. Ground PV and inputs of summing block which are not in use.
4. Apply square wave to the set point (SP).
5. Check the output of summer block  $\Sigma$  of summing block on CRO that will look like as shown in figure.
6. Vary slowly the KP, KI & Kd value and observe the changes in the output.



**Objective:** Study of Proportional + Integrator + Derivative (PID) in close loop

**Procedure:**

1. Connections for Proportional + Integrator + Derivative (PID) controller are as shown in the figure.
2. After making, all required connection on board Switch on the power supply and start the experiment.
3. Ground inputs of summing block which are not in use.
4. Apply square wave to the set point (SP).
5. Check output of summing block on CRO, you will find that after adjusting K<sub>p</sub>, K<sub>i</sub> & K<sub>d</sub> output signal will be same as input applied at SP of error detector.



**Result:**

**Experiment No: 04**  
**Study the effect of P, PI, PD and PID controller on the**  
**step response of a feedback control system**

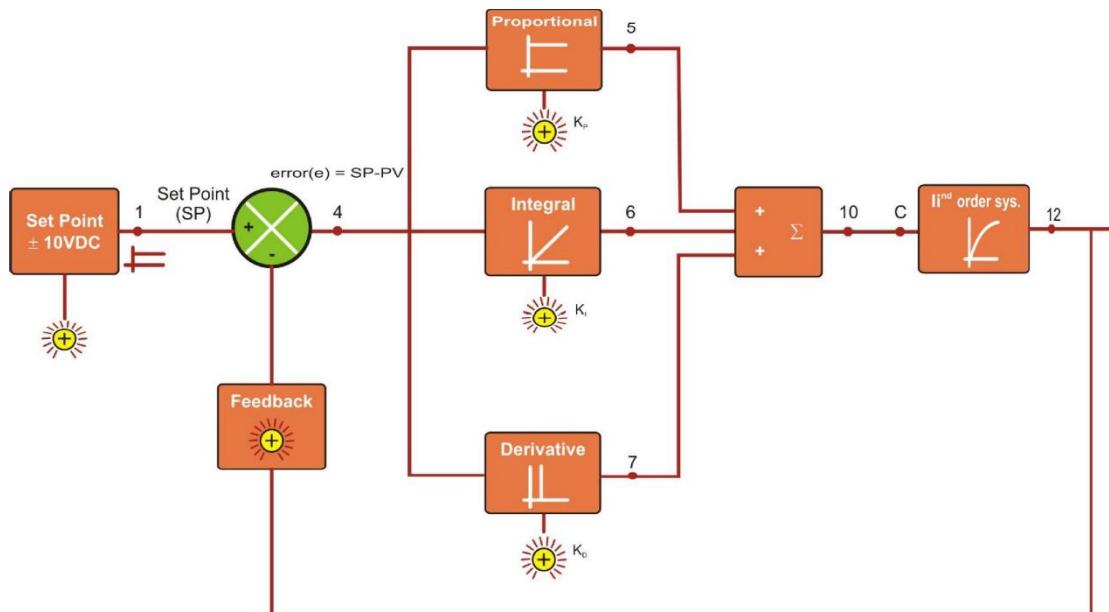
**Objective:** To Implement PID Controller to closed loop second order system with unit step input.

**Apparatus Required:**

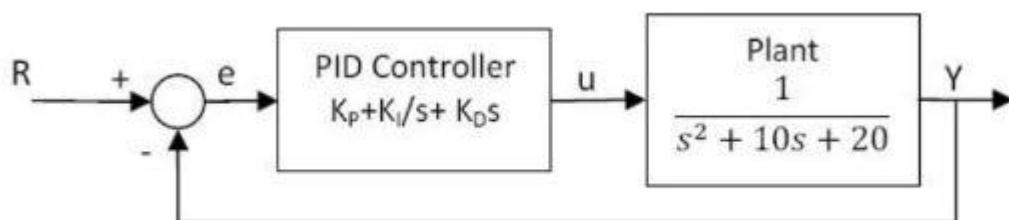
1. PID kit	1 No.
2. Patch Cord 16"	20 No.
3. Mains Cord	1 No.
4. TechBook Power Supply	1 No

**Procedure:**

1. The Connections for Proportional + Integrator + Derivative (PID) with second order system are as shown in the figure.
2. After making, all required connection on board which on the power supply and start the experiment.
3. Ground inputs of summing block which are not in use.
4. Check the transient response of II<sup>nd</sup> order system output on Digital storage oscilloscope, you will observe the response. You can easily observe the effect of PID by adjusting K<sub>P</sub>, K<sub>I</sub> & K<sub>D</sub> knobs.

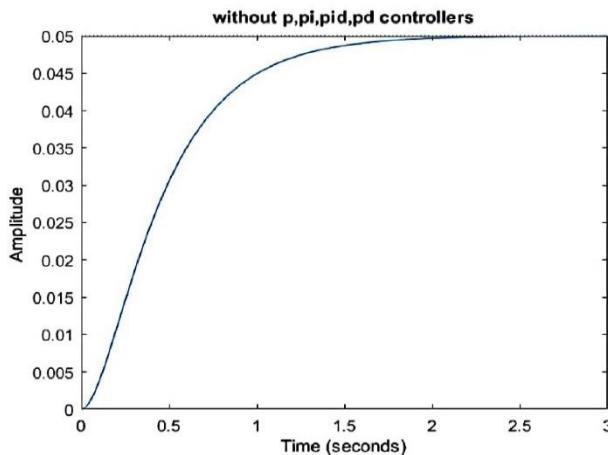


**Note:** Repeat the same experiment in Simulation for P, PI, PD, PID implementation.



# Step Response Without any controller:

```
1 clc;
2 clear;
3 close all;
4 s=tf('s');
5 G=1/(s^2+10*s+20);
6 figure(1)
7 step(G)
8 title('without p,pi,pid,pd controllers');
```



Command Window

```
>> stepinfo(G)

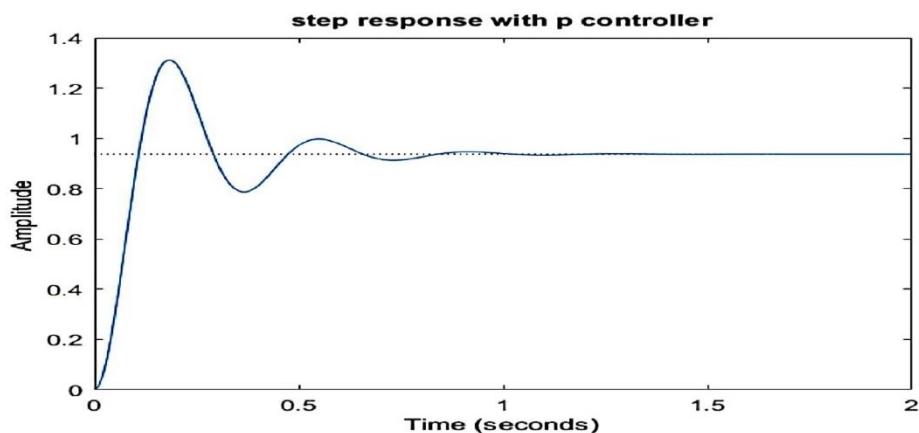
ans =
```

**struct** with fields:

```
RiseTime: 0.8843
SettlingTime: 1.5894
SettlingMin: 0.0452
SettlingMax: 0.0500
Overshoot: 0
Undershoot: 0
Peak: 0.0500
PeakTime: 3.2966
```

# With P controller:

```
11 % p-controller
12 kp=300;
13 C=pid(kp,0,0);
14 plant=C*G;
15 a=feedback(plant,1);
16 b = 0:0.01:2;
17 figure(2)
18 step(a,b)
19 title('step response with p controller');
```



```
>> stepinfo(a)

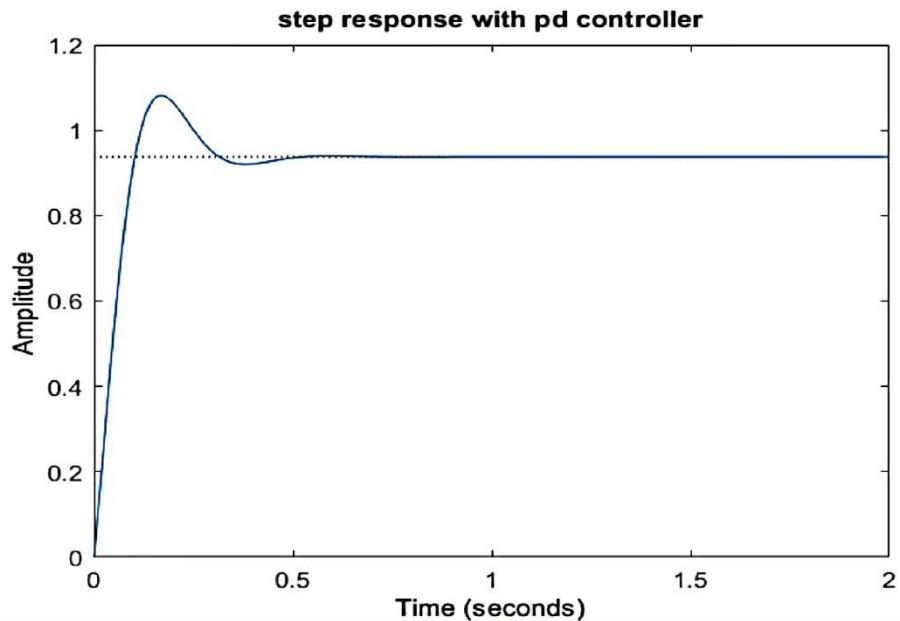
ans =
```

**struct** with fields:

```
RiseTime: 0.0727
SettlingTime: 0.7724
SettlingMin: 0.7871
SettlingMax: 1.3131
Overshoot: 40.0588
Undershoot: 0
Peak: 1.3131
PeakTime: 0.1842
```

# With PD Controller:

```
22 kd=10;
23 kp=300;
24 C=pid(kp,0,kd);
25 plant=C*G;
26 a1=feedback(plant,1);
27 b1=0:0.01:2;
28 figure(3);
29 step(a1,b1)
30 title('step response with pd controller');
```



```
>> stepinfo(a1)

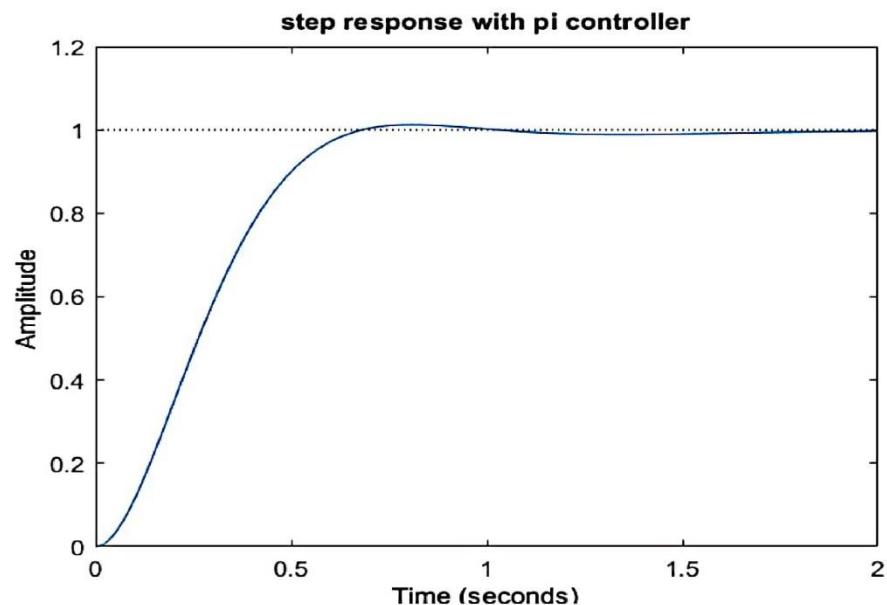
ans =

    struct with fields:

        RiseTime: 0.0777
        SettlingTime: 0.2897
        SettlingMin: 0.8490
        SettlingMax: 1.0813
        Overshoot: 15.3418
        Undershoot: 0
        Peak: 1.0813
        PeakTime: 0.1704
```

# With PI controller:

```
34 kp=30;
35 ki=70;
36 C=pid(kp,ki);
37 plant=C*G;
38 a2=feedback(plant,1);
39 b2=0:0.01:2;
40 figure(4);
41 step(a2,b2)
42 title('step response with pi controller');
```



```
>> stepinfo(a2)

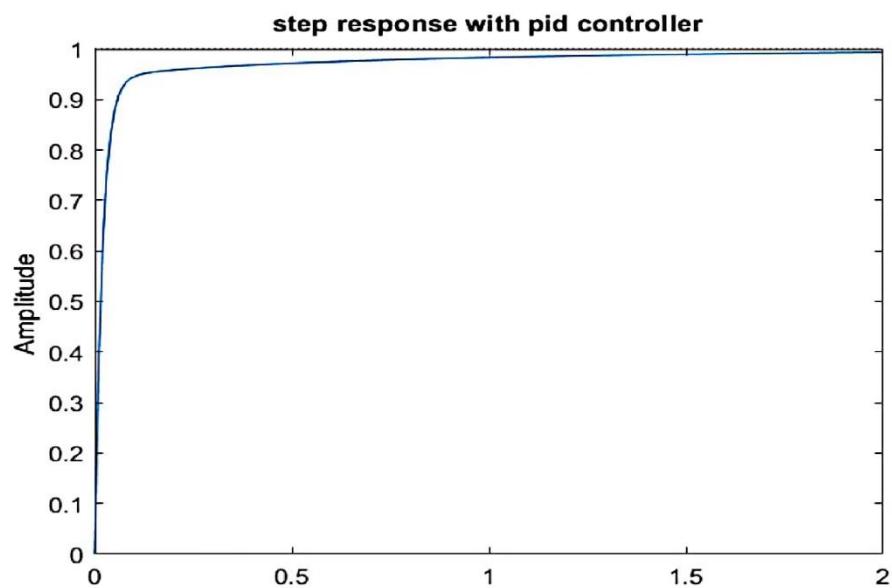
ans =

struct with fields:

    RiseTime: 0.4084
    SettlingTime: 0.6182
    SettlingMin: 0.9058
    SettlingMax: 1.0126
    Overshoot: 1.2588
    Undershoot: 0
    Peak: 1.0126
    PeakTime: 0.8143
```

# With PID Controller:

```
46 kp=350;
47 ki=300;
48 kd=50;
49 C=pid(kp,ki,kd);
50 plant=C*G;
51 a3=feedback(plant,1);
52 b3=0:0.01:2;
53 figure(5)
54 step(a3,b3)
55 title('step response with pid controller');
```



```
>> stepinfo(a3)

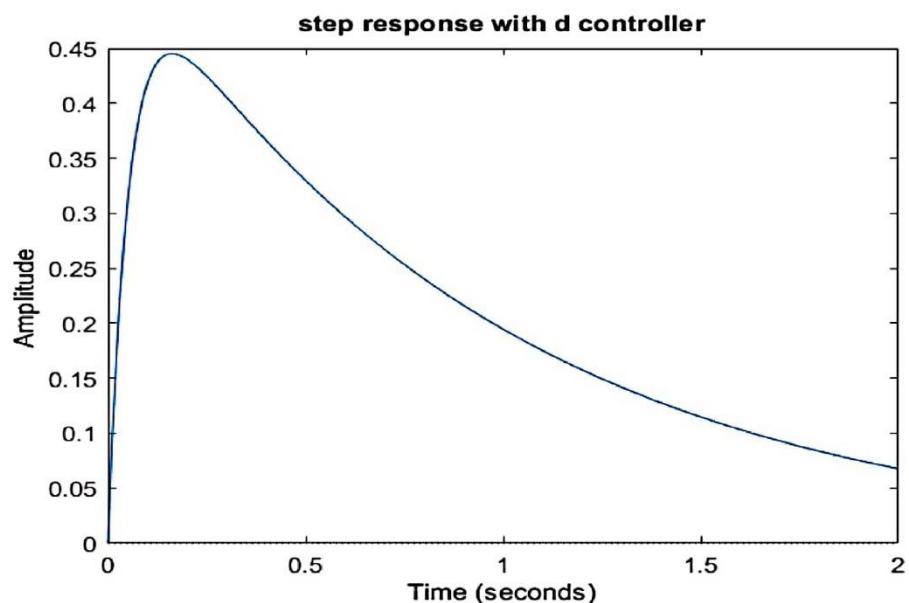
ans =

struct with fields:

    RiseTime: 0.0548
    SettlingTime: 0.8308
    SettlingMin: 0.9006
    SettlingMax: 0.9959
    Overshoot: 0
    Undershoot: 0
    Peak: 0.9959
    PeakTime: 2.4775
```

# With D Controller:

```
58 %d
59 kd=10;
60 C=pid(0,0,kd);
61 plant=C*G;
62 a4=feedback(plant,1);
63 b4=0:0.01:2;
64 figure(6)
65 step(a4,b4)
66 title('step response with d controller');
```



```
>> stepinfo(a4)
```

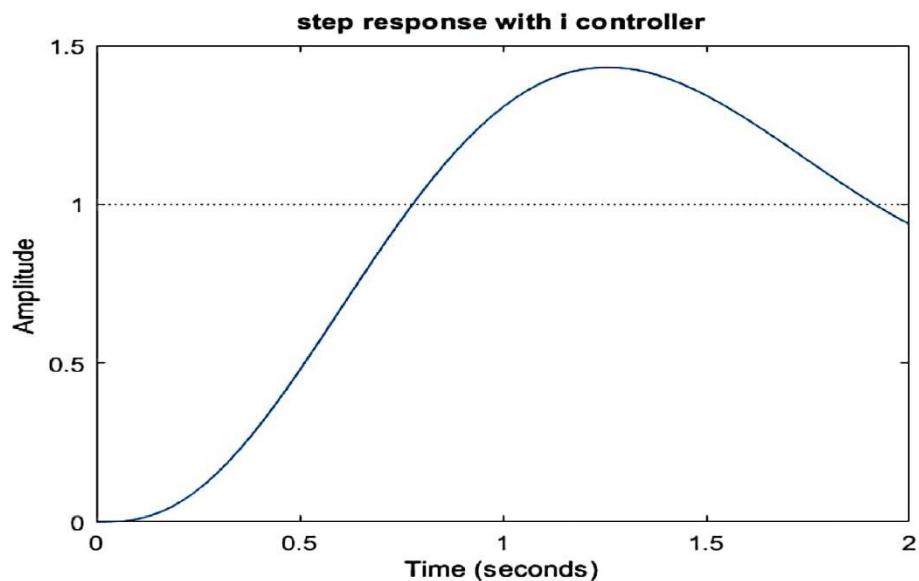
```
ans =
```

**struct** with fields:

```
RiseTime: 0
SettlingTime: 3.9213
SettlingMin: 5.7893e-04
SettlingMax: 0.4452
Overshoot: Inf
Undershoot: 0
Peak: 0.4452
PeakTime: 0.1604
```

# With I Controller:

```
69 %i
70 ki=70;
71 C=pid(0,ki,0);
72 plant=C*G;
73 a5=feedback(plant,1);
74 b5=0:0.01:2;
75 figure(7)
76 step(a5,b5)
77 title('step response with i controller');
```



```
>> stepinfo(a5)
```

```
ans =
```

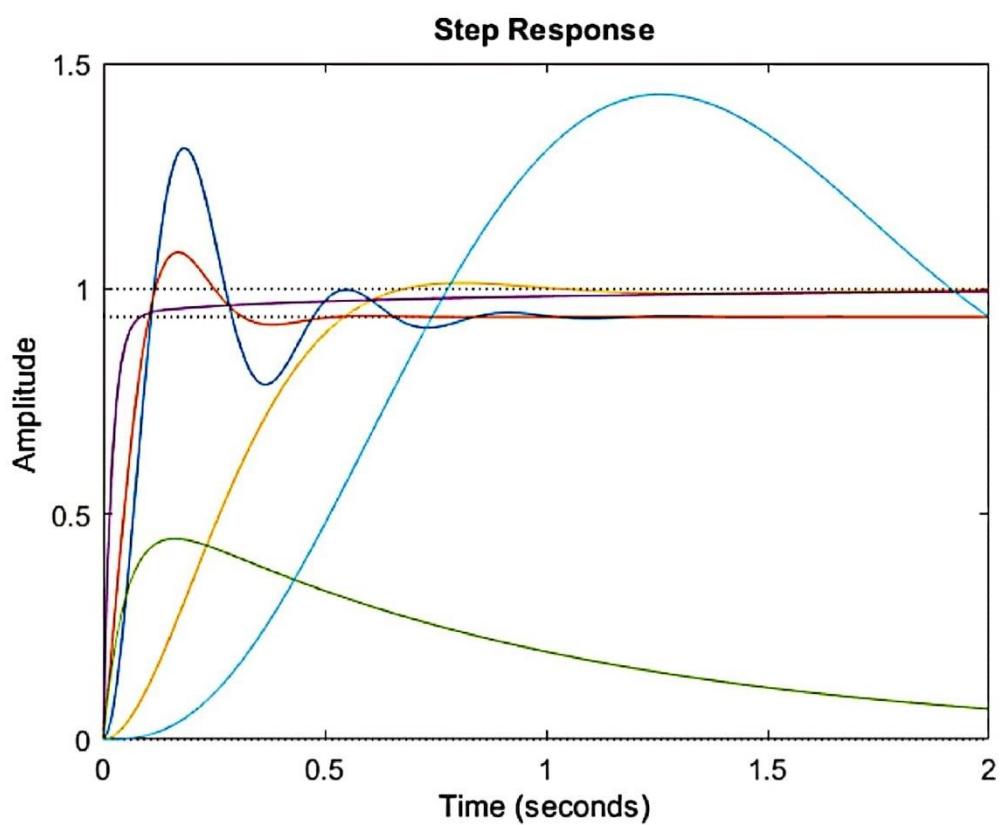
struct with fields:

```
RiseTime: 0.4734
SettlingTime: 5.0784
SettlingMin: 0.8028
SettlingMax: 1.4315
Overshoot: 43.1471
Undershoot: 0
Peak: 1.4315
PeakTime: 1.2605
```

