Quantum Mechanics

Imp Wave brushin, if of physical meaning

The wavebruckers, denoted by 4 m an Important quantity in Quantum Mechanics. A quantity whose variations are related with matter waves called wavebrucking. [Matter waves means the wave associated with particles or waves]

If in a mathematical function which describes
the state of a particle It is a bunding of
position and time co-ordinales It is generally
a complexe bunction.

of the system.

The normalization andition of the wavefunts

de in the volume element.

Quantern Mechanics

Dr. Hameshya

The Uncertainty painciple

It is one of the most significand physical haw and was boundaled by Werney Heisenberg. It states that it is impossible to lenow both the exact possition of crenact momentum of an object at the same line.

It is quantitalinely stated as A DE A POR 2 1/2 Where to = 1/2 1

Bimilas relatives can le written ough with to parameters like angular displacement, a and angular momenting

ii, AQAJ2 2 1/2 also, time of Energy, E 10, ATDE Z top.

Apphialins

D. Absence of és in a nucleus / Can és remain in a nucleus / Non-exerting of tree is in le

NATARAJ. 621 SCALE (A) . (Ta) Mormally, a nuclei have kadii value of the order 1014m. For an E to be contined within the nucleus, the uncertainty in its passition may not exceed 1014 m. ii Ax = 10 m By ustry the principle, axapa x 5 is APR ~ Ask to ≈ 1+1 × 10 20 kg m/s This is the uncertainty in the momentum of E. The momentum itself is of the order ob 1.1 x 10 20 kg mls -- Px x 1-1 x 10 20 leg for ls = p2c2+m2c4 -- Px x 1-1 x 10 20 leg for ls -- Pc x 1-1 x 10 20 leg for ls -- Px x 1-1 x 10 20 leg for ls -- Px x 1-1 x 10 20 leg for ls -- Px x 1-1 x 10 20 leg for ls According to let of e, T = Pact T= PC = 1.1 x 10 20 x 3 x 18] = 1-1 x1020 x3x108 1.6x1517eV = ROMeV

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ni, the k E of this must be more than 20 MeV, ni, it to be a nuclear constituent. (es, protens neutrons etc). Emperiments prove that in is associated with unstable atoms never have more than a brailier ob this energy - So we conclude that es cannot present within the nuclei.

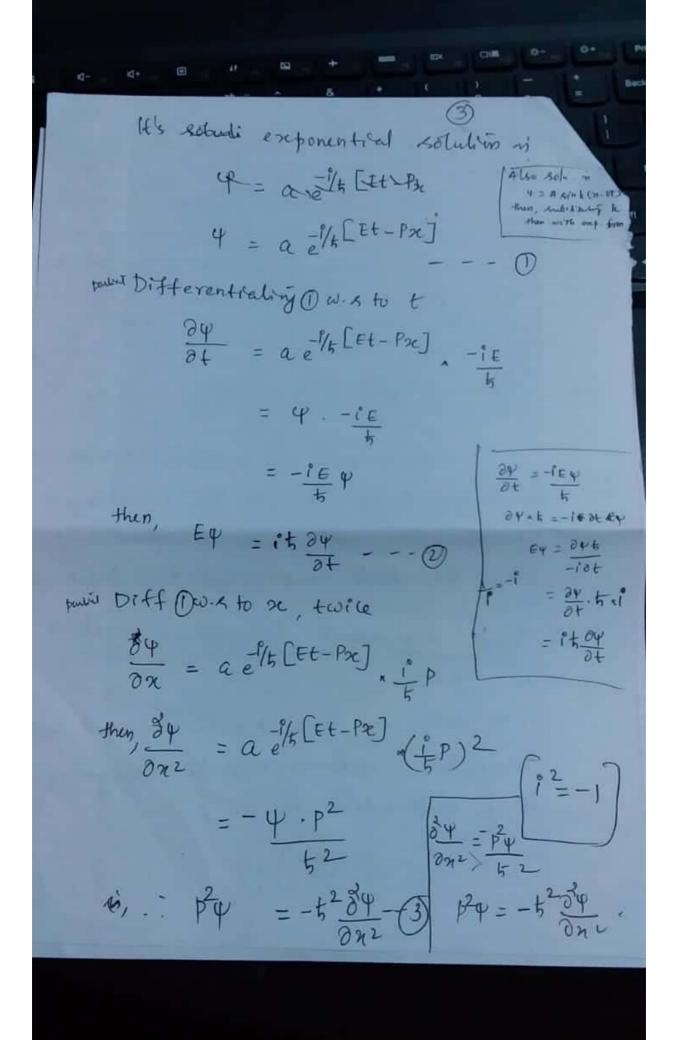
Imp Schrodinger's Equalities

Schrödinger's egn- in con most impertant ferndamental egn. of Q.M. The Schrodinger gn. has two parts - , one in which cent time dependent and other time independent

a) Time dependent Schrodinger equality

The diff. egn. et a one dimensional wave associated with a particle, propagating along x-directoris so.

