Final Writeup

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The Data

```
data <- read.csv("data/data-train.csv")
```

Final Model and Predictions

```
attach(data)
set.seed(3)
train_ind <- sample(x = nrow(data), size = 0.8 * nrow(data))
test_ind_neg <- -train_ind
training <- data[train_ind, ]
testing <- data[test_ind_neg, ]
training</pre>
```

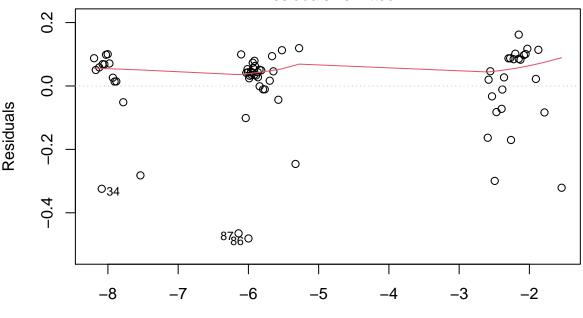
```
##
           Re
                  Fr R moment 1 R moment 2 R moment 3 R moment 4
                 Inf 0.00036945 6.2242e-03 1.2649e-01 2.5714e+00
## 5
     0.70 398
## 58 2.00
            90 0.052 0.15433000 1.0269e+03 8.8700e+06 7.6700e+10
## 12 0.30 398
                 Inf 0.00036022 6.2830e-03 1.3546e-01 2.9211e+00
## 36 0.90 224 0.300 0.00280490 4.1143e-02 7.5132e-01 1.3729e+01
## 88 0.60 224
                 Inf 0.00291710 4.4317e-02 8.5282e-01 1.6431e+01
                 Inf 0.00574730 1.1966e-01 2.7480e+00 6.3159e+01
      3.00 224
## 20 0.20
           90 0.052 0.11760000 5.1774e+02 3.8100e+06 2.8000e+10
           90 0.052 0.14184000 8.7019e+02 7.2500e+06 6.0400e+10
## 55 0.40 398 0.052 0.00029691 4.1375e-03 7.6124e-02 1.4014e+00
## 40 0.20 224 0.052 0.00257870 2.6830e-01 3.9080e+01 5.6959e+03
## 48 0.30 224 0.052 0.00256750 2.6547e-01 3.7665e+01 5.3451e+03
## 84 0.90 398 0.052 0.00034145 5.0555e-03 9.4083e-02 1.7522e+00
## 37 0.40 224
                 Inf 0.00292630 4.6261e-02 9.2914e-01 1.8681e+01
## 66 2.00 398 0.052 0.00039644 6.1040e-03 1.1209e-01 2.0593e+00
           90 0.052 0.12261000 6.2727e+02 4.9100e+06 3.8500e+10
## 29 0.30
                 Inf 0.00370310 6.0910e-02 1.1829e+00 2.2990e+01
## 89 1.50 224
## 77 0.60
           90 0.052 0.12946000 7.1816e+02 5.7200e+06 4.5600e+10
     0.90 224
                 Inf 0.00302150 4.5244e-02 8.4530e-01 1.5809e+01
## 72 0.20 224 0.300 0.00246950 3.4818e-02 6.7088e-01 1.2939e+01
## 18 1.00 90 0.300 0.11236000 1.1261e+00 1.7335e+01 2.8261e+02
## 16 0.60 224 0.300 0.00257400 3.6621e-02 6.7102e-01 1.2309e+01
## 25 0.90 398
                 Inf 0.00038344 6.4432e-03 1.2925e-01 2.5935e+00
## 87 0.05 224 0.300 0.00135380 1.0303e-04 5.1400e-05 4.1600e-05
## 80 3.00
           90 0.052 0.15538000 1.0443e+03 9.1400e+06 8.0000e+10
                 Inf 0.00036800 6.3559e-03 1.3341e-01 2.8013e+00
## 22 0.50 398
                 Inf 0.07694500 3.2652e-01 3.4052e+00 4.1042e+01
## 60 0.30
                 Inf 0.17234000 2.2386e+00 4.0454e+01 7.6198e+02
## 51 3.00
```

```
## 6 2.00 90 0.300 0.14780000 2.0068e+00 3.6249e+01 6.7167e+02
## 76 0.20 90 0.300 0.07798500 2.5598e-01 2.0965e+00 2.0849e+01
## 15 0.50 90 0.052 0.12670000 6.8596e+02 5.4300e+06 4.2900e+10
## 10 0.60 398 0.052 0.00031431 4.4672e-03 8.2060e-02 1.5077e+00
## 11 0.90 90
                 Inf 0.09102700 5.9539e-01 7.2454e+00 9.5166e+01
