

# stream-membership: A Python package for empirical density modeling of stellar streams

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## Summary

stream-membership is a Python package that provides a flexible framework for creating and fitting probabilistic models of stellar stream properties. It is built on top of [jax](#) ([Bradbury et al., 2018](#)) and [numpyro](#) ([Bingham et al., 2019](#); [Phan et al., 2019](#)) both of which significantly simplify and accelerate the model creation and fitting process compared to previous codes.

The overarching purpose of stream-membership is to serve as an easy-to-use tool to characterize a large number of streams in the Milky Way. Specifically, stream-membership is built to characterize known stellar streams, as opposed to discovering new streams. However, it is able to recover new extensions or features of existing streams. The main properties that stream-membership is designed to model are: 1) astrometric properties (positions and velocities) and 2) density of stars along the stream. It is written with no specific stream in mind and can be applied to a diverse set of stellar streams. This should allow statistical population-level analyses which will constrain the structure of the Milky Way and the nature of dark matter.

stream-membership is designed to be accessible by researchers of all levels, especially those with a grasp of probability distributions. Additionally, a slight modification of this framework could lead to applications in other scientific fields where a density model is sought or required.

## Statement of Need

Stellar streams are one of the most powerful tools for understanding the structure of galaxies. They form when a bound group of stars (either a globular cluster or a dwarf galaxy) gets stripped of its members as it falls into a larger host galaxy (e.g. the Milky Way). This creates a thin stream of stars along the sky which approximately traces the orbits of its member stars. Precise orbits are critical for constraining the shape of the Milky Way's gravitational potential and understanding the structure of our galaxy's dark matter halo. Furthermore, inhomogeneities in a stream's density along its length are sensitive probes of small-scale structure and are one of the only probes of low-mass dark matter subhalos. Stellar streams are therefore key structures in our ongoing search for dark matter.

The past decade has seen a number of astronomy papers presenting density models of stellar streams ([Erkal et al., 2017](#); [Ferguson et al., 2022](#); [Koposov et al., 2019](#); [Li et al., 2021](#); [Patrick et al., 2022](#); [Starkman et al., 2023](#); [Tavangar et al., 2022](#)). These studies tend to apply their method to one or two streams at a time (see [Patrick et al. \(2022\)](#) for an exception). This has been useful to uncover the complex morphology of multiple Milky Way streams and has led to analysis of individual features in some streams ([Bonaca et al., 2019](#)). However, it is difficult or impossible to constrain the nature of dark matter or global properties of the Milky Way halo with just one or two streams. The real constraining power comes from statistical analyses of dozens of stellar streams, but such studies are extremely rare ([Ibata et al., 2024](#)). In fact, a

41 population-level analysis of inhomogeneities in streams has never been attempted. For many  
42 years, this was partly because we did not know of enough Milky Way streams to make such an  
43 analysis possible. Now, with more than 140 discovered streams (Mateu, 2023), we have the  
44 inverse problem: we have too few streams with characterized inhomogeneities.

45 stream-membership is designed to solve this problem by providing a framework with which  
46 to characterize streams quickly and easily. It has three major improvements over previous  
47 stream modeling techniques. First, it uses jax and numpyro to simplify and accelerate the  
48 model creation and fitting process. Jax is a numerical Python library for easy implementation  
49 of program transformations in Python and NumPy (Harris et al., 2020). Numpyro is a Python  
50 library built atop jax for creating probabilistic programs with an easy-to-use NumPy interface.

51 Second, stream-membership is the first package which includes the ability to model offtrack  
52 and non-Gaussian features of streams. Streams in a smooth gravitational potential are expected  
53 to lie along a single track. However, offtrack features have been observed in a few streams thus  
54 far (Ferguson et al., 2022; Li et al., 2021; Price-Whelan & Bonaca, 2018; Shipp et al., 2018)  
55 and they provide the strongest constraints on past interactions with small-scale Milky Way  
56 structure, including dark matter subhalos (Bonaca et al., 2019). While stream-membership is  
57 primarily designed for stream characterization as opposed to stream discovery, it is capable of  
58 recovering these previously unidentified offtrack and non-Gaussian features in known streams.

59 Lastly, stream-membership is written with no specific stream in mind and is designed to be  
60 broadly applicable to many stellar streams. It will enable the rapid generation of dozens of  
61 stream density models. We believe the outputs of these models have the potential to create  
62 the tightest constraints thus far of Milky Way structure and even the nature of dark matter.

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