LL System Design

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Introduction

- Motivation
- Language
 - Scheme but not just Scheme
- Implementation
 - Still buggy and slow after 10 years :)
 - Similar to Oaklisp:
 - but has flonum, but no bignum.
 - all method invocations are by C function pointer call.

«Because LL is self-referential, concepts and constructs to be illuminated later will be marked with "☆".»

Why Bother?

- Wanted an embeddable Scheme:
 - with a clean C namespace
 - with proper tail-calls
 - with an object-oriented foundation
 - with introspection
- Platform for ideas:
 - Interpreter multiplicity, self-referential systems
 - Tagging, memory, GC, linkage, compilation, FFI.
- Another plate of hubris? :)

Language

- LL is an pure object-oriented, lexically-scoped Lisp
- Supports multiple inheritance and mixins
- R4RS Scheme compliance is built on objectoriented core
- Based on Oaklisp and Dylan syntax and semantics
- Extensible and embedded in C
- Introspection

Constructs

Objects

→ #<<type> <object>>

Types

- → #<<type> <type>>
- Operations
- → #<<type> <operation>>

Messages

→ #<<type> <message>>

Methods

→ #<<type> <method>>

Locatives

→ #<<type> <locative>>

Objects

- Have a type.
- Have a fixed number of slots.
- Immediate objects have no slots:
 - <fixnum>, <flonum>, <locative> ☆
- Are created by sending the make operation to a type object with arguments for a type-specific initialize method.

<object>

```
    (get-type 5)

                       ; => <fixnum>
                       ; => <flonum>
(get-type 5.5)
(get-type <fixnum>) ; => <type>
(get-type <type>)
                       ; => <object>
(make <pair> 1 2)
                   ; => (1.2)
(eq? (make <symbol> "foo") 'foo)
                       : => #t
• (%%slot (make <pair> 1 2) 1) ;;; unsafe! ☼
                       ; => 1
```

Types

- Are subtypes of <object>.
- Are named < something > by convention.
- Can be anonymous.
- Can be subtyped (meta-types).
- Have a list of supertypes.
- Have a list of slots.
- Have a mapping of operations to methods.
- Core LL types have analogous C structs.

<type>

```
(type-supers <object>)
                           ; => ()
                           ; => (<object>)
(type-supers <type>)
                           ; => (<list> <object>)
(type-supers <pair>)
                           ; => ((isa 0)) 🌣
(type-slots <object>)
(type-slots (get-type '(1 2))
                           ; => ((car 0) (cdr 4)) 🌣
(define <my-cons>
   (make <type>
    (list <object>)
                           ; supertypes
    (list 'car 'cdr)))
                           ; slots
```

Mutable .vs. Immutable

 By convention mutable types are subtypes of immutable types.

Operations

- Are objects.
- Can be anonymous.
- Can be subtyped.
- Have a mapping of types to methods.
- Contain a method lookup cache.
- Associate the receiver type (the first argument or <object>) and an implementation method.
- Are the only objects that can be "applied".

<operation>

```
(define my-car (make <operation>))
```

```
(define my-cdr (make <operation>))
```

```
(define my-func
(lambda (x) ; ☼
(+ (my-car x) (my-cdr x))))
```

Settable Operations

Are operations that have a setter <operation>.

```
; => #<locatable-operation car> 🌣
car
(type-supers (get-type car))
                   ; => (<settable-operation>)
                   ; => #<operation set-car!>
(setter car)
                   ; => #<locatable-operation setter>
setter
(define x (cons 1 2))
                  ; => (1.2)
                   :=>1
 (car x)
  ((setter car) x 'a)
                   ; => (a.2)
```

(set! (op . op-args) value)

 Syntax is transformed into the application of the setter of a <settable-operation>:

```
(set! (op . op-args) value) =>
((setter op) . op-args value)
```

```
(define x (car 1 2))(set! (car x) 'b)x; => (b . 2)
```

(define v (make <vector> 4 'a))
 (set! (vector-ref v 2) 'b)
 v

Messages

- Are objects.
- Are created by the application of an operation to a receiver and some arguments.
- Lookup is based on the <type> of the receiver.
- Without arguments are messages to a nonexistent <object>.
- Implementation:
 - Created on a message stack.
 - Arguments and results are on a separate value stack.