                 Inf 0.00036977 6.4986e-03 1.3933e-01 2.9880e+00
## 75 0.40 398
## 23 0.20 224
                 Inf 0.00269160 3.9016e-02 7.6384e-01 1.4978e+01
## 3 0.70 224
                 Inf 0.00290540 4.3499e-02 8.2200e-01 1.5551e+01
## 73 3.00 398 0.052 0.00040188 5.4492e-03 9.1871e-02 1.5565e+00
## 78 1.50 90 0.300 0.13678000 1.8254e+00 3.2833e+01 6.0903e+02
## 59 0.90
           90 0.300 0.10962000 1.0319e+00 1.5797e+01 2.6136e+02
     0.05
           90
                 Inf 0.06352800 9.0653e-02 4.6746e-01 3.2696e+00
## 33 1.50
           90 0.052 0.15181000 9.9690e+02 8.5500e+06 7.3300e+10
## 19 0.70 224 0.052 0.00285610 3.1273e-01 4.4529e+01 6.3423e+03
## 38 0.80 398 0.052 0.00033341 4.9036e-03 9.1143e-02 1.6948e+00
## 26 0.50 224 0.052 0.00274240 3.0355e-01 4.3911e+01 6.3530e+03
## 45 0.80 224 0.052 0.00295750 3.3361e-01 4.8161e+01 6.9539e+03
## 7 0.20 90
                 Inf 0.08127300 3.2450e-01 3.0363e+00 3.2976e+01
## 1 0.10 224 0.052 0.00215700 1.3035e-01 1.4374e+01 1.5865e+03
## 71 0.80 224 0.300 0.00268160 3.7714e-02 6.7549e-01 1.2112e+01
## 41 0.30 224
                 Inf 0.00283770 4.3589e-02 8.6962e-01 1.7373e+01
## 82 0.05 90 0.052 0.08786800 5.3449e-01 2.2205e+01 1.5679e+03
## 62 0.50 90 0.300 0.08477300 4.9728e-01 6.0317e+00 8.3287e+01
## 31 1.50 224 0.052 0.00341630 4.0300e-01 5.8417e+01 8.4710e+03
                 Inf 0.00153380 2.5653e-04 3.0407e-04 5.4466e-04
## 86 0.05 224
## 14 1.00 224 0.052 0.00312380 3.6478e-01 5.3322e+01 7.7958e+03
## 43 2.00 224 0.300 0.00381230 6.1927e-02 1.1844e+00 2.2705e+01
## 81 2.00 224 0.052 0.00363470 4.4512e-01 6.5387e+01 9.6105e+03
## 63 0.80 398
                 Inf 0.00037399 6.2457e-03 1.2542e-01 2.5193e+00
## 67 0.70 224 0.300 0.00260870 3.6438e-02 6.5445e-01 1.1765e+01
## 70 0.90 224 0.052 0.00305410 3.5419e-01 5.1795e+01 7.5758e+03
## 17 0.10 90
                 Inf 0.07722700 2.2120e-01 1.8833e+00 2.0190e+01
## 69 0.30 398 0.052 0.00030066 4.3488e-03 8.3446e-02 1.6023e+00
                 Inf 0.00022202 1.0055e-03 1.0857e-02 1.1782e-01
## 34 0.05 398
## 61 0.50 224 0.300 0.00250710 3.5152e-02 6.4378e-01 1.1801e+01
                Inf 0.09691800 6.7696e-01 8.2384e+00 1.0602e+02
## 44 1.00 90
## 13 2.00 224
                 Inf 0.00447250 8.0804e-02 1.6668e+00 3.4408e+01
## 2 3.00 224 0.052 0.00379030 4.7042e-01 6.9940e+01 1.0404e+04
## 21 0.10 90 0.300 0.06125200 6.9867e-02 2.4338e-01 1.1379e+00
## 68 0.60 224 0.052 0.00279390 3.0594e-01 4.3745e+01 6.2554e+03
## 46 1.00 224 0.300 0.00289530 4.2300e-02 7.6755e-01 1.3941e+01
## 52 1.00 224
                 Inf 0.00309680 4.6454e-02 8.6381e-01 1.6077e+01
## 28 0.40 224 0.052 0.00268090 2.8897e-01 4.1585e+01 5.9861e+03
## 54 0.80 90 0.052 0.13793000 8.2524e+02 6.8000e+06 5.6100e+10
testing
```

