

Write a function that returns true if all of the roots in the tree are unique.

```
>>> t = tree(4, [])
>>> unique_roots(t)
True
>>> t = tree(4, [tree(2, [tree(4)])])
>>> unique_roots(t)
False
```

```
def unique_roots(t):
```

```
    past_roots = [root(t)]
```

```
    unique = True
```

```
    def helper(t):
```

```
        for branch in branches(t):
```

```
            nonlocal past_roots, unique
```

```
            if root(branch) in past_roots:
```

```
                return False
```

```
            past_roots += [root(branch)]
```

```
            unique = helper(branch)
```

```
        return unique
```

```
    return helper(t)
```

Check Yourself:

1. Why do we check if root is in past\_roots first?
2. Why do we declare past\_roots and unique as nonlocal?
3. Why do we need to keep track of whether or not we have seen a repeat yet (unique variable)?

```
def unique_roots2(t):
```

```
    def helper(t, past_roots, unique=True):
```

```
        for branch in branches(t):
```

```
            if root(branch) in past_roots:
```

```
                return False
```

```
            past_roots += [root(branch)]
```

```
            unique = helper(branch, past_roots, unique)
```

```
        return unique
```

```
    return helper(t, [root(t)])
```

Check Yourself:

1. What is yet another way to keep track of the variables?

Approach: We know that we will somehow have to compare all of the nodes to each other. A priori we might do something like:

```
def unique_roots(t):
    past_roots = [root(t)]
    for branch in branches(t):
        do something
        past_roots += [root(branch)] #keep adding roots
```

Running through a quick example of this though will show that this will only compare the roots inside each subtree.

So we need a way to keep adding in roots to past\_roots across function calls/across the branches horizontally

=nonlocal or parameters

The point of the function is to determine if all of the nodes are unique

⇒ We must keep track of all the roots we have seen so far as we recursive through the tree

This function will:

1. Iterate through the branches
2. Add all roots to past\_roots
3. Compare each root to the roots in past\_roots
4. Return False if there is a repeat

This is an alternative approach.

Instead of using nonlocal, here we use function arguments to keep passing past\_roots and unique. The key ideas are the same.

Initially it is not clear why we need unique, come back to this variable at the end