Message Lookup

- (cons 1 2) =>
 - Receiver type => <fixnum>
 - Implementation type => <object>
- (newline) => ...
 - Receiver type => <object>
 - Implementation type => <object>
- (+ 1 2) => ...
 - Receiver type => <fixnum>
 - Implementation type => <fixnum>

Methods

- Are objects.
- Are anonymous.
- Can be subtyped.
- Can lexically "close-over" global bindings, formal arguments or object slots.
- Give lexical scope to slots in an object of the method's implementation type.
- Are resolved at run-time by operation and type.
 Implemented with a primitive C function pointer.

(add-method ...)

• The primitive closure special form:

```
(%method slots formals . body) 🌣
```

- Handled directly by the compiler.
- (add-method (op (type . slots) . formals) . body)
 ; =>
 (%add-method type op
 (%method slots formals . body))
 - %add-method is defined on <type> and returns op.

<method>

```
(add-method
   (initialize (<my-cons> car cdr) self a d)
    (set! car a)
    (set! cdr d)
    self))
(define my-car (make <settable-operation>))
 (add-method
    (my-car (<my-cons> car) self)
      car)
  (add-method
    ((setter my-car) (<my-cons> car) self value)
       (set! car value))
```

Operation Overloading

```
    (define add (make <operation>))
        (add-method (add (<string>) a b))
        (string-concat a b))
        (add-method (add (<number>) a b))
        (+ a b))
```

```
    (add "foo" "bar") ; => "foobar"
    (add 2 3) ; => 5
    (add "foo" 3) ; => #<ERROR!>
```

Lambda

- Lambdas are anonymous operations.
- An anonymous lambda <operation> is implemented by a <method> defined on <object>.
- Lambda operations can be overloaded for other receiver (first argument) types.

(lambda formals . body)

```
(define (foo bar)
   (+ bar 5))
 =>
 (define foo (lambda (bar)
   (+ bar 5))
=>
 (define foo
   (add-method ((make <operation>) (<object>)
    bar)
    (+ bar 5)))
```

Locatives

- Locatives are safe, language-level pointers to value locations, such as:
 - arguments, global bindings or object slots.
- Simplify implementation of closures, call/cc, great for mutable object slots.
- <method> environment vectors contain locatives to closed-over formals and slots which have been moved to the heap.

Locative Operations

- (make-locative variable-or-application)
 - creates a locative; closes-over a variable.
- (contents locative)
 - gets the contents of the location.
- (set-contents! locative value)
 - sets the contents of the locative.
- Identity Transforms:
 - (locative-contents locative) => locative ☼
 - (contents (make-locative x)) => x
 - (make-locative (contents x)) => x

<locative>

```
    (define x 5)

  (define I (make-locative x))
                                    ; => 5
  (contents I)
                                    : => 5
  (set-contents! I 10)
  (contents I)
                                    ; => 10
                                    : => 10
(define x (cons 1 2))
  (define I ((locater car) x))
  (set-contents! I 'foo)
                                    ; => (foo . 2)
  X
```

(set! (contents . args) x)

- (set! (contents locative) value) =>
 ((setter contents) locative value) =>
 (set-contents! locative value)
 - (define x (cons 1 2))
 (define I (make-locative (car x)))
 (set! (contents I) 'a)
 x

Locatable Operation

- A <locatable-operation> is a <settableoperation> that has a locater <operation>.
- (locator op) returns an <operation> that returns a <locative> to a value:

```
car ; => #<locatable-operation car>
(setter car) ; => #<operation set-car!>
(locater car) ; => #<operation locative-car>
(define x (cons 1 2)) (define f (locater car)) (f x) ; => #<locative (car x)> (contents (f x)) ; => 1
```

(make-locative (op . args))

 (make-locative x) on a global binding, lexical variable or object slot is a special form.

Messaging

- Message Object
 - Operation
 - Receiver and Type
 - Arguments
- Method Lookup
 - Method
 - Implementation type
 - Type offset ☆
- Method Application

Message Object

- Message objects have:
 - An operation
 - An argument list (including the receiver in car)
- Method lookup computes:
 - The receiver type
 - The method implementing the operation for the receiver type
 - The type that implemented the method
- Method application:
 - Calls the method with the message.