St Re Fr R_moment_1 R_moment_2 R_moment_3 R_moment_4 ## 24 1.50 398 0.052 0.00038321 5.9338e-03 1.1156e-01 2.1004e+00 ## 27 0.10 398 0.052 0.00027479 3.2549e-03 5.8006e-02 1.0344e+00 ## 30 0.05 224 0.052 0.00173740 1.6633e-03 2.0228e-02 3.6438e-01 ## 32 0.80 90 Inf 0.09107400 6.1825e-01 7.4973e+00 9.7048e+01 ## 35 0.80 224 Inf 0.00298090 4.4580e-02 8.3764e-01 1.5759e+01 ## 39 1.50 224 0.300 0.00341050 5.4101e-02 1.0222e+00 1.9340e+01 ## 42 0.30 224 0.300 0.00250630 3.5881e-02 6.8596e-01 1.3132e+01

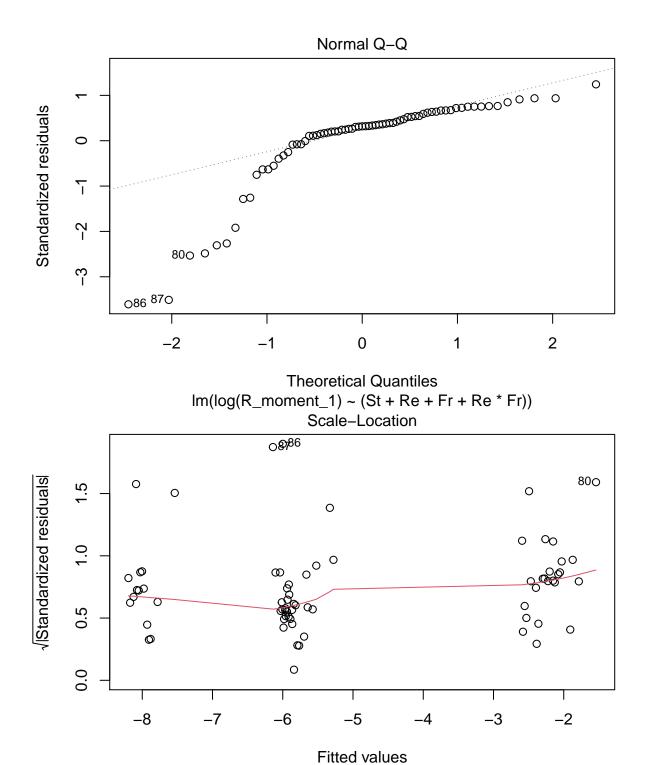
```
## 47 0.70 90 0.300 0.09471100 6.9751e-01 9.1793e+00 1.3187e+02
## 49 0.40 224 0.300 0.00262070 3.9502e-02 7.6851e-01 1.4966e+01
## 50 0.10 224 0.300 0.00221530 2.4475e-02 4.2167e-01 7.2842e+00
                 Inf 0.00053647 1.0022e-02 2.1023e-01 4.4109e+00
## 53 2.00 398
## 56 0.50 398 0.052 0.00030716 4.3494e-03 8.0143e-02 1.4770e+00
## 57 0.70 90
                 Inf 0.09217600 5.6482e-01 6.7191e+00 8.8723e+01