$$\frac{\partial \varphi}{\partial n^2} = \frac{1}{\sqrt{2}} \frac{\partial \varphi}{\partial + 2}$$



$$n', E = \frac{p^2}{2m} + V$$

multiply my both sides by y

$$i$$
, $E\psi = \frac{\beta\psi}{am} + v\psi$

substituting the values of

$$E = 5 \cdot E + p \cdot C$$

$$= \frac{1}{2} m v^{2} + V$$

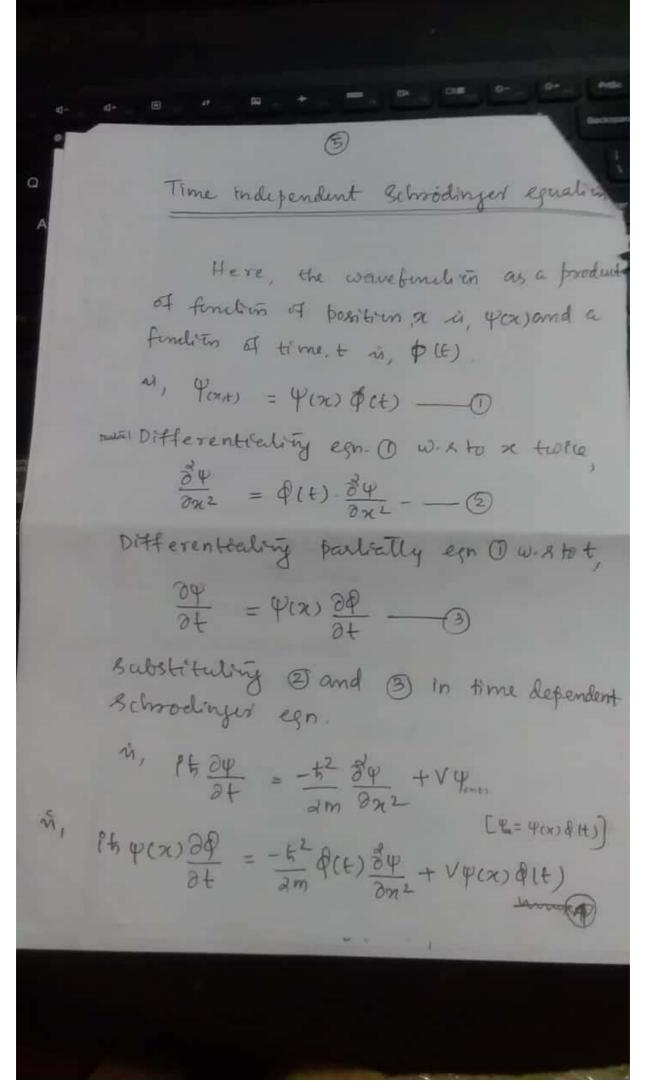
$$= \frac{1}{2} \frac{m v^{2} v^{2}}{m} + V$$

$$= \frac{1}{2} m v^{2} p$$

$$= \frac{p^{2}}{2m} + V$$

$$\int_{0}^{1} \frac{\partial \psi}{\partial t} = -\frac{t^{2}}{2m} \frac{\partial \psi}{\partial x^{2}} + V\psi$$