Mutual Tail Recursion

```
(define (f a)
   (write (cons 'f a)) (newline)
   (q (+ a 1)))
                                     ; tail call
  (define (g b)
   (write (cons 'g b)) (newline)
   (f (* b 2)))
                                     ; tail call
                                     ; normal call
  (f 0)
```

Message Protocol

- <message> objects are created.
- Two explicit stacks:
 - <message> stack.
 - Value stack for arguments and results.
- Two stacks simplify tail-calls.
- Both stacks use stack buffers for fast call/cc.
- Do not create locatives to arguments on stack for compatibility with call/cc.
- Avoid passing arguments to lookup primitives, use stack pointers.

Operation Application

- (operation . arguments) =>

 (apply operation arguments)
- Pseudo-code to implement (apply ...) =>
 - (define *value-stack* ())
 - (define *method-stack* ())
 - (define (%call operation . arguments) ...)
 - (define (%call-tail operation . arguments) ...)
 - (define (%return result) ...)

(%call operation . arguments)

```
(define (%call operation . arguments)
   (%push-each! *value-stack* arguments)
   (%push! *message-stack*
    (make <message>
     operation (%length arguments)))
   (while (%lookup-and-apply)
  ;; nothing
  (%pop! *value-stack*))
```

(%lookup-and-apply)

(%lookup message)

```
(define (%lookup message)
  (let* ((type (%receiver-type message))
      (meth (assq (%operation message)
                 (%op-meth-alist type)))
    (if meth
         (begin
         (%set-method! message meth)
        (%set-method-impl! message type)
         meth
      (%lookup-super message))))
```

(%return result)

```
    (define (%return result))
        (%pop-arguments!)
        (%pop! *message-stack*)
        (%push! *value-stack* result)
        #f)
```

#f tells caller's %apply (while ...) loop to stop.

(%call-tail operation . arguments)

 #t tells caller's %apply (while ...) loop to keep going.

Interpreter Implementation

- Values, Boxing and Tagging
- Object Layouts
- Runtime Bootstrapping
- Messaging
- Continuations, Catch/Throw
- Evaluation
- Performance

Values, Boxing and Tagging

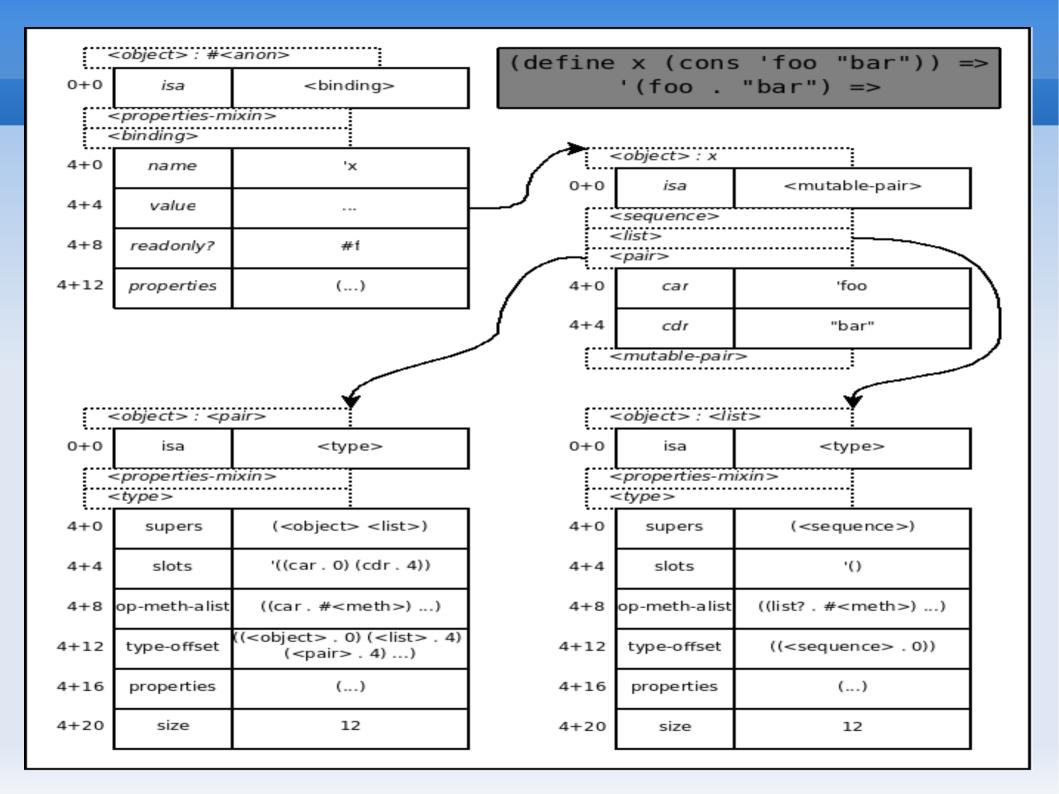
- Values are machine words: *
 - 32-bit words => 4 byte alignment.
 - Defined in C as typedef unsigned int 11 v.
- Boxing Values
 - Some objects cannot fit in a machine word.
- Tagging Values
 - Not all values are pointers.
 - Tagging takes up space in machine words.
- Tagging Schemes
 - Some schemes are better than others.