# Comparison Graph:

## comparision graph

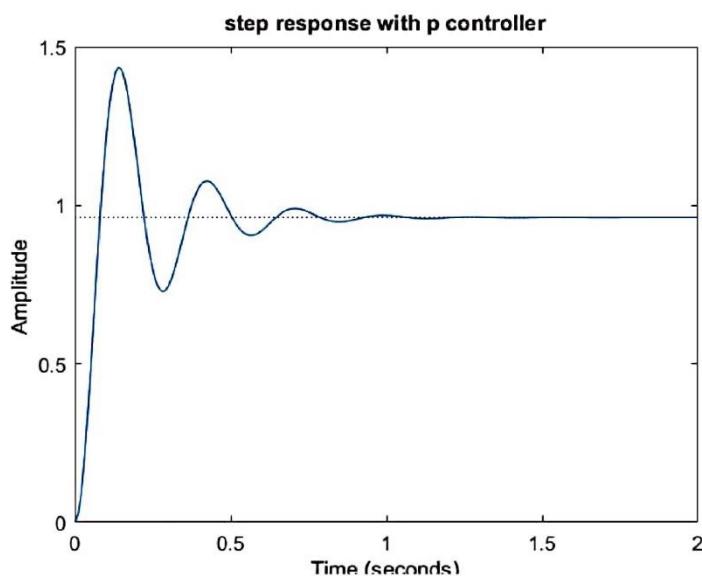
```
78 figure(8)
79 step(a,b);
80 hold on;
81 step(a1,b1);
82 hold on;
83 step(a2,b2);
84 hold on;
85 step(a3,b3);
86 hold on;
87 step(a4,b4);
88 hold on;
89 step(a5,b5);
90 hold on;
```



# $K_p=500$ :

## With P controller:

```
%% p-controller
kp=500;
C=pid(kp,0,0);
plant=C*G;
a=feedback(plant,1);
b = 0:0.01:2;
figure(2)
step(a,b)
title('step response with p controller');
```



```
Command Window
>> stepinfo(a)

ans =

    struct with fields:

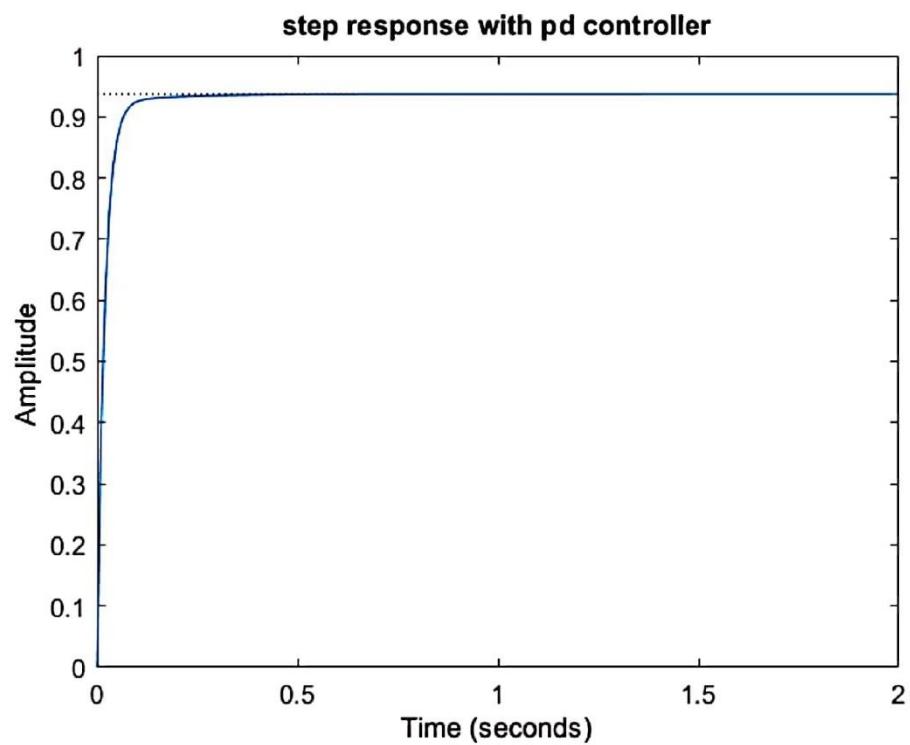
        RiseTime: 0.0540
        SettlingTime: 0.7443
        SettlingMin: 0.7278
        SettlingMax: 1.4350
        Overshoot: 49.2400
        Undershoot: 0
        Peak: 1.4350
        PeakTime: 0.1382

fx >> |
```

**K<sub>p</sub>=300, k<sub>d</sub>=50**

**PD controller:**

```
19 % pd-controller
20 kd=50;
21 kp=300;
22 C=pid(kp,0,kd);
23 plant=C*G;
24 a1=feedback(plant,1);
25 b1=0:0.01:2;
26 figure(3);
27 step(a1,b1)
28 title('step response with pd controller');
```



```

>> stepinfo(a1)

ans =

struct with fields:

    RiseTime: 0.0427
    SettlingTime: 0.0839
    SettlingMin: 0.8459
    SettlingMax: 0.9339
    Overshoot: 0
    Undershoot: 0
    Peak: 0.9339
    PeakTime: 0.2376

```

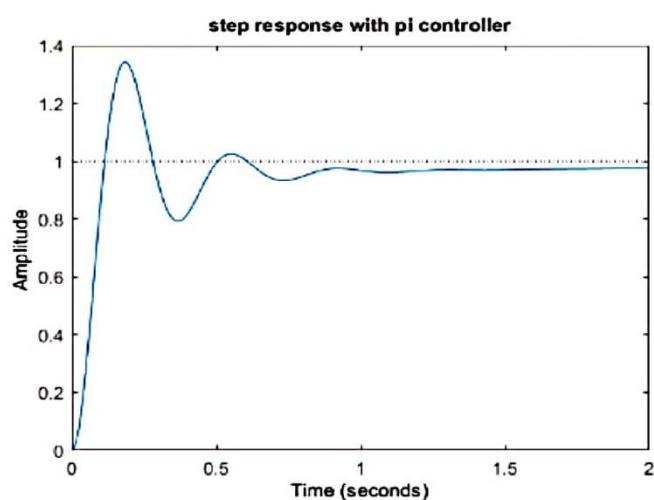
**K<sub>p</sub>=300,K<sub>i</sub>=120**

**PI controller:**

```

33 % pi-controller
34 kp=300;
35 ki=120;
36 C=pid(kp,ki,0);
37 plant=C*G;
38 a2=feedback(plant,1);
39 b2=0:0.01:2;
40 sys=(100*s+5)/(s^2+10*s+20);
41 [y,t]=step(sys);
42 serror=abs(1-y(end));
43 figure(4);
44 step(a2,b2)
45 title('step response with pi controller');

```



```

>> stepinfo(a2)

ans =

struct with fields:

    RiseTime: 0.0760
    settlingTime: 2.5328
    SettlingMin: 0.7925
    SettlingMax: 1.3432
    Overshoot: 34.3160
    Undershoot: 0
    Peak: 1.3432
    PeakTime: 0.1819

```

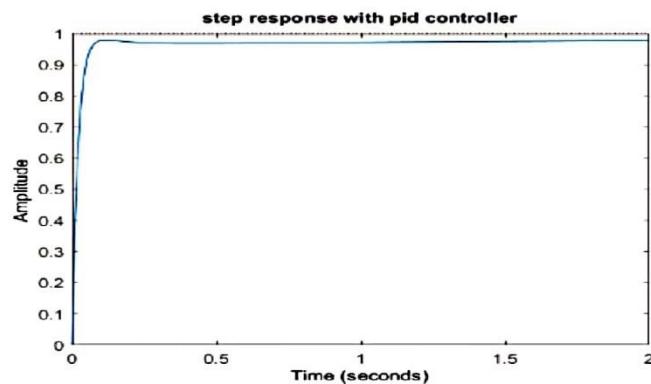
**Kp=500, Kd=50, Ki=120**

**PID controller:**

```

46
47      % pid-controller
48      kp=500;
49      kd=50;
50      ki=120;
51      C=pid(kp,ki,kd);
52      plant=C*G;
53      a3=feedback(plant,1);
54      b3=0:0.01:2;
55      figure(5)
56      step(a3,b3)
57      title('step response with pid controller');

```



```

>> stepinfo(a3)

ans =

struct with fields:

    RiseTime: 0.0449
    SettlingTime: NaN
    SettlingMin: 0.9017
    SettlingMax: 0.9790
    Overshoot: 0
    Undershoot: 0
    Peak: 0.9790
    PeakTime: 0.1152

```

Effect of each controller on the closed loop response are summarized below:

CL Response	Rise time	Overshoot	Settling time	Steady state error
$K_P =$				
$K_P = K_I =$				
$K_P = K_D =$				
$K_P = K_I = K_D =$				
$K_P = K_I = K_D =$ (Ziegler–Nichols)				

**Result:**

## Experiment No:05

- a) Evaluation of effect of pole location on stability
- b) Effect of loop gain of a negative feedback system on stability

**AIM:** Evaluation of effect of pole location and loop gain of a negative feedback system on stability

**Apparatus:** PC loaded with MATLAB

**Procedure:**

1. Open MATLAB
2. Create new script
3. Enter code run the program and obtain the required details
4. Observe the plots and note the values
5. Save and compare the observations

**Theoretical Calculation:**

**Program:**

**Effect of poles and zeroes on stability**

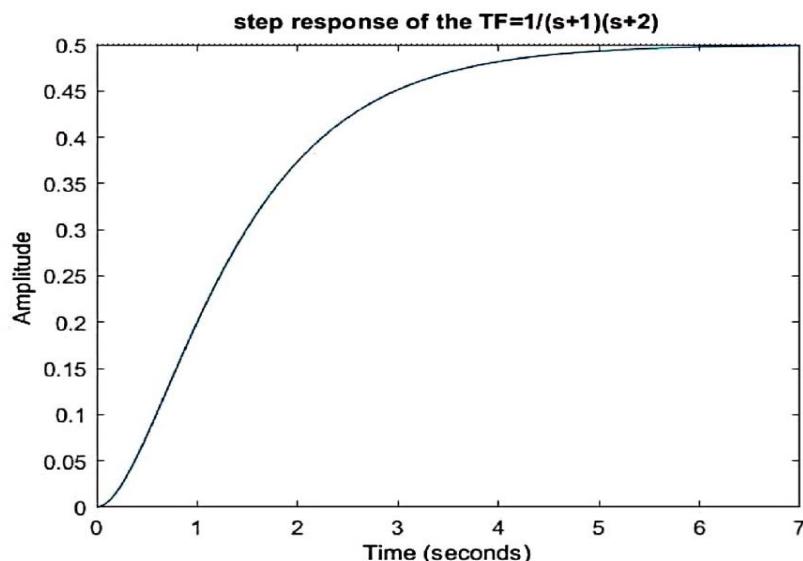
1.TF=1/(s+1)(s+2)

**Open Loop response of transfer function 1/(s+1)(s+2)**

```
p=[1];
q=[1 3 2];
G=tf(p,q);
figure(1)
step(G);
stepinfo(G)

ans = struct with fields:
    RiseTime: 2.5901
    SettlingTime: 4.6002
    SettlingMin: 0.4511
    SettlingMax: 0.4996
    Overshoot: 0
    Undershoot: 0
    Peak: 0.4996
    PeakTime: 7.7827

title('step response of the TF=1/(s+1)(s+2)');
```



**closed loop response for unity negative feedback system of the transfer function  $1/(s+1)(s+2)$**

```
p=[1];
q=[1 3 2];
G=tf(p,q);
t=feedback(G,1)
```

```
t =
```

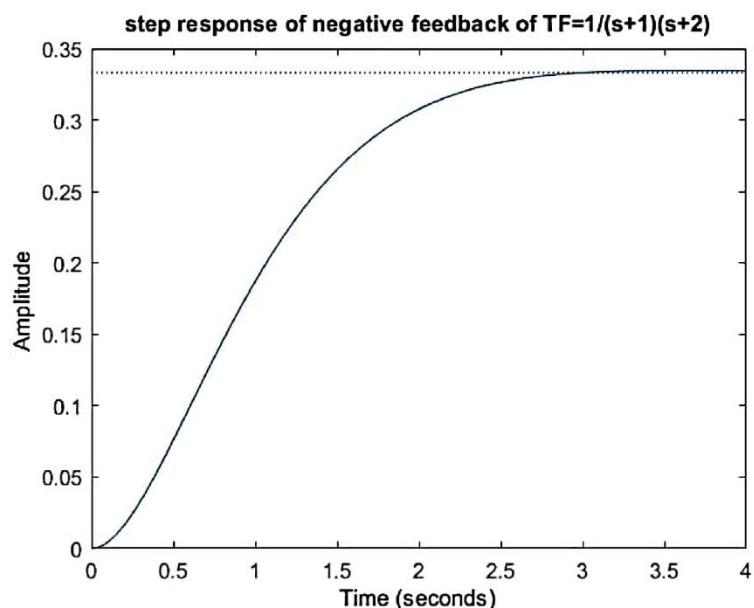
$$\frac{1}{s^2 + 3s + 3}$$

Continuous-time transfer function.

```
figure(2)
step(t);
stepinfo(t)
```

```
ans = struct with fields:
    RiseTime: 1.5787
    SettlingTime: 2.5089
    SettlingMin: 0.3017
    SettlingMax: 0.3348
    Overshoot: 0.4333
    Undershoot: 0
    Peak: 0.3348
    PeakTime: 3.6227
```

```
title('step response of negative feedback of TF=1/(s+1)(s+2)');
```



**closed loop response for unity positive feedback system of the transfer function  $1/(s+1)(s+2)$**

```
p=[1];
q=[1 3 2];
G=tf(p,q);
t=feedback(G,-1)
```

```
t =
```

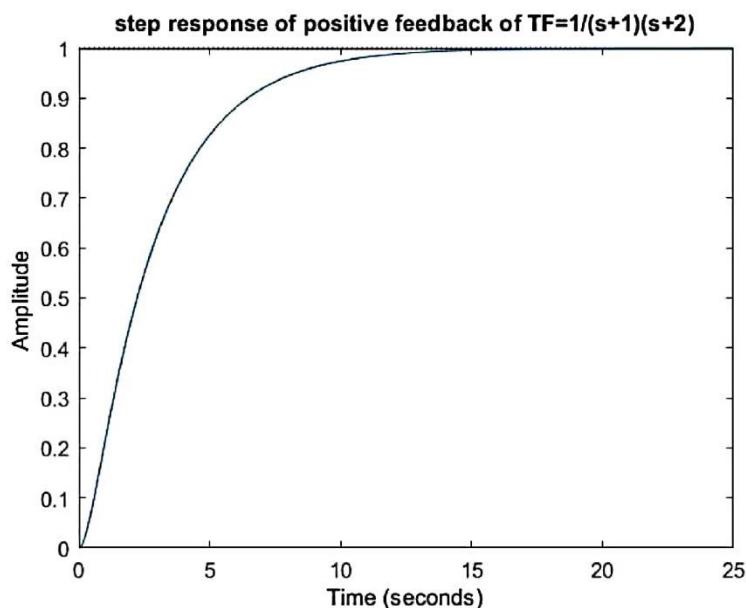
$$\frac{1}{s^2 + 3s + 1}$$

```
Continuous-time transfer function.
```

```
figure(3)
step(t);
stepinfo(t)
```

```
ans = struct with fields:
    RiseTime: 5.8584
    SettlingTime: 10.6547
    SettlingMin: 0.9012
    SettlingMax: 0.9999
    Overshoot: 0
    Undershoot: 0
    Peak: 0.9999
    PeakTime: 25.9983
```

```
title('step response of positive feedback of TF=1/(s+1)(s+2)');
```

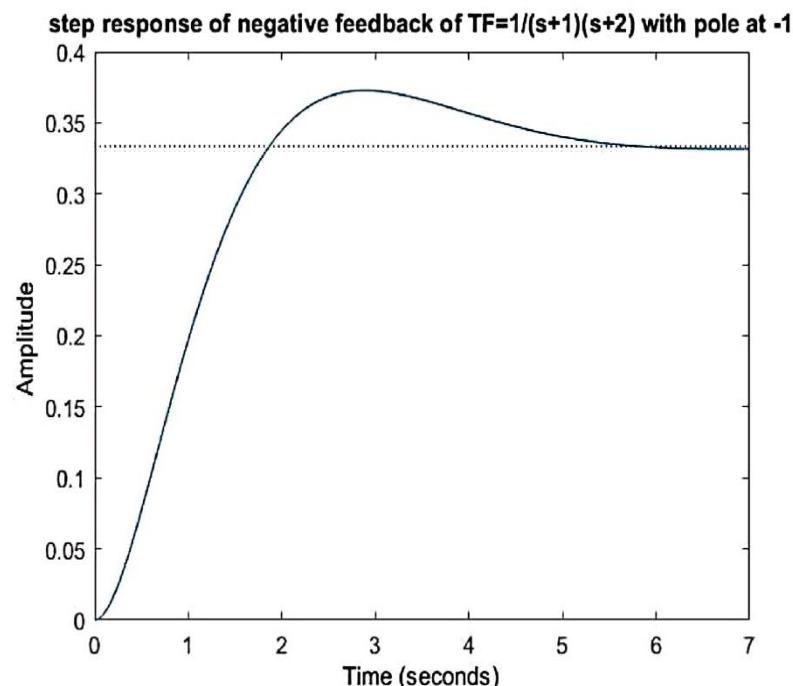


**closed loop response for the  $TF=1/(s+1)(s+2)$  with pole at -1 in negative feedback path**

```
p=[1 1];
q=[1 4 5 3];
G=tf(p,q);
figure(4)
step(G);
stepinfo(G)
```

```
ans = struct with fields:
    RiseTime: 1.2722
    SettlingTime: 5.0078
    SettlingMin: 0.3047
    SettlingMax: 0.3728
    Overshoot: 11.8450
    Undershoot: 0
    Peak: 0.3728
    PeakTime: 2.8764
```

```
title('step response of negative feedback of  $TF=1/(s+1)(s+2)$  with pole at -1');
```



**closed loop response for the  $TF=1/(s+1)(s+2)$  with pole at -1 in positive feedback path**

```
p=[1 1];
q=[1 4 5 1];
G=tf(p,q);
figure(5)
step(G);
stepinfo(G)
```

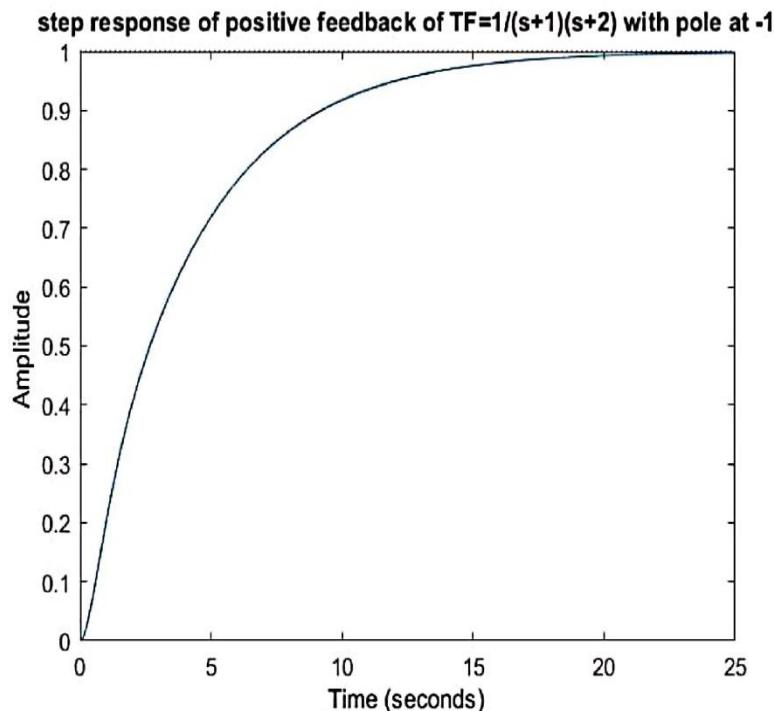
```
ans = struct with fields:
```

```

RiseTime: 8.6212
SettlingTime: 15.7786
SettlingMin: 0.9003
SettlingMax: 0.9988
Overshoot: 0
Undershoot: 0
Peak: 0.9988
PeakTime: 27.4234

```

```
title('step response of positive feedback of TF=1/(s+1)(s+2) with pole at -1');
```



### **closed loop response for the $TF=1/(s+1)(s+2)$ with zero at -1 in negative feedback path**

```

p=[1];
q=[1 4 3];
G=tf(p,q);
figure(6)
step(G);
stepinfo(G)

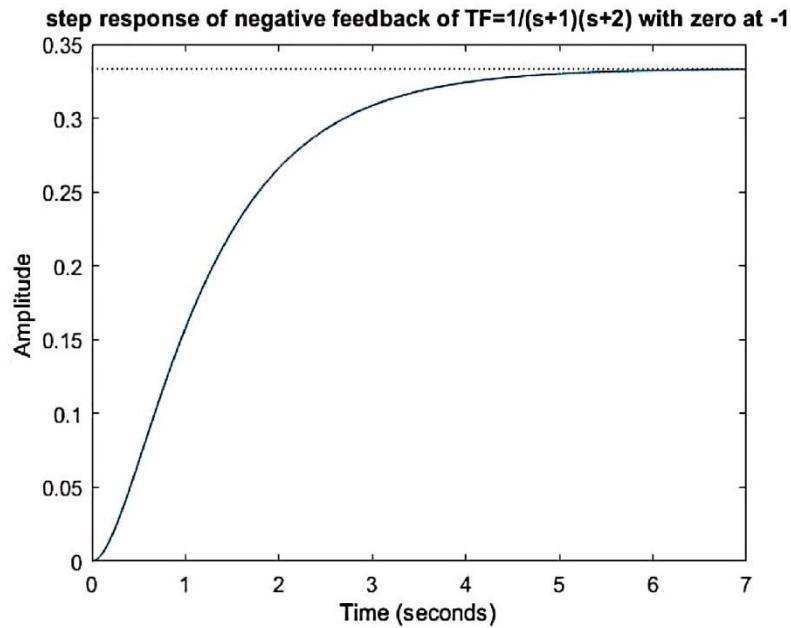
```

```

ans = struct with fields:
    RiseTime: 2.3911
    SettlingTime: 4.3175
    SettlingMin: 0.3008
    SettlingMax: 0.3332
    Overshoot: 0
    Undershoot: 0
    Peak: 0.3332
    PeakTime: 7.9516

