Module 6

Q. Principal Component Analysis (PCA) for Dimension Reduction

=>

- 1. Principal Component Analysis (PCA) is a **statistical technique used to reduce dimensions** in large datasets.
- 2. It helps in converting many **correlated variables** into a smaller number of **uncorrelated components**.
- 3. The main purpose of PCA is to simplify the data while keeping most of the important information.
- 4. It helps in reducing data complexity without losing much of the variation present in it.
- 5. PCA is mainly used in **machine learning and data science** for data preprocessing and feature reduction.
- 6. Example In a dataset containing 100 features, PCA can reduce it to 10 important features while maintaining 90–95% of the information.

2. Concept and Working of PCA

- 1. PCA works by finding new axes or directions that **capture the highest variance** in the data.
- 2. Each new axis is called a Principal Component (PC).
- 3. The first principal component captures the maximum variance in the data.
- 4. The **second component** captures the next most variance and is **perpendicular (uncorrelated)** to the first.
- 5. The process continues to find more components until all significant variations are captured.
- 6. The components are arranged in decreasing order of importance, based on how much variance they explain.
- 7. PCA changes the coordinate system of the data but not the actual information.

3. Mathematical Steps Involved

1. Step 1 – Standardization:

The data is standardized so that all features have equal weight (mean = 0, variance = 1).

2. Step 2 - Covariance Matrix:

A covariance matrix is computed to study how variables are related to one another.

3. Step 3 - Eigenvalues and Eigenvectors:

PCA calculates eigenvalues and eigenvectors from the covariance matrix.

4. Step 4 – Selecting Principal Components:

Eigenvalues show the importance of each component. The top ones are selected.

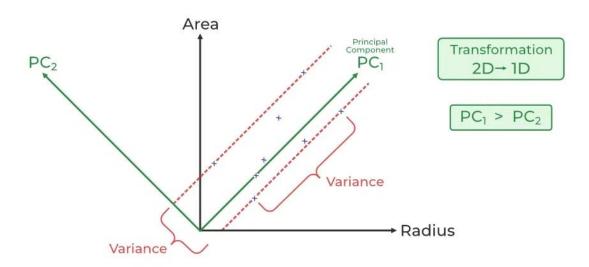
1

5. Step 5 - Formation of New Dataset:

A new dataset is formed using the selected principal components.

6. Example:

If a dataset has 5 features, and the first 2 components explain 95% of the total variance, PCA will keep only those 2 for further analysis.



4. Applications of PCA

1. Image Processing:

PCA reduces thousands of pixel values into a few main image features.

Example – Face recognition systems use PCA to extract key facial patterns.

2. Finance:

PCA helps to identify main financial indicators from many correlated market variables.

3. Genetics:

PCA is used to find key patterns in thousands of gene expression data points.

4. Education:

PCA can combine several test scores into a few major academic performance factors.

5. Machine Learning:

It is used for **feature extraction** before applying algorithms like K-Means or SVM.

Q. Linear Discriminant Analysis (LDA)

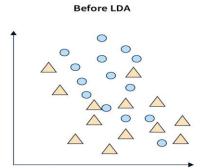
=>

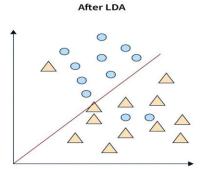
1. Introduction

- 1. **Linear Discriminant Analysis (LDA)** is a **supervised dimensionality reduction** technique used in machine learning.
- 2. It helps to **reduce the number of features** in the dataset while keeping the **class-separating** information.
- 3. Unlike PCA (which is unsupervised), LDA uses **class labels** to maximize separation between multiple classes.
- 4. LDA finds a new axis (or line) that best separates different classes in the data.
- 5. It is commonly used in **classification problems** to improve model accuracy and reduce complexity.
- 6. Example LDA can separate email data into "spam" and "not spam" categories using fewer features.

2. Basic Concept of LDA

- 1. The main goal of LDA is to **maximize the distance between different classes** and **minimize the spread within the same class**.
- 2. It projects high-dimensional data onto a **lower-dimensional space** where the separation between classes is most visible.
- 3. It helps in improving the **decision boundary** of classification algorithms such as Logistic Regression, SVM, or KNN.
- 4. LDA assumes that each class's data points follow a normal (Gaussian) distribution.
- 5. It also assumes that each class has the **same covariance matrix**, which simplifies calculations.





3. Mathematical Steps in LDA

1. Step 1 - Compute Mean Vectors:

Find the mean (average) of each class.

Example - Mean of "spam" emails and mean of "non-spam" emails.

2. Step 2 - Compute Scatter Matrices:

- a. Within-Class Scatter (SW): Measures how data points vary inside each class.
- b. Between-Class Scatter (SB): Measures how far apart the means of classes are.

3. Step 3 - Compute Projection Matrix:

The algorithm finds a matrix that maximizes the ratio of SB to SW.

This ensures better separation between classes.

4. Step 4 - Compute Eigenvalues and Eigenvectors:

Eigenvectors corresponding to the largest eigenvalues are selected.

These vectors form the new axes (discriminant functions).

5. Step 5 - Project Data:

The data is projected onto these new axes to get reduced-dimensional data.

6. Example – If data has 5 features but only 2 classes, LDA can reduce it to **1 feature** that best separates the classes.

4. Applications of LDA

1. Face Recognition:

LDA is used to identify faces by reducing image pixels into class-separating features.

Example - The Fisherfaces method for face recognition uses LDA.

2. Text Classification:

LDA helps in separating documents into different categories like "sports," "politics," or "technology."

3. Medical Diagnosis:

It helps doctors classify patients as "healthy" or "diseased" based on clinical features.

4. Finance:

Used to classify customers into "high risk" or "low risk" groups for loan approval.

5. Speech Recognition:

LDA reduces the number of features from voice signals while keeping class information.

5. Example for Better Understanding

- 1. Suppose we have a dataset of **students' marks** in Mathematics and English.
- 2. Each student is classified as either "Passed" or "Failed."
- 3. The marks of both subjects are plotted on a graph with two axes (Math and English).
- 4. LDA finds a line (discriminant axis) that best separates "Passed" and "Failed" students.
- 5. This line becomes the **new 1D feature**, reducing 2D data into 1D while preserving class information.