Boxing and Tagging

- Most CPUs do not support latent typing in microcode.
- Some interpreter objects can fit in machine words, many cannot.
- Allocating memory for every object (including integers, floats) is expensive, if not impossible.
- Trade off space, precision, performance and complexity.
- Play nice with C but don't give up the good fight.

Allocated Object Layout

- Each slot is a word. *
- Each ancestor type is given one block of slots.
- Offsets of each ancestor type is stored in each type.
- Mixins have no slots.
- Core types are defined by C macros:
 - Define C structures with inheritance.
 - Create interpreter <type> objects for introspection.



<pair> type definition

- (get-type (cons car cdr)) => <mutable-pair> ☆
 - <pair> C definition
 - <pair> C struct (generated)
 - <pair> LL <type> definition (generated)

<pair> C definition

```
    Il_define_type(object, type)

            Il_define_type_slot(object, type, Il_v, isa)
            Il_define_type_end(object, type)

    Il_define_type(pair, type)
```

- II_define_type_super(pair, type, object)
 II_define_type_slot(pair, type, II_v, car)
 II_define_type_slot(pair, type, II_v, cdr)
 II_define_type_end(pair, type)
- II_define_type(mutable_pair, type)
 II_define_type_super(pair, type, pair)
 II_define_type_end(pair, type)

<pair> C struct generated

```
/* type slot blocks */
struct II ts object { II v isa; };
struct II ts pair { II v car; II v cdr; };
struct II ts mutable pair { /* empty */ };
                                        /* type actual structure */
struct II tsa object {
   Il v isa;
struct II_tsa_pair {
   struct II ts object super object;
   struct II ts pair
                         super cons;
struct II_tsa mutable pair {
   struct II tsa pair super pair;
};
```

<pair> LL definition generated

```
(define <object>
     (make <type>
                         ; supers
        '(isa) ))
                         : slots
(define <pair>
     (make <type>
        (list <object>); supers
        '(car cdr) ))
                         ; slots
(define <mutable-pair>
     (make <type>
        (list <pair>)
                         ; supers
                         ; slots
```

Tagging

- Tagging is a compromise between the statically-typed world of the hardware and the latently-typed world of the interpreter under the performance constraints of the machine.
- After tagging most native machine object values can fit in machine words; objects that cannot fit in machine words must be allocated.
- Tagging schemes effect:
 - GC, memory layout, code size, FFI, performance.

Tagging Schemes

- Trade off word precision for indirection and storage reduction.
 - High-bit tags
 - Low-bit tags
 - Variable-width tags
 - Fixed-width tags
 - Dedicated tags:
 - Lisp machines.
 - Some experimental HW with dedicated GC support.

High Bit Tagging

- Requires special memory management: mmap(), etc.
- Presumes small type domain and limited object frequency.
- Complicate GC.
- Older Common Lisp implementations.

Low Bit Tagging

- Requires no special memory management.
- Open-ended type domain and object frequency.
- Compatible with off-the-shelf conservative GCs.
- Use tag bits normally unused due to machine alignment.
- Most new language implementations.