```

```
title('step response of negative feedback of TF=1/(s+1)(s+2) with zero at -1');
```

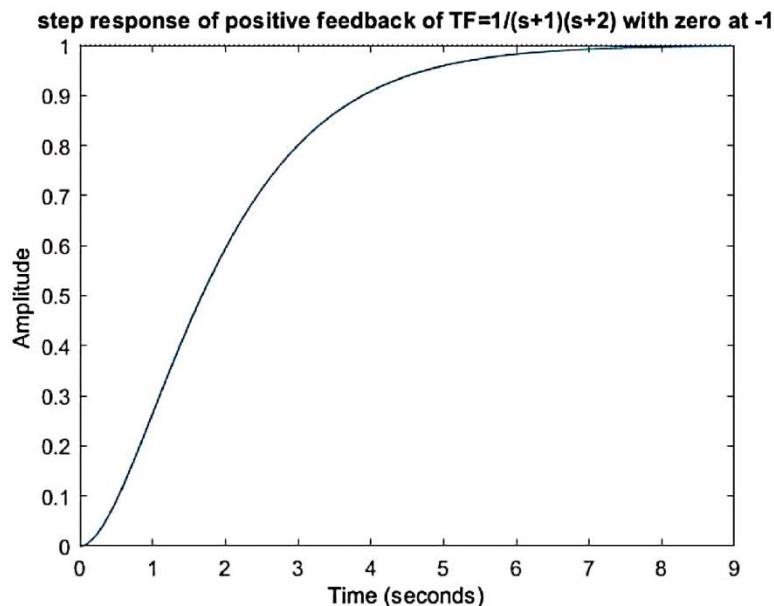


**closed loop response for the  $TF=1/(s+1)(s+2)$  with zero at -1 in positive feedback path**

```
p=[1];
q=[1 2 1];
G=tf(p,q);
figure(7)
step(G);
stepinfo(G)
```

```
ans = struct with fields:
    RiseTime: 3.3579
    SettlingTime: 5.8339
    SettlingMin: 0.9000
    SettlingMax: 0.9994
    Overshoot: 0
    Undershoot: 0
    Peak: 0.9994
    PeakTime: 9.7900
```

```
title('step response of positive feedback of TF=1/(s+1)(s+2) with zero at -1');
```



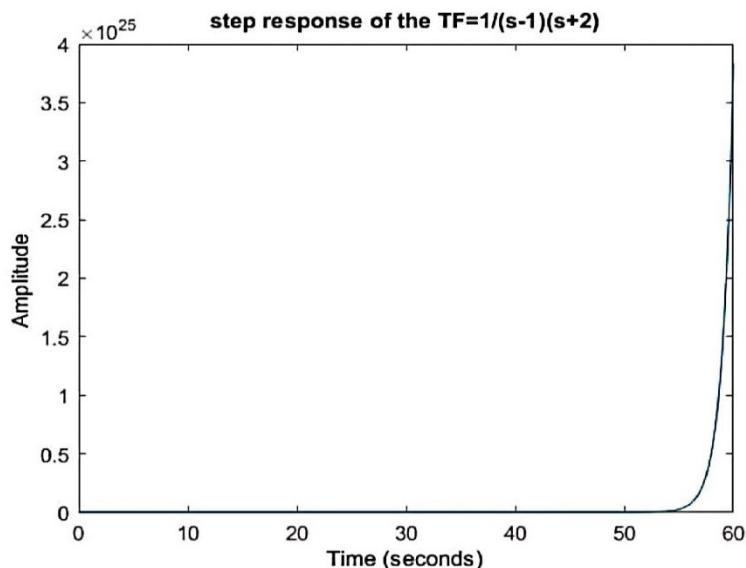
## 2.TF=1/(s-1)(s+2)

### Open Loop response of transfer function 1/(s-1)(s+2)

```
p=[1];
q=[1 1 -2];
G=tf(p,q);
figure(8)
step(G);
stepinfo(G)

ans = struct with fields:
    RiseTime: NaN
    SettlingTime: NaN
    SettlingMin: NaN
    SettlingMax: NaN
    Overshoot: NaN
    Undershoot: NaN
    Peak: Inf
    PeakTime: Inf

title('step response of the TF=1/(s-1)(s+2)');
```



### closed loop response for unity negative feedback system of the transfer function 1/(s-1)(s+2)

```
p=[1];
q=[1 1 -2];

G=tf(p,q);
t=feedback(G,1)

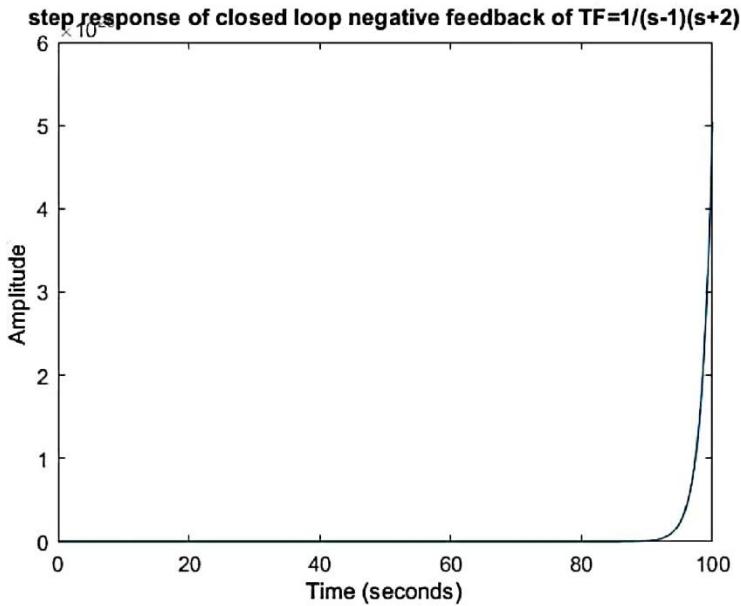
t =
1
-----
s^2 + s - 1

Continuous-time transfer function.

figure(9)
step(t);
stepinfo(t)

ans = struct with fields:
    RiseTime: NaN
    SettlingTime: NaN
    SettlingMin: NaN
    SettlingMax: NaN
    Overshoot: NaN
    Undershoot: NaN
    Peak: Inf
    PeakTime: Inf

title ('step response of closed loop negative feedback of TF=1/(s-1)(s+2)');
```



**closed loop response for unity positive feedback system of the transfer function  $1/(s-1)(s+2)$**

```
p=[1];
q=[1 1 -2];
G=tf(p,q);
t=feedback(G,-1)

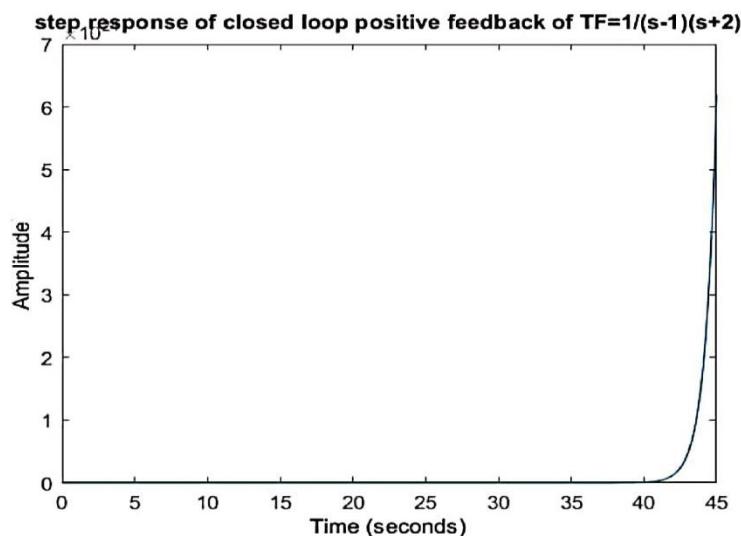
t =
1
-----
s^2 + s - 3

Continuous-time transfer function.

figure(10)
step(t);
stepinfo(t)

ans = struct with fields:
    RiseTime: NaN
    SettlingTime: NaN
    SettlingMin: NaN
    SettlingMax: NaN
    Overshoot: NaN
    Undershoot: NaN
    Peak: Inf
    PeakTime: Inf

title('step response of closed loop positive feedback of TF=1/(s-1)(s+2)');
```

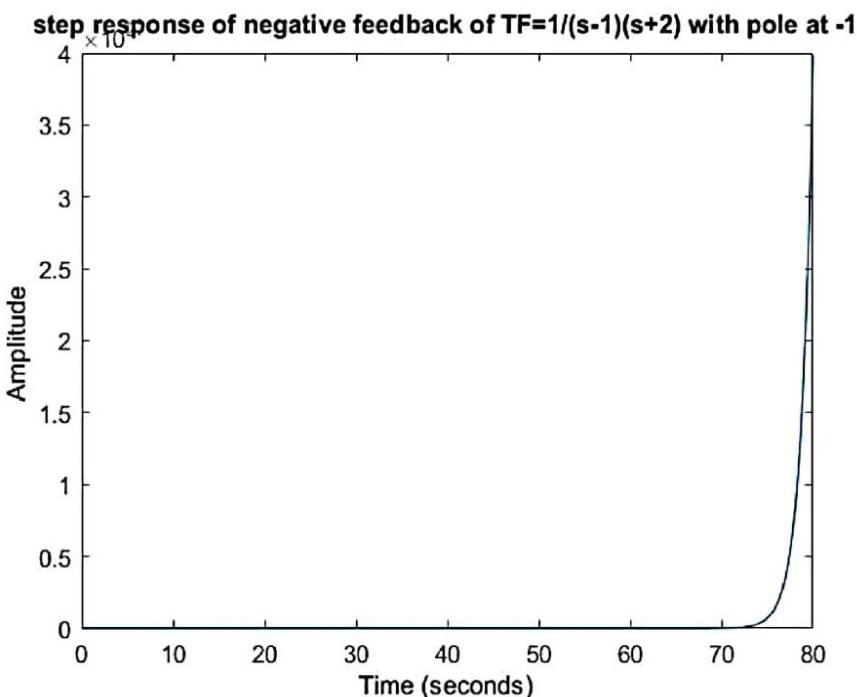


**closed loop response for the  $TF=1/(s-1)(s+2)$  with pole at -1 in negative feedback path**

```
p=[1 1];
q=[1 2 -1 -1];
G=tf(p,q);
figure(11)
step(G);
stepinfo(G)
```

```
ans = struct with fields:
    RiseTime: NaN
    SettlingTime: NaN
    SettlingMin: NaN
    SettlingMax: NaN
    Overshoot: NaN
    Undershoot: NaN
    Peak: Inf
    PeakTime: Inf
```

```
title('step response of negative feedback of  $TF=1/(s-1)(s+2)$  with pole at -1');
```



**closed loop response for the  $TF=1/(s-1)(s+2)$  with pole at -1 in positive feedback path**

```
p=[1 1];
q=[1 2 -1 -3];
G=tf(p,q);
figure(12)
step(G);
stepinfo(G)
```

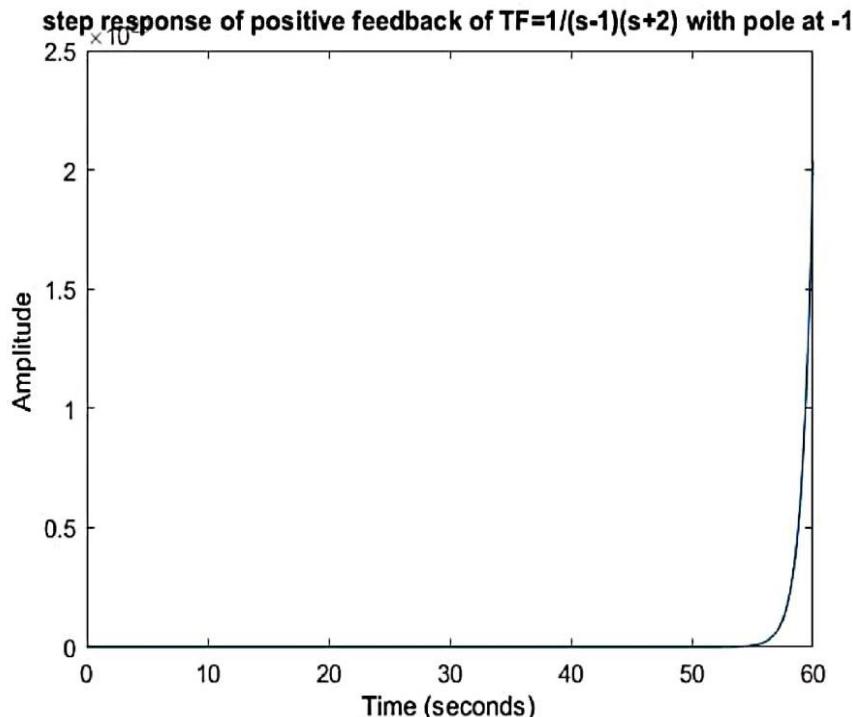
```
ans = struct with fields:
```

```

RiseTime: NaN
SettlingTime: NaN
SettlingMin: NaN
SettlingMax: NaN
Overshoot: NaN
Undershoot: NaN
Peak: Inf
PeakTime: Inf

title('step response of positive feedback of TF=1/(s-1)(s+2) with pole at -1');

```



### **closed loop response for the $TF=1/(s-1)(s+2)$ with zero at -1 in negative feedback path**

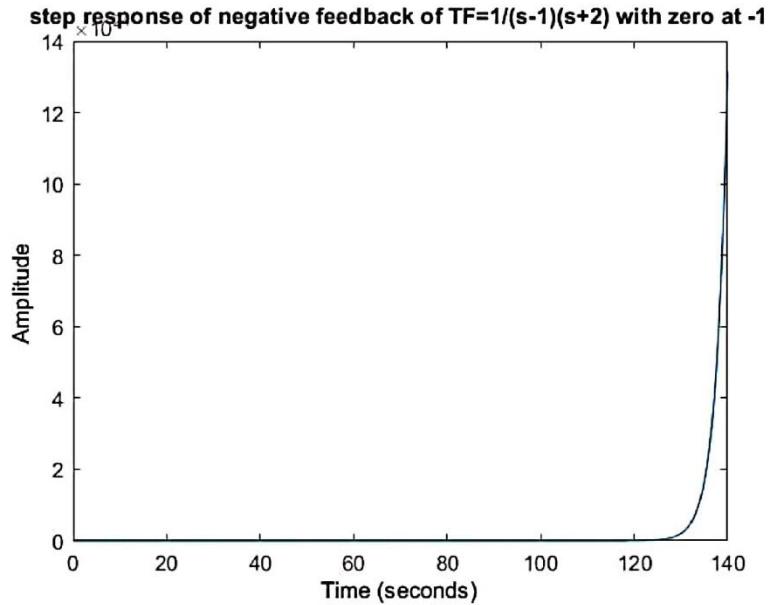
```

p=[1];
q=[1 2 -1];
G=tf(p,q);
figure(13)
step(G);
stepinfo(G)

ans = struct with fields:
    RiseTime: NaN
    SettlingTime: NaN
    SettlingMin: NaN
    SettlingMax: NaN
    Overshoot: NaN
    Undershoot: NaN
    Peak: Inf
    PeakTime: Inf

```

```
title('step response of negative feedback of TF=1/(s-1)(s+2) with zero at -1');
```

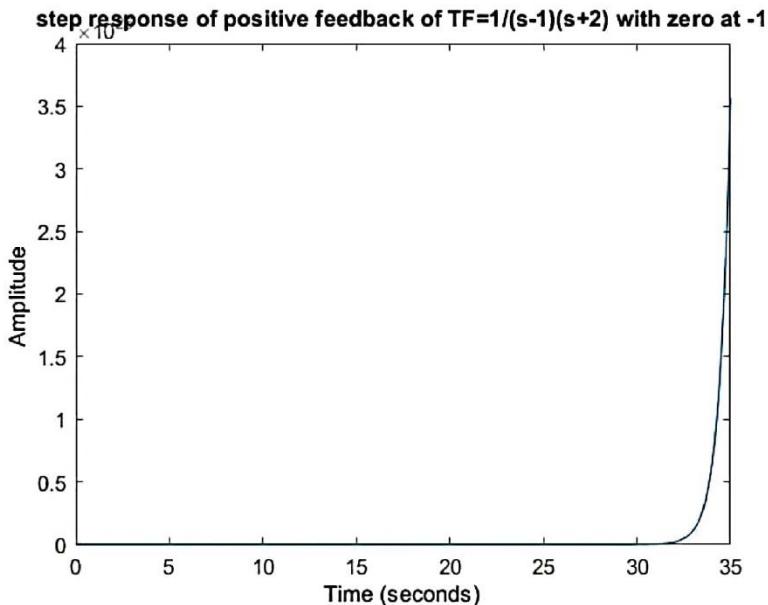


**closed loop response for the  $TF=1/(s-1)(s+2)$  with zero at -1 in positive feedback path**

```
p=[1];
q=[1 0 -3];
G=tf(p,q);
figure(14)
step(G);
stepinfo(G)
```

```
ans = struct with fields:
    RiseTime: NaN
    SettlingTime: NaN
    SettlingMin: NaN
    SettlingMax: NaN
    Overshoot: NaN
    Undershoot: NaN
    Peak: Inf
    PeakTime: Inf
```

```
title('step response of positive feedback of TF=1/(s-1)(s+2) with zero at -1');
```



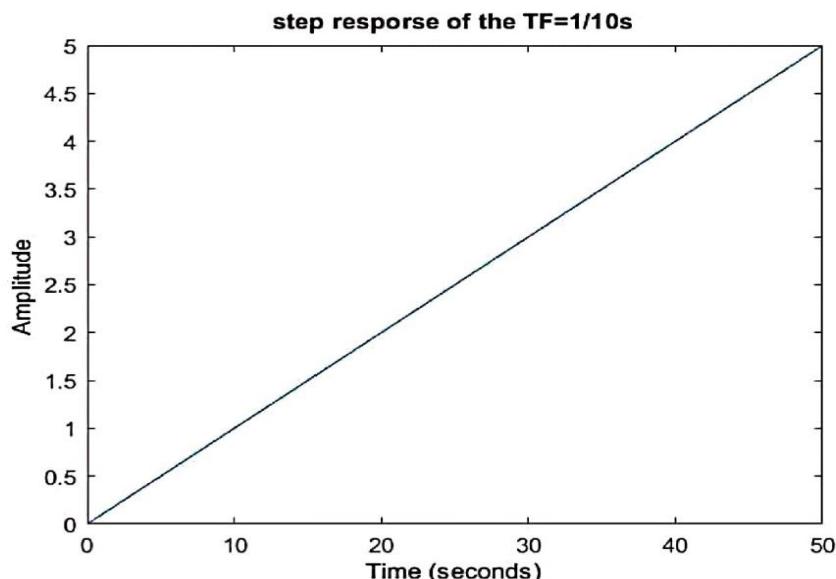
### 3.TF=1/10s

#### Open Loop response of transfer function 1/10s

```
p=[1];
q=[10 0];
G=tf(p,q);
figure(15)
step(G);
stepinfo(G)

ans = struct with fields:
    RiseTime: NaN
    SettlingTime: NaN
    SettlingMin: NaN
    SettlingMax: NaN
    Overshoot: NaN
    Undershoot: NaN
    Peak: Inf
    PeakTime: Inf

title('step response of the TF=1/10s');
```



#### closed loop response for unity negative feedback system of the transfer function 1/10s

```
p=[1];
q=[10 0];
G=tf(p,q);
t=feedback(G,1)

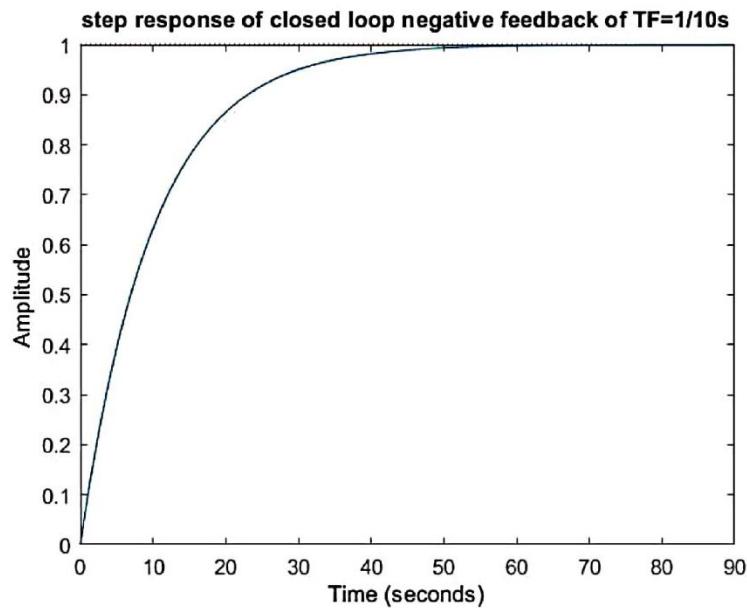
t =
 
 1
 -----
 10 s + 1

Continuous-time transfer function.

figure(16)
step(t);
stepinfo(t)

ans = struct with fields:
    RiseTime: 21.9701
    SettlingTime: 39.1207
    SettlingMin: 0.9045
    SettlingMax: 1.0000
    Overshoot: 0
    Undershoot: 0
    Peak: 1.0000
    PeakTime: 105.4584

title('step response of closed loop negative feedback of TF=1/10s');
```



