## **Assignment 3** (Due 27/04/2024):

Note all tests use the 5% significance level for type-I error and use ten lags in all ACF or ARCH-effect tests.

- 1. The file d-sbuxsp0106.txt contains the daily simple returns of Starbucks stock (SBUX) and the S&P 500 composite index from 1996 to 2006. The file consists of date, SBUX return, and S&P returns in three columns. The returns include dividends. Convert the simple returns into percentage log returns.
- a. Is there any serial correlation in the log returns of Starbucks stock?
- b. Is there any ARCH effect in the log returns of Starbucks stock?
- c. Fit a GARCH(1,1) model for the percentage log return of Starbucks stock using normal distribution for the innovations. Perform model checking and write down the fitted model.
- 2. Consider the daily percentage log returns of S&P 500 index in Problem 1.
- a. Is there any serial correlation in the log returns of S&P index?
- b. Is there any ARCH effect in the log return series of S&P index?
- c. Fit an IGARCH(1,1) model for the log return series of the index using normal distribution for the innovations.
- d. Compute 1- to 4-step ahead forecasts for the daily percentage log return and its 1-step forecasting interval.
- **3**. Again, consider the daily percentage log returns of Starbucks stock in Problem 1.
- a. Fit a GARCH(1,1)-M model for the series with normal distribution. Write down the fitted model.
- b. Is the ARCH-in-mean parameter significant at the 5% level?
- c. Fit a EGARCH(1,1) model with normal innovations to the log return series. Perform model checking and write down the fitted model.
- d. Is the leverage parameter significant?

- 4. The data file m-pg5606.txt contains the date and monthly simple returns of Procter & Gamble (PG) stock from 1956 to 2006. Transform the simple returns into percentage log returns.
- a. Is there any serial correlation in the monthly log returns of PG stock?
- b. Fit a GARCH(1,1) model to the monthly percentage log returns of PG stock using normal distribution for the innovations. Write down the fitted model.
- c. Use the fitted model to calculate 1-step to 5-step ahead forecasts for the log returns series and its 1-step forecasting interval.
- 5. The file d-exuseu.txt contains the daily exchange rate between U.S. Dollars and Euro from January 1999 to March 20, 2007. Compute the percentage log returns of the exchange rate.
- a. Is there any serial correlation in the log return series?
- b. Is there any ARCH effect in the log return series?
- c. Fit an IGARCH(1,1) model to the log return series using normal innovations. Perform model checking and write down the fitted model.
- d. Use the model to produce 1-step to 4-step ahead forecasts for the log return series and its 1-step forecasting interval.