II_TAG(II_v)

- Tags are low-bit tags: (log2(sizeof(int)))
 - 32-bit words => 2-bit tags; 64 bits => 3-bit tags
- From II/value.h:

Tagging

- Values converted from statically-typed values (CPU) to latently-typed values (interpreter).
- Lower 2-bit tags for all values:

```
II_BOX_fixnum(x) =>x >> 2 ==x * 4
```

 Some integer word values cannot be tagged, must be dynamically allocated as boxed object: bignums.

Fixnum Tagging/Boxing

- II_BOX_fixnum(int)
 - II_BOX_fixnum(0) => 0 << 2 => (II_v) 0
 - II_BOX_fixnum(1) => 1 << 2 => (II_v) 4
 - II_BOX_fixnum(-5) => -5 << 2 => (II_v) -20
- II_UNBOX_fixnum(II_v)
 - II_UNBOX_fixnum(0) => (int) 0
 - II UNBOX fixnum(4) => (int) 1
 - II_UNBOX_fixnum(-20) => (int) -5

Why II_TAG(fixnum) == 0?

- Fixnum addition, subtraction and vector element offset are common.
- X >> 2 == X * 4
- sizeof(II_v) == sizeof(int) == 4
- 0 >> 2 == 0 * 4 == 0
- Overflow/underflow still an issue but uncommon in practice.

If II_TAG(fixnum) != 0

```
Scheme: (+ x y) =>
 C: II BOX fixnum(
        II UNBOX fixnum(x) +
        II UNBOX fixnum(y))
Scheme: (+ x y) =>
 C: II BOX fixnum(
        II UNBOX fixnum(x) -
        II UNBOX fixnum(y))
Scheme: (vector-ref v i) =>
 C: *(II v*) (((char*) II vector ptr(v))) +
               II_UNBOX fixnum(i) * 4)
```

If II_TAG(fixnum) == 0

- Scheme: (+ x y) => C: (x + y)
- Scheme: (- x y) => C: (x y)
- Scheme: (vector-ref v i) => C:
 (Il_v) (((char*) Il_vector_ptr(v)) + i)
- Scheme: (string-ref s i) => C:
 (Il_v) ((char*) Il_string_ptr(s)) + (i >> 2))
- Still need to check for underflow/overflow, but checks can be done in a separate pipeline.

Allocated Reference Tagging/Boxing

- First slot in all allocated objects is the object's <type>.
- Lowest 2 bit of 32-bit word addresses are 00 due to machine word alignment.
- Offset allocated object address with II_TAG_ref:

```
    II_BOX_ref(x) => (((char*) x) + II_TAG_ref)
    II_UNBOX_ref(x) => ((void*)((x) - II_TAG_ref))
    II_SLOTS_ref(x) => ((II_v*)II_UNBOX_ref(x))
    II_TYPE_ref(x) => II_SLOTS_ref(x)[0]
```

Why II_TAG_ref == 3

- Most slot access will be an offset from C pointer to allocated structure.
- C: ((type*) ptr)->slot => *(typeof(type, slot)*)(ptr + offsetof(type, slot))
- Most slot accesses are unaffected by subtracting tag bits after C compiler optimizations.
- Getting the object's type (object slot 0) is more complex at the expense of making <fixnum> tagging faster.

If II_TAG_ref == 0

- (car x) =>
 - *(II_v*)(II_UNBOX_ref(x) +
 offsetof(II_ts_pair, car)) =>
 (II_v)(x + 0 + 4) =>
 (II_v)(x + 4)
 - Non-zero offset has cost.
- (get-type x) =>
 - *(II_v*)(II_UNBOX_ref(x) +
 offsetof(II_ts_object, isa)) =>
 (II_v)(x + 0 + 0) =>
 (II_v)(x)
 - Zero offset has no cost.

If II_TAG_ref == 3

- (car x) =>
 - *(II_v*)(II_UNBOX_ref(x) +
 offsetof(II_ts_pair, car)) =>
 (II_v)(x 3 + 4) =>
 (II_v)(x + 1)
 - Tag removal has no additional cost with offset.
- (get-type x) =>
 - *(II_v*)(II_UNBOX_ref(x) +
 offsetof(II_ts_object, isa)) =>
 (II_v)(x 3 + 0) =>
 (II_v)(x 3)
 - Tag removal and offset has a unified cost.