this is the One dimensional timedependent Schrödinger equalities. then, 3D is,





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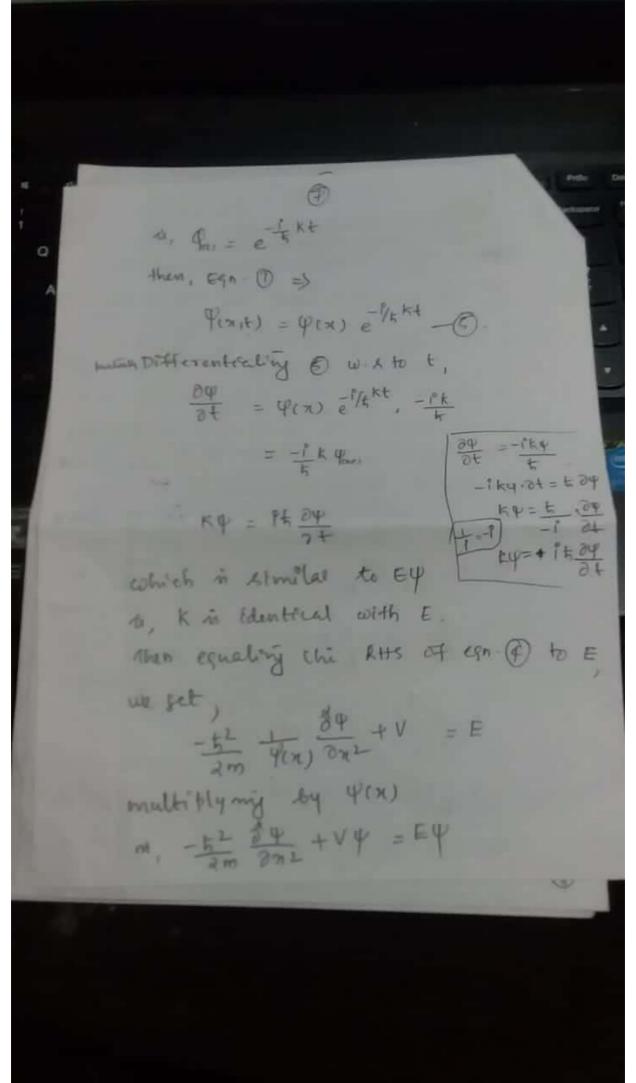
15 to 100 ot = -52 to 34 + V

LHS of this go in a function of t alone and RHS function of so. For the egn. to be consistent, each side must be equal to same constant, k.

is, equality the LHS of egn @ with k

1, Ph dit) St = K

then, $\frac{\partial Q}{\partial w} = \frac{-i}{5} k \partial t$

Integraling, Spit) = -ik Sat 108 191 = -ik . t 

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ni, Dividing throughout by - 52

m, 34 + - 2m vp + am E4 = 0 m, 34 + 2m (E-V) 4 = 0.

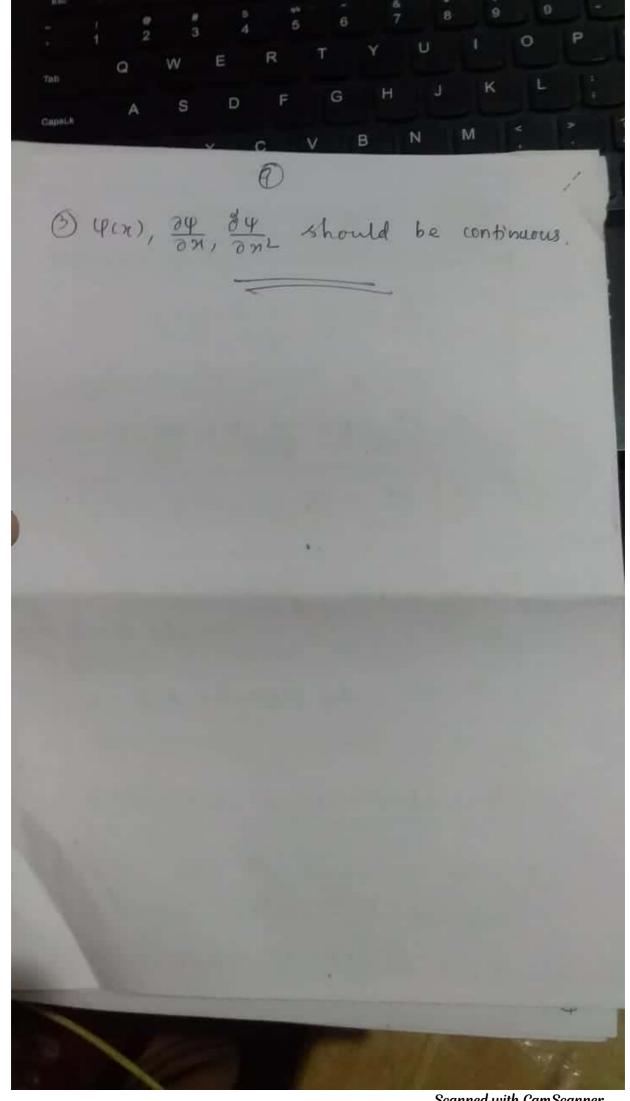
This is the Schrodinger's time independent equalitin in ID. Or steady state egn.