**closed loop response for unity positive feedback system of the transfer function 1/10s**

```
p=[1];
q=[10 0];
G=tf(p,q);
t=feedback(G,-1)

t =

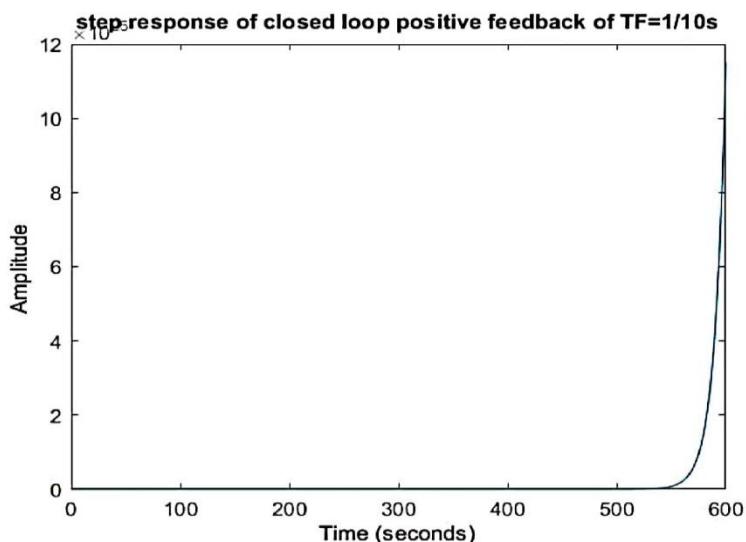
$$\frac{1}{10s - 1}$$


Continuous-time transfer function.

figure(17)
step(t);
stepinfo(t)

ans = struct with fields:
    RiseTime: NaN
    SettlingTime: NaN
    SettlingMin: NaN
    SettlingMax: NaN
    Overshoot: NaN
    Undershoot: NaN
    Peak: Inf
    PeakTime: Inf

title('step response of closed loop positive feedback of TF=1/10s');
```

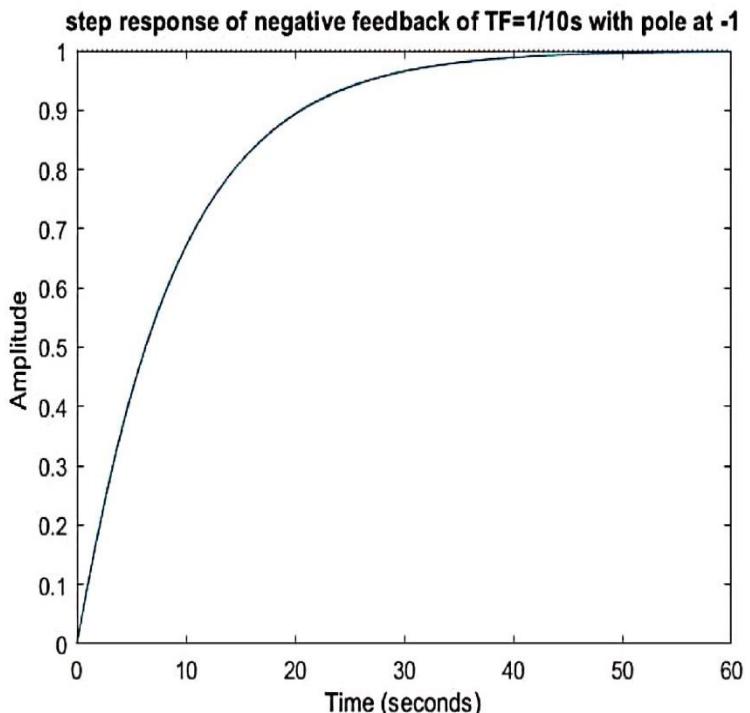


**closed loop response for the TF=1/10s with pole at -1 in negative feedback path**

```
p=[1 1];
q=[10 10 1];
G=tf(p,q);
figure(18)
step(G);
stepinfo(G)
```

```
ans = struct with fields:
    RiseTime: 19.5623
    SettlingTime: 34.8576
    SettlingMin: 0.9029
    SettlingMax: 0.9993
    Overshoot: 0
    Undershoot: 0
    Peak: 0.9993
    PeakTime: 64.9699
```

```
title('step response of negative feedback of TF=1/10s with pole at -1');
```



**closed loop response for the TF=1/10s with pole at -1 in positive feedback path**

```
p=[1 1];
q=[10 10 -1];
G=tf(p,q);
figure(19)
step(G);
stepinfo(G)
```

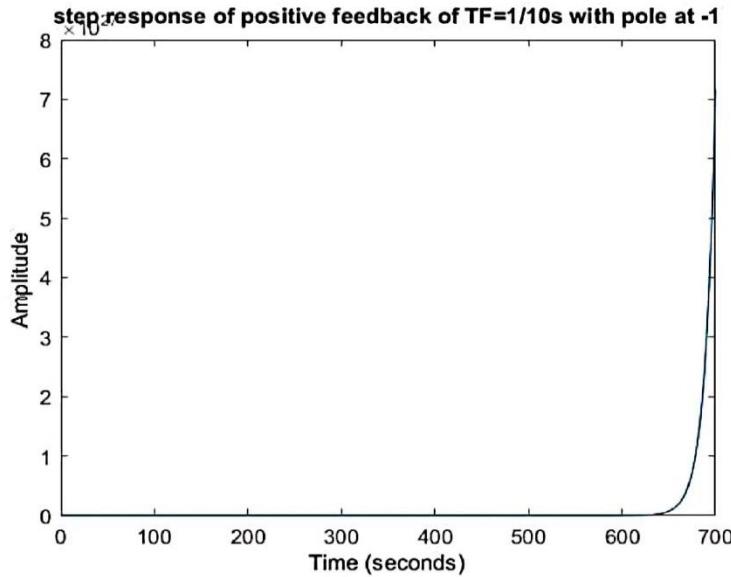
```
ans = struct with fields:
```

```

RiseTime: NaN
SettlingTime: NaN
SettlingMin: NaN
SettlingMax: NaN
Overshoot: NaN
Undershoot: NaN
Peak: Inf
PeakTime: Inf

title('step response of positive feedback of TF=1/10s with pole at -1');

```



**closed loop response for the TF=1/10s with zero at -1 in negative feedback path**

```

p=[1];
q=[11 1];
G=tf(p,q);
figure(20)
step(G);
stepinfo(G)

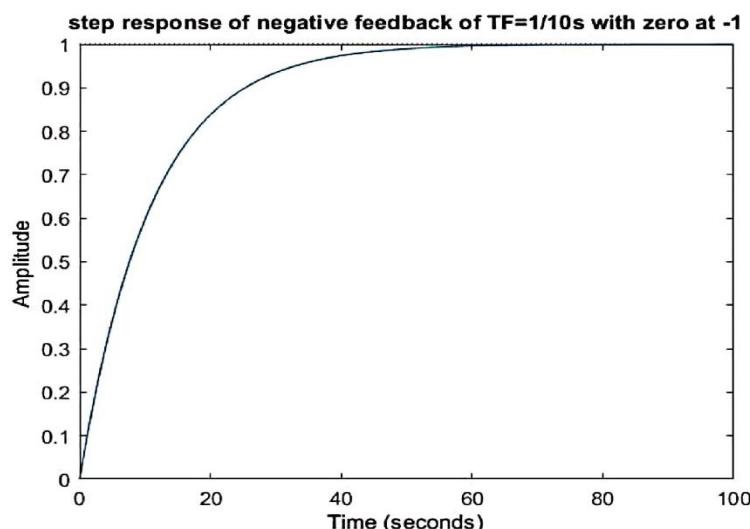
ans = struct with fields:
    RiseTime: 24.1671
    SettlingTime: 43.0328
    SettlingMin: 0.9045
    SettlingMax: 1.0000
    Overshoot: 0
    Undershoot: 0
    Peak: 1.0000
    PeakTime: 116.0042

```

```

title('step response of negative feedback of TF=1/10s with zero at -1');

```



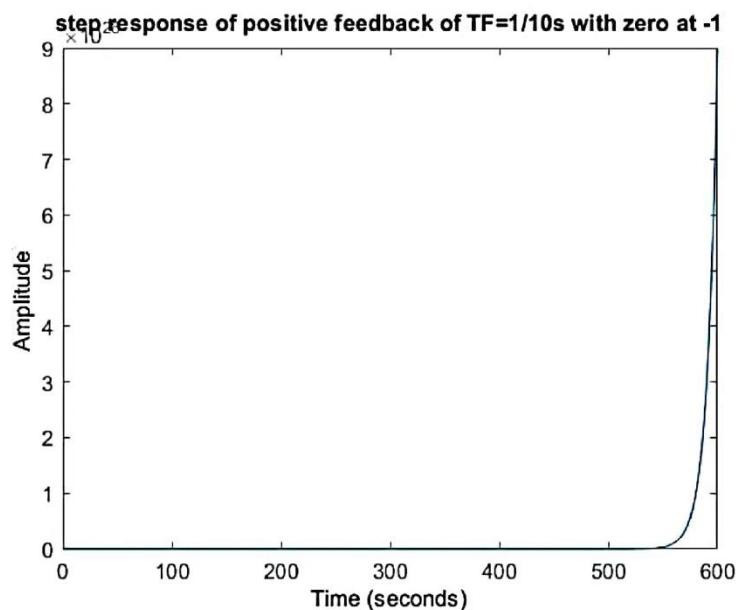
**closed loop response for the TF=1/10s with zero at -1 in positive feedback path**

```
p=[1];
q=[9 -1];
G=tf(p,q);
figure(21)
step(G);
stepinfo(G)
```

```
ans = struct with fields:
```

```
RiseTime: NaN
SettlingTime: NaN
SettlingMin: NaN
SettlingMax: NaN
Overshoot: NaN
Undershoot: NaN
Peak: Inf
PeakTime: Inf
```

```
title('step response of positive feedback of TF=1/10s with zero at -1');
```



**Result:**

## **Experiment No.06**

- a) **Effect of open loop and zeroes on root locus contour**
- b) **To estimate the effect of open loop gain on the transient response of closed loop system by using Root locus**
- c) **Comparative study of Bode, Nyquist and Root locus with respect to Stability**

**AIM:** To Find the Effect of open loop and zeroes on root locus contour

**Apparatus:** PC loaded with MATLAB

### **Theory:**

Root locus technique is used to find the roots of the characteristic's equation. This technique provides a graphical method of plotting the locus of the roots in the s plane as a given parameter usually gain is varied over the complete range of values. This method brings in to focus the complete dynamic response of the system. By using root locus method, the designer can predict the effects location of closed loop poles by varying the gain value or adding open loop poles and/or open loop zeroes. The closed loop poles are the roots of the characteristic equation.

Various terms related to root locus technique that we will use frequently in this article.

1. **Symmetry of Root Locus:** Root locus is symmetric about the x axis or the real axis.
2. **Characteristic Equation Related to Root Locus Technique:**  $1 + G(s)H(s) = 0$  is known as characteristic equation. Now on differentiating the characteristic equation and on equating  $dk/ds$  equals to zero, we can get break away points.
3. **Break away Points:** Suppose two root loci which start from pole and moves in opposite direction collide with each other such that after collision they start moving in different directions in the symmetrical way. Or the breakaway points at which multiple roots of the characteristic equation  $1 + G(s)H(s) = 0$  occur. The value of K is maximum at the points where the branches of root loci break away. Break away points may be real, imaginary or complex.
4. **Break in Point:** Condition of break in to be there on the plot is written below: Root locus must be present between two adjacent zeros on the real axis.
5. **Centre of Gravity:** It is also known centroid and is defined as the point on the plot from where all the asymptotes start. Mathematically, it is calculated by the difference of summation of poles and zeros in the transfer function when divided by the difference of total number of poles and total number of zeros. Centre of gravity is always real & it is denoted by  $\sigma_A$ . Where N is number of poles & M is number of zeros.

$$\sigma_A = \frac{(Sum\ of\ real\ parts\ of\ poles) - (Sum\ of\ real\ parts\ of\ zeros)}{N - M}$$

6. **Asymptotes of Root Loci:** Asymptote originates from the centre of gravity or centroid and goes to infinity at definite some angle. Asymptotes provide direction to the root locus when they depart break away points.
7. **Angle of Asymptotes:** Asymptotes makes some angle with the real axis and this angle can be calculated from  $Angle\ of\ asymptotes = \frac{(2p+1) \times 180}{N - M}$  the given formula,  
Where  $p = 0, 1, 2 \dots (N-M-1)$
8. **Angle of Arrival or Departure:** We calculate angle of departure when there exists complex poles in the system. Angle of departure can be calculated as  $180 - \{(sum\ of\ angles\ to\ a\ complex\ pole\ from\ the\ other\ poles) - (sum\ of\ angle\ to\ a\ complex\ pole\ from\ the\ zeros)\}$ .

9. Intersection of Root Locus with the Imaginary Axis: In order to find out the point of intersection root locus with imaginary axis, we have to use Routh Hurwitz criterion. First, we find the auxiliary equation then the corresponding value of K will give the value of the point of intersection.

### **Procedure:**

- 1.open the MATLAB and create a new file and open it
- 2.Run the code by entering it and by entering root locus
- 3.Repeat it by adding poles and zeroes
- 4.Observe the effect of pols and zeroes on root locus contour

Transfer fuction:  $\frac{36}{s^3+6s^2+11s+6}$

### **Theoretical Calculation:**

#### **Program:**

#### **To obtain Root Locus of a Transfer Function**

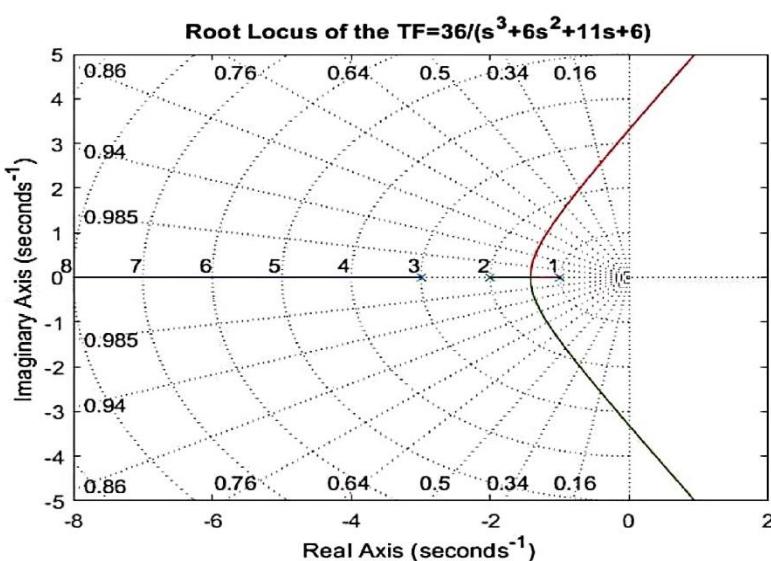
##### **Root Locus of the TF= $36/(s^3+6s^2+11s+6)$**

```
p=[36];
q=[1 6 11 6];
sys1=tf(p,q);
figure(1)
zpk(sys1)

ans =
 
      36
      -----
      (s+3) (s+2) (s+1)

Continuous-time zero/pole/gain model.

rlocus(sys1)
grid
title('Root Locus of the TF=36/(s^3+6s^2+11s+6)')
```



##### **Root Locus of the TF= $36/(s^3+6s^2+11s+6)$ with pole at +1**

```
p=[36];
q=[1 5 5 -5 -6];
sys2=tf(p,q);
figure(2)
```

```
zpk(sys2)
```

```
ans =
```

```
36
```

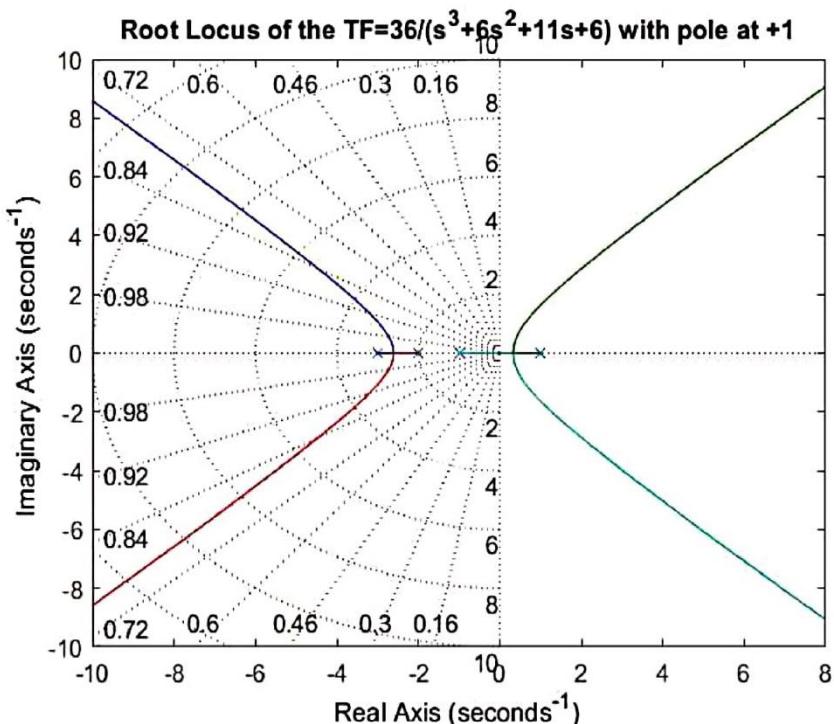
```
-----  
(s+3) (s+2) (s+1) (s-1)
```

```
Continuous-time zero/pole/gain model.
```

```
rlocus(sys2)
```

```
grid
```

```
title('Root Locus of the TF=36/(s^3+6s^2+11s+6) with pole at +1')
```



### Root Locus of the TF=36/(s<sup>3</sup>+6s<sup>2</sup>+11s+6) with pole at -1

```
p=[36];  
q=[1 7 17 17 6];  
sys3=tf(p,q);  
figure(3)  
zpk(sys3)
```

```
ans =
```

```
36
```

```
-----  
(s+3) (s+2) (s+1)^2
```

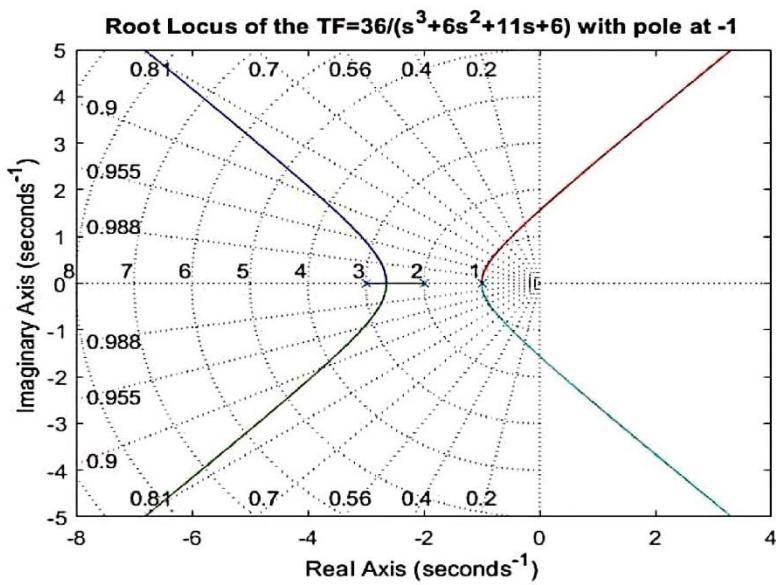
```
Continuous-time zero/pole/gain model.
```

```
rlocus(sys3)
```

```

grid
title('Root Locus of the TF=36/(s^3+6s^2+11s+6) with pole at -1')

```



### Root Locus of the TF=36/(s<sup>3</sup>+6s<sup>2</sup>+11s+6) with zero at +1

```

p=[36 -36];
q=[1 6 11 6];
sys4=tf(p,q);
figure(4)
zpk(sys4)

```

```

ans =

```

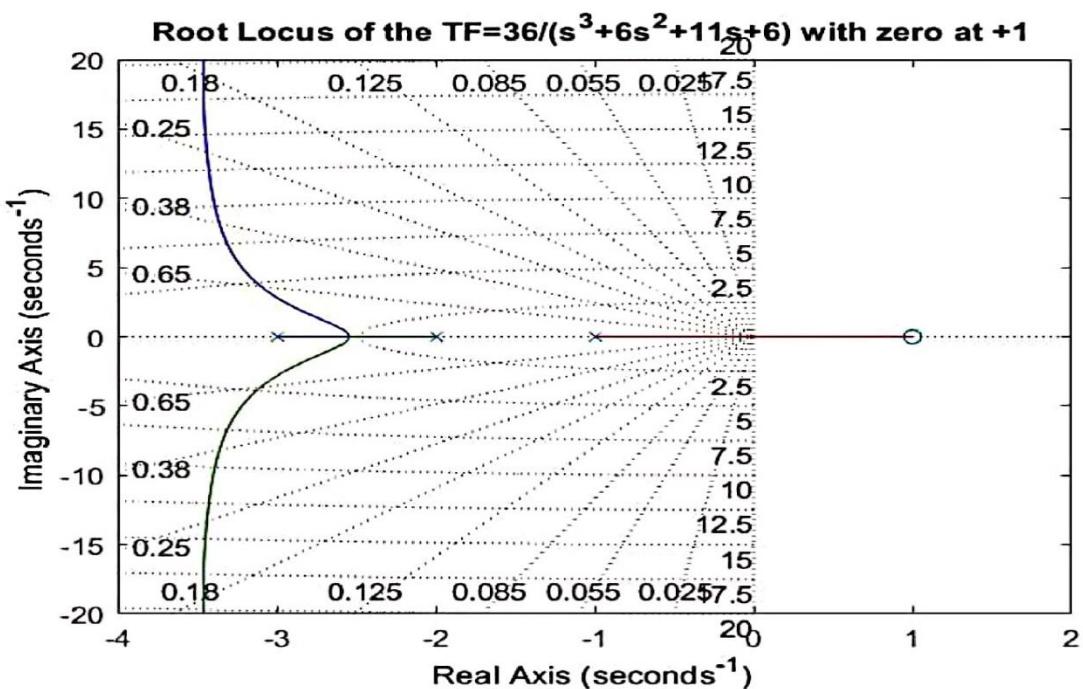
$$\frac{36 (s-1)}{(s+3) (s+2) (s+1)}$$

Continuous-time zero/pole/gain model.

```

rlocus(sys4)
grid
title('Root Locus of the TF=36/(s^3+6s^2+11s+6) with zero at +1')