II_TAG(flonum)

- Trade lower 2-bits of C float mantissa precision for tag bits instead of allocating objects.
- C inline functions II_BOX_float(float) and II_UNBOX_float(II_v) use a i386 C union.
- Some C float values cannot be represented.
- Reasonable trade-off since operations on floats are often inexact anyway.
- Does not prevent creation of full precisions float or double boxed values using a new <type>.

Runtime Bootstrapping

- The runtime itself is accessible by the user as a <%runtime> object.
- Some objects are statically allocated in the II_tsa__runtime C structure:
 - Symbols
 - Global bindings
 - Character objects, nil, #f, #t.
- nil != Il_BOX_ref(0)
- The runtime system can be modified by itself.

Bootstrapping

- Because LL is self-referential, bootstrapping requires very controlled object allocation and initialization:
- Type layout and initialization is implemented in C and LL.
- At a certain point, the core constants, types, bindings, operations and methods are complete enough allow Il_send() to be usable for the remainder the initialization.
- LL DEBUG INIT=1./IIt

nil != II_BOX_ref(0)

- If nil was a boxed reference to NULL, the entire system would need NULL checks.
- There is a single object instance of the <null>
 type.
- The nil symbol has a read-only global binding and is specially recognized by the compiler.
- This complicates bootstrapping the runtime but this simplifies the system by not introducing special cases in the very lowest levels of the message protocol.

Messaging in C

- C macros
 - Normal calls:II_v II_call(op, _N(arg1, ... argN))
 - Tail calls: void II_call_tail(op, _N(arg1, ... argN))
 - Return from call: void II_return(val)
 - Manipulate stacks inline.
 - Allocate and use inline lookup caches.

Tail-calls in C

- Il_call() puts a new <message> on the message stack and loops while the return value of method function is true (non-zero).
- Il_call_tail() removes current arguments from value stack and replaces current <message> with new message operation and arguments and returns true (non-zero).
- II_return() pops the current arguments, pushes the result onto the value stack and returns 0.

Mutual Tail Recursion: C

```
/*pseudo-C: vs is the value stack, ms is the method stack*/
  int f( /* a = vs.top() */ ) { /* (g (+ a 1)) */ }
     II v temp = vs.pop() + II_BOX_fixnum(1);
     vs.push(temp); ms.top().operation = II o(g);
     return 1;
  int g( /* b = vs.top() */ ) { /* (f (* b 2)) */
     II v temp = vs.pop() / 4 * II BOX_fixnum(2);
     vs.push(temp); ms.top().operation = II o(f);
     return 1;
  int temp func() {
   vs.push(0); ms.push(f); /* f(0) */
   while ( ms.top().lookup()->func() );
```

Method Lookup Performance

- Lambda operation
- Operation lookup cache
- Call site lookup cache
- Move-to-front Heuristic
- Supertypes lookup

Lambda Operations

- Each <operation> object has a lambda cache for operations with methods defined on only one <type>.
 - <object> is a pinned global and its operationmethod association lists is also pinned.
- The lambda <method> is moved into <object> if a <method> on another <type> is added.

Operation lookup cache

- Each <operation> object has a single-entry lookup cache.
 - Cache is invalidated when a <method> is added or removed from the <operation>.
- Each < operation > object has a version number.
 - Version number is incremented when a <method>
 is added or removed from the <operation>.

Call site lookup cache

- Each call site has a multi-entry lookup cache table.
 - Each entry keeps track of the operation version at time of cache fill.
 - If the operation version has changed, the entry is refilled.
 - Most-popular entries are moved to the front of the table.
 - Caveats: inaccessible operations may be stuck in caches.

Move-to-front Heuristic

- The <type>'s op-meth-alist is scanned if the previous caches are not filled.
- The matched association of the op-meth-alist is moved to the front of the list.
- Commonly-applied methods are at the front of the list.
- Consider making op-meth associations weak.

Supertype Lookup

- Supertype lookup routines:
 - Are recursive.
 - Do not pass the <message> object.
 - Return 1 if match is found.
 - Return 0 if more searching is required.
 - Could be changed to use an explicit stack.

Catch/Throw

- Catch/Throw
 - Lighter than call/cc
 - II_CATCH(type)
 - C setjmp()
 - Creates an anonymous <operation> with a <method> that references the C jmpbuf.
 - <catch-method> subtype of <method>
 - C func invokes longjmp().