In 3D, PP+ 2m (E-V) P=0

Characteristics of wavefindin

The solution of the wave bindrin should be binite and

4(21) Should be single valued.

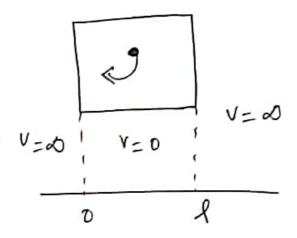


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Quantium Hechanics

Particle is a Brx

Consider a free particle [means a particle to my fixers, their for the most subjected to my fixers, their for is constant in V = 0] moving worked a box. The particle is bouncing back of fixeth blis the walls of the box. If it is the length (width) of the box. The p. E. V of the particle is institute is institute on both wides of the box.



$$V=0$$
 if $0<2<1$
 $V=0$ if $0<2<1$

Disthin the box, the time independent Schrödinger egn. is $\frac{d^2 \psi}{d n^2} + \frac{2m}{\hbar^2} (E-V) \psi = 0$

[for a par free particle, v= 0] (3) hen, $\frac{d^2 \varphi}{d \alpha z} + \frac{a m}{h^2} E \varphi = 0$ [:: $k = \sqrt{\frac{m E}{h^2}}$] $\frac{d^2q}{dx^2} + k^2\psi = 0$ The general solution of this equ. is 4 = A & sinkx + B cos fx _ @ Applying boundary conditions is, q=0 at n=0 -6 4=0 at x=1 -0 When applying O condition, then B=0. Apply my @ condition, 0 = A sink x menandonal N, A sint & = 0. itl=nx, while ·: K = 'nx , n = 1, 2, 3. substituting the value of k in the egn. a 4n(x) = A sin nn x , where n=1,2,3... we know, 52 = 2mE

artice

E

hī

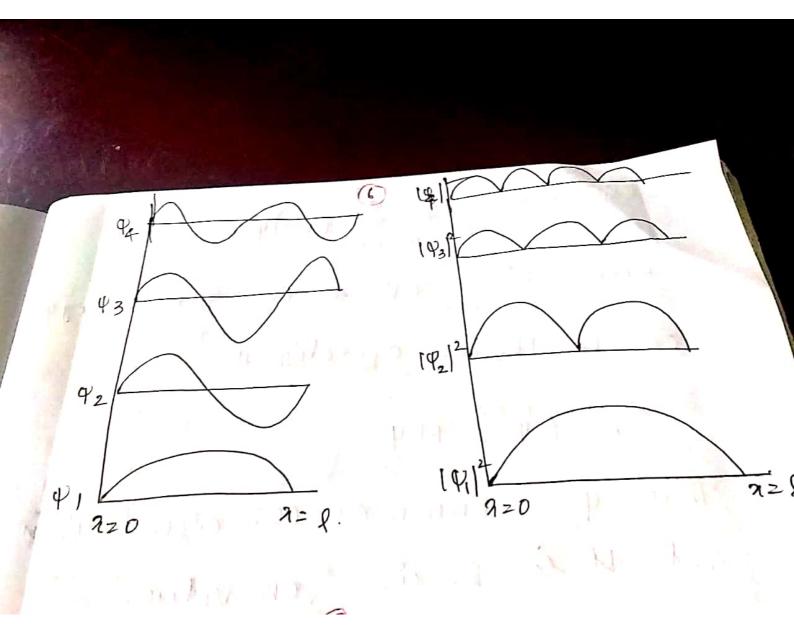
th)