```



## **Root Locus of the TF=36/(s^3+6s^2+11s+6) with zero at -1**

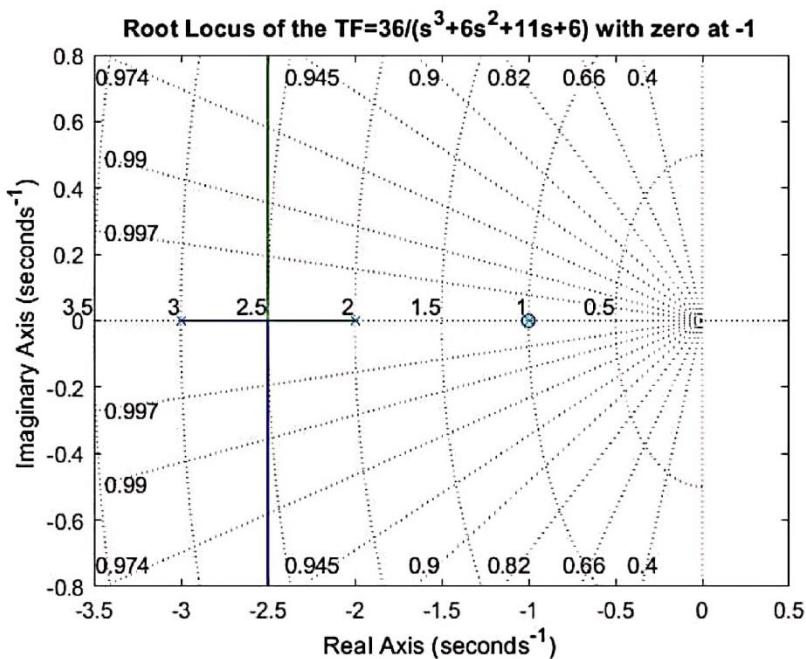
```
p=[36 36];
q=[1 6 11 6];
sys5=tf(p,q);
figure(5)
zpk(sys5)
```

ans =

$$\frac{36(s+1)}{(s+3)(s+2)(s+1)}$$

Continuous-time zero/pole/gain model.

```
rlocus(sys5)
grid
title('Root Locus of the TF=36/(s^3+6s^2+11s+6) with zero at -1')
```



### **Experiment No: 6(B)**

**To estimate the effect of open loop gain on the transient response of closed loop system by using Root locus.**

**AIM:** To estimate the effect of open loop gain on the transient response of closed loop system by using Root locus

**Apparatus:** PC loaded with MATLAB

#### **Procedure:**

1. Open MATLAB Command window
2. Click on new script file and enter the code
3. Obtain root locus plots for different values of K and compare them
4. Observe how the open loop gain effects the transient response of the closed loop system
5. Save the waveforms and exit the MATLAB window

# Effect of loop gain on closed loop system by using Root Locus

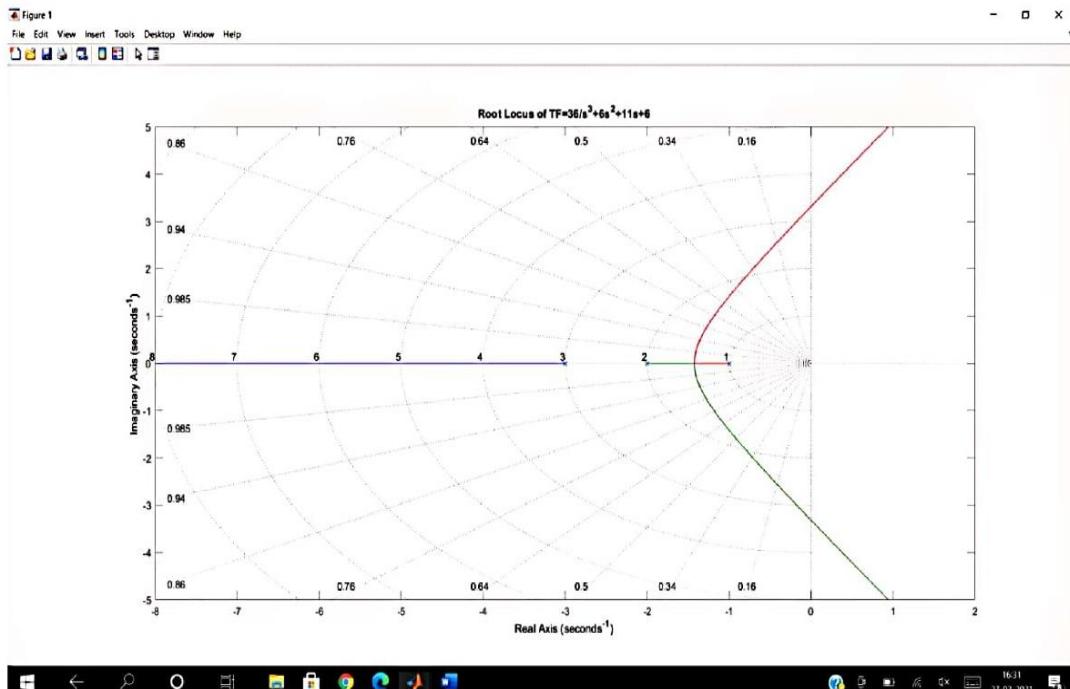
Transfer Function  $G(s)=k/s^3+6s^2+11s+6$

```
p=[36];
q=[1,6,11,6];
sys=tf(p,q);
figure(1);
zpk(sys);
rlocus(sys);
grid
title('Root Locus of TF=36/s^3+6s^2+11s+6');
```

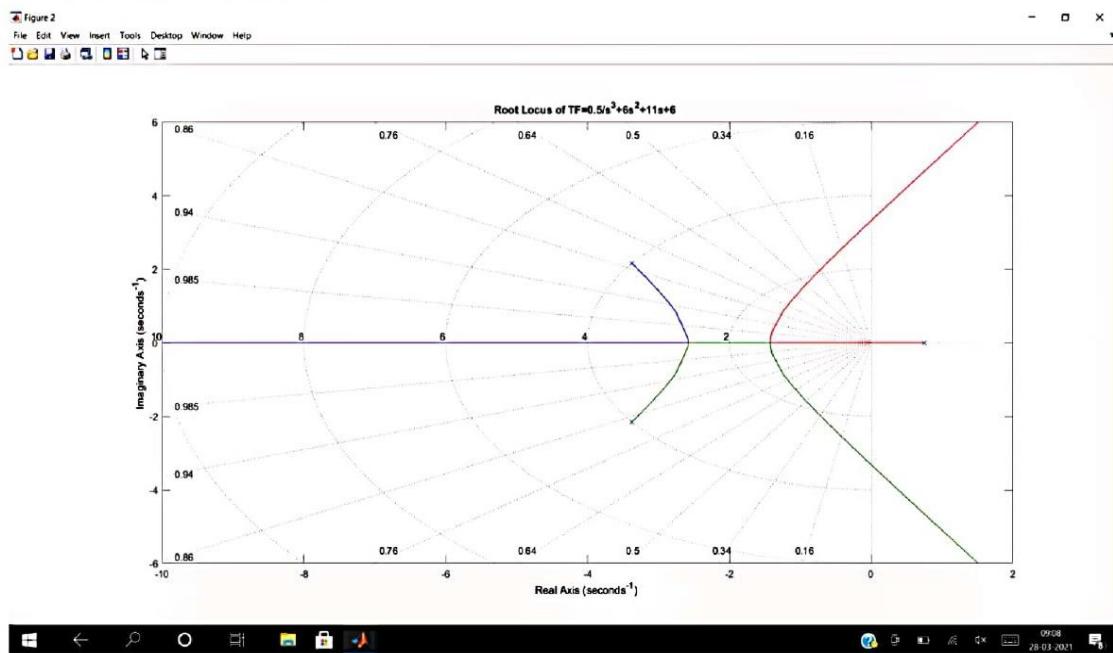
For Different Values of k

```
for i=1:4
    ki=input('enter k value');
    gi=feedback(sys*ki,-1);
    figure(i+1)
    zpk(gi);
    rlocus(gi);
    title('Root Locus of TF=36/s^3+6s^2+11s+6 for k=');
end
```

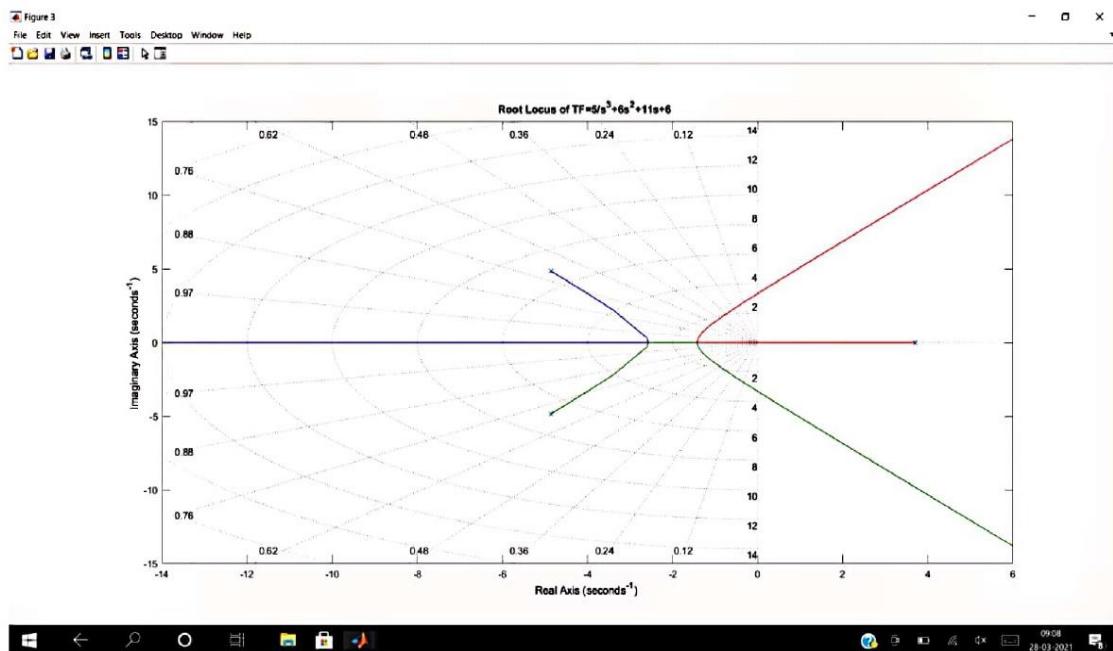
For  $k=1$ :



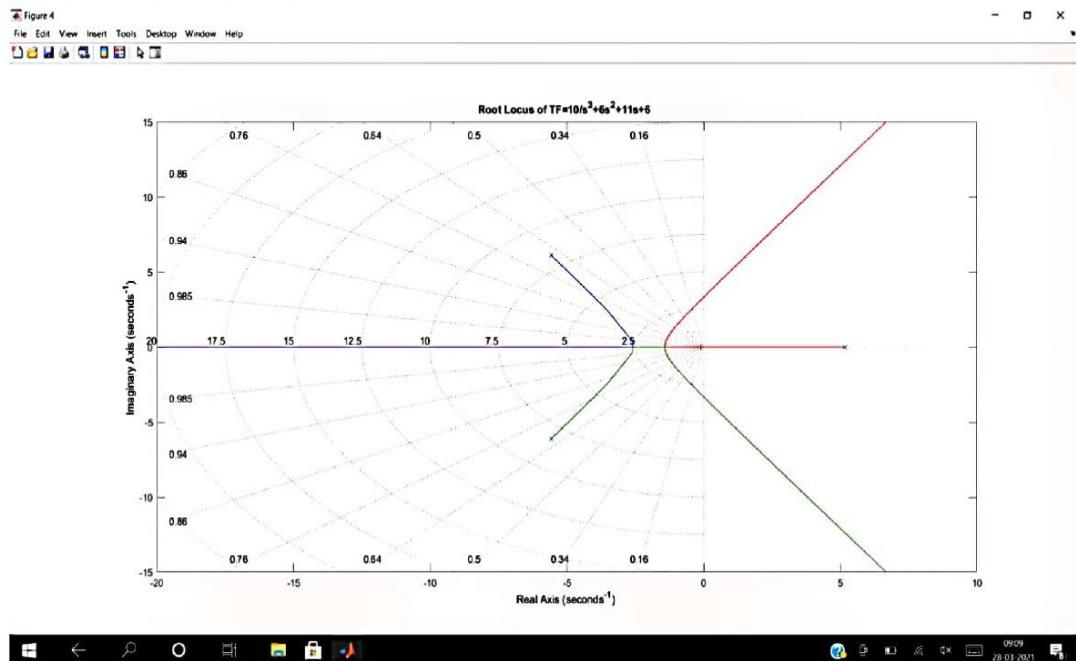
## For $k=0.5$ :



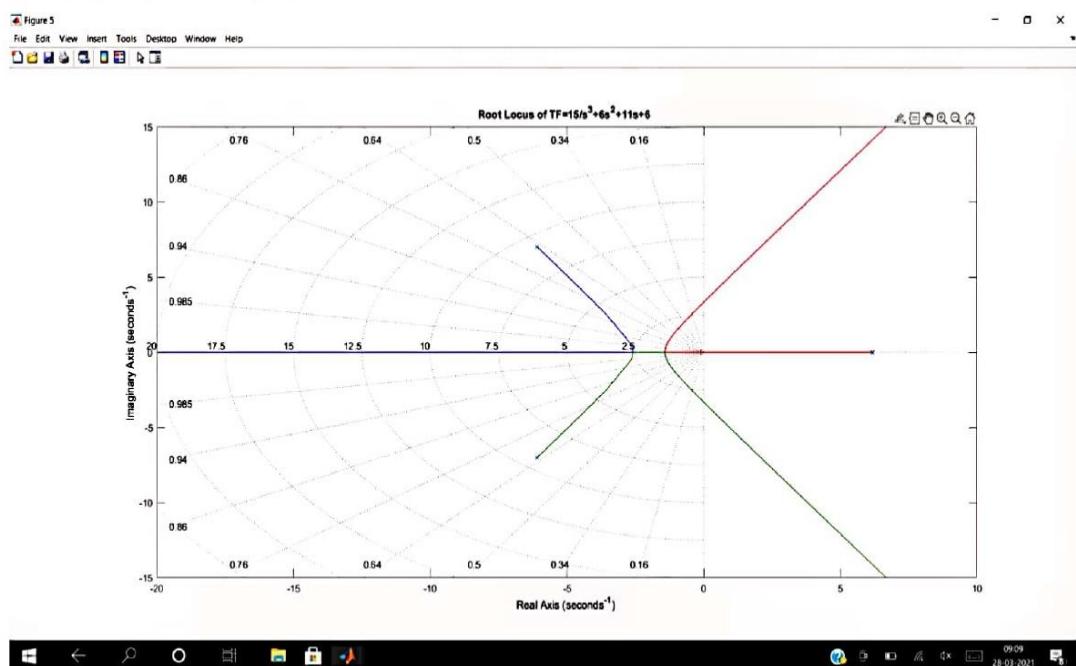
## For $k=5$ :



## For k=10:



## For k=15:



## **Experiment No: 6(C)**

### **Comparative study of Bode, Nyquist and Root locus with respect to Stability**

**AIM:** Comparative study of Bode, Nyquist and Root locus with respect to Stability

#### **Theory:**

One of the most useful representation of transfer function is a logarithmic plot which consists of two graphs, one giving the logarithm of  $[G(jw)]$  and the other phase angle of  $G(jw)$  both plotted against frequency in logarithmic scale. These plots are called bode plots. The main advantage of using bode diagram is that the multiplication of magnitudes can be converted into addition. Bode plots are a good alternative to the Nyquist plots.

#### **Frequency response specifications:**

1.Gain cross over frequency  $w_{gc}$  = It is the frequency at which magnitude of  $G(jw) H(jw)$  is unity i.e. 1.

2.Phase cross over frequency  $w_{pc}$  = It is the frequency at which phase angle of  $G(jw) H(jw)$  is  $-180^\circ$

3.Gain margin G.M = It is defined as the margin in gain allowable by which gain can be increased till system reaches on the verge of instability. Mathematically it is defined as the reciprocal of the magnitude of the  $G(jw) H(jw)$  measured at phase cross over frequency.

4.Phase margin P.M = Amount of additional phase lag which can be introduced in the system till system reaches on the verge of instability. Mathematically it can be defined as

$$P.M = 180^\circ + \angle G(jw)H(jw) \text{ at } w=w_{gc}$$

#### **Theoretical Calculation:**

#### **Procedure:**

1. Open MATLAB command window and open new script file
2. Enter the code for different transfer functions to plot bode plot.
3. Tabulate the observations gain margins, phase margin, and different observations for different plots.
4. Compare the stability between the different tables and exit from MATLAB

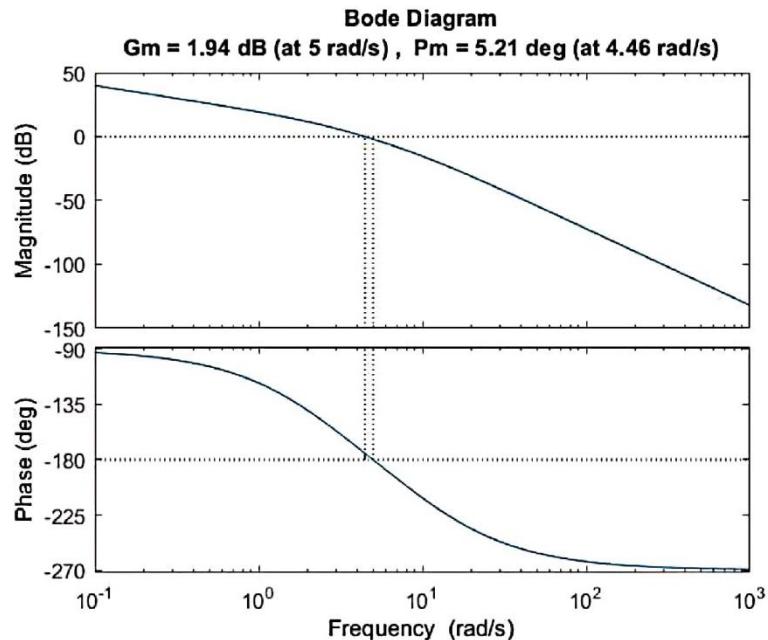
1. Transfer fuction:  $\frac{10}{s(1+0.4s)(1+0.1s)}$

2. Transfer fuction:  $\frac{36}{s^3 + 6s^2 + 11s + 6}$

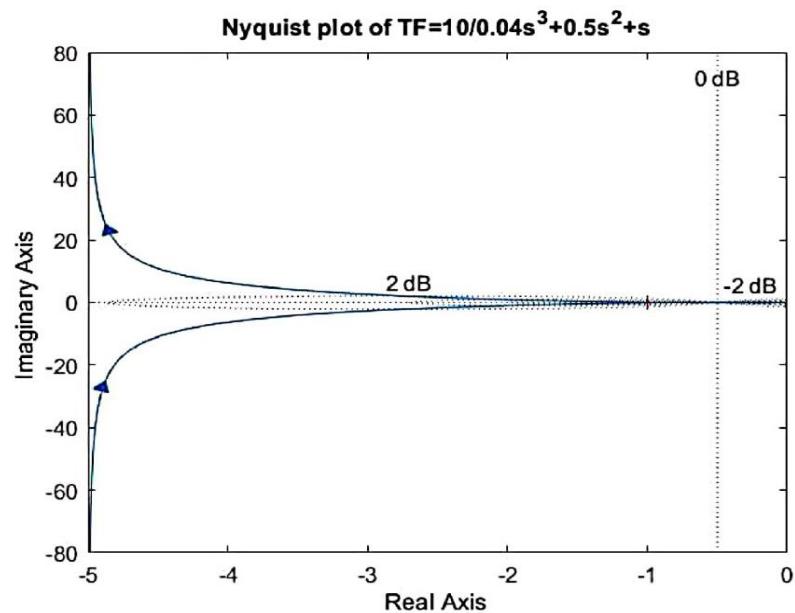
## Study of Bode,Nyquist and Root Locus on stability

1.TF= $10/0.04s^3+0.5s^2+s$

```
num=[10];
den=[0.04,0.5,1,0];
g1=tf(num,den);
figure(5)
margin(g1);
```



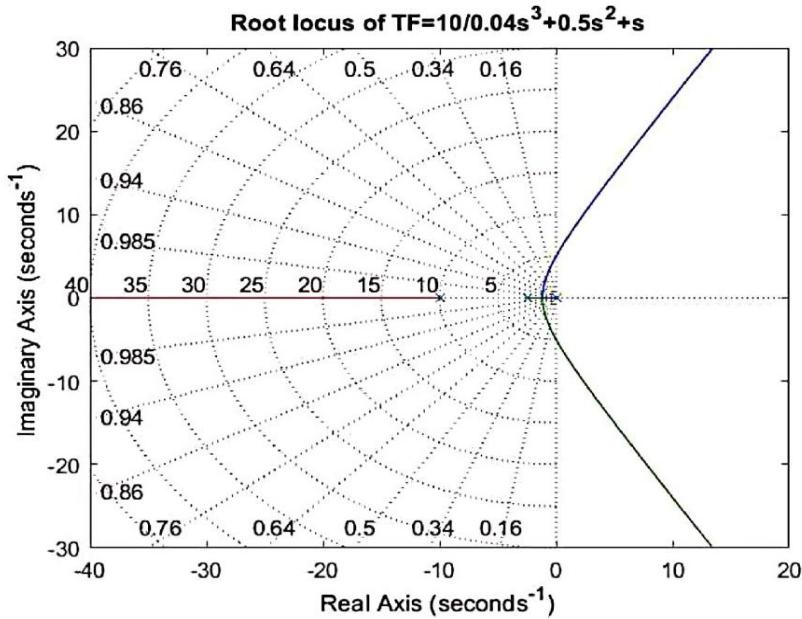
```
figure(6);
nyquist(g1);
grid
title('Nyquist plot of TF=10/0.04s^3+0.5s^2+s');
```



```

figure(7);
rlocus(g1);
grid
title('Root locus of TF=10/0.04s^3+0.5s^2+s');