## 64 0.20 398
                 Inf 0.00033521 5.4505e-03 1.1408e-01 2.3884e+00
## 65 0.70 90 0.052 0.13173000 7.3694e+02 5.8700e+06 4.6700e+10
## 79 0.10
           90 0.052 0.10464000 1.6015e+02 6.9900e+05 3.0700e+09
## 83 0.40 90 0.300 0.08095700 3.9996e-01 4.3303e+00 5.3618e+01
## 85 3.00 90 0.300 0.16433000 2.3317e+00 4.4516e+01 8.8779e+02
ftraining <- training
ftesting <- testing
ftraining$Fr <- factor(ftraining$Fr, levels = c(0.052, 0.300, Inf))</pre>
ftraining$Re <- factor(ftraining$Re, levels = c(90, 224, 398))
ftesting$Fr <- factor(ftesting$Fr, levels = c(0.052, 0.300, Inf))
ftesting$Re <- factor(ftesting$Re, levels = c(90, 224, 398))</pre>
fit.lm1 <- lm(log(R_moment_1) ~ (St + Re + Fr + Re*Fr), data = ftraining)
pred.lm1 <- predict(fit.lm1, ftesting)</pre>
## Warning in predict.lm(fit.lm1, ftesting): prediction from a rank-deficient fit
## may be misleading
```

Residuals vs Fitted



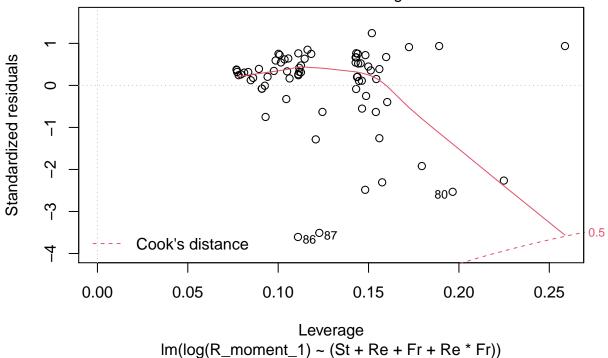
plot(fit.lm1)

Fitted values Im(log(R_moment_1) ~ (St + Re + Fr + Re * Fr))