E = k2 k2 2m I Rince k = Mx , h = h - E = (nx)2(6)2 $= \frac{m^2 \sqrt{2h^2}}{2h^2} = \frac{m^2 h^2}{8m R^2}, m = 1, n = 1$ 12×2m×41/2 Here $\Psi_n(x) = A \sin n\pi x$, where n = 1, 2, 3. is the eigen function and its corresponding $E_n = n^2h^2 - (b)$ eigen value is 8mg2, n-1,2,3-To find the constant A in the eigen fundin are apply my normalization condition of Wavefinchins m, $\int_{-\infty}^{\infty} |\psi|^2 dx = 1$. $\int_{0}^{x} \left| A \sin n\pi x \right|^{2} dx = 1$

is far sintage de = 1 $\frac{A^2}{2}\int_{-\infty}^{\infty}(1-\cos2\pi x)dx=1$ 12 [2- Bib 2000 = 1 12 [1 - Sindnx . 1 = 1 りなまり 南, 成1[1-0]=1 No = 1 A 2 = 3 - : A = 12/2 The eigen finelin, $(Y_n (x)) = \sqrt{y_n} + 8in \frac{n\pi x}{2}$ where n=1,9,3.00 Egn. 6) represents the stationary energy states possible to the parlicle in a bon. The energy of the partiels in a box in the ground state is obtained by putting n21 In egn. 6. n', $E_1 = \frac{h^2}{8m\ell^2}$ m=1 m

Thus, a partite continued to a box cannot have any arbitrary or continuous value of theory.

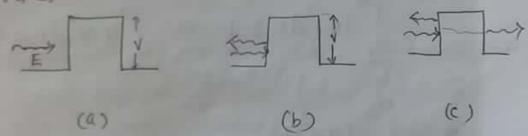
The following fig. represents the wavefinding of probability density $|\psi|^2$ for a single partie in a box.



Quantum mechanical Tunnelling

consider a plane wave through a sularyular barrier the transmission is based on lunnel obtest, if a particle is impinging on a barrier barrier with energy less than the height of the potential barrier, it will not totally reflected by the barrier but there is always a trobability that it may cross the barrier and continued its motion.

E - partile energy



- (a) A partitle with energy ELV approaching a potential barrier
- (6) From, classical mechanics, the particle must be reflected by the barrier
- on Q.M, the particle are partial partly reflected of partly transmitted si, the porticle has the probability to penetrality the bank

1 The wavefendin ob a particle ris Ψ = A cos'x for the interval - 1/2 to Find che value of A? 4 = A cos oc for - 1/2 to 1/2 The Normalization condition of wavel $\int_{0}^{\infty} |\psi|^{2} dv = 1 \quad \text{or} \quad \int_{-\infty}^{\infty} \psi \psi^{*} dv = 1$ $\frac{\pi}{2}$ $\int_{-\pi/2}^{\pi/2} |\psi|^2 dx = 1$ $\int_{0}^{\pi/2} |A \cos^2 \alpha c|^2 d\alpha = 1$ A^2 $\int_{-\infty}^{\pi/2} \cos^4 x \, dx = 1$ 2 A 1 1 cost x dx = 1

Integrating the buchin then, $2A^2\frac{3\pi}{10}=1$ $A = \sqrt{\frac{8}{3\pi}}$ @ Calculate the separation bow the two lowest energy levels of an electron in a 10 box of width 4 A° in joules. Given me = 9.1 x1031 kg, h=6.625 x 10 34 Js We know, the egn. of Energy in apartich in a lox, $E_m = \frac{n^2 h^2}{8ma^2}$ First to calculate, E, is, n=1 $E_{1} = (6.625 \times 10^{34})^{2} \qquad \left[l = 44^{\circ} \right]_{=4 \times 10^{10}}$ $8 \times 9.1 \times 10^{31} \times (4 \times 10^{10})^{2}$ = 0.0376 × 10 1

thun,
$$n=a$$
.

 $\frac{1}{2} = 2^{2} \times (6.625 \times 10^{-34})^{2}$
 $\frac{1}{2} = 2^{2} \times (6.625 \times 10^{-34})^{2}$
 $\frac{1}{2} = 2 \times (6.625 \times 10^{-34})^{2}$
 $\frac{1}{$