```

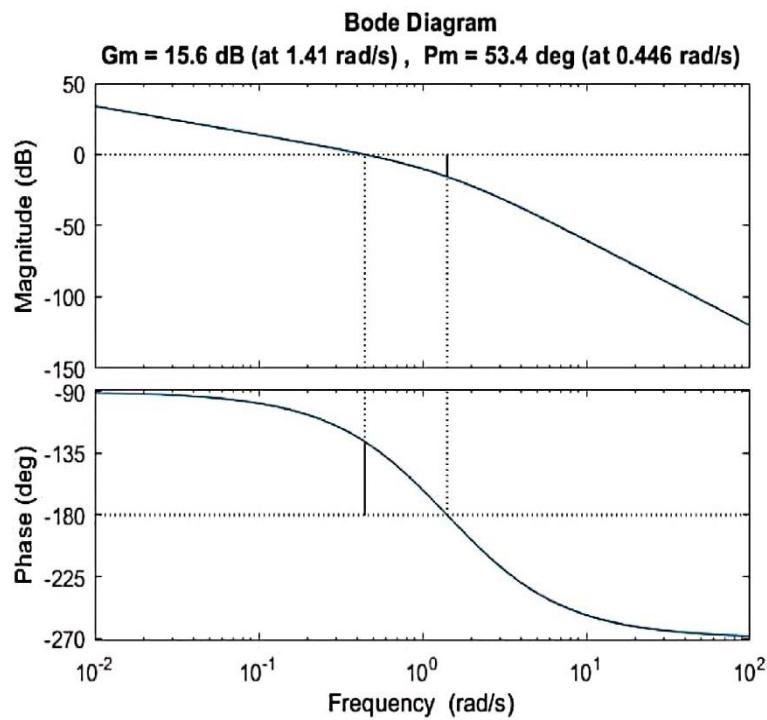


**2.TF=1/s(s+1)(s+2)**

```

num=[1];
den=[1 3 2 0];
g3=tf(num,den);
figure(11);
margin(g3);

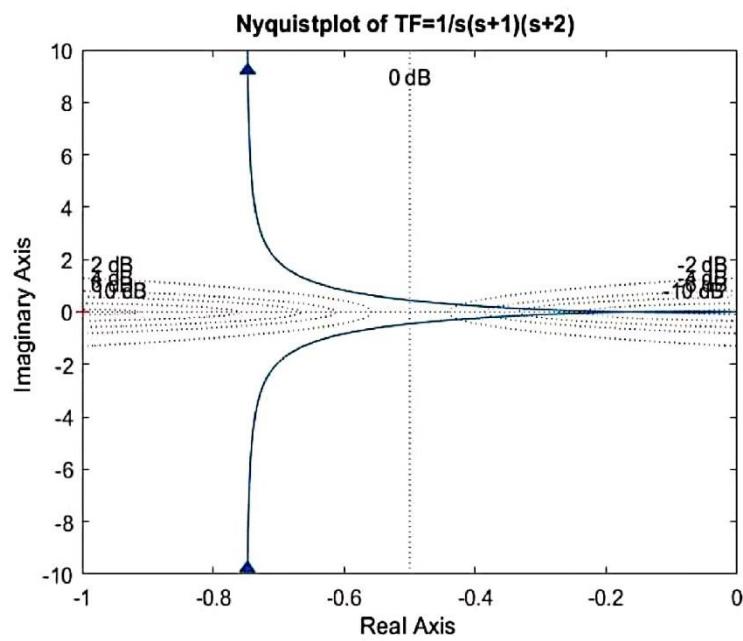
```



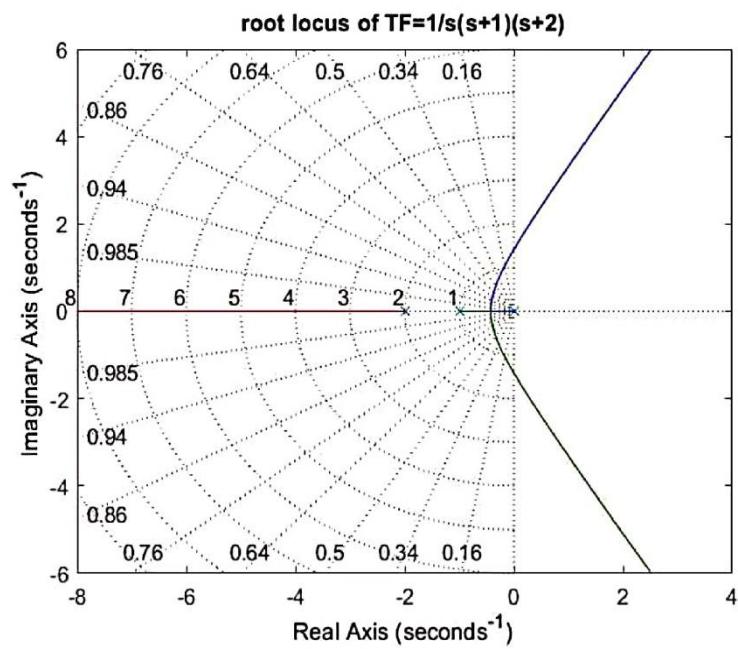
```

figure(12);
nyquist(g3);
grid
title('Nyquistplot of TF=1/s(s+1)(s+2)');

```

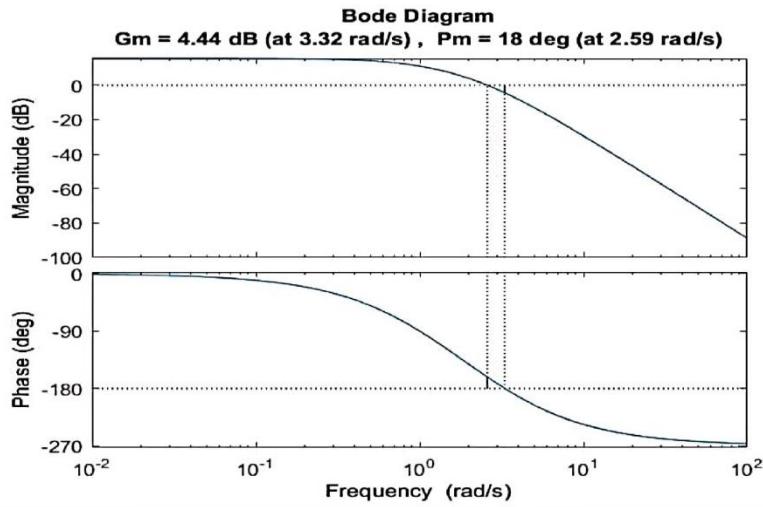


```
figure(13);
rlocus(g3);
grid
title('root locus of TF=1/s(s+1)(s+2)');
```

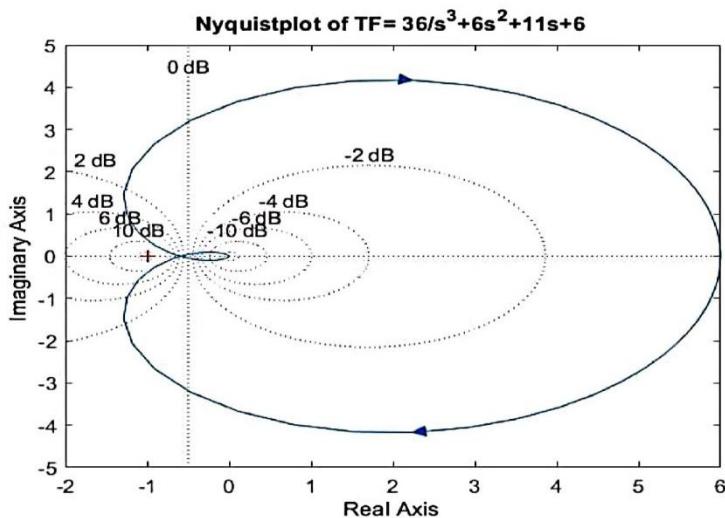


### 3.TF=36/s^3+6s^2+11s+6

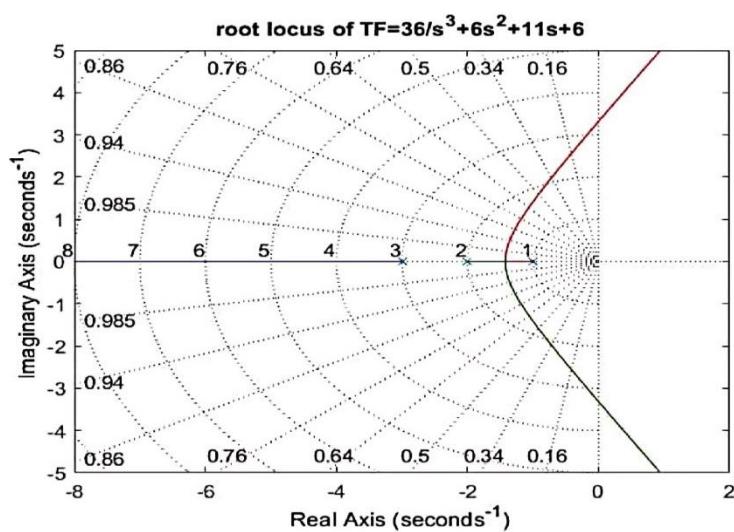
```
num=[ 36];
den=[1,6,11,6];
g2=tf(num,den);
figure(8);
margin(g2);
```



```
figure(9);
nyquist(g2);
grid;
title('Nyquistplot of TF= 36/s^3+6s^2+11s+6');
```



```
figure(10);
rlocus(g2);
grid;
title('root locus of TF=36/s^3+6s^2+11s+6');
```

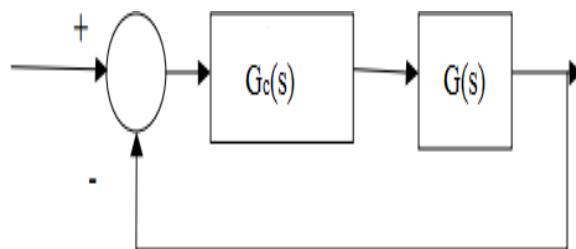


**Experiment No.07**  
**Design and study of lag, lead and Lag-lead compensator networks**

**AIM:** To Design and study of lag, lead and Lag-lead compensator networks.

**Apparatus:** PC with MATLAB software.

**Theory:**



**Procedure:**

1. Consider uncompensated system  $G(s)$ .
2. Design the lead, lag and lag-lead compensators for given specifications.
3. Plot the time response and frequency responses for compensated and uncompensated systems.
4. Compare the theoretical values with practical values.

### Design of Lead Compensator:

Design a lead compensator for a unity feedback system with an open-loop transfer function

$$G(s) = \frac{K}{s(s+1)}$$

For the specifications of  $K_v = 10 \text{ s}^{-1}$  and  $\phi = 35^\circ$

### Lead compensator

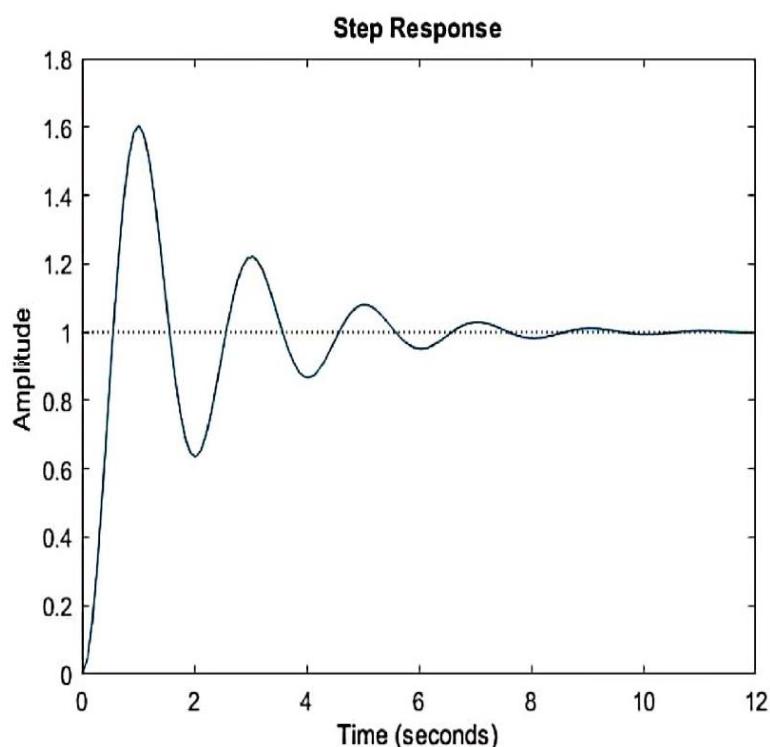
```
clc;
clear;
close all;

s=tf('s');
G_F=10/(s^2+s)
```

$$G_F = \frac{10}{s^2 + s}$$

Continuous-time transfer function.

```
figure(1)
step(feedback(G_F,1))
```



```
stepinfo(feedback(G_F,1))
```

```
ans = struct with fields:
    RiseTime: 0.3738
    SettlingTime: 7.3148
    SettlingMin: 0.6347
    SettlingMax: 1.6045
    Overshoot: 60.4530
```

```

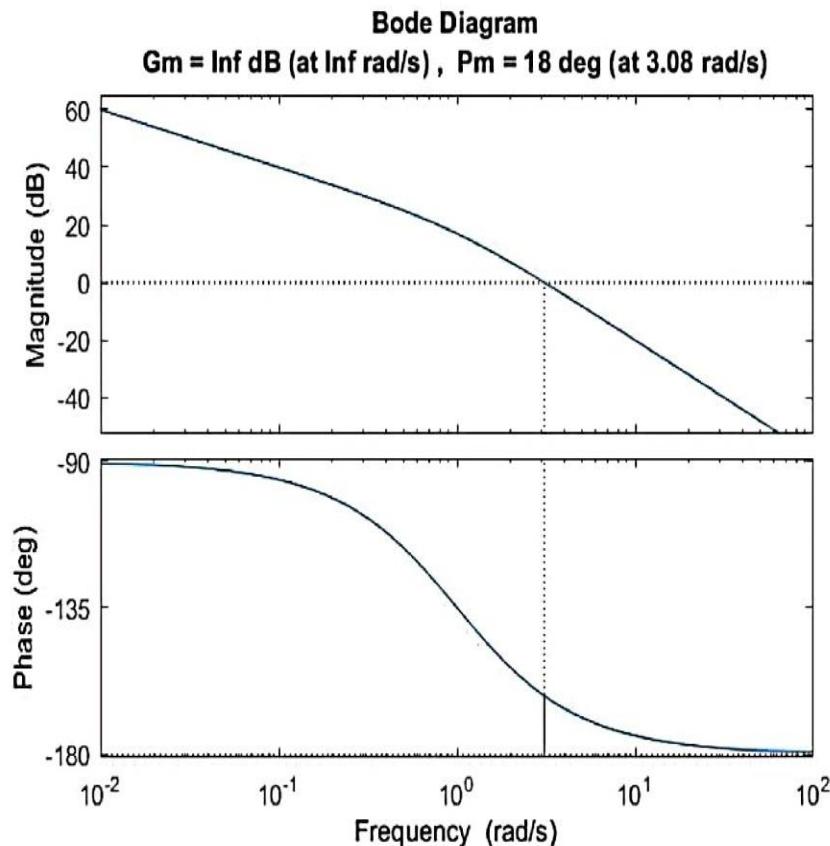
Undershoot: 0
Peak: 1.6045
PeakTime: 1.0131

```

```

figure(2)
margin(G_F)

```



```
[m_r,w_r]=getPeakGain(feedback(G_F,1))
```

```

m_r = 3.2026
w_r = 3.0818

```

$$G_C = (1 + 0.385s) / (1 + 0.162s)$$

G\_C =

$$\frac{0.385 s + 1}{0.162 s + 1}$$

Continuous-time transfer function.

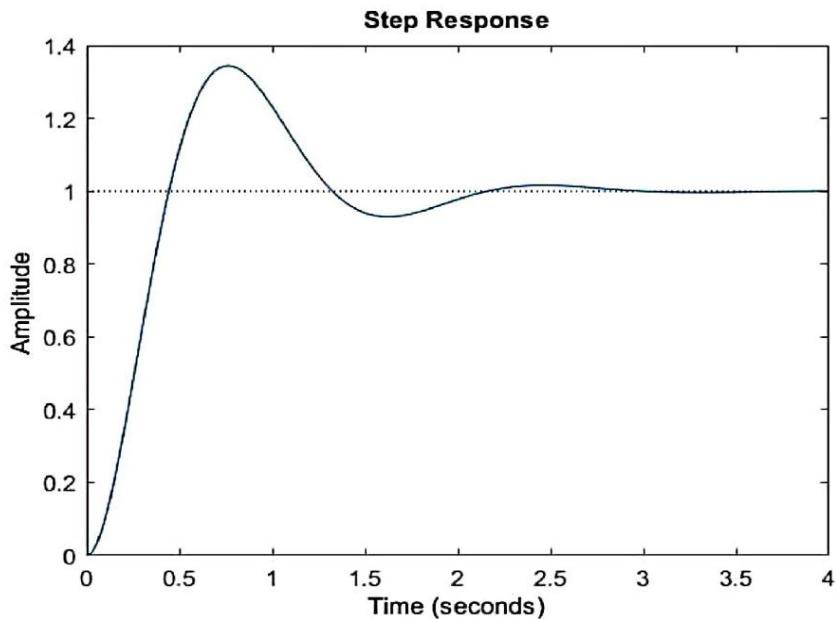
$$G = G_F * G_C$$

G =

$$\frac{3.85 s + 10}{0.162 s^3 + 1.162 s^2 + s}$$

Continuous-time transfer function.

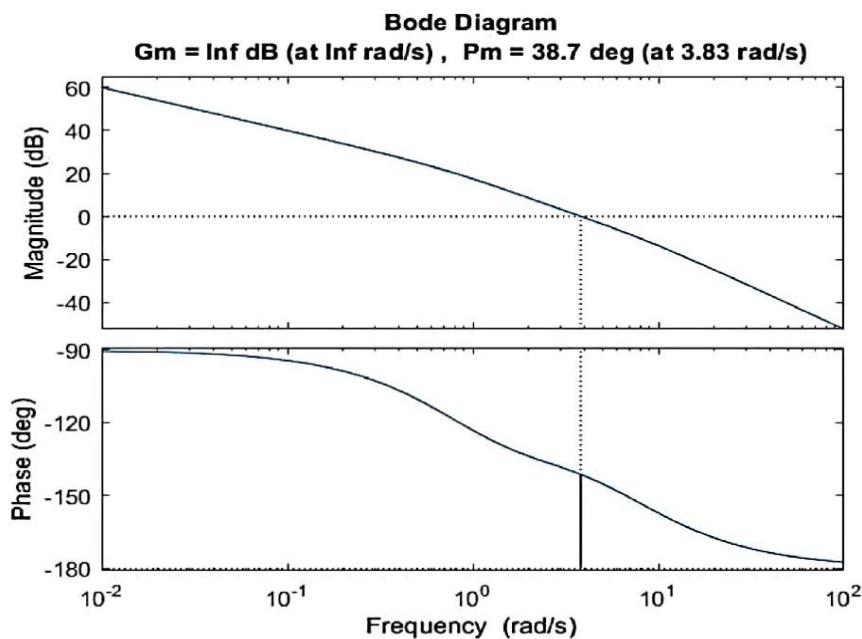
```
figure(3)
step(feedback(G,1))
```



```
stepinfo(feedback(G,1))
```

```
ans = struct with fields:
    RiseTime: 0.3020
    SettlingTime: 2.0151
    SettlingMin: 0.9164
    SettlingMax: 1.3445
    Overshoot: 34.4478
    Undershoot: 0
    Peak: 1.3445
    PeakTime: 0.7644
```

```
figure(4)
margin(G)
```



```
[m_r_cont,w_r_cont]=getPeakGain(feedback(G,1))
```

```
m_r_cont = 1.5418
w_r_cont = 3.4600
```

### Design of Lag Compensator:

Compensate the system with the open – loop transfer function

$$G(s) = \frac{K}{s(s+1)(s+5)}$$

To meet the following specifications:

- Damping Ratio  $\zeta = 0.3$
- Settling time  $t_s = 12s$
- Velocity error constant  $K_v \geq 8 s^{-1}$

### Lag compensator

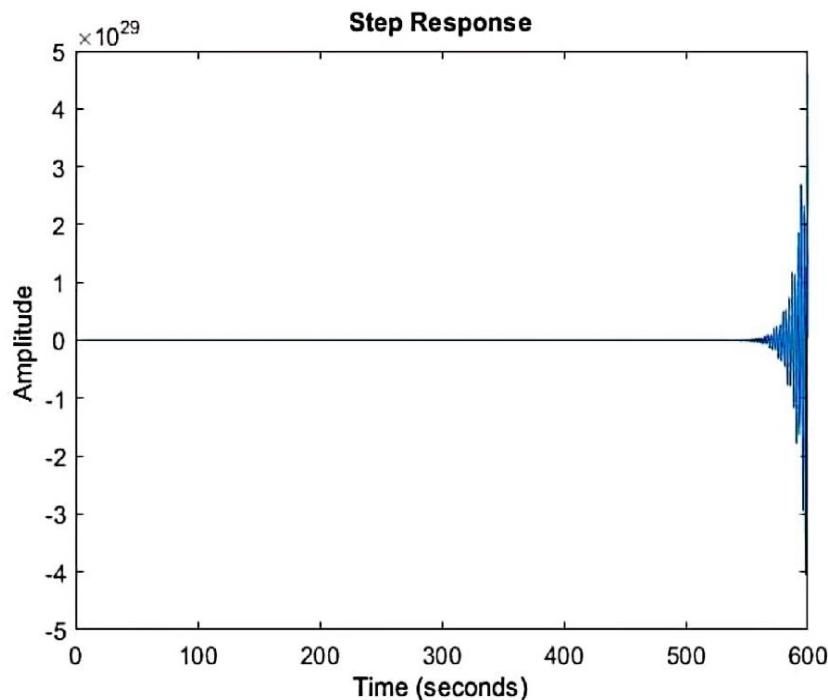
```
clc;
clear;
close all;

s=tf('s');
G_F=8/((s)*(s+1)*(1+0.2*s))
```

```
G_F =
8
-----
0.2 s^3 + 1.2 s^2 + s
```