 $Im(log(R_moment_1) \sim (St + Re + Fr + Re * Fr))$

Residuals vs Leverage

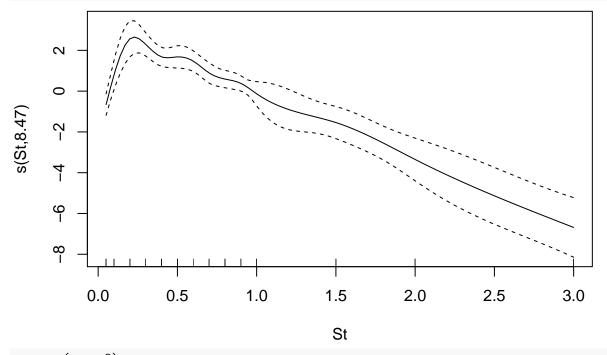


summary(fit.lm1)

```
##
  lm(formula = log(R_moment_1) ~ (St + Re + Fr + Re * Fr), data = ftraining)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
  -0.48100 -0.01056 0.04300 0.08114
                                        0.16195
  Coefficients: (1 not defined because of singularities)
##
               Estimate Std. Error t value Pr(>|t|)
##
                           0.04961 -45.828 < 2e-16 ***
## (Intercept) -2.27376
## St
                0.24431
                           0.02181 11.203 < 2e-16 ***
## Re224
               -3.78857
                           0.05950 -63.669
                                           < 2e-16 ***
## Re398
               -5.99652
                           0.06978 -85.932 < 2e-16 ***
               -0.24403
                           0.06973
                                    -3.500 0.000869 ***
## Fr0.3
               -0.33146
                                    -4.747 1.26e-05 ***
## FrInf
                           0.06982
## Re224:Fr0.3
               0.15420
                           0.09285
                                     1.661 0.101811
## Re398:Fr0.3
                     NA
                                NA
                                        NA
                                                 NA
                           0.09078
                                     4.214 8.28e-05 ***
## Re224:FrInf
               0.38257
## Re398:FrInf 0.50112
                           0.10325
                                     4.853 8.55e-06 ***
##
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 0.1414 on 62 degrees of freedom
## Multiple R-squared: 0.9963, Adjusted R-squared: 0.9959
## F-statistic: 2106 on 8 and 62 DF, p-value: < 2.2e-16
```

```
mse_test1 <- mean((pred.lm1 - log(testing$R_moment_1))^2)
mse_test1
## [1] 0.008822464</pre>
```

gam.m2 = gam(log(R_moment_2) ~ s(St) + Re + Fr + St:Re + St:Fr + Re:Fr, data = ftraining)
plot(gam.m2)

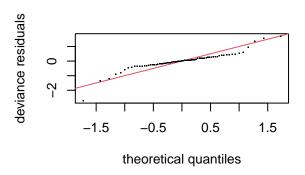


summary(gam.m2)

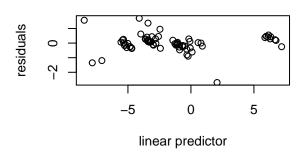
```
##
## Family: gaussian
## Link function: identity
##
## Formula:
## log(R_moment_2) ~ s(St) + Re + Fr + St:Re + St:Fr + Re:Fr
##
## Parametric coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 2.54657
                                       6.788 1.24e-08 ***
                            0.37518
                            0.37585 -18.933 < 2e-16 ***
## Re224
                -7.11591
## Re398
               -11.08527
                            0.52216 -21.230
                                              < 2e-16 ***
## Fr0.3
                -6.87397
                            0.49181 -13.977
                                              < 2e-16 ***
## FrInf
                -6.17375
                            0.42687 -14.463 < 2e-16 ***
                                     10.665 1.60e-14 ***
## Re90:St
                 3.77928
                            0.35437
## Re224:St
                 3.63936
                            0.36826
                                       9.883 2.19e-13 ***
## Re398:St
                 3.26669
                            0.38455
                                       8.495 2.71e-11 ***
## Fr0.3:St
                 0.51261
                            0.38567
                                       1.329
                                                0.190
## FrInf:St
                -0.07419
                            0.25302
                                     -0.293
                                                0.771
## Re224:Fr0.3
                 4.06642
                                       8.601 1.86e-11 ***
                            0.47277
## Re398:Fr0.3
                 0.00000
                            0.00000
                                          NA
                                                   NA
## Re224:FrInf
                 4.15555
                            0.46108
                                       9.013 4.39e-12 ***
## Re398:FrInf
                 6.74397
                            0.55523 12.146 < 2e-16 ***
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
## edf Ref.df    F p-value
## s(St) 8.467   8.799 17.03   <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Rank: 21/23
## R-sq.(adj) = 0.965   Deviance explained = 97.5%
## GCV = 0.69646   Scale est. = 0.49431    n = 71</pre>
```

gam.check(gam.m2)

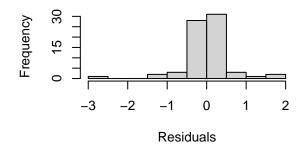


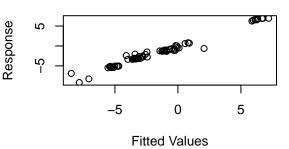
Resids vs. linear pred.