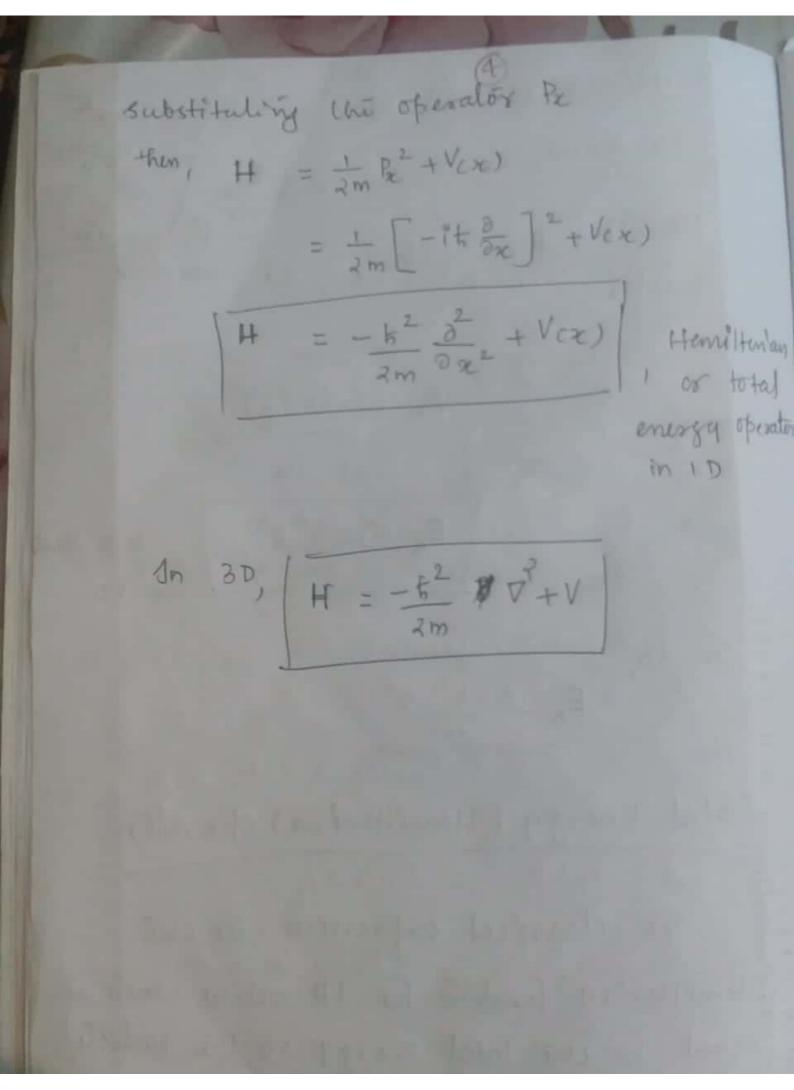
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de Broglie's Wavelength, $\lambda = \frac{h}{P}$ = 6-625 × 10 34 m=9.1 × 10 31 = 6-625 × 10 34 m= 6. E=100× 1-6 × 10 15 - 2×9-1×1531×100×1.6×1519 = 1,22 x10 m

Operators in Quantim Hechanics An operator fromsforms one benefits into amother cs the differential operator of which applied to a lunchin fox), we get the differential coefficient of fix), denoted by bix. in, of [fix] = fix Here, of in the operator and best in the operand. In Q.M, we represent the operator by a bold letter A. operators in Q.M are linear, in A intere it satisfies the condition A[4,+42] = A4,+A4, A [C4] = CAY, Cisa const.

Energy and Momentin Operators Consider the wavefundin bor a free partitle Y(7/t) = A e 1/5 [Et-Pac] Diff. W. S to 2 of t. Qφ = a = 1/2 [Et-Px] = FP $= \frac{P_i^{\circ} \psi}{k} - 0$ 24 = a = 1/5 [Et-P2] (-1° E $=-\frac{iE}{F}\psi$ Form D, Py = -it 34. EY = 1 = 24 - The momentum and Energy operators are Pr = - 1 5 2 E = i°tay

Kinetic Energy Operator We know, the k E, Ek = B2 We have, Be = - 1 to Dx, the momentum operator then O=> Ex = (-15 3x) E. E. Ofento In 30, Total Energy (Homiltonian) operator The classical expression for the "E Home Henean fundion for ID motion which is 3 = 1 = Pot + Vox) Va > P. E of i, $H = \frac{Px^2}{am} + Vox)$ the partie



Ergen values and Ergen finitions of Operalos An operator A operating on a function q is to multiply 4 by a constant factor, 2. is, A = > 4 Here 4 is an eigen fundition of 4 and corresponding eigen value is 2. We know the some dependent schoolinger egn. Eq = - 52 34 + VY

i, $E\Psi = \left(-\frac{1}{2}\frac{3}{3}\frac{3}{2}+V\right)\Psi -$ Here - 52 2 + V is the total energy Or Hamiltonian Operator, H i, EY = HY Thus, of is known as the eigen benelin and It is E is eigen value.