Continuations

- Save/restore C stack segments since last continuation (see ccont library).
- Flush <message> and value stack buffers.
- Save/restore <message> and value stack pointers.
- Save/restore fluid variable bindings.
- Save/restore current catch.

Interpreter Evaluation

- All (eval) expressions are byte-compiled
 - Phase 1: macro-expansion
 - Simple quasiquote expander.
 - Phase 2: intermediate representation
 - (lambda ...) => (%add-method <object> ... (%method ...))
 - (%method slots formals ...) => <%ir ...>
 - Phase 3: semantics
 - car-position lambda inlining
 - closure generation and environment planning
 - constant-folding
 - Phase 4: assembly generation

<method>

- Abstract base class.
- Slots:
 - func: points to address of primitive C function.
 - formals: parameter list (for debugging)
 - code: code value (for debugging)

 byte-code-method>

- Supers: <method>
- Slots:
 - func: Primitive method function points to primitive byte-code execution function.
 - code: A byte-code <string>
 - constants: A constants <vector>
 - Contents be shared between multiple methods defined in an expression:
 - A <vector> of global symbols.
 - A <vector> of global <bindings> for each global symbol.
 - Other (quote)'ed expressions or constants.

Constant Folding

- (constant-fold symbol scope) =>
 - If symbol is a <symbol > AND
 - If symbol is bound to a global AND
 - If (readonly? binding) THEN
 - (value binding) ELSE op
- (constant-fold (op . args) scope) =>
 - If (constant-fold op scope) is constant? AND
 - If all (map constant-fold args) are constant? AND
 - If (%lookup op rcvr) has no-side-effect? THEN
 - (eval-no-constant-fold (cons op args)) ELSE
 - (cons op args)

Without Constant Folding

(define x (cons 1 2))(lambda (y . args) (set! (car x) y))

```
( (probe 0)
                                                 value stack
 (nargs-rest-1)
                                          ; temps
                                                              args
    (probe 3)
 (arg 0 y)
                                          ; &y
 (contents)
                                          ; y
 (glo 2 x)
                                          ; x y
    (probe 2)
                                          ; x y
 (glo 1 car)
                                          ; car x y
 (glo 0 setter)
                                          ; setter x y
 (call 1)
                                          ; set-car! x y
 (call-tail 2)
 (rtn))
```

With Constant Folding

(define x (cons 1 2))(lambda (y . args) (set! (car x) y))

```
( (probe 0)
                                              value stack
 (nargs-rest-1)
                                        ; temps
                                                          args
    (probe 3)
 (arg 0 y)
                                        ; &y
 (contents)
                                       ; y
 (glo 2 x)
                                       ; x y
 (const 4 #<operation set-car!>)
                                       ; set-car! x y
 (call-tail 2)
 (rtn))
```

Tak Benchmark

Recursion, Fixnum +, -

```
    (define (tak x y z)
        (if (not (< y x))
        z
        (tak (tak (- x 1) y z)
            (tak (- y 1) z x)
            (tak (- z 1) x y))))</li>
```

Performance Comparision

(tak 18 12 6) (tak 30 15 9)
 (tak 33 15 9) (tak 40 15 9)

ikarus 0.25 sec

chicken 1.41 sec (precompiled)

oaklisp 2.63 sec

mzscheme 2.65 sec

scheme-r5rs 5.89 sec

guile 7.91 sec

larceny 10.35 sec

LL 12.93 sec

Future Work

- Vary more levels of self-reference to improve performance?
- Inline primitives into byte-code executor?
- Imbed TinyCC C compiler?
- Re-implement using COLA libid?
- Scheme is the New Assembler?
- Re-implement LL as a library of Scheme procedures and syntax using Ikarus?

Conclusion

- Q & A
- Discussion

Resources

- 🌣
- http://github.com/kstephens/ll/tree/master
- http://kurtstephens.com/page/article.html/5
- http://kurtstephens.com/node/53
- http://www2.lib.uchicago.edu/~keith/crisis/benchmarks/tak/
- http://www.cs.indiana.edu/~aghuloum/ikarus/
- The Art of The Metaobject Protocol Gregor Kiczales
- http://www.amazon.com/Brain-Makers-HP-Newquist/dp/0672304120