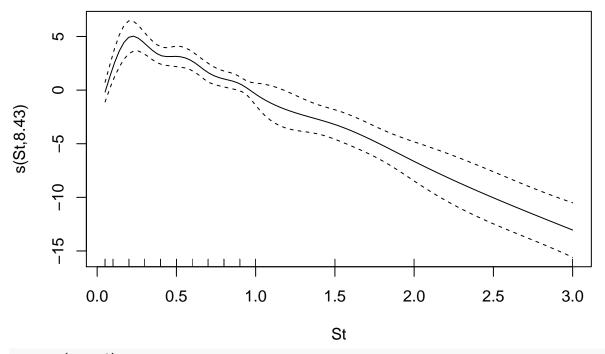
Histogram of residuals

Response vs. Fitted Values





```
##
                 Optimizer: magic
## Method: GCV
## Smoothing parameter selection converged after 8 iterations.
\#\# The RMS GCV score gradient at convergence was 3.715048e-07 .
## The Hessian was positive definite.
## Model rank = 21 / 23
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
           k' edf k-index p-value
## s(St) 9.00 8.47
                      1.08
                              0.71
gam.m3 = gam(log(R_moment_3) ~ s(St) + Re + Fr + St:Re + St:Fr + Re:Fr, data = ftraining)
plot(gam.m3)
```

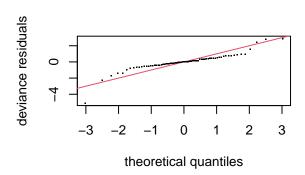


summary(gam.m3)

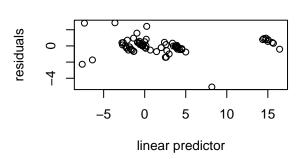
```
##
## Family: gaussian
## Link function: identity
##
## Formula:
## log(R_moment_3) ~ s(St) + Re + Fr + St:Re + St:Fr + Re:Fr
##
## Parametric coefficients:
               Estimate Std. Error t value Pr(>|t|)
                            0.6534 12.251 < 2e-16 ***
## (Intercept)
                 8.0050
## Re224
               -10.6005
                            0.6575 -16.124
                                           < 2e-16 ***
## Re398
               -16.4306
                            0.9132 -17.993 < 2e-16 ***
## Fr0.3
               -13.0638
                            0.8601 -15.188 < 2e-16 ***
               -11.7892
                            0.7467 -15.788 < 2e-16 ***
## FrInf
## Re90:St
                 7.1596
                            0.6164
                                    11.614 7.29e-16 ***
## Re224:St
                 6.8820
                            0.6412
                                    10.734 1.26e-14 ***
## Re398:St
                 6.2334
                            0.6705
                                     9.296 1.63e-12 ***
## Fr0.3:St
                 0.6865
                            0.6746
                                     1.018
                                              0.314
## FrInf:St
                -0.3003
                            0.4426
                                    -0.678
                                              0.501
## Re224:Fr0.3
                 7.8560
                            0.8270
                                     9.499 8.08e-13 ***
## Re398:Fr0.3
                 0.0000
                            0.0000
                                        NA
                                                 NA
## Re224:FrInf
                 7.8729
                            0.8066
                                     9.761 3.30e-13 ***
## Re398:FrInf
               12.7630
                            0.9712 13.141 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
           edf Ref.df
                          F p-value
## s(St) 8.435 8.788 19.87 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Rank: 21/23
## R-sq.(adj) =
                0.955
                        Deviance explained = 96.8%
          2.13 Scale est. = 1.5127
```

gam.check(gam.m3)

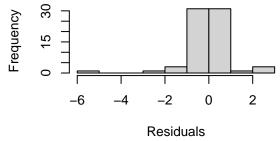


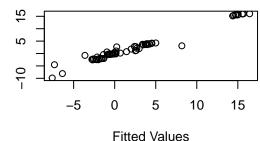
Resids vs. linear pred.