Continuous-time transfer function.

```
figure(1)
step(feedback(G_F,1))
```

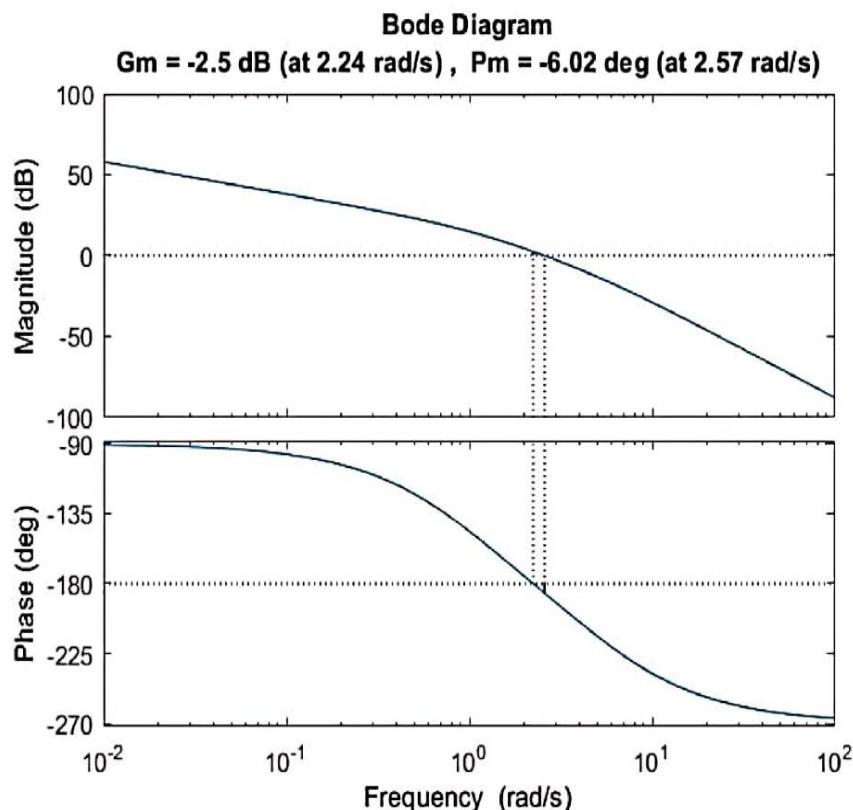


```
stepinfo(feedback(G_F,1))
```

```
ans = struct with fields:
    RiseTime: NaN
    SettlingTime: NaN
    SettlingMin: NaN
    SettlingMax: NaN
    Overshoot: NaN
```

```
Undershoot: NaN  
Peak: Inf  
PeakTime: Inf
```

```
figure(2)  
margin(G_F)
```



```
[m_r,w_r]=getPeakGain(feedback(G_F,1))
```

```
m_r = 10.2932  
w_r = 2.5284
```

```
G_C=(1+5*s)/(1+40*s)
```

```
G_C =  
5 s + 1  
-----  
40 s + 1
```

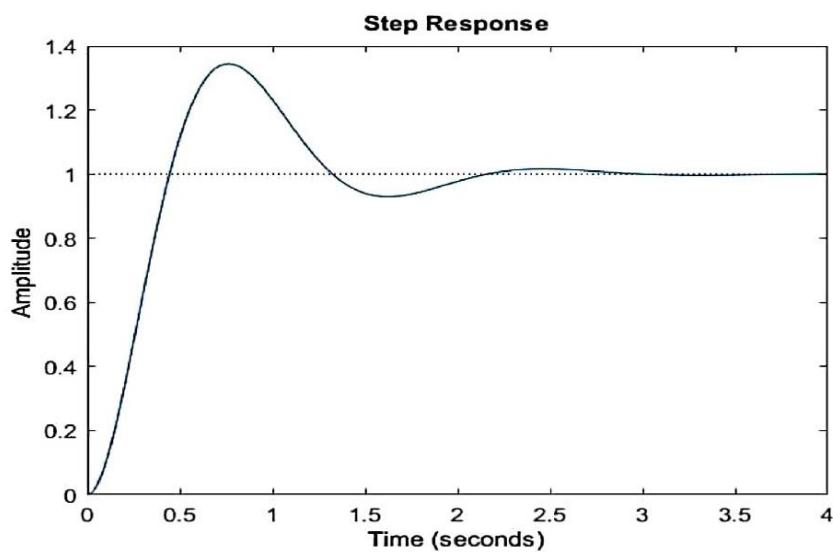
Continuous-time transfer function.

```
G=G_F*G_C
```

```
G =  
40 s + 8  
-----  
8 s^4 + 48.2 s^3 + 41.2 s^2 + s
```

Continuous-time transfer function.

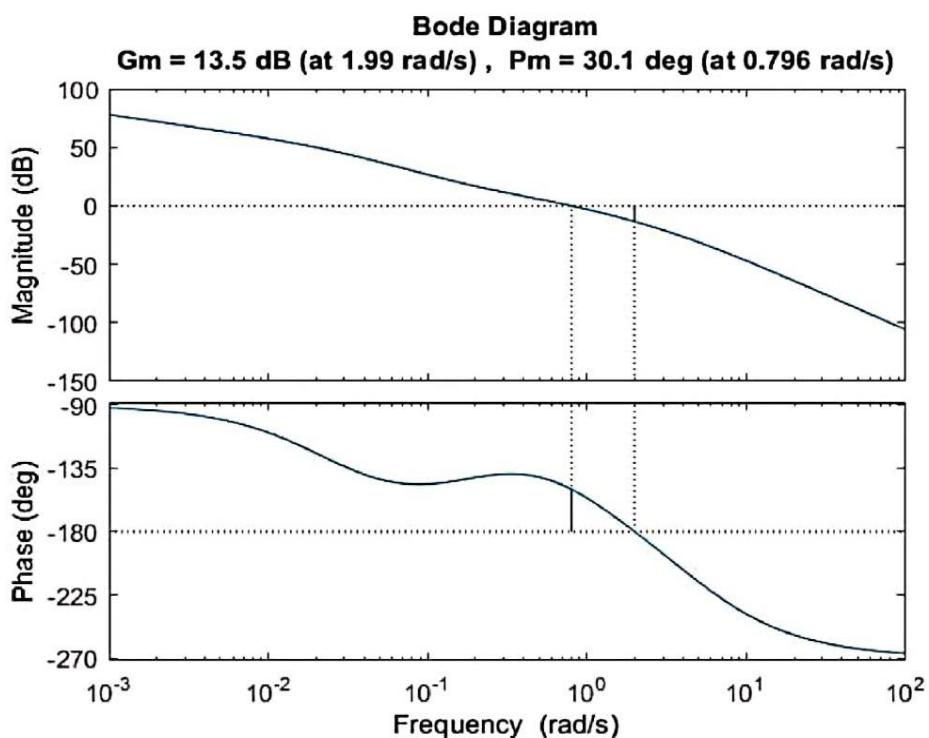
```
figure(3)
step(feedback(G,1))
```



```
stepinfo(feedback(G,1))
```

```
ans = struct with fields:
    RiseTime: 0.3020
    SettlingTime: 2.0151
    SettlingMin: 0.9164
    SettlingMax: 1.3445
    Overshoot: 34.4478
    Undershoot: 0
    Peak: 1.3445
    PeakTime: 0.7644
```

```
figure(4)
margin(G)
```



```
[m_r_cont,w_r_cont]=getPeakGain(feedback(G,1))
```

```
m_r_cont = 1.9250
w_r_cont = 0.8062
```

### Design of Lag – Lead Compensator:

The open – loop transfer function of a unity feedback control system is given by

$$G(s) = \frac{K}{s(1+0.5s)(1+0.1s)}$$

Compensate the system to meet the following specifications:

- Velocity error constant  $K_v \geq 25 \text{ s}^{-1}$
- Phase Margin  $\phi_s \geq 60^\circ$
- Band width  $w_b = 10 \text{ rad/s}$

### Lag-Lead compensator

```
clc;
clear;
close all;

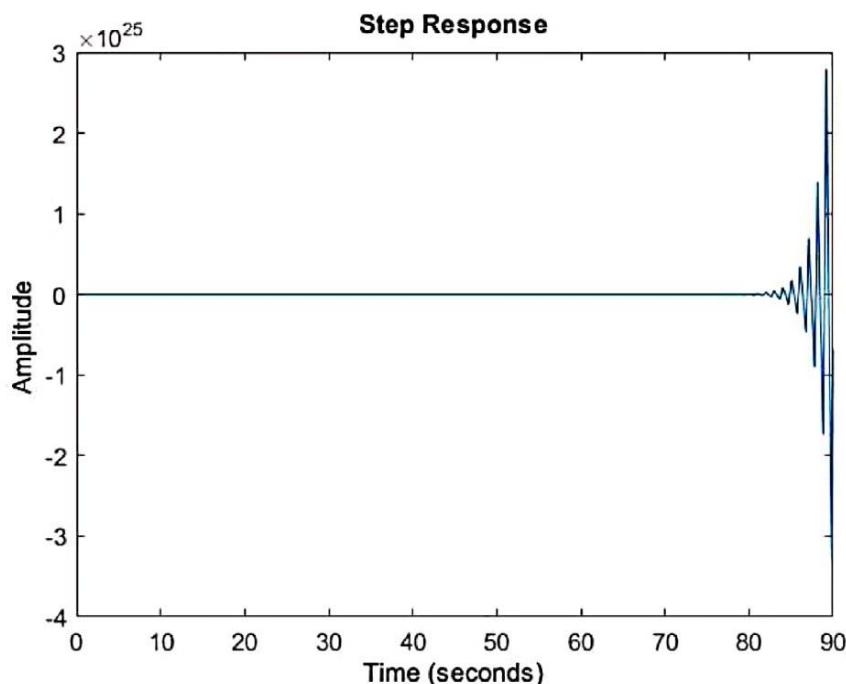
s=tf('s');
G_F=(25)/((s)*(1+0.5*s)*(1+0.1*s))
```

G\_F =

$$\frac{25}{0.05 s^3 + 0.6 s^2 + s}$$

Continuous-time transfer function.

```
figure(1)
step(feedback(G_F,1))
```



```
stepinfo(feedback(G_F,1))
```

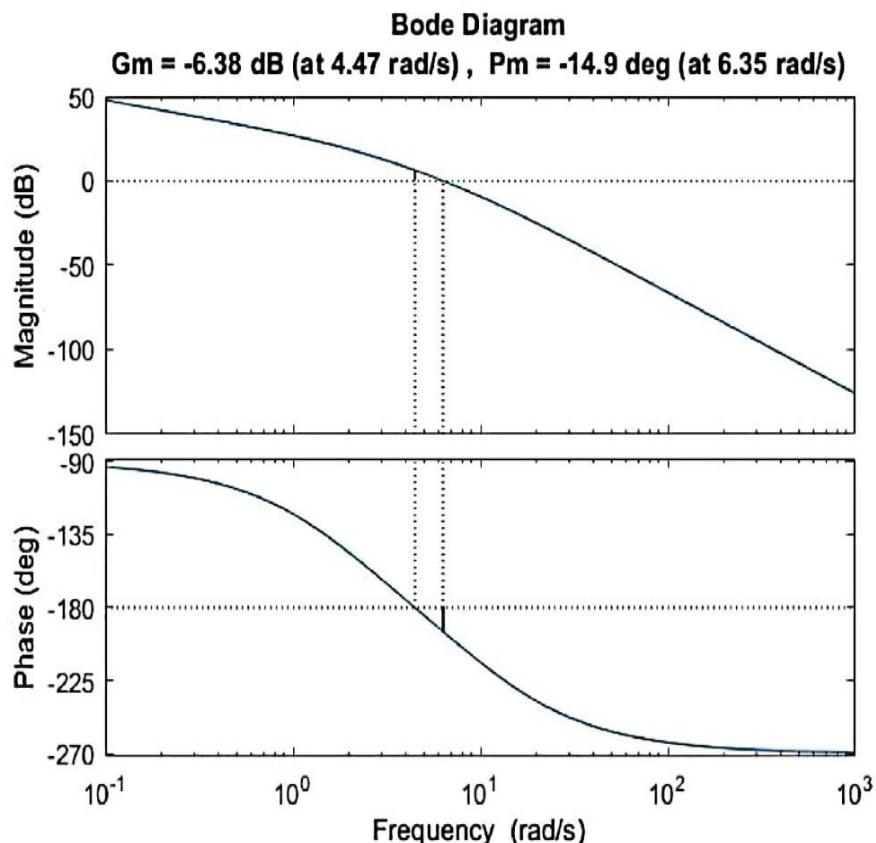
```
ans = struct with fields:
    RiseTime: NaN
    SettlingTime: NaN
    SettlingMin: NaN
    SettlingMax: NaN
    Overshoot: NaN
```

Undershoot: NaN

Peak: Inf

PeakTime: Inf

```
figure(2)  
margin(G_F)
```



```
[m_r,w_r]=getPeakGain(feedback(G_F,1))
```

m\_r = 4.2592

w\_r = 6.0439

```
G_C=(1+0.746*s)/((1+16*s)*(1+0.093*s))
```

G\_C =

$$0.746 s + 1$$

$$\frac{1}{1.488 s^2 + 16.09 s + 1}$$

Continuous-time transfer function.

```
G=G_F*G_C
```

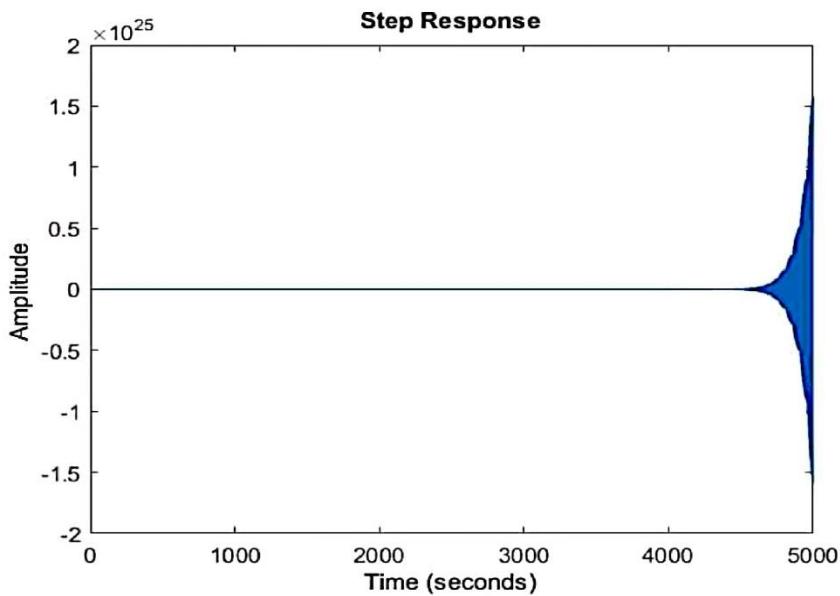
G =

$$18.65 s + 25$$

$$\frac{1}{0.0744 s^5 + 1.697 s^4 + 11.19 s^3 + 16.69 s^2 + s}$$

Continuous-time transfer function.

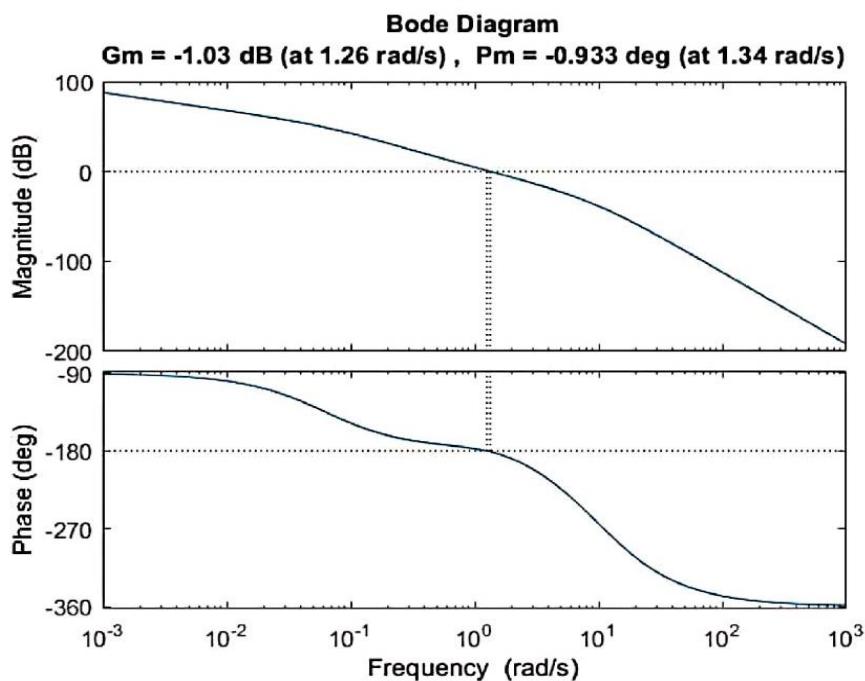
```
figure(3)
step(feedback(G,1))
```



```
stepinfo(feedback(G,1))
```

```
ans = struct with fields:
    RiseTime: NaN
    SettlingTime: NaN
    SettlingMin: NaN
    SettlingMax: NaN
    Overshoot: NaN
    Undershoot: NaN
    Peak: Inf
    PeakTime: Inf
```

```
figure(4)
margin(G)
```



```
[m_r_cont,w_r_cont]=getPeakGain(feedback(G,1))
```

```
m_r_cont = 62.1395
w_r_cont = 1.3413
```

**Result:**

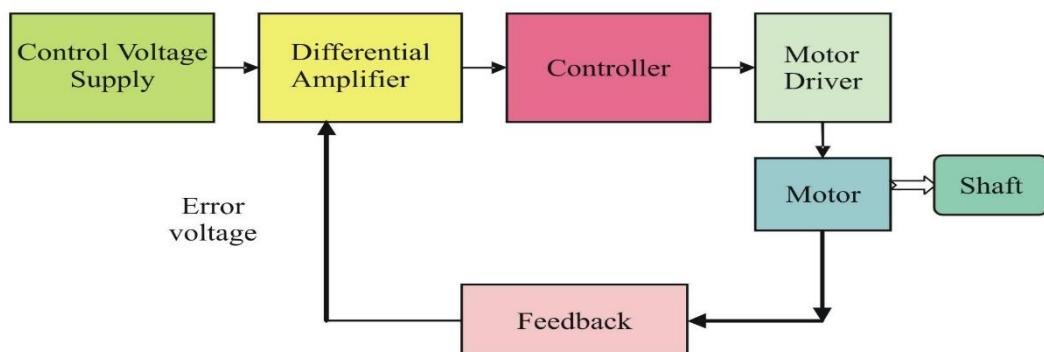
## Experiment No - 08

### Position Control

**Objective:** To observe the position control system for different values of the forward gain at different values of angular position commands.

#### Equipments needed:

1. Scientech 2453 DC Position Control
2. Additional unit Motor Cabinet for Scientech 2453.
3. DIN Cable.



**Procedure:**

1. Connect the Motor Cabinet to the Scientech 2453 DC Position Control through DIN cable at the connector provided in the motor block on the board.
2. Connect the power supply to Scientech 2453 DC Position Control.
3. Switch “On” the supply.
4. Set Toggle switch to upwards i.e. to Reference input.
5. Set the angular positioning command through the pointer as shown on the board that will be the reference angle for the DC motor.
6. Observe the voltage value at the reference input before Error block.
7. Now set the forward gain through the knob provided in the controller block on the board at maximum position.
8. Observe the response at different values of angular command and feedback in the feedback block on the board.

NOTE: Error in command and output calibrated dial of  $\pm 5$  degree is permissible.