Histogram of residuals

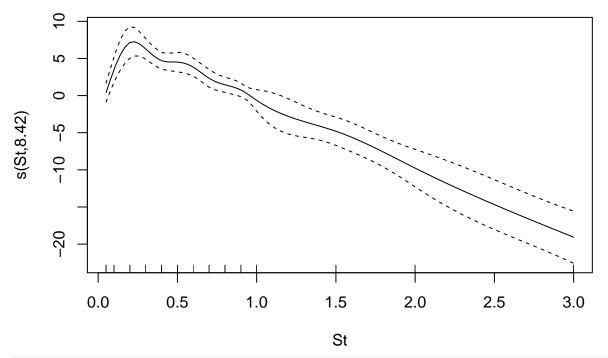
Response vs. Fitted Values





```
##
## Method: GCV
                 Optimizer: magic
## Smoothing parameter selection converged after 7 iterations.
\#\# The RMS GCV score gradient at convergence was 8.319095e-05 .
## The Hessian was positive definite.
## Model rank = 21 / 23
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
##
  indicate that k is too low, especially if edf is close to k'.
##
##
           k'
               edf k-index p-value
## s(St) 9.00 8.43
                      1.08
gam.m4 = gam(log(R_moment_4) ~ s(St) + Re + Fr + St:Re + St:Fr + Re:Fr, data = ftraining)
plot(gam.m4)
```

Response

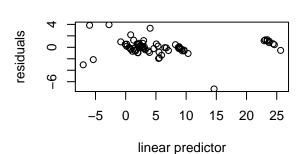


summary(gam.m4)

```
## Family: gaussian
## Link function: identity
##
## Formula:
## log(R_moment_4) ~ s(St) + Re + Fr + St:Re + St:Fr + Re:Fr
## Parametric coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                            0.9028 15.171 < 2e-16 ***
               13.6971
## Re224
               -14.1498
                            0.9106 -15.538 < 2e-16 ***
## Re398
               -21.8583
                            1.2647 -17.284
                                           < 2e-16 ***
## Fr0.3
               -19.1353
                            1.1913 -16.063
                                           < 2e-16 ***
## FrInf
               -17.3592
                            1.0342 -16.784
                                           < 2e-16 ***
## Re90:St
                10.3389
                            0.8511 12.148 < 2e-16 ***
## Re224:St
                 9.9495
                            0.8857
                                    11.234 2.46e-15 ***
## Re398:St
                 9.0499
                            0.9271
                                     9.762 3.27e-13 ***
## Fr0.3:St
                 0.8019
                            0.9343
                                     0.858
                                              0.395
## FrInf:St
                                    -0.848
                -0.5199
                            0.6131
                                              0.400
## Re224:Fr0.3 11.6078
                            1.1455
                                    10.134 9.28e-14 ***
## Re398:Fr0.3
                0.0000
                            0.0000
                                        NA
                                                 NA
## Re224:FrInf
               11.5630
                            1.1172
                                    10.350 4.49e-14 ***
## Re398:FrInf
               18.7047
                            1.3453
                                    13.904 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Approximate significance of smooth terms:
           edf Ref.df
                          F p-value
## s(St) 8.416 8.782 22.52 <2e-16 ***
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Rank: 21/23
## R-sq.(adj) = 0.954 Deviance explained = 96.7%
## GCV = 4.0851 Scale est. = 2.9023 n = 71
gam.check(gam.m4)
```

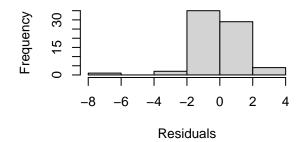
deviance residuals deviance residuals -4 -2 0 2 4 theoretical quantiles

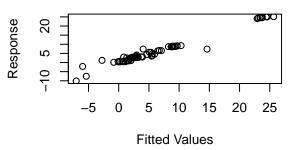


Histogram of residuals

Response vs. Fitted Values

Resids vs. linear pred.





```
##
## Method: GCV
                  Optimizer: magic
## Smoothing parameter selection converged after 7 iterations.
\#\# The RMS GCV score gradient at convergence was 0.0001068624 .
## The Hessian was positive definite.
## Model rank = 21 / 23
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
##
           k' edf k-index p-value
## s(St) 9.00 8.42
                       1.08
                                0.73
pred.gam2 <- predict(gam.m2, ftesting)</pre>
pred.gam3 <- predict(gam.m3, ftesting)</pre>
pred.gam4 <- predict(gam.m4, ftesting)</pre>
mse_gam2 <- mean((pred.gam2 - log(ftesting$R_moment_2))^2)</pre>
mse_gam3 <- mean((pred.gam3 - log(ftesting$R_moment_3))^2)</pre>
mse_gam4 <- mean((pred.gam4 - log(ftesting$R_moment_4))^2)</pre>
mse_gam2
```

```
## [1] 0.8611115
mse_gam3
## [1] 2.292613
mse_gam4
## [1] 4.100509
Predictions on the Test Data
datat <- read.csv("data/data-test.csv")</pre>
datat$Fr <- factor(datat$Fr, levels = c(0.052, 0.300, Inf))</pre>
datat$Re <- factor(datat$Re, levels = c(90, 224, 398))</pre>
predt.lm1 <- predict(fit.lm1, datat)</pre>
## Warning in predict.lm(fit.lm1, datat): prediction from a rank-deficient fit may
## be misleading
predt.gam2 <- predict(gam.m2, datat)</pre>
predt.gam3 <- predict(gam.m3, datat)</pre>
predt.gam4 <- predict(gam.m4, datat)</pre>
Prediction Consolidation
Creating a csv of predictions:
dataframe all <- bind rows(predt.lm1, predt.gam2, predt.gam3, predt.gam4)
dataframe_all <- exp(dataframe_all)</pre>
dataframe all
## # A tibble: 4 x 23
##
         `1`
                 `2`
                          `3`
                                  `4`
                                           `5`
                                                   `6`
                                                           `7`
                                                                    .8.
                                                                            `9`
       <dbl> <dbl> <dbl> <dbl>
                                               <dbl>
                                                                  <dbl>
##
                                        <dbl>
                                                         <dbl>
                                                                          <dbl>
## 1 2.59e-4 2.69e-4 3.04e-4 3.27e-4 3.11e-4 3.51e-4 3.87e-4 4.38e-4 6.31e-4
## 2 1.19e-4 4.91e-3 4.70e-3 4.51e-3 1.06e-3 1.03e-2 7.40e-3 8.91e-3 6.25e-3
## 3 2.49e-4 1.06e-1 8.81e-2 7.64e-2 9.05e-3 3.04e-1 1.50e-1 1.72e-1 6.72e-2
## 4 6.77e-4 2.22e+0 1.64e+0 1.28e+0 8.55e-2 8.48e+0 2.92e+0 3.24e+0 7.44e-1
## # ... with 14 more variables: `10` <dbl>, `11` <dbl>, `12` <dbl>, `13` <dbl>,
```

`14` <dbl>, `15` <dbl>, `16` <dbl>, `17` <dbl>, `18` <dbl>, `19` <dbl>,

`20` <dbl>, `21` <dbl>, `22` <dbl>, `23` <dbl>

write.csv(dataframe_all, "data/predictions.csv", row.names = FALSE)