**Observations:**

S.No	Reference Angular position	Actual Angular position + Correction Factor
1.	30	25+5
2.	60	55+5
3.	90	85+5
4.	150	145+5
5.	180	175+5
6.	210	205+5
7.	240	235+5
8.	270	265+5
9.	300	295+5
10.	330	325+5
11.	350	345+5

**Result:**

## Experiment No - 09

### DC Motor Speed Control

#### Experiment No – 09(A)

**Objective:** Study of effect of loading on the speed of the Motor in the open loop(Eddy Current Brake)

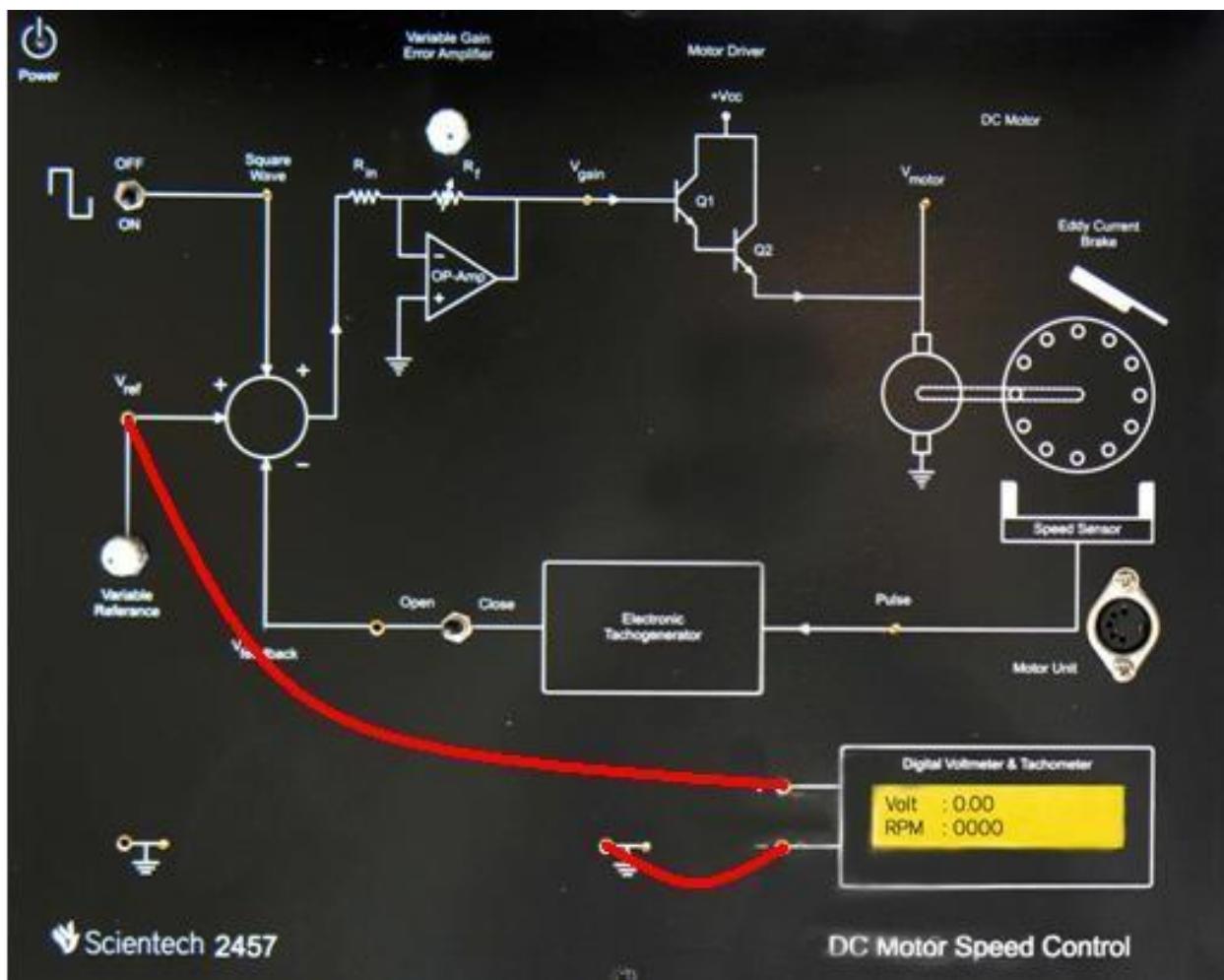
#### **Equipments Required:**

1. Scientech 2457 Techbook
2. Techbook power supply
3. Mains cord
4. Additional unit Motor Cabinet for Scientech 2457.
5. Digital Storage oscilloscope (DSO)
6. DIN Connector Cable.

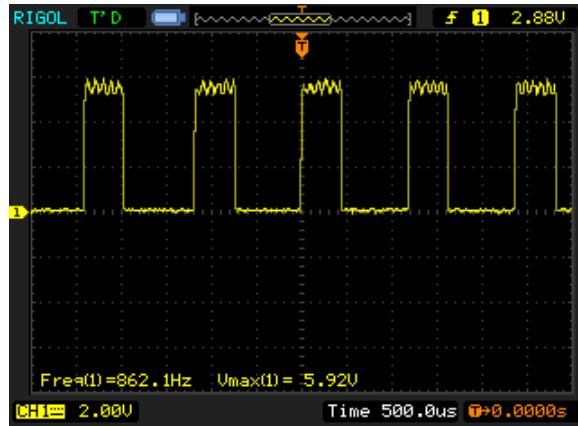


#### **Procedure:**

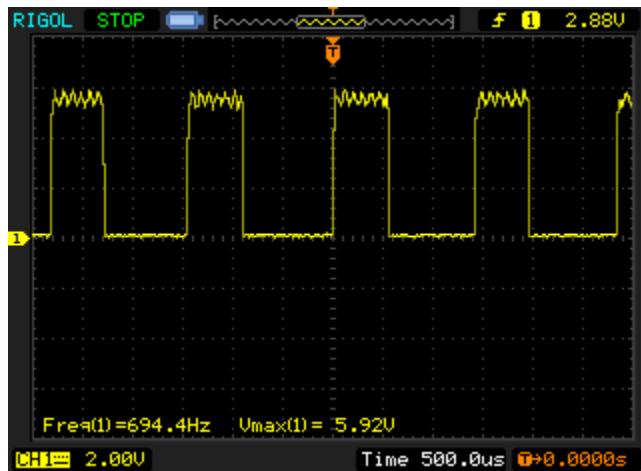
- Connect the Motor Cabinet to the Scientech 2457 DC Motor Speed Control through DIN Connector cable.
- Turn the square wave toggle switch in “OFF” position.
- Turn the Feedback toggle switch in “Open” position.
- Connect the Techbook power supply to the Scientech 2457. Touch over the power LED to turn ON the power.
- Connect a Digital Storage oscilloscope (DSO) between the test point “Pulse” and GND.



- Rotate the “Variable Reference” pot at the maximum position and observe the waveform at the “Pulse” test point on the Digital Storage oscilloscope (DSO). The waveform is as shown in the figure.



- Rotate the knob on the Motor cabinet and bring the magnet closer to the rotating wheel of the DC Motor.
- Observe the waveform on the Digital Storage oscilloscope (DSO). The frequency at the “Pulse” test point will start to decrease and the speed of the Motor will also start to reduce.



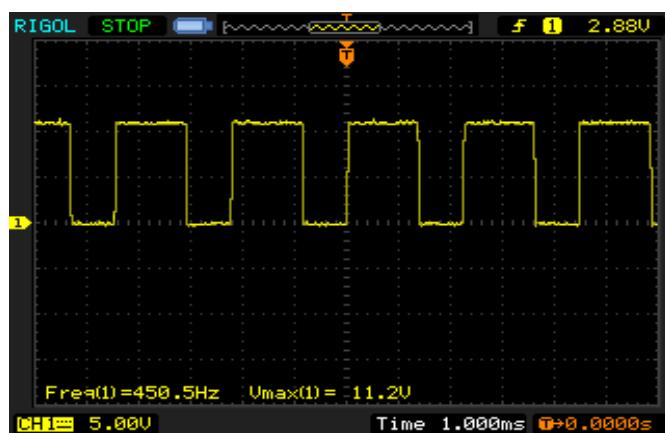
- This Phenomenon is known as Eddy Current Brake.

### Experiment 9(B)

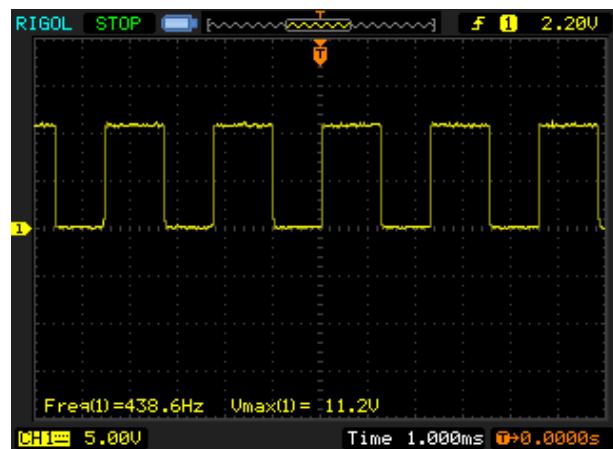
**Objective:** Effect of loading on the speed of the Motor in the closed loop

**Procedure:**

- Connect the Motor Cabinet to the Scientech 2457 DC Motor Speed Control through DIN Connector cable.
- Turn the square wave toggle switch in OFF position.
- Turn the Feedback toggle switch in Close position.
- Connect the Techbook power supply to the Scientech 2457. Touch over the power LED to turn ON the power.
- Connect a Digital Storage oscilloscope (DSO) between the point VMotor and GND.
- Rotate the “Variable Reference” pot at some middle position so that the waveform viewed in the Digital Storage oscilloscope (DSO) is as shown in figure.



- Rotate the knob on the Motor cabinet and bring the magnet closer to the rotating wheel of the DC Motor.



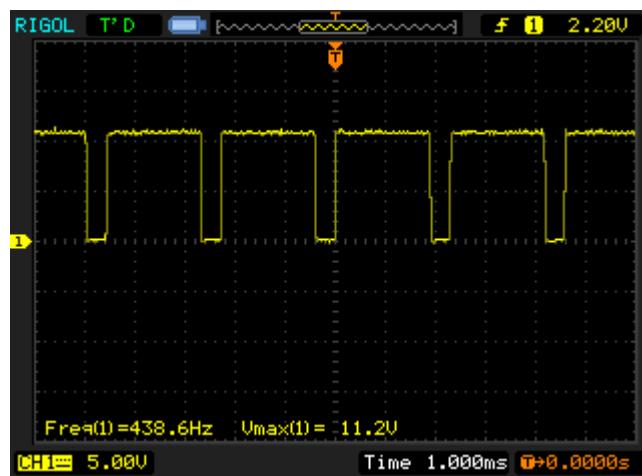
- The speed of the DC Motor gets reduced when the magnet is brought near the wheel. This is due to the eddy current effect.
- Observe the waveform on the Digital Storage oscilloscope (DSO). As the magnet is brought near the wheel, the duty cycle of the pulse increases indicating that the controller is trying to maintain the speed of the Motor that is reduced by the eddy current effect. Repeat the above procedure for different “Variable Reference” input.

## Experiment 9(C)

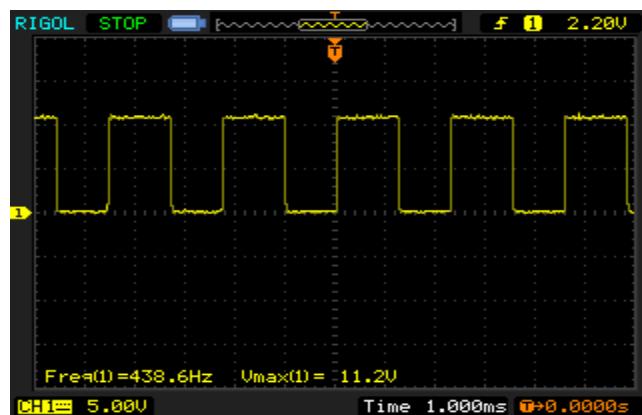
**Objective:** Study the speed control of a DC Motor.

**Procedure:**

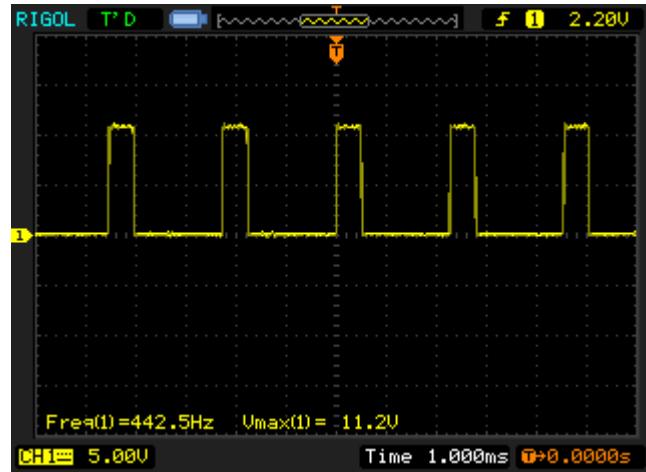
- Connect the Motor Cabinet to the Scientech 2457 DC Motor Speed Control through DIN Connector cable.
- Turn the square wave toggle switch in OFF position.
- Turn the Feedback toggle switch in Close position.
- Connect the Techbook power supply to the Scientech 2457. Touch over the power LED to turn ON the power.
- Connect a Digital Storage oscilloscope (DSO) between the point VMotor and GND.
- Now vary the “Variable Reference” potentiometer and observe the speed variation of the Motor.
- A pulse appears on the Digital Storage oscilloscope (DSO) whose duty cycle varies as the variable reference pot is moved.
- When the pot is at maximum position, the pulse is as shown in figure below. At this position the Motor is at its maximum speed.



- Now rotate the pot towards minimum position. The duty cycle of the pulse will also decrease. This is as shown by the figure.



- When the pot is almost at the minimum, the speed of the Motor is too low and the signal on Digital Storage oscilloscope (DSO) is as shown in Fig.



- Beyond this point the Motor will stop and there will be no signal to drive the Motor.

S.No	Voltage Reading in Volts	Speed in RPM
1.	0.62	382
2.	0.85	735
3.	1.25	1290
4.	1.56	1690
5.	1.88	2012
6.	2.43	2430

**Result:**

**Experiment No – 10(A)**  
**Block diagram reduction technique using MATLAB**

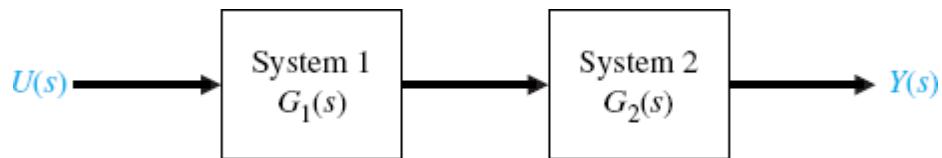
**Aim:** simulation of multi feedback system

**SOFTWARE REQUIRED:** MATLAB – Personal Computer with MATLAB

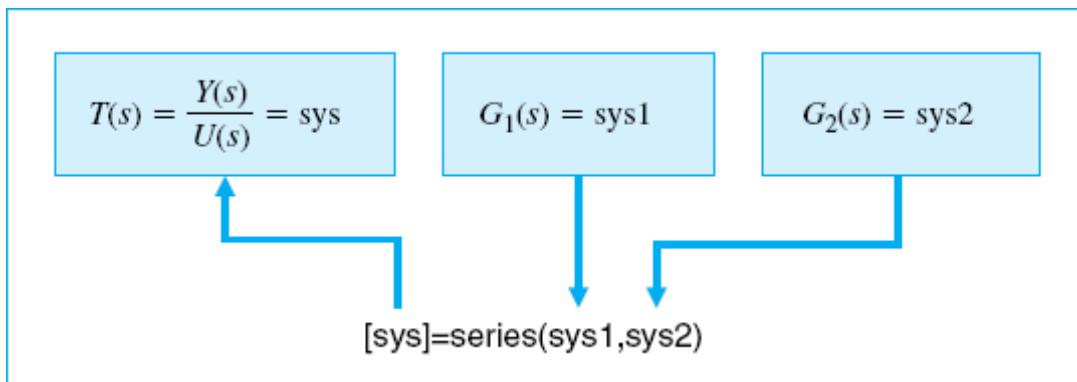
**Theory:**

**Series configuration:** If the two blocks are connected as shown below then the blocks are said

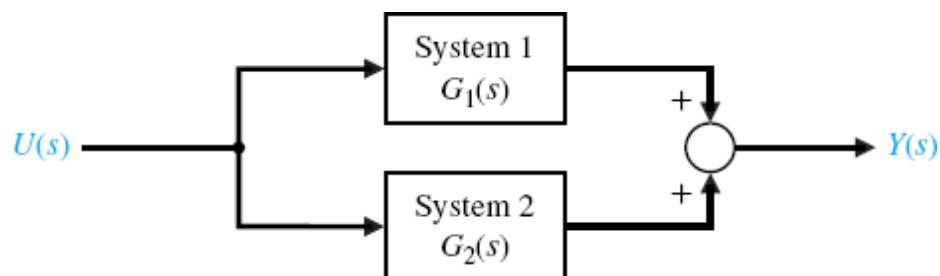
to be in series. It would like multiplying two transfer functions. The MATLAB command for the such configuration is “series”.



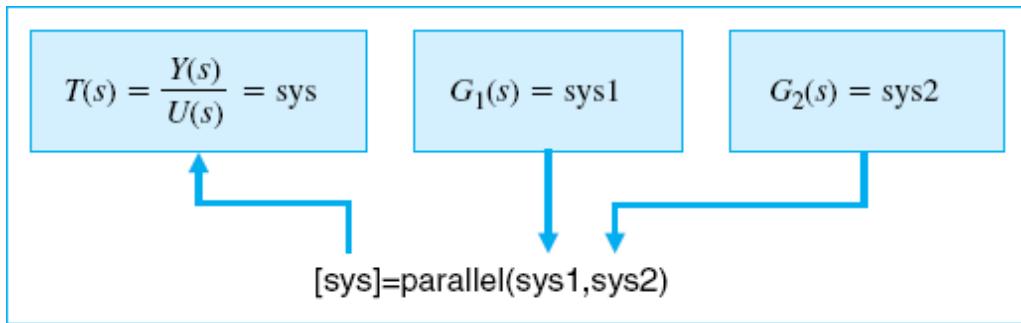
The series command is implemented as shown below



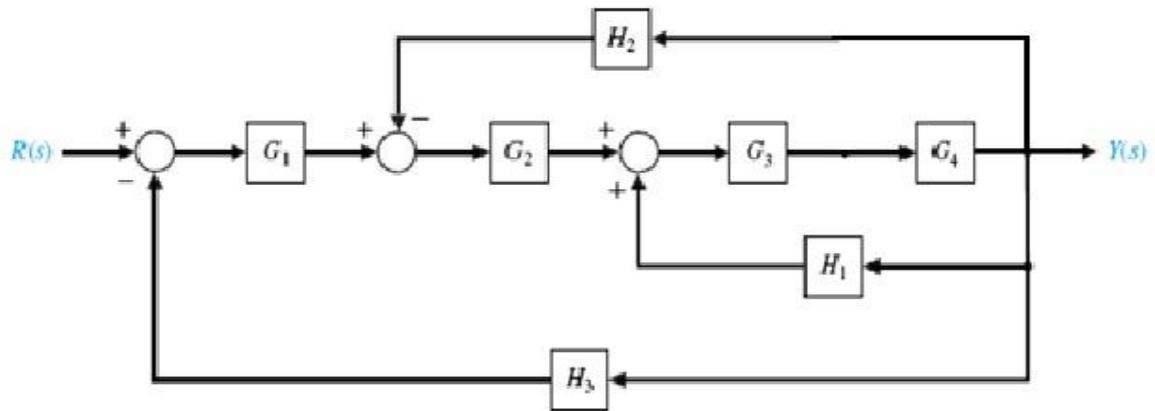
**Parallel configuration:** If the two blocks are connected as shown below then the blocks are said to be in parallel. It would like adding two transfer functions



The MATLAB command for implementing a parallel configuration is “parallel” as shown below:



**Block diagram:**



**Program:**

```

n1=[1]; d1=[1 0]; sys1=tf(n1, d1)
n2=[1]; d2=[1 0]; sys2=tf(n2, d2)
n3=[1]; d3=[1 0]; sys3=tf(n3, d3)
n4=[1]; d4=[1 0]; sys4=tf(n4, d4)
nh1=[1]; dh1=[1]; sys_h1=tf(nh1,dh1)
nh2=[1]; dh2=[1]; sys_h2=tf(nh2,dh2)
nh3=[1]; dh3=[1]; sys_h3=tf(nh3,dh3)
sys1=series(sys3,sys4)
sys2=feedback(sys1,sys_h1,+1)
sys3=series(sys2,sys2)
sys4=feedback(sys3,sys_h2,-1)
sys5=series(sys1,sys4);
sys=feedback(sys5,[1])

```

**Theoretical calculations:**

Compare the theoretical calculations for the above block diagram with MATLAB

All the transfer functions are given in the program.

	Theoretical Calculations	MATLAB
Block Diagram	T.F=	T.F=

**Result:**

## **Experiment No – 10(B)**

### **STATE MODEL FOR CLASSICAL TRANSFER FUNCTION & VICE VERSA USING MATLAB**

**AIM:** To find state model for classical transfer function and transfer from state model using MATLAB

**APPARATUS:** Computer with MATLAB software.

#### **PROCEDURE:**

1. Write the programme in MATLAB text editor using mat lab instructions for state model of classical transfer function and for tranfer function from state model.
2. Run the programs.
3. Note down the outputs.

#### **PROGRAM 1:**

$$A = \begin{bmatrix} 0 & 2 \\ 1 & -1 \end{bmatrix} \quad B = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \quad C = [1 \quad 0]$$

```
a=input ('Enter the values of a matrix');  
b=input('Enter the values of b matrix');  
c=input('Enter the values of c matrix');  
d=input('Enter the values of d matrix');  
[num,den]=SS2 tf (a,b,c,d,1)  
Transfer function=tf (num,den);
```

#### **PROGRAM 2:**

$$T.F = \frac{2}{(s - 1)(s + 2)}$$

```
num = input('Entre numerator polynomial values in the form of matrix array');  
den1=input('Enter denominator 1 values');  
den2=input('enter denominator 2 values');  
den=conv(den1,den2);  
H=tf(num,den);  
P=SS(H);  
[a,b,c,d]=SS data(P);
```

### **PROGRAM3:** Controllability and Observability

```
% State Space Representation  
%  $\dot{x} = Ax + Bu$   
%  $y = Cx + Du$   
% Check Controllability and Observability of a 3rd order System  
% Given -----  
MatrixA = [-3 -1 0; 2 0 0; 0 -1 -1];  
MatrixB = [1; 0; 1];  
MatrixC = [1 0 1];  
MatrixD = 0;  
% Objective -----  
% 1) To Find Controllable Matrix Qc, its rank and check controllability  
% 2) To Find Observable Matrix Qb, its rank and check observability  
% Controllable Matrix -----  
Qc = ctrb(MatrixA, MatrixB);  
rankQc = rank(Qc);  
disp('Controllable Matrix is Qc = ');  
disp(Qc);  
if(rankQc == rank(MatrixA))  
    disp('Given System is Controllable.');?>  
else  
    disp('Given System is Uncontrollable');  
end  
% Observable Matrix -----  
Qb = obsv(MatrixA, MatrixC);  
rankQb = rank(Qb);  
disp('Observable Matrix is Qb = ');  
disp(Qb);  
if(rankQb == rank(MatrixA))  
    disp('Given System is Observable.');?>
```

```

else
    disp('Given System is Unobservable');
end
% End of Program -----

```

### **Observations:**

Compare the Theoretical calculations with MATLAB.

	Theoretical Calculations	MATLAB
Program 1	T.F=	T.F=
Program 2	A= B= C= D=	A= B= C= D=
Program 3	Controllability matrix = Observable Matrix=	Controllability matrix = Observable Matrix=

### **